

# Emperical Fluid Dynamics & Dimensional Analysis

## (DA)

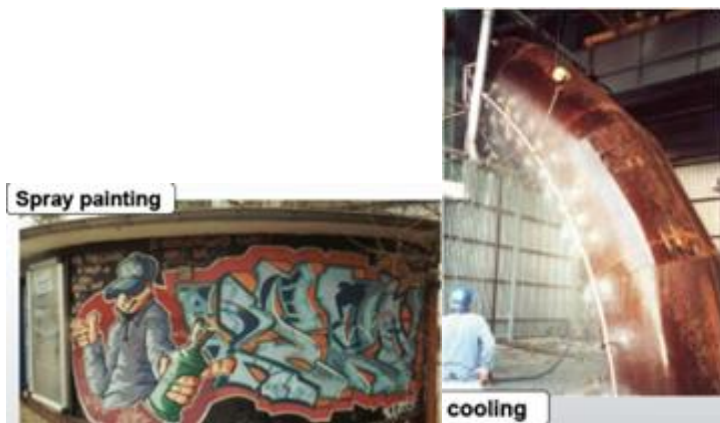
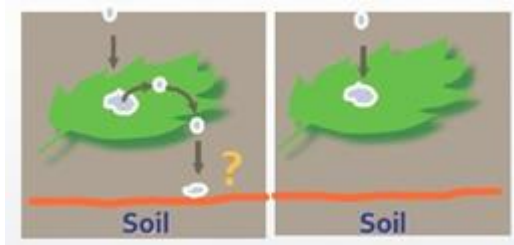
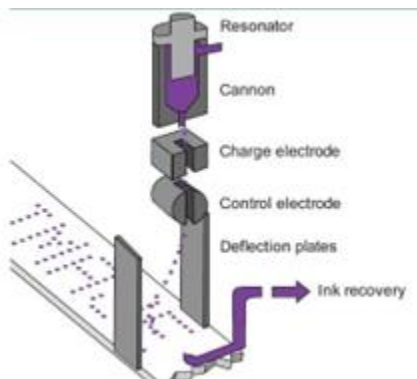
### Chapter 5 of F. White's Fluid Mech Book

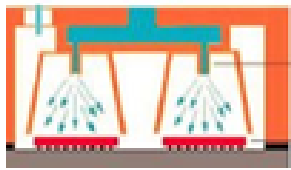
#### Learning Goals:

1. Introduction to empirical (experimental Fluids Dyn.)
2. Let's look at two experiments:
3. Drop impact onto a surface
4. Drop transfer between to surfaces
5. How to construct Dimensionless numbers
6. How to use Dimensionless numbers in:
7. Planning for experiments
8. Interpreting the data from experiments

Similarity of Flow in Fluids Dynamics and its application

## Why Study Drop Impact on Surfaces

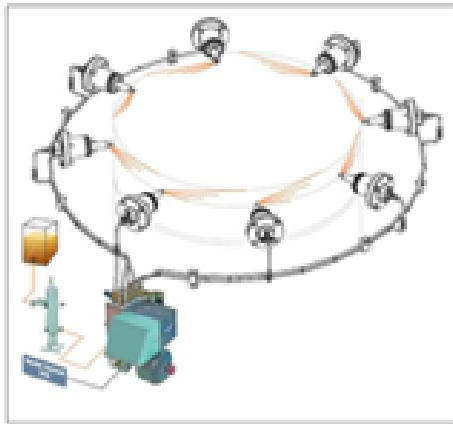




*chip cooling*



*steel*

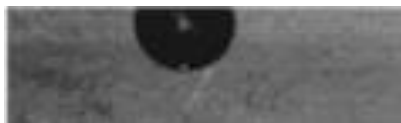


Lubrication of big ship engines



*direct injection engine*

A drop impacting a dry solid surface under normal atmospheric conditions!



