# Lecture 9

Collective communications

#### Introduction

Collective communication involves all the processes in a communicator We will consider:

Broadcast

Reduce

Gather

Scatter

Reason for use: convenience and speed

#### Broadcast\*

Broadcast: a single process sends data to all processes in a communicator

```
int MPI_Bcast (void *buffer , int count, MPI_Datatype datatype,
    int root, MPI_Comm comm)
```

buffer - starting address of buffer (in/out)
count - number of entries in buffer

datatype - data type of buffer

root - rank of broadcast root

comm - communicator



MPI\_Bcast sends a copy of the message on process with rank root to each process in comm .

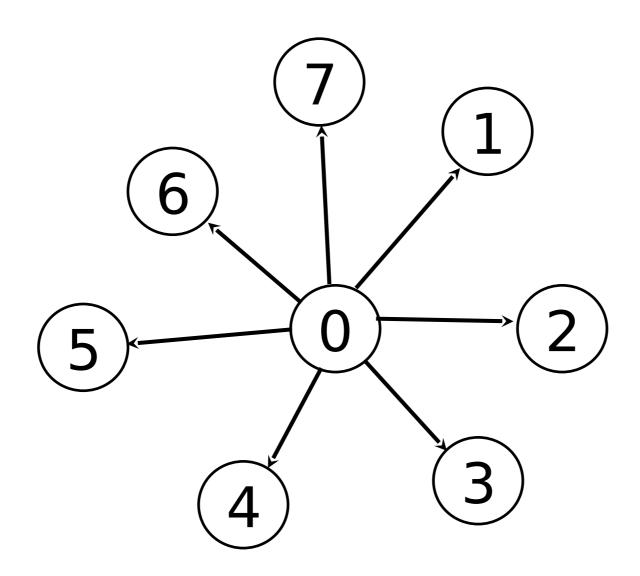
Must be called in each process.

Data is sent in *root* and received by all other processes.

Buffer is 'in' parameter in *root* and 'out' parameter in the rest of processes.

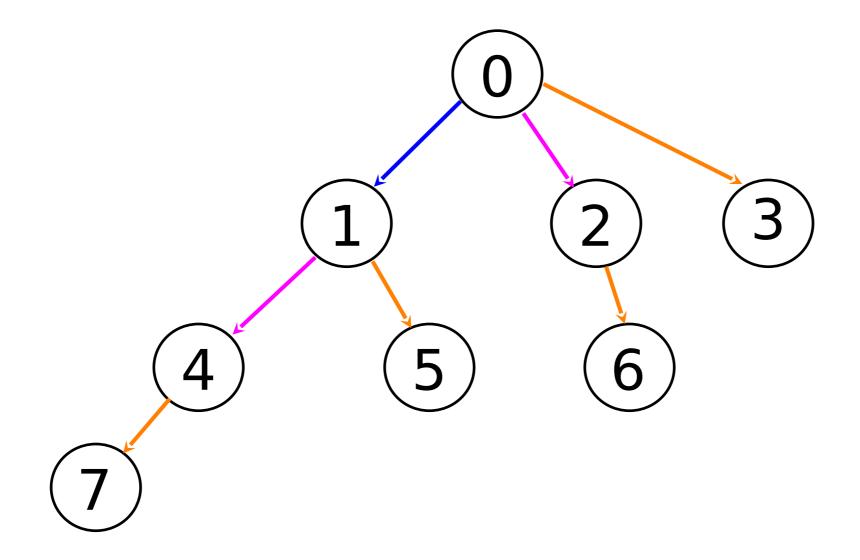
Cannot receive broadcasted data with MPI\_Recv .

