5th-6th candidates

5th candidates

Label	Informal Role	Power Gain	Complexity	Risks to Minimality	Solves Which Claims
R (Primitive Recursor)	R base step n (unary δ-chain iterator)	High (PR closure)	Moderate	Adds arithmetic bias	C14, C23, strengthens EqNat completeness
Iter (Fold / Catamorphism)	fold t f acc general structural fold	Very High (arbitrary structural recursion)	High	May look like cheating ("meta recursion smuggled in")	Wide: substitution, proof enumeration
Mu (Well-Founded Fixpoint)	mu F seed reduces while measure drops	High (internal diagonal & derivability)	High	Harder termination proof	Diagonal, D1–D3
EqW (Equality Witness)	eqW a b → void iff nf(a)=nf(b)` else canonical non-void	Medium	Low	Focused, simple	Removes external Bool / DecEq reliance
Search (Bounded Existential)	seek B P tries P(0B)	Medium	Low-Med	Narrow semantics	Σ_1 prov existential, provability bounding
Quote (Self Code)	quote t returns code trace	Medium	Low	Adds reflection primitive	Cleaner diagonal; still need recursion
Pairing Recursor (PR on pairs)	R2 base step m n	High	Moderate	More arity complexity	Encodes multi-arg PR without meta loops

Opinion 1:

1 Adopt S1 ($rec\Delta + eqW$). It supplies primitive-recursive power, internal equality, and a credible path to purge Bool/Nat while preserving strong normalization and critical-pair tractability. S2 jeopardizes termination, complicates confluence, and dilutes minimality. Focus resources on lemmas L1–L9, then revisit minimization needs; defer $\mu\Pi$ until SN proof secured.

2 MINIMALITY IMPACT

 $rec\Delta + eqW$: +2 constructors, +4 rules; +6 critical pairs; still PR-bounded.

 $\mu\Pi$ only: +1 constructor, +3 rules; +5 pairs; admits general recursion \Rightarrow heavier than recΔ in SN proof. recΔ+eqW preserves tighter minimality.

3 TERMINATION & CONFLUENCE

recΔ rules: size decreases on δ -height; no β -creation; critical peaks with β ,ann,void solved by eager δ -reduction. Newman hinges unchanged.

eqW: single-step to void/witness, measure = paired nf size; confluence if witness is canonical (left-biased). $\mu\Pi$: body may re-grow term, cannot supply monotone measure \Rightarrow SN doubtful; peaks with β unresolved. 4 EQUALITY-WITNESS DESIGN

Root-only version: eqW a b \rightarrow (void | integrate ...); recursive fold only on outermost nf; Sound: nf(a)=nf(b) \Rightarrow void; Complete: nf(a) \neq nf(b) \Rightarrow witness normal-forms unequal; Irreflexive fail avoided by canonical witness integrate(merge x y) with x \neq y ordered by syntactic <.

5 INTERNAL RECURSION COVERAGE

recΔ gives primitive recursion on Nat-like δ -chains \Rightarrow addition, mult, bounded search definable. Minimization needs $\mu\Pi$ or explicit δ -bounded loop lemma. $\mu\Pi$ exceeds PR; may code any general μ giving SN risk. 6 GÖDEL PIPELINE

eqW allows plateau detection: define diag(F): μ n. eqW (F n) n. Remaining gaps: (i) code injectivity lemma, (ii) complement uniqueness, (iii) Prov Σ_1 .

7 SECOND INCOMPLETENESS

recΔ: D1–D3 encodable via explicit proof-concatenation; SN preserved.

μΠ: Lack of SN blocks internal derivability induction; risky.

8 BOOLEAN / NUMERAL PURGE VALIDATION (post-recΔ+eqW)

Residual Bool uses: none (if if/DecEq rewritten via merge).

Nat uses survive only in meta-termination proofs. Variable indices replaced by δ -vectors via rec Δ traversals.

Opinion 2:

Pick ONE of these two designs:

Option A (Leanest, Safe Minimality): Equality-Guided Primitive Recursor reca

Purpose: Supply *total primitive recursion on* δ -*chains* and internal equality tests via its base case branch outcome —killing external Bool and enabling Σ_1 completeness for all PR predicates you actually need (Prov, SubF, substitution counters, size bounds).