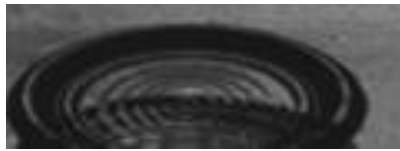
$T=0$



$T = 0.3 \text{ ms}$



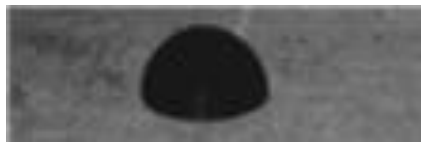
$T = 2.6 \text{ ms}$



T = 6.6 ms



T = 14.6 ms



T = 750 ms

## A drop on to solid dry isothermal surfaces



Deposition



Prompt splash



Corona splash



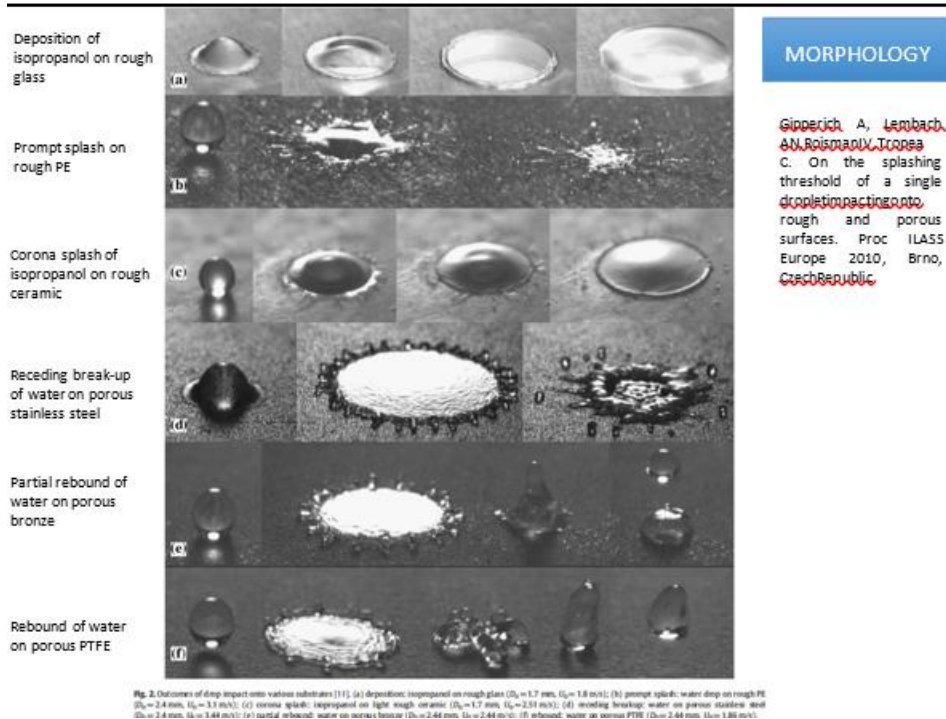
Receding break-up



Partial rebound

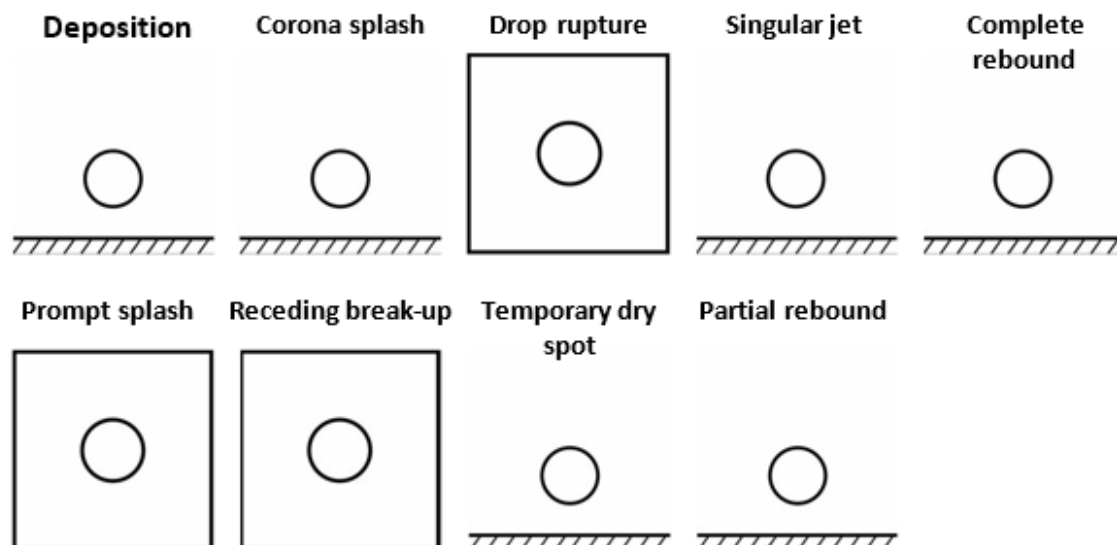


Rebound



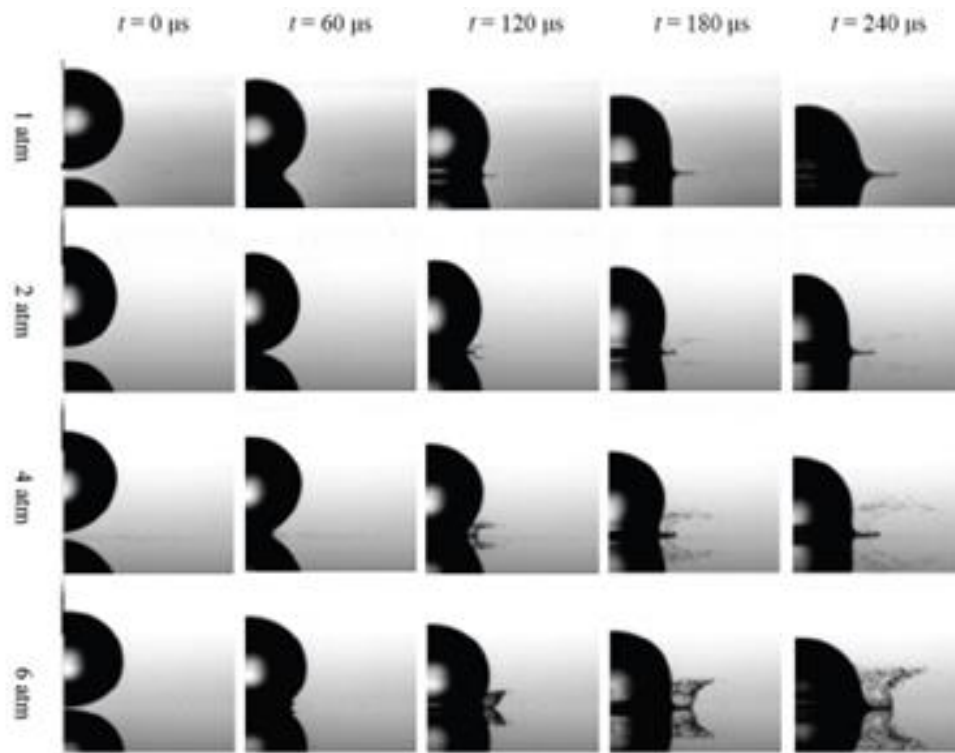
## Drop Impact Outcomes

**But wait!!!**

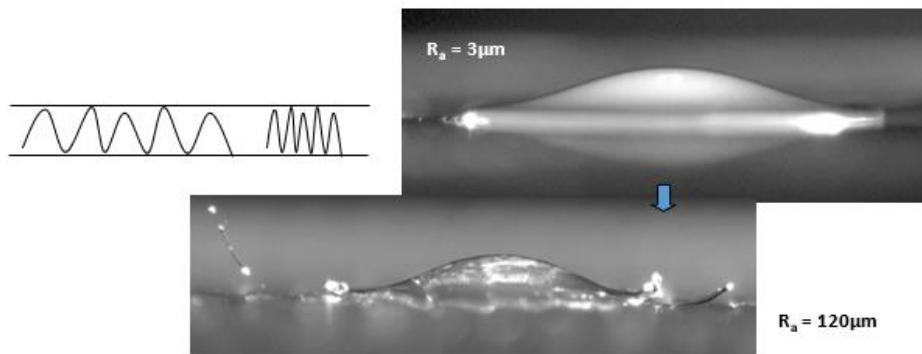