## Broadcast - poor implementation



Not parallel, 7 time steps needed

Broadcast - actual, parallel implementation



3 time steps needed

## Example: reading and broadcasting data

Code adapted from P. Pacheco, PP with MPI

```
/* getdata2.c */
/* Function Get data2
* Reads in the user input a, b, and n.
* Input parameters:

    int my_rank: rank of current process.

      2. int p: number of processes.
 * Output parameters:

    float* a_ptr: pointer to left endpoint a.

      2. float* b_ptr: pointer to right endpoint b.
       3. int* n ptr: pointer to number of trapezoids.
  Algorithm:
       1. Process 0 prompts user for input and
          reads in the values.
       2. Process 0 sends input values to other
           processes using three calls to MPI Bcast.
*/
```

```
#include <stdio.h>
#include "mpi.h"
void Get_data2(float* a_ptr, float* b_ptr, int* n_ptr,
               int my rank)
  if (my_rank == 0)
      printf("Enter a, b, and n\n");
      scanf("%f %f %d", a_ptr, b_ptr, n_ptr);
    }
 MPI_Bcast(a_ptr, 1, MPI_FLOAT, 0, MPI_COMM_WORLD);
 MPI_Bcast(b_ptr, 1, MPI_FLOAT, 0, MPI_COMM_WORLD);
  MPI_Bcast(n_ptr, 1, MPI_INT, 0, MPI_COMM_WORLD);
```

#### Reduce

Data from all processes are combined using a binary operation

```
int MPI_Reduce ( void *sendbuf , void *recvbuf , int count ,
MPI_Datatype datatype , MPI_Op op ,int root, MPI_Comm comm)
```

sendbuf - address of send buffer

recvbuf - address of receive buffer, significant only at root

count - number of entries in send buffer

datatype - data type of elements in send buffer

op - reduce operation; predefined, e.g. MPI\_MIN, MPI\_SUM, or user
defined

root - rank of root process

comm - communicator

Must be called in all processes in a communicator, BUT result only available in root process.

## MPI Reduce operations

- MPI\_MAX Returns the maximum element.
- MPI\_MIN Returns the minimum element.
- MPI\_SUM Sums the elements.
- MPI\_PROD Multiplies all elements.
- MPI\_LAND Performs a logical "and" across the elements.
- MPI\_LOR Performs a logical "or" across the elements.
- MPI\_BAND Performs a bitwise "and" across the bits of the elements.
- MPI\_BOR Performs a bitwise "or" across the bits of the elements.
- MPI\_MAXLOC Returns the maximum value and the rank of the process that owns it.
- MPI\_MINLOC Returns the minimum value and the rank of the process that owns it.

# MPI datatypes for data-pairs used with the MPI\_MAXLOC and MPI\_MINLOC

- MPI\_2INT : pair of ints
- MPI\_SHORT\_INT : short and int
- MPI\_LONG\_INT : long and int
- MPI\_LONG\_DOUBLE\_INT : long double and int
- MPI\_FLOAT\_INT : float and int
- MPI\_DOUBLE\_INT : double and int

## MPI\_MINLOC example

```
int myrank, minrank;
float minval;
struct {
  float value;
  int rank;
} in, out;
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
in.value = A;
in.rank = myrank;
MPI_Reduce( in, out, 1, MPI_FLOAT_INT, MPI_MINLOC, root, comm );
/* At this point, the answer resides on process root */
if (myrank == root) {
/* read answer out */
  minval = out.value;
  minrank = out.rank;
```

## Example: trapezoid with reduce

```
Code adapted from P. Pacheco, PP with MPI
/* redtrap.c */
#include <stdio.h>
#include "mpi.h"
extern void Get_data2(float* a_ptr, float* b_ptr,
                     int* n_ptr, int my_rank);
extern float Trap(float local_a, float local_b,
                 int local n, float h);
int main(int argc, char** argv)
 int
     my_rank, p;
 float
             a, b, h;
 int
             n;
 float
             local_a, local_b, local_n;
 float
             integral; /* Integral over my interval */
 float
             total; /* Total integral
 MPI Init(&argc, &argv);
 MPI Comm_rank(MPI_COMM_WORLD, &my_rank);
 MPI Comm size(MPI COMM WORLD, &p);
              ~syam/ces745/mpi/collective
```

```
Get_data2(&a, &b, &n, my_rank);
h = (b-a)/n;
local_n = n/p;
local a = a + my rank*local n*h;
local b = local a + local n*h;
integral = Trap(local_a, local_b, local_n, h);
/* Add up the integrals calculated by each process */
MPI Reduce(&integral, &total, 1, MPI FLOAT,
           MPI SUM, 0, MPI COMM WORLD);
if (my rank == 0)
    printf("With n = %d trapezoids, our estimate\n", n);
    printf("of the integral from %f to %f = %f\n",
           a, b, total);
  }
MPI Finalize();
Return 0;
```