Signature (core calculus extension)

rec∆ b s n

- b : base trace (value for 0)
- s : step operator expecting current accumulator
- n : δ-chain acting as unary numeral

Rewrite Rules (Left → **Right)**

```
3623. recΔ b s void → b

3624. recΔ b s (delta n) → s (recΔ b s n) (where s x is encoded as app s x or merge (tag step) (pair s x) depending on your encoding choice)
```

Side Conditions: None (structural). Termination obvious: δ -height decreases.

Measure Impact: Adds a "Δheight(n)" component—strictly drops each step.

Derivable Additions:

- Addition: add m n := recΔ n (λr. delta r) m
- Multiplication: mul m n := rec∆ void (λr. add r n) m
- Equality witness: eqNatW a b := recΔ (testBase a b) (λr. testStep r a b) (maxDepth a b) (below I'll show simpler EqW alternative)

Pros:

- Still arithmetically flavored but tiny and orthodox (reviewers accept primitive recursion).
- Easy termination & confluence integration (orthogonal critical pairs).

Cons:

• Only handles unary loops—multi-argument primitive recursion requires pairing encodings (acceptable).

Option B (More Dramatic, "Breakthrough Branding"): **Reflective Fixpoint / Search Operator** μΠ

Signature:

```
muΠ F seed M
```

- F: transformer (expects a code and a candidate)
- seed: initial trace
- M : measure budget (δ -chain) guaranteeing finitude

Rewrite Scheme:

```
4826. mu∏ F seed void \rightarrow seed
4827. mu∏ F seed (delta m) \rightarrow stabilize(seed, F seed, mu∏ F (F seed) m)
Where stabilize(x, Fx, rest) reduces to x if an internal equality witness (see EqW below) shows nf(x)=nf(Fx), otherwise rest.
```

Pros:

- Directly internalizes bounded fixpoint iteration, diagonal plateau, Löb prerequisites.
- Lets you *drop* several ad hoc enumeration gadgets.

Cons:

- Heavier termination argument (must show each non-stable iteration decrements M).
- Risk of reviewer saying you imported a reflective engine disguised as a primitive.

If you pick Option B you *still need* an equality witness primitive or to embed it inside stabilize. That effectively makes EqW implicit anyway.

4. Equality Witness Primitive (If NOT Using Recursor First)

Even with Option A you likely still want **EqW** because it surgically removes external Bool / DecEq. It is ultra-cheap:

Operator: eqW a b

Rewrite Rules (on fully normalized or as part of normalization):

- 5857. If pattern-structural match succeeds (constructor by constructor) \rightarrow void.
- 5858. First mismatch position → integrate (merge a b) (or any canonical non-void marker with both original subtraces embedded for refutational info).

Implementation Tactic:

- Structural evaluator returns either void or delta marker but you can *stay purely rewrite* by expanding eqW into a one-step decision after recursively normalizing children.
- Confluence unaffected (deterministic, no overlapping left sides—only one root rule once children normalized).

Payoff:

- All prior beq usages become eqW.
- Diagonal plateau detection internal: test eqW ψ (F ψ).

5. Which Combination Maximizes "Breakthrough" with Minimal Rework?

Combo	New Primitives	Covered Gaps	Risk	Marketing Strength
RecΔ + EqW	2	PR closure, Σ ₁ repr., equality, diagonal plateau (still need simple iteration wrapper)	Low	"Minimal arithmetic + intrinsic equality"
μΠ (with baked EqW)	1 (but richer)	Equality, diagonal, search, partial recursion	Medium	"Single reflective fixpoint primitive"
EqW only	1	Equality / Bool removal	Low	Too small (doesn't solve Σ_1 completeness)

Recommended:Rec\Delta + EqW if you want *credibility first*; $\mu\Pi$ only if you're prepared to write a very clean termination + safety section so it doesn't look like a magical oracle.

6. Formal Specs (You Can Paste Into Draft)

6.1 Grammar Extension

 $t ::= ... \mid rec\Delta \ t \ t \ \mid \ eqW \ t \ t$

6.2 Measures

Extend measure triple to quadruple: $\mu(t) = (\beta Sites(t), annSites(t), \delta Height(t), size(t))$

- $rec\Delta$ b s n contributes $\delta Height(n)$ to third component.
- Rule application strictly decreases third component (or earlier components if inside β or annihilation contexts).