**9 outcomes..... >600 papers**

## Influence of Gas Pressure



## Surface roughness influence



Silicon oil ( $\mu=20$  cSt;  $\sigma=0.0206$  N/m);  $V_{\text{imp}}=3.16$  m/s;  $D=2.24$  mm

An increase of	Deposition	Prompt Splash	Receding Break-up	Complete Rebound	Corona Splash	Partial Rebound
$V$	↓	↑	↑		↑	↑
$D$	↓	↑				
$\sigma$		↓	↑	↑	↓	↑
$\mu$	↑	↓	↓		↓	
$R_d$	↓	↑			↓	
$R_w$		↓		↑		
$\theta_{\text{rec}}$			↑	↑		↑

(silicon oil)

Wettability influence on drop impact



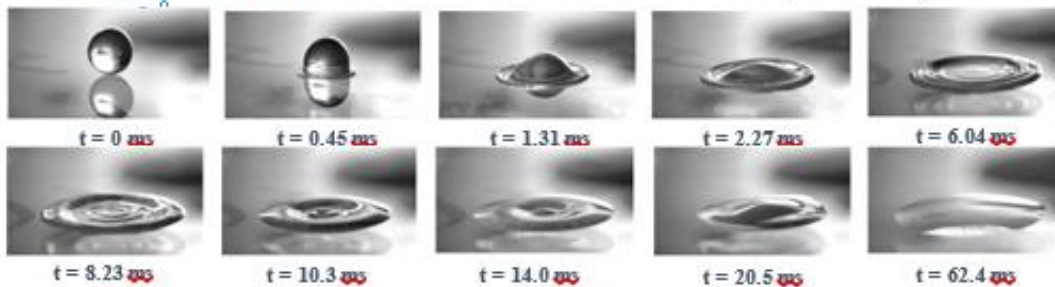
( $D = 2.75$  mm)

wax  
 $\theta$   
 $=95^\circ$

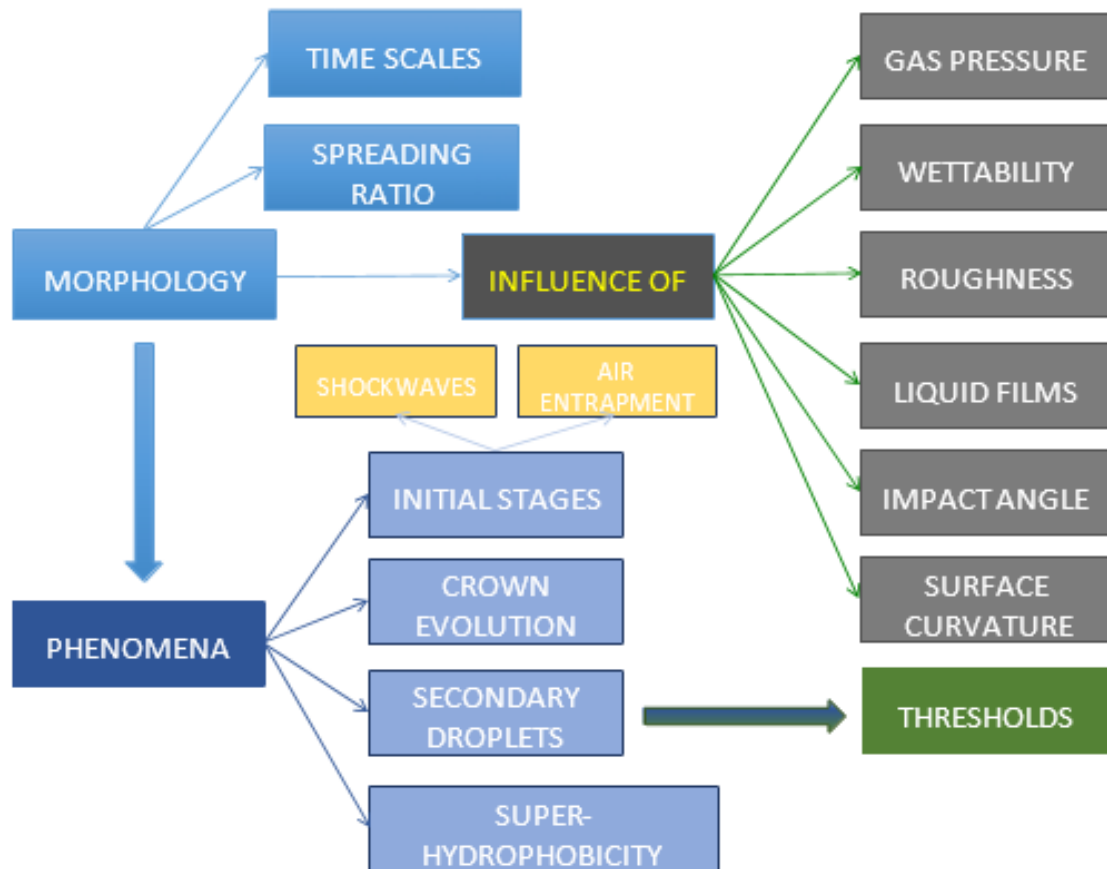
$V = 1.18$  m/s

Glass  $\theta_{\text{rec}}$

( $D = 3.04$  mm)