## Example: Dot Product

```
Adapted from P. Pacheco, PP with MPI
/* parallel_dot.c -- compute a dot product of vectors
   distributed among the processes.
 * Uses a block distribution of the vectors.
 * Input:
      n: global order of vectors
      x, y: the vectors
 * Output:
      the dot product of x and y.
 * Note: Arrays containing vectors are statically allocated.
 * Assumes n, the global order of the vectors, is divisible
 * by p, the number of processes.
 */
#include <stdio.h>
#include "mpi.h"
#define MAX LOCAL ORDER 100
void Read_vector(char* prompt, float local_v[], int n_bar,
                   int p,int my rank);
float Parallel_dot(float local_x[], float local_y[],
                     int n bar);
```

```
main(int argc, char* argv[])
 float local_x[MAX_LOCAL_ORDER];
 float local_y[MAX_LOCAL_ORDER];
  int n;
 int n bar; /* = n/p */
 float dot;
  int p, my_rank;
 MPI Init(&argc, &argv);
 MPI Comm size(MPI_COMM_WORLD, &p);
 MPI Comm rank(MPI_COMM_WORLD, &my_rank);
  if (my rank == 0)
      printf("Enter the order of the vectors\n");
      scanf("%d", &n);
    }
 MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
 n bar = n/p;
 Read vector("the first vector",
              local_x, n_bar, p, my_rank);
```

```
Read vector("the second vector",
           local_y, n_bar, p, my_rank);
 dot = Parallel dot(local x, local y, n bar);
 if (my rank == 0)
   printf("The dot product is %f\n", dot);
 MPI Finalize();
void Read vector(
             char* prompt /* in */,
             float local_v[] /* out */,
             int n_bar /* in */,
             int p /* in */,
             int my_rank /* in */)
 int i, q;
 float temp[MAX LOCAL ORDER];
 MPI_Status status;
```

```
if (my_rank == 0)
     printf("Enter %s\n", prompt);
     for (i = 0; i < n_bar; i++)
       scanf("%f", &local_v[i]);
     for (q = 1; q < p; q++)
         for (i = 0; i < n_bar; i++)
           scanf("%f", &temp[i]);
         MPI_Send(temp, n_bar, MPI_FLOAT, q, 0,
                  MPI COMM WORLD);
else
     MPI_Recv(local_v, n_bar, MPI_FLOAT, 0, 0,
              MPI COMM WORLD, &status);
 /* Read_vector */
```

```
float Serial dot(float x[],float y[],int n)
   int i;
   float sum = 0.0;
   for (i = 0; i < n; i++)
      sum = sum + x[i]*y[i];
   return sum;
} /* Serial dot */
float Parallel_dot(float local_x[],float local_y[],int n_bar)
 float local dot;
 float dot = 0.0;
 float Serial dot(float x[],float y[],int m);
 local_dot = Serial_dot(local_x,local_y,n_bar);
 MPI Reduce(&local_dot, &dot, 1, MPI_FLOAT,
         MPI SUM, 0, MPI COMM WORLD);
 return dot;
} /* Parallel_dot */
```

#### Allreduce

```
int MPI_Allreduce (void *sendbuf , void *recvbuf , int count ,
MPI_Datatype datatype , MPI_Op op, MPI_Comm comm)
```