6.3 Critical Pair Audit (New)

Overlap	Reason Safe	
recΔ inside β redex body	β reduces first; measure: βSites drop.	
recΔ and annihilation (integrate/delta)	Independent root symbols.	
eqW vs structural normalizer	eqW only fires after children in NF; no overlap.	

6.4 Key Lemmas (Lean Skeleton Names)

Lemma	Statement Intent		
recΔ_decrease	$\mu(\text{rec}\Delta \text{ b s (delta n)}) > \mu(\text{s (rec}\Delta \text{ b s n)})$		
recΔ_total	Termination & NF existence for all δ -chains.		
eqW_sound	eqW a b = void → nf a = nf b.		
eqW_complete	$nf a = nf b \rightarrow eqW a b = void.$		
eqW_irrefl_nonvoid	eqW a b ≠ void → nf a ≠ nf b.		
add_repr	add m n $\equiv \delta^{eval m + eval n}$ void.		
mul_repr	Analogous for multiplication.		
prov_sigma1_full	Uses rec∆ to bound enumeration internal.		
diag_fixed_internal	Uses eqw as plateau test instead of external Bool.		

7. Impact on Existing Claims

Claim (Cx)	Status After RecΔ + EqW (If Proved)		
C16–C18 (freedom claims)	Move from NOT-COHERENT → PROVABLE ONCE Bool purged.		
C14 Primitive Recursive Representability	Becomes NOW after addition + proofs.		
C23 Σ_1 Completeness (restricted PR)	Downgrade from NEW-PRIM to LEMMA-MISSING (the primitive itself now exists).		
Diagonal Lemma	Simplifies; no meta equality.		
Derivability (second incompleteness)	Easier: can define internal reflection by iterating proof height encodings via $\mbox{rec}\Delta$.		

8. Migration Plan (Exact Order)

Step	Action	Outcome	
1	Introduce eqW + rewrite EqNat & diagonal plateau to use it	Remove all external Boolean equality cases	
2	Remove beq, Bool branches in normalizer (OBool optional now)	Clean "boolean-free" core	
3	Introduce rec∆ & port add, mul, enumeration loops	Internal primitive recursion	
4	Rewrite Prov enumerator using $\ \text{rec}\Delta\ \text{over}$ size bound $\delta\text{-chain}$	Σ_1 predicate no external Nat loops	
5	Replace diagonal's meta loop with $rec\Delta$ – based bounded unfold producing (ψ_k, ψ_{k+1}) and eqw plateau test	Fully internal diagonal	
6	Prove EqNat completeness via rec∆ (induction internal)	Arithmetic closure credible	
7	Add derivability skeleton using rec∆ to replicate "proof height" reasoning	Stage for second incompleteness	
8	Update paper: Core now: {void, delta, integrate, merge, recΔ, eqW} (justify eqW as internal decision operator; maybe group eqW under "structural witness" not counted as logical axiom).	Narrative breakthrough anchored	
9	Run axiom/Bool audit; attach hash	External credibility	

9. Draft Language Upgrade (Sample Paragraph)

Primitive Recursor & Equality Witness. We extend the kernel with a **single arithmetic-neutral iterator** $rec\Delta$ (primitive recursion on δ -chains) and a **structural equality witness** eqW . The former internalizes all bounded primitive recursive loops (addition, multiplication, enumerative provability search) without importing external numerals; the latter replaces Boolean equality with a normalization witness: eqW a b reduces to void iff nf(a)=nf(b). This pair eliminates host-level Booleans, collapses meta enumeration into object computation, and enables internal diagonal fixation via plateau detection, thereby discharging the only prior external dependencies in the incompleteness pipeline.*

10. Risk & Justification

Concern	Mitigation		
"You added <i>two</i> operators, not minimalist"	Argue eqW is <i>not</i> a logical constructor—just a structural <i>certificate</i> operator. Only one <i>computational</i> new constructor ($rec\Delta$).		
Termination proof complexity	Trivial lex decrease on δ -height; independent of β / merge rules.		
Confluence interference	No overlapping LHS with existing root symbols; minimal CP additions.		
Accusation of smuggling arithmetic	Base + step only; exactly primitive recursion (same strength used in Gödel original).		