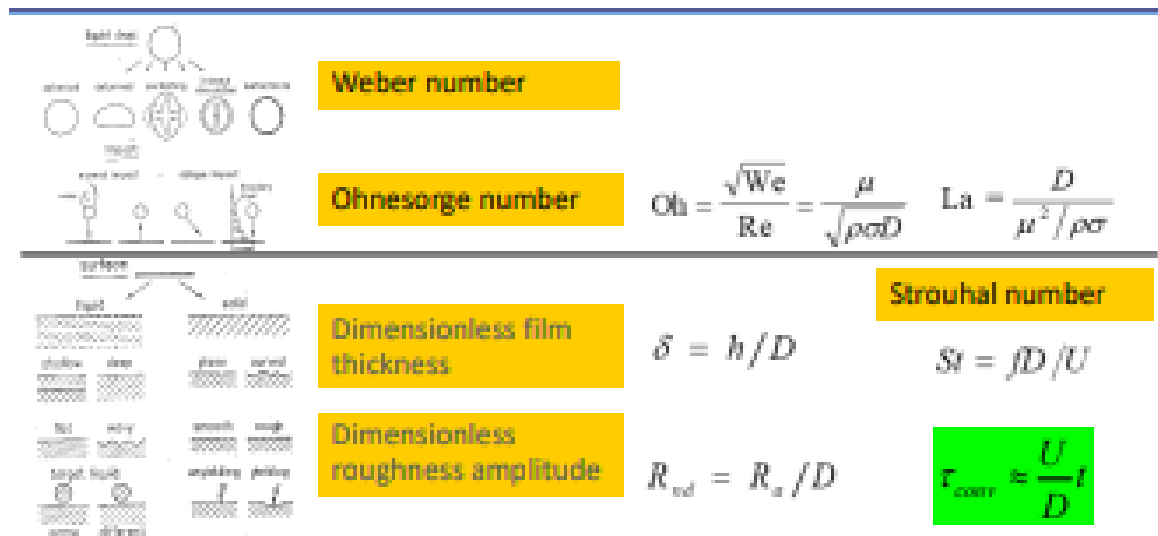


## Isothermal Impacts of Newtonian drops



## Drop Impact parameters: how to reduce them

$U, D, \rho, \sigma, \mu, g, P_{amb}, h, R_a, \lambda_R, \theta, E$  and time  $t$

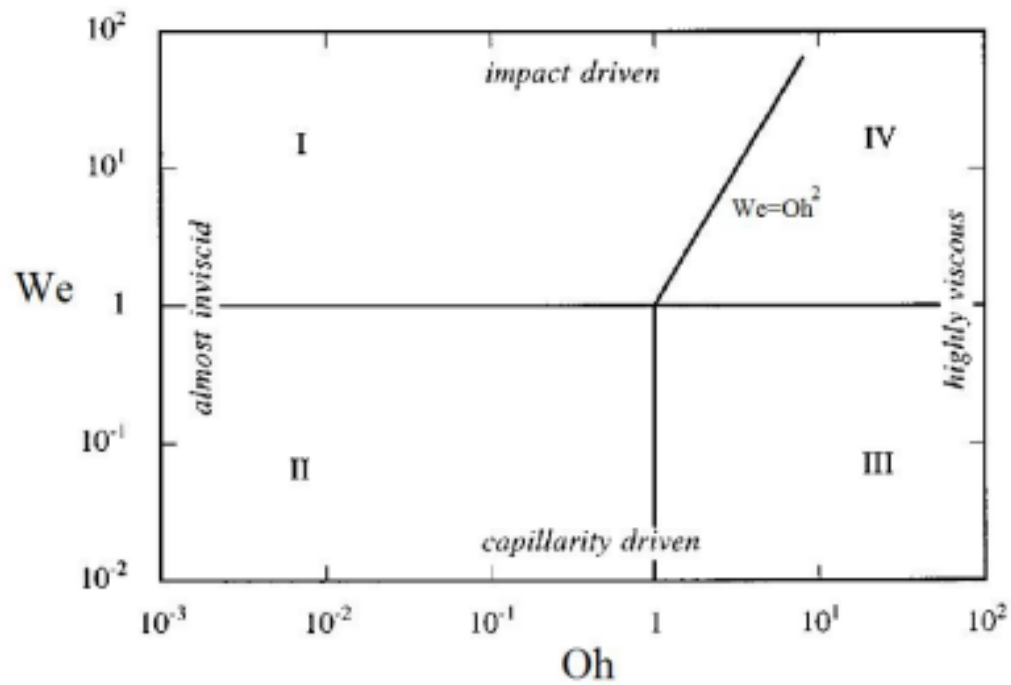


- We (inertial/superficial forces)  $We = \frac{\rho V^2 D}{\sigma}$
- Oh (viscous / superficial forces)  $Oh = \frac{\mu}{\sqrt{\rho\sigma D}}$
- Re (inertial viscous forces)  $Re = \frac{\rho V D}{\mu} = \frac{\sqrt{We}}{Oh}$