Similar to MPI Reduce except the result is returned to the receive buffer *recvbuf* of each process in *comm* 

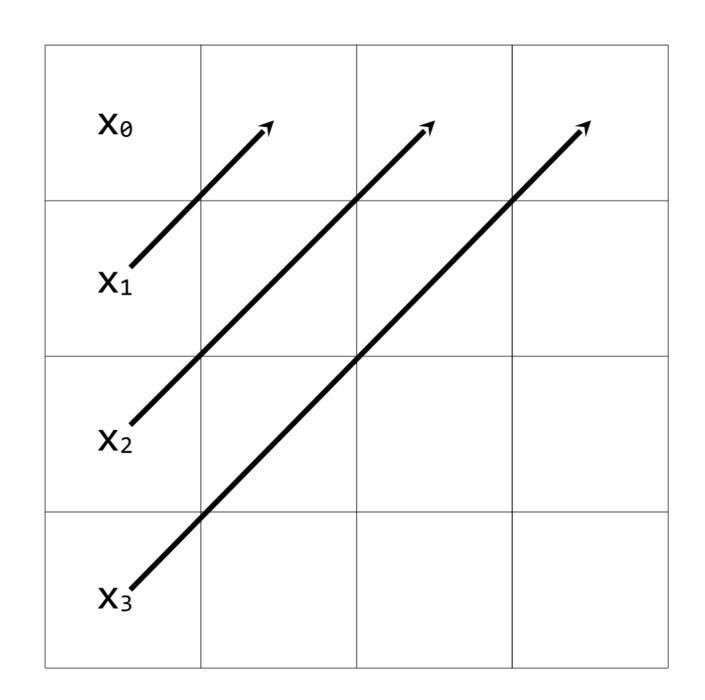
## Gather

Process 0

Process 1

Process 2

Process 3



#### Gather

int MPI\_Gather (void \*sendbuf, int sendcount, MPI\_Datatype sendtype,

Gathers together data from a group of processes.

comm - communicator

```
void *recvbuf, int recvcount, MPI Datatype recvtype, int root,
MPI Comm comm )
sendbuf - starting address of send buffer
sendcount - number of elements in send buffer
sendtype - data type of send buffer elements
recvbuf - address of receive buffer (significant only at root)
recvcount - number of elements for any single receive (significant only
at root)
recvtype - data type of recv buffer elements (significant only at root)
root - root rank of receiving process
```

MPI\_Gather collects data, stored at *sendbuf*, from each process in *comm* and stores the data on *root* at *recvbuf* .

Data is received from processes in order, i.e. from process 0, then from process 1 and so on.

Usually sendcount, sendtype are the same as recvcount, recvtype.

root and comm must be the same on all processes.

The receive parameters are significant only on root .

Amount of data sent/received must be the same.

If gathered data needs to be available to all processes, use:

```
int MPI_Allgather ( void *sendbuf , int sendcount , MPI_Datatype
sendtype, void *recvbuf , int recvcount , MPI_Datatype recvtype ,
MPI_Comm comm )
```

The block of data sent from the jth process is received by every process and placed in the jth block of the buffer recvbuf.