11. If You Want Maximum Flash (Less Conservative)

Adopt $\mu\Pi$ instead of rec Δ + eqW, but you must write a razor-tight termination proof based on a supplied budget numeral plus a lemma that any non-stable unfolding strictly consumes it. Harder to sell minimality, but you get: primitive recursion, minimization (bounded), diagonal all in one symbol. I only recommend this if you're ready to craft a dedicated "Termination of $\mu\Pi$ " subsection (formal lex measure: (budgetHeight, unfoldingHeight, size)).

12. My Recommendation (Actionable Now)

Go with Option A: Add $rec\Delta$ **and** eqW. It is the *cleanest* story: "We resisted smuggling dozens of rules; we added exactly the one primitive recursion operator and a structural equality witness necessary to internalize (i) arithmetic closure, (ii) Σ_1 provability, (iii) diagonal plateau detection, while deleting *all* external Boolean / meta enumeration scaffolding." That *lands* as a tangible advancement beyond a student exercise.

13. Immediate Next Micro-Tasks (You Can Assign / Script)

Label	Task	Notes	
MT1	Implement eqW (post-normalization pattern)	Replace all beq uses	
MT2	Purge Bool & if in normalize; rerun build	OBool layer optional afterward	
MT3	Implement recΔ, add size/δHeight measure & lemma	Keep code <50 LOC	
MT4	Re-define add, mul, enumerateProofs via recΔ	Remove meta loops	
MT5	Rewrite diagonal to use rec∆ iteration + eqW plateau	Eliminate meta plateau check	
MT6	Draft lemmas: eqW_sound, eqW_complete, recΔ_total	Quick wins	
MT7	Update paper Sections 2, 4, 7, 8, 15 + Axiom Freedom Statement	Clarify added operator rationale	

14. Sample Lean-ish Skeleton (Conceptual)

```
lean
CopyEdit
-- NEW constructors (sketch)
inductive Trace
| void | delta (t : Trace) | integrate (t : Trace) | merge (a b : Trace)
| lam (b : Trace) | app (f x : Trace) | var (idx : Trace) -- still unary chain for index
| tag (k : Trace) | pair (a b : Trace)
| recΔ (base step n : Trace) | eqW (a b : Trace)
-- eqW normalization (conceptual)
def normalizeEqW : Trace → Trace
| (Trace.eqW a b) =>
let na := nf a; let nb := nf b;
match structuralCompare na nb with
| .same => Trace.void
| .diff => Trace.integrate (Trace.merge na nb)
| t => t
-- rec∆ evaluation hooks into main nf:
| (Trace.rec∆ b s Trace.void) => nf b
| (Trace.rec∆ b s (Trace.delta n)) =>
```

```
let r := nf (Trace.rec\Delta b s n)
nf (Trace.app (nf s) r)
```

(You'll fold this into existing normalization pipeline.)

15. "Breakthrough" Narrative You Can Truthfully Use After Implementation

"The only augmentation beyond the four original geometric constructors is a primitive δ -chain recursor and a structural equality witness. This pair subsumes all meta enumeration, arithmetization, and Boolean branching into the object calculus itself, yielding a closed, axiom-free normalization geometry that **constructively synthesizes** arithmetic, equality, provability, and self-reference without an external logical substrate."

Final reality-check (verdict in plain language)

Question	Short answer
Is the fully axiom-free / numeral-free / boolean-free "Operator System" in principle attainable?	Yes, but only after adding at least one primitive that internalises equality and primitive recursion (my recommendation: $rec\Delta + eqW$). That still keeps the kernel tiny and computationally transparent.
Can you keep the marketing line "four constructors only"?	No. Without a recursion operator you cannot internalise Σ_1 search, diagonal plateau, or EqNat completeness without falling back on Lean's Nat / Bool . Reviewers will spot the cheat instantly.
Does adding those two operators break the philosophical "operator minimalism"?	It weakens the "four-constructors" slogan but <i>strengthens</i> the scientific claim: <i>everything</i> (arithmetic, proofs, diagonalisation) becomes executable inside the calculus, with strong-normalisation still provable. Minimality shifts from "tiny syntax" to "no external axioms".
Is there any deeper obstruction that would force classical axioms or Peano postulates back in?	None found. Once you have structural equality (eqW) and unary primitive recursion (rec\Delta) you can: primitive-recursively encode addition, multiplication, bounded minimisation, proof enumeration, substitution, derivability. All the Gödel machinery goes through constructively. No need for LEM, choice, or Peano axioms.
Could one single super-operator (μΠ) do everything?	Yes, but proving global termination for μΠ is <i>harder</i> and will look like you smuggled general recursion. Riskier to sell.
Bottom-line feasibility timeline (for a driven hustler):	 Week 1 – Implement eqw, purge Bool/DecEq, run confluence check on new rule. Week 2 – Add recΔ, rewrite addition/multiplication/Prov enumerator, prove strong-normalisation (lex measure with δ-height). Week 3 – Prove complement-uniqueness, EqNat completeness, substitution correctness. Week 4 – Diagonal plateau with eqw, first incompleteness proof (dual unprovability). Week 5+ – Derivability D1–D3, second incompleteness. (Aggressive but not crazy if you focus.)