Example: atmospheric Water Drop

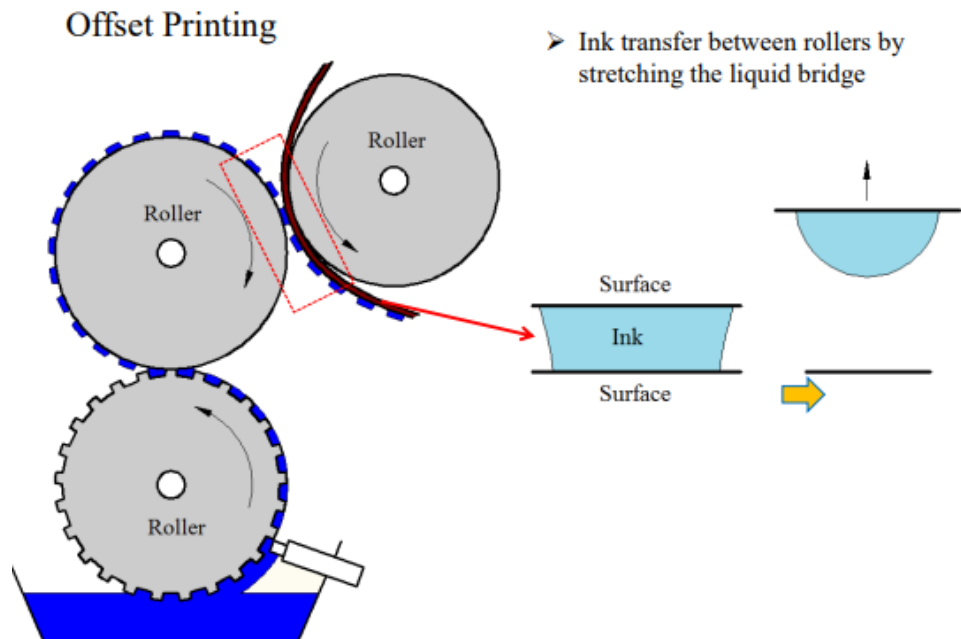
- $V = 50 \text{ M/S}$
- $D = \mu \text{ m}$
- $We = 1700$
- $Oh = 0.03$





## DA for Data Analysis/Interpretation

Example of liquid bridge case for printing industry:



## Industrial Application

### Other applications

- Dispensing of glue for packaging
- Electro wetting-assisted drop deposition
- Micromachined fountain-pen techniques

### Glue dispenser



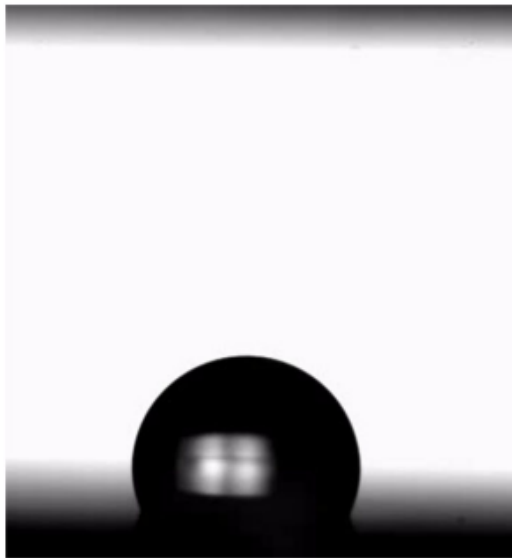
In Nature:

Cat laps

Liquid adhering to the dorsal side of the tongue tip is drawn upward, forming a liquid bridge.



Process of liquid transfer from one surface to another



Acceptor surface: PMMA surface

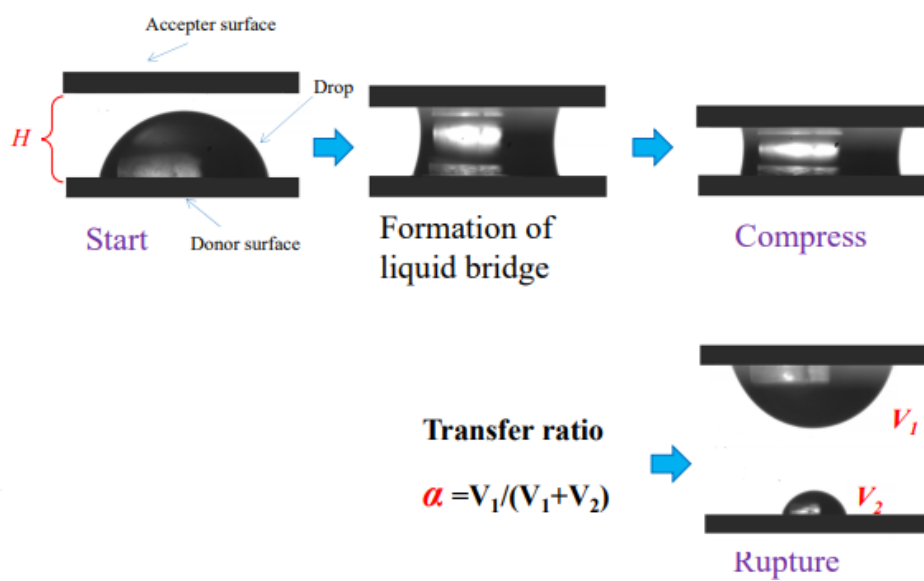
➤ Water drop transfer

Donor surface: Teflon AF surface

Typical process of liquid transfer

Transfer ratio-

$$\alpha = \frac{V_1}{(V_1 + V_2)}$$



Governing parameters for the transfer ratio:

- Donor Surface: Teflon AF

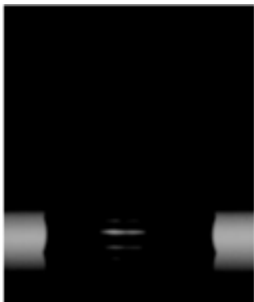
- Acceptor surface: PMMA
- Stretching speed (U): 25 mm/s



- Donor surface: Teflon AF
- Acceptor surface: PMMA
- Stretching speed (U): 1mm/s

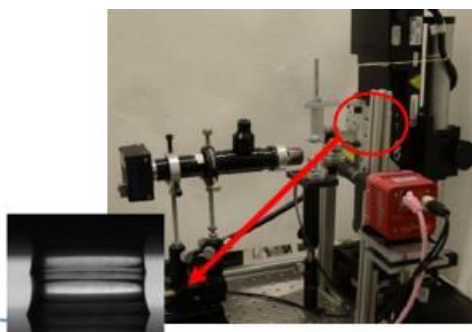
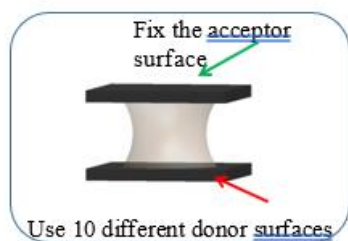


- Donor surface : Silicon
- Acceptor Surface: PMMA
- Stretching speed: 1 mm/s



What maybe parameters of interest?