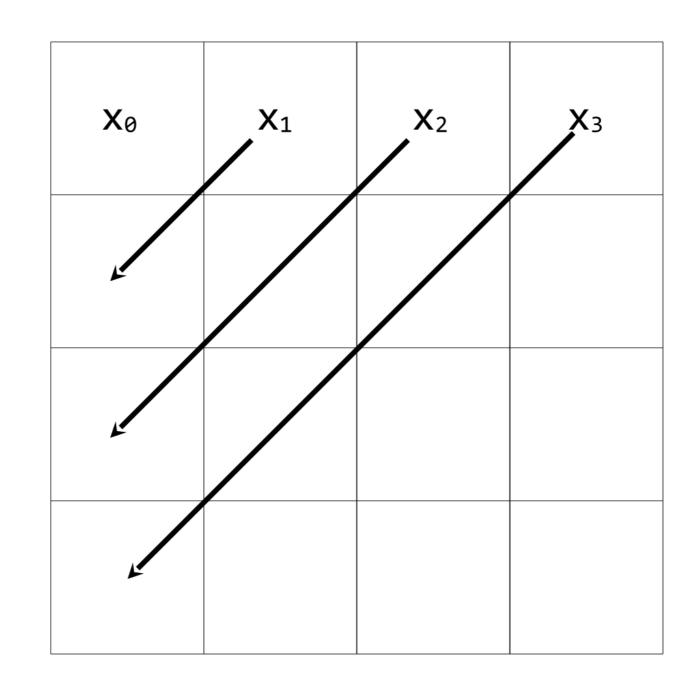
## Scatter

Process 0

Process 1

Process 2

Process 3



#### Scatter

Sends data from one process to all other processes in a communicator.

```
int MPI_Scatter ( void *sendbuf , int sendcount, MPI_Datatype
sendtype, void *recvbuf, int recvcount, MPI_Datatype recvtype,
int root , MPI_Comm comm )
sendbuf - starting address of send buffer (significant only at root)
sendcount - number of elements sent to each process (significant only
at root )
sendtype - data type of send buffer elements (significant only at root)
recvbuf - address of receive buffer
recvcount - number of elements for any single receive
recvtype - data type of recv buffer elements
root - rank of sending process
comm - communicator
```

MPI\_Scatter splits data at *sendbuf* on *root* into p segments, each of *sendcount* elements, and sends these segments to processes 0, 1, ..., p-1 in order.

Inverse operation to MPI\_Gather .

The outcome is as if the root executed n send operations,

and each process executed a receive,

```
MPI_Recv (recvbuf, recvcount, recvtype, i, ...).
```

Amount of data send must be equal to amount of data received.