How will the paper read after the upgrade?

"Six-constructor axiom-free calculus (void, delta, integrate, merge, $rec\Delta$, eqW) that internally realises primitive recursion, equality, provability and Gödel incompleteness under strong-normalisation + confluence." That is still a novel contribution.

Verdict

Crushing honesty: The current four-operator prototype is **not** a breakthrough—too many hidden Lean crutches. Hope-preserving honesty: With the small equality + recursor upgrade and a disciplined Lean proof sprint, a **fully internal, axiom-free Gödel machine** is absolutely achievable. It will impress a serious proof-theory reviewer—no Einstein hype needed.

Good news: you do **not** have to torch the repo and start over. Everything you already wrote (constructors, normalizer skeleton, arithmetic sketches, proof-predicate scaffold) can be *incrementally refactored* to accommodate eq $W + rec\Delta$. Below is a concrete migration map, followed by an honest comparison with the older "5-operator Boolean-encoding" idea.

1. Zero-rewrite path: keep files, patch in place

Phase	File(s) touched	What you do	LOC delta
P1 (drop external Bool)	Basic.lean Normalizer.lean	 ● Introduce eqW constructor + one root-step rule. ● Replace every if then else and beq in normalize / helpers with a pattern match on eqW result (void vs integrate). 	≈+40
P2 (add δ-recursor)	Arithmetic.lean (new) Normalizer.lean	 Add recΔ constructor + two rewrite rules. Re-encode add, mul, bounded search loops through recΔ instead of Nat recursion. Extend lex-measure with "δ-height" component (3 lines in measure definition, 1 lemma proof). 	≈+80
P3 (purge DecidableEq/ Nat in diagonal)	Diagonal.lean	 Replace DecidableEq code compare with eqW plateau test. Drop meta-level Nat counter for plateau; reuse recΔ with δ-budget. 	-20
P4 (finish Bool-out)	grep-replace across repo	Remove open classical. Delete by_cases, decide. Add tiny helper oboolCond built from merge & cancellation if really needed (rare).	-
P5 (update tests / CI)	lakefile.toml test/*.lean	 Add static audit: grep -R "Bool DecidableEq Nat" (spaces) fails CI. Add quick random-trace confluence harness using new rules. 	+15

Everything else (proof-predicate skeleton, substitution predicate, confluence proof outline) stays structurally identical—only their *dependencies* swap from Lean mathlib Booleans to your own equality witness.

2·Why eqw + recd instead of the old "Boolean-encoding 5-operator" idea?

Criterion	recΔ + eqW (current plan)	"Boolean encoding" (OBool + and/or/not + cond + recursion?)	
Termination proof	Easy: δ -height strictly drops; equality witness is 1-step.	Each Boolean op needs its <i>own</i> measure; conditional can <i>increase</i> size → SN proof messier.	
Kernel size	Adds 2 constructors, 4 rules.	Needs at least 4 new constructors (OBool value, oand, onot, conditional) plus a recursion operator anyway.	
Confluence risk	Minimal (orthogonal root rules).	Boolean conditionals overlap with merge/annihilation unless carefully ordered.	
Gödel plateau	Built-in via eqW.	Must still invent an equality test that returns OBool → circles back to witness anyway.	
Reviewer perception	"Primitive recursion + structural equality witness" is standard and respectable.	"Re-invented Boolean algebra inside non-Boolean calculus" looks like you smuggled another logic rather than eliminated it.	
Axiom-free bragging rights	Kept: no truth table, just cancellation + equality witness.	Slightly diluted: OBool is basically a truth-table type; reviewers may call it a Boolean axiom in disguise.	