- liquid viscosity
- Separation velocity of surfaces
- Surface tension of liquid
- Type of surfaces



### Ten Different Donor Surfaces

CaseNo.	SurfaceName	Contactangle(degree)
1	SiliconWafer	$\theta_a=55.1$ ; $\theta_r=45.7$
2	PMMA(3)	$\theta_a=71.9$ ; $\theta_r=52.7$
3	PMMA(2)	$\theta_a=72.8$ ; $\theta_r=57.9$
4	Blend(1)	$\theta_a=73.1$ ; $\theta_r=59.7$
5	Blend(2)	$\theta_a=79.4$ ; $\theta_r=63.9$
6	PS(1)	$\theta_a=88.6$ ; $\theta_r=66.0$
7	PEMA	$\theta_a=77.6$ ; $\theta_r=68.2$
8	PS(2)	$\theta_a=91.8$ ; $\theta_r=75.3$
9	OTS	$\theta_a=111.1$ ; $\theta_r=98.2$
10	TeflonAF	$\theta_a=126.4$ ; $\theta_r=116.4$

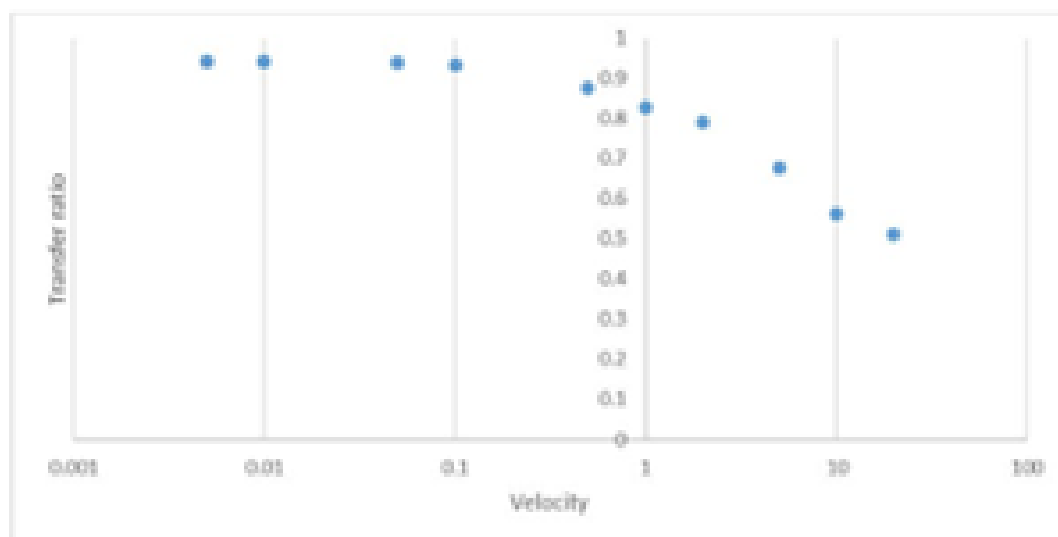
### Acceptor surface

PMMA(1):  $\theta_a=72.5^\circ$ ,  $\theta_r=60.3^\circ$

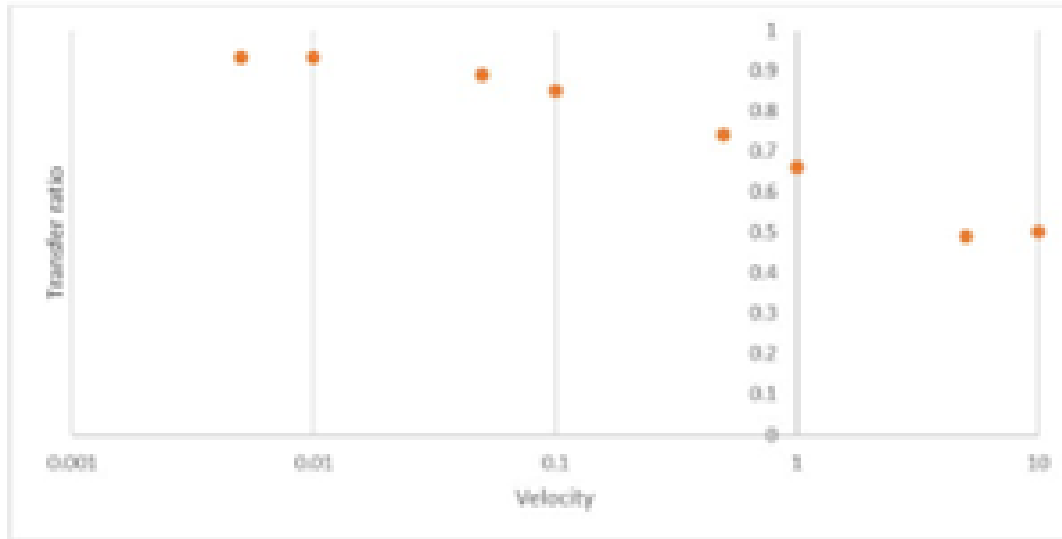
Speed of surface:  
 $5\mu\text{m/s}$

Volume of liquid:  
 $2\mu\text{l}$

20 cSt silicone oil:

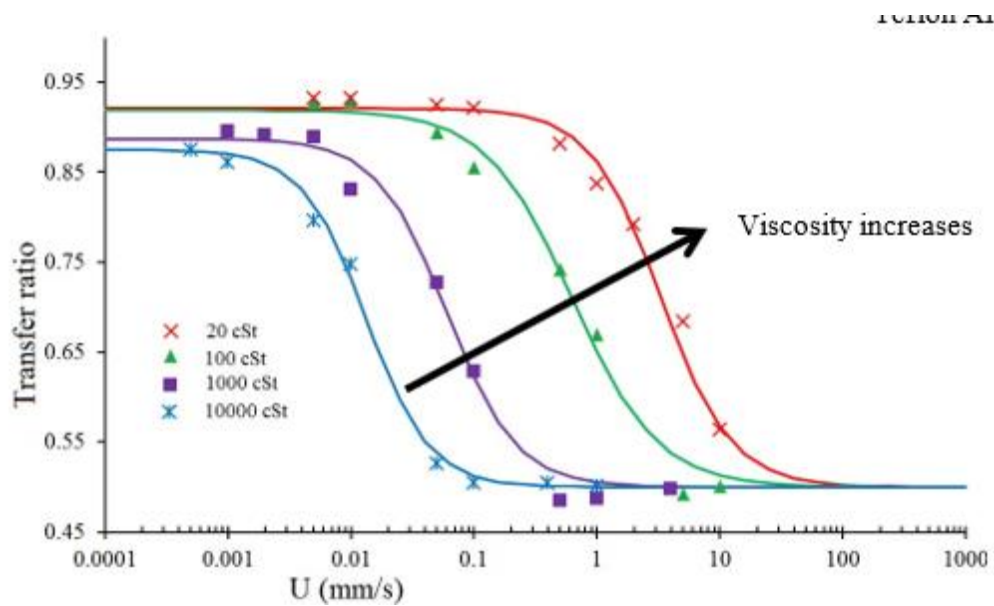


100 cSt silicone oil:



## Roles of liquid viscosity

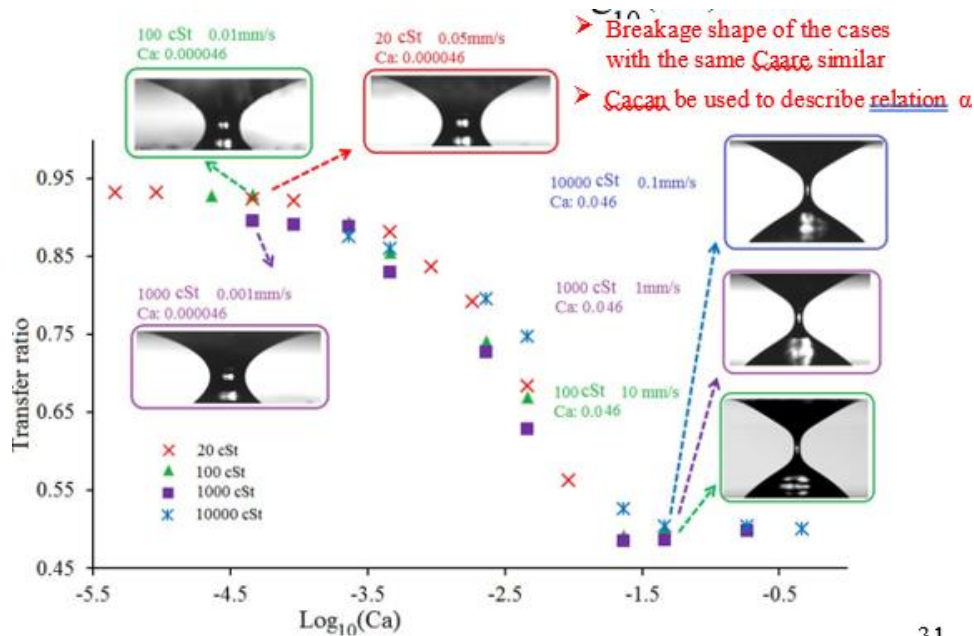
Four types of silicon oil transfer from Teflon AF to PEMA



What nondimensional parameters we can use?

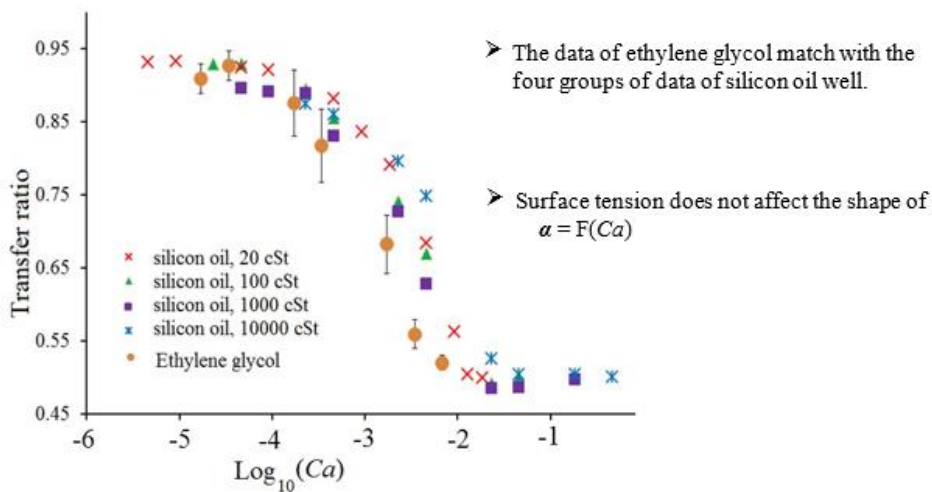
Capillary number  $Ca$  ( $Ca = \frac{\mu V}{\sigma}$ ) [viscos forces over surface tension forces]

Transfer Ratio as Function of Lof ( $Ca$ )



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### Effects of liquid surface tension



### Goals for today's lecture – Lecture 10

1. Introduction of 3<sup>rd</sup> way to study fluid dynamics, i.e., empirical studies
2. Discussion of an experiment and parameters that can be involved
3. How to handle many parameters that can be involved in an empirical study
4. Dimensional Analysis as a way of interpreting data and managing experiment parameters in a study

### Chapter 5: Dimensional Analysis (DA) & Similarity

DA is basically a way to reduce the numbers of variables to allow for planning on data interpretation in/from an experimental work.