#### Parallel Matrix Multiplication

Ax=y - data distributed on 4 processes

	A		X		У
Process 0					
Process 1		*			
Process 2		T		=	
Process 3					

## Example: parallel matrix times vector

Code adapted from P. Pacheco, PP with MPI

```
/* parallel_mat_vect.c -- computes a parallel
* matrix-vector product.
* Matrix is distributed by block rows.
 * Vectors are distributed by blocks.
*
  Input:
      m, n: order of matrix
      A, x: the matrix and the vector to be multiplied
 *
  Output:
       y: the product vector
 *
  Notes:
       1. Local storage for A, x, and y
           is statically allocated.
          Number of processes (p) should evenly
           divide both m and n.
 */
             ~syam/ces745/mpi/collective/parallel mat vect.c
```

```
#include <stdio.h>
#include "mpi.h"
#include "matvec.h"
int main(int argc, char* argv[])
        my rank, p;
 int
 LOCAL_MATRIX_T local_A;
       global_x[MAX_ORDER];
 float
 float
                local x[MAX ORDER];
 float
                 local y[MAX ORDER];
 int
                 m, n;
 int
                 local_m, local_n;
 MPI Init(&argc, &argv);
 MPI Comm size(MPI_COMM_WORLD, &p);
 MPI Comm rank(MPI COMM WORLD, &my rank);
 if (my rank == 0)
     printf("Enter the order of the matrix (m x n)\n");
     scanf("%d %d", &m, &n);
   }
 MPI_Bcast(&m, 1, MPI_INT, 0, MPI_COMM_WORLD);
 MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
```

```
local m = m/p;
local n = n/p;
Read matrix("Enter the matrix",
            local_A, local_m, n, my_rank, p);
Print matrix("We read",
             local_A, local_m, n, my_rank, p);
Read vector("Enter the vector",
            local x, local n, my rank, p);
Print vector("We read",
             local_x, local_n, my_rank, p);
Parallel_matrix_vector_prod(local_A, m, n, local_x,
                            global_x, local_y, local_m,
                             local n);
Print_vector("The product is", local_y, local_m,
             my_rank, p);
MPI_Finalize();
return 0;
```

```
/* matvec.h */
#define MAX_ORDER 100
typedef float LOCAL MATRIX T[MAX ORDER][MAX ORDER];
void Read matrix(char* prompt, LOCAL MATRIX T local A,
                 int local m, int n, int my rank, int p);
void Read vector(char* prompt, float local_x[],
                 int local n, int my rank, int p);
void Parallel matrix vector_prod(LOCAL_MATRIX_T local_A,
                                 int m, int n, float local x[],
                                 float global x[],
                                 float local_y[],
                                 int local m, int local n);
void Print_matrix(char* title, LOCAL_MATRIX_T local_A,
                  int local_m, int n, int my_rank, int p);
void Print_vector(char* title, float local_y[],
                  int local_m, int my_rank, int p);
```

```
/* parmatvec.c */
#include "mpi.h"
#include "matvec.h"
void Parallel_matrix_vector_prod(
  LOCAL MATRIX T local A, int m, int n,
  float local x[], float global x[], float local y[],
  int local m, int local n)
 /* local_m = m/p, local_n = n/p */
  int i, j;
 MPI_Allgather(local_x, local_n, MPI_FLOAT,
                global x, local n, MPI FLOAT,
                MPI COMM WORLD);
  for (i = 0; i < local_m; i++)
      local y[i] = 0.0;
      for (j = 0; j < n; j++)
        local_y[i] = local_y[i] +
          local A[i][j]*global x[j];
```

```
/* readvec.c */
#include <stdio.h>
#include "mpi.h"
#include "matvec.h"
void Read_vector(char *prompt, float local_x[], int local_n,
                 int my rank, int p)
  int i;
  float temp[MAX_ORDER];
  if (my_rank == 0)
      printf("%s\n", prompt);
      for (i = 0; i < p*local_n; i++)
        scanf("%f", &temp[i]);
    }
  MPI_Scatter(temp, local_n, MPI_FLOAT,
              local_x, local_n, MPI_FLOAT,
              0, MPI COMM WORLD);
```

```
/* readmat.c */
#include <stdio.h>
#include "mpi.h"
#include "matvec.h"
void Read matrix(char *prompt, LOCAL MATRIX T local A,
                 int local_m, int n, int my_rank,int p)
  int i, j;
  LOCAL_MATRIX_T temp;
  /* Fill dummy entries in temp with zeroes */
  for (i = 0; i < p*local m; i++)
    for (j = n; j < MAX_ORDER; j++)
      temp[i][j] = 0.0;
  if (my_rank == 0)
      printf("%s\n", prompt);
      for (i = 0; i < p*local m; i++)
        for (j = 0; j < n; j++)
          scanf("%f",&temp[i][j]);
    }
    MPI_Scatter(temp, local_m*MAX_ORDER, MPI_FLOAT,
              local A, local m*MAX ORDER, MPI FLOAT,
              0, MPI COMM WORLD);}
```

```
/* printvec.c */
#include <stdio.h>
#include "mpi.h"
#include "matvec.h"
void Print_vector(char *title, float local_y[] ,
                  int local_m, int my_rank,
                  int p)
  int
  float temp[MAX_ORDER];
 MPI_Gather(local_y, local_m, MPI_FLOAT,
             temp, local_m, MPI_FLOAT,
             0, MPI COMM WORLD);
  if (my rank == 0)
      printf("%s\n", title);
      for (i = 0; i < p*local_m; i++)
        printf("%4.1f ", temp[i]);
      printf("\n");
```

```
/* printmat.c */
#include <stdio.h>
#include "mpi.h"
#include "matvec.h"
void Print matrix(char *title, LOCAL MATRIX T local A,
                  int local_m, int n, int my_rank, int p)
  int i, j;
  float temp[MAX_ORDER][MAX_ORDER];
  MPI_Gather(local_A, local_m*MAX_ORDER, MPI_FLOAT,
             temp, local m*MAX ORDER, MPI FLOAT,
             0, MPI COMM WORLD);
  if (my rank == 0)
    printf("%s\n", title);
    for (i = 0; i < p*local_m; i++)
        for (j = 0; j < n; j++)
          printf("%4.1f ", temp[i][j]);
        printf("\n");
```

#### Some details

Amount of data sent must match amount of data received .