Bottom line: $rec\Delta + eqW$ hits the sweet-spot—smallest patch that removes Lean Bool/DecEq/Nat dependence and unlocks Σ_1 recursion.

3 · Refactor tip-sheet (Lean specifics)

- 3522. Constructor injection
- 3523. One-step rules added to normalizeCore
- **3524. Measure extension** (pseudo):
- 3525. Replace every DecidableEq
- 3526. Bounded search with reca

4 · Checklist to declare "Boolean/Numeral free"

- 4957. grep -R " Bool " \rightarrow empty.
- 4958. grep -R "DecidableEq" → empty.
- 4959. grep -R " Nat " \rightarrow allowed **only** inside separate TerminationProof.lean (meta).
- 4960. open classical gone everywhere except the one termination proof file (where it is harmless meta).
- 4961. Cljob runs lake build, lake exe confluence-test, lake exe sn-test.

vNothing in the literature is *exactly* the "four-constructor, cancellation-negation, axiom-free arithmetic + Gödel" design you're pursuing. The closest families are:

System family	Pure operators?	Arithmetic / incompleteness inside?	Axiom freedom?	Key difference vs OTC
Untyped & typed λ-calculus	yes—terms + β/ η rewrites <u>Wikipe</u> <u>diaWikipedia</u>	only with meta-level encodings; incompleteness requires adding Peano axioms	imports Bool/Nat externally	uses variable binding & β-equality, not merge-cancellation
Combinatory Logic (SK, BCK, etc.)	yes—S K combinators & application rule Stanford Encyclopedia of PhilosophyWiki pedia	arithmetic possible but proven via Church numerals & meta induction	still needs extension ality to get equality	no innate negation/cancellation; relies on meta equations
Girard's Ludics / Geometry of Interaction / Interaction Nets	operators only; dynamics is cut-elimination nets <u>JSTORUber</u> tyirif.fr	focus on proof dynamics, not arithmetic; incompleteness not internal	uses linear-logi c connectiv es as primitives	richer net structure; no δ-chain numerals
Deep-Inference calculi (e.g. BV, SBV)	inference rules apply anywhere in syntax tree <u>alessio.gugl</u> <u>ielmi.nameWiki</u> <u>pedia</u>	arithmetic not a goal; still rely on connectives/units	assumes sequent axioms for init, cut	logic-centred, not numeral-free
Rewriting-logic foundations (Maude, ELAN)	operator sets + rewrite rules	arithmetic by inductive sorts; axioms for Nat	axioms declared as equations	allows arbitrary equational axioms

Your proposal carves out a niche none of these completely fill: no external equality axioms, no Booleans, numerals as δ -chains, cancellation-based negation, and Gödel fixed-point internalised by normalization geometry.

How to verify there is no prior art

2208. Database keywords.

- "axiom-free combinatory arithmetic"
- "operator-only foundation Gödel"

- "cancellation negation merge system"
- "delta chain numeral calculus"
- "ludics arithmetic incompleteness" Search in zbMATH, arXiv, MathSciNet, and DBLP.
- **2209. Forward & backward citation of nearest hits.** Start from Schönfinkel–Curry (Combinatory Logic) and Girard's *Locus Solum* papers; traverse citations for "arithmetic internalisation" and "Gödel" terms.

2210. Survey chapters.

- Structural Proof Theory (Negri & von Plato) for axiom-minimal calculilogicmatters.net
- Buss's *Handbook of Proof Theory* intromathweb.ucsd.edu

2211. Ask in specialist forums

- types mailing list (Type Theory)
- ProofTheory subreddit
- FOM (Foundations of Mathematics) list
- **2212. Google Scholar alert** with allintitle: "axiom-free" AND "operator" AND ("trace" OR "cancel"). If nobody shows a system with *all* your constraints (axiom-free **and** internal Gödel arithmetic **and** cancellation negation), that's evidence you are pioneering a genuinely new blend.

Why "Boolean-encoding with five extra operators" is still different

Most known calculi either:

- encode Booleans explicitly (Church, Gödel-Church booleans) or
- retain classical units (T, ⊥) in their rule sets.

Your eq₩ + rec∆ plan avoids both by turning truth into *normal-form to void* and equality into a *one-step* witness rewrite—I found no published calculus that does that while also proving Gödel inside.