DA saves time and money, as we can reduce the number of experimental runs. Experimental work is an important part of F.D. as many cases are too complex in mission critical to use analytical or CFD methods (alone).

Note: Read Sec. 5.1 & 5.2 \

### Sec. 5.3 The Pi Theorem

We will use Ipsen method rather than Buckingham method to do the DA. In DA we create non dimensional compound variables, out of dimensional variables. The non-dimensional compound variables are called Pi (due to symbol -  $\pi$ ).

If phenomenon (e.g. drag on airfoil) depends on "n" dimensional variables (e.g. velocity, density, etc), the DA reduces the problem to "K" dimensionless parameters (e.g.  $C_D$  &  $Re$ ).

Generally  $n - k$  is equal to number of fundamental (or basic) dimensions (e.g. M, L, T, etc) **something**

Do you know some non-dimensional variables?

$$Re = \frac{\rho V L}{\mu} (L \Rightarrow \text{characteristic length for the system}), Ma = \frac{V}{a}, K = \frac{c_p}{c_v} (\text{specific heat})$$

The non-dimensional variables usually have or signify physical meaning, e.g.

$Re = \frac{\text{inertial forces}}{\text{viscous forces}} \Rightarrow$  signify how much inertial forces should be longer than viscous forces to transmit turbulent flow.

$$We = \frac{\rho v^2 L}{\sigma} = \frac{\text{inertial forces}}{\text{surface tension forces}} (We \#)$$

$$Bo = \frac{\rho g L^2}{\sigma} = \frac{\text{gravity forces}}{\text{surface tension forces}}, k = \frac{c_p}{c_v} = \frac{\text{enthalpy}}{\text{internal energy}}$$

$$\text{Drag coefficient } C_D = \frac{D}{\frac{1}{2} \rho v^2 L} = \frac{\text{drag force}}{\text{inertia force}}$$

1. How to use this information to make plans for experiments?
2. How to use this information to interpret data?

1. Planning: should I worry about liquid surface tension when designing a channel flow?

Channel dimensions: 30 x 20 mm and 2m long

Flow velocity: 0.1 m/s

Liquid: water or ethanol ( $\rho_w = 1000 \frac{kg}{m^3}$ ,  $\rho_e = 790 \frac{kg}{m^3}$ ,  $\sigma_w = 72 \frac{mN}{m}$ ,  $\sigma_e = 22 \frac{mN}{m}$ )

Which # to use? We

$$We_w = \frac{1000 \times 10^{-2} \times 3 \times 10^{-1}}{72 \times 10^{-3}} = 41.7 \Rightarrow \text{Inertia is 42 times more important than surface forces.}$$



What if the channel is angled (effect of gravity) ?

$$Bo_w = \frac{1000 \times 9.8 \times (3 \times 10^{-1})^2}{72 \times 10^{-5}} = 12250 \Rightarrow \text{So not important at all}$$

$$Bo_e = 31,672$$

How about viscous forces?

$$Re_w = \frac{\rho UL}{\mu} = 200,000 \Rightarrow \text{Not to worry about viscous forces ,}$$

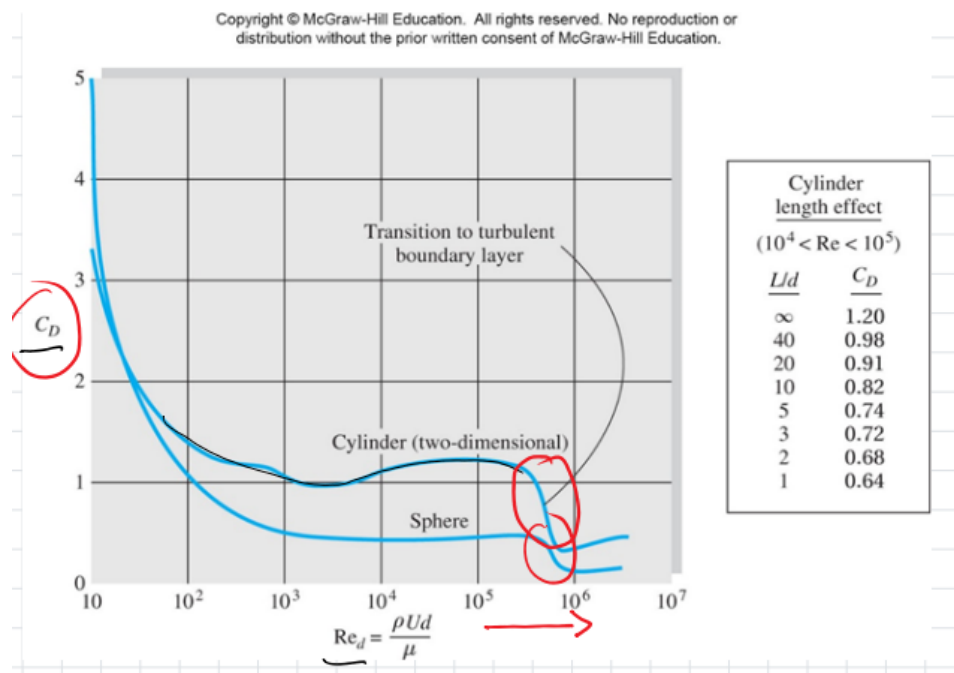
What if the velocity B is reduced to 1mm/min  $\rightarrow Re_w \approx 23, Re_e \approx 26 \rightarrow$  now viscous forces are more important.

How about surface forces ?