Blocking versions only.

No tags: calls are matched according to order of execution.

A collective function can return as soon as its participation is complete.



#### Outline

- Communicators, groups, contexts
- When to create communicators
- Some group and communicator operations
- Examples

## Communicators, groups, contexts

Processes can be collected into groups.

A group is an ordered set of processes.

- Each process has a unique rank in the group.
- Ranks are from 0 to  $p\,-\,1$ , where p is the number of processes in the group.

A communicator consists of a:

- group
- context, a system-defined object that uniquely identifies a communicator

Every communicator has a unique context and every context has a unique communicator.

Two distinct communicators will have different contexts, even if they have identical underlying groups.

Each message is sent in a context, and must be received in the same context.

## Communicators, groups, contexts. Cont.

A process is identified by its rank in the group associated with a communicator.

MPI\_COMM\_WORLD is a default communicator, whose group contains all initial processes.

A process can create and destroy groups at any time without reference to other processes—local to the process.

The group contained within a communicator is agreed across the processes at the time when the communicator is created.

Two types of communicators exist:

Intra-communicator is a collection of processes that can send messages to each other and engage in collective communications. This is the more important type, and this lecture will focus on those.

Inter-communicator are for sending messages between processes of disjoint intra-communicators. These are less important for most MPI programming tasks, so we will not be covering them.

#### When to create a new communicator?

To achieve modularity; e.g. a library can exchange messages in one context, while an application can work within another context. (Use of tags is not sufficient, as we need to know the tags in other modules.)

To restrict a collective communication to a subset of processes.

To create a virtual topology that fits the communication pattern better.

# Some group and communicator operations

int MPI\_Comm\_group (MPI\_Comm comm, MPI\_Group \*group)

Returns a handle to the group associated with comm .

Obtain group for existing communicator: MPI\_Comm -> MPI\_Group .

## MPI\_Group\_incl

Creates a new group from a list of processes in old group (a subset).

E.g., can be used to reorder the elements of a group.

The number of processes in the new group is n .

The processes to be included are listed at ranks .

Process i in new\_group has rank rank[i] in group.

#### MPI\_Comm\_create

Associates a context with new group and creates new\_comm .

All the processes in new\_group belong to the group of the underlying
comm .

This is a collective operation.

All process in comm must call MPI\_Comm\_create, so all processes choose a single context for the new communicator.

#### Example

```
Code from N. Nedialkov
                             ~syam/ces745/mpi/communicators/comm.c
/* comm.c */
#include <stdio.h>
#include <stdlib.h>
#include "mpi.h"
#define NPROCS 8
int main(int argc, char *argv[])
  int rank, new_rank,
    sendbuf, recvbuf,
    Numtasks;
  int ranks1[4]=\{0,1,2,3\};
  int ranks2[4]={4,5,6,7};
  MPI Group orig group, new group;
  MPI Comm
           new comm;
  MPI_Init(&argc,&argv);
  MPI_Comm_rank(MPI_COMM_WORLD, &rank);
  MPI Comm size(MPI_COMM_WORLD, &numtasks);
```

```
if (numtasks != NPROCS && rank==0)
    printf("Must specify MP PROCS = %d. Terminating.\n",
           NPROCS);
   MPI_Finalize();
    Exit(0);
/* store the global rank in sendbuf */
sendbuf = rank;
/* Extract the original group handle */
MPI Comm group(MPI COMM WORLD, &orig group);
/* Divide tasks into two distinct groups based upon rank */
if (rank < numtasks/2)</pre>
  /* if rank = 0,1,2,3, put original processes 0,1,2,3
      into new group */
 MPI_Group_incl(orig_group, 4, ranks1, &new_group);
else
  /* if rank = 4,5,6,7, put original processes 4,5,6,7
     into new group */
 MPI Group incl(orig group, 4, ranks2, &new group);
```

```
/* Create new communicator and then perform collective
communications */
 MPI Comm create(MPI COMM WORLD, new group, &new comm);
 /* new_comm contains a group with processes 0,1,2,3
     on processes 0,1,2,3 */
 /* new_comm contains a group with processes 4,5,6,7
     on processes 4,5,6,7 */
 MPI Allreduce(&sendbuf, &recvbuf, 1, MPI INT,
                MPI SUM, new comm);
 /* new_rank is the rank of my process in the new group */
 MPI Group rank (new group, &new rank);
 printf("rank= %d newrank= %d recvbuf= %d\n",
         rank, new rank, recvbuf);
 MPI Finalize();
 return 0;
```

## MPI\_Comm\_split

Partitions the group associated with *comm* into disjoint subgroups, one for each value of *color*.

Each subgroup contains all processes marked with the same color.

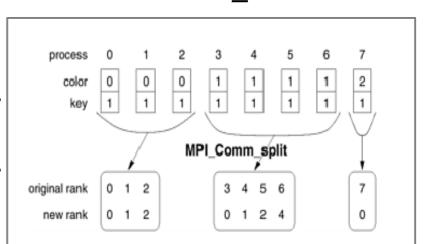
Within each subgroup, processes are ranked in order defined by the value of key.

Ties are broken according to their rank in the old group.

A new communicator is created for each subgroup and returned in comm out.

Although a collective operation, each process is allowed to provide different values for color and key.

The value of color must be greater than or equal to 0.



N=q\*q processes arranged on a q by q grid (q=3 in this example)

Row 0	0	1	2
Row 1	3	4	5
Row 2	6	7	8

Need to define communicator for each row of processes i.e. processes  $\{0,1,2\}$ ,  $\{3,4,5\}$  and  $\{6,7,8\}$ , for easy communication between them.

MPI\_Comm\_split provides an easy way to do this, more convenient than using MPI\_Group\_incl and MPI\_Comm\_create .

#### Example

```
Code from P. Pacheco, PP with MPI
/* comm_split.c -- build a collection of q
   communicators using MPI Comm split
 * Input: none
 * Output: Results of doing a broadcast across each of
            the q communicators.
 * Note: Assumes the number of processes, p = q^2
 */
#include <stdio.h>
#include "mpi.h"
#include <math.h>
int main(int argc, char* argv[])
  int
     p, my_rank;
 MPI_Comm my_row_comm;
 int
           my_row, my_rank_in_row;
  int q, test;
 MPI_Init(&argc, &argv);
                          ~syam/ces745/mpi/communicators/comm split.c
```

```
MPI_Comm_size (MPI_COMM_WORLD, &p);
MPI Comm rank (MPI COMM WORLD, &my rank);
q = (int) sqrt((double) p);
/* my_rank is rank in MPI_COMM_WORLD.
     q*q = p */
my row = my rank/q;
MPI_Comm_split (MPI_COMM_WORLD, my_row, my_rank,
                &my row comm);
/* Test the new communicators */
MPI Comm_rank (my_row_comm, &my_rank_in_row);
if (my_rank_in_row == 0) test = my row;
else test = 0;
MPI_Bcast (&test, 1, MPI_INT, 0, my_row_comm);
printf("Process %d > my row = %d,"
        "my_rank_in_row = %d, test = %d\n",
        my rank, my row, my rank in row, test);
MPI Finalize();
return 0;
```

## Implementation

Groups and communicators are opaque objects.

The details of their internal representation depend on the particular implementation, and so they cannot be directly accessed by the user.

To use these objects, the user accesses a handle that references the opaque object, and the opaque objects are manipulated by special MPI functions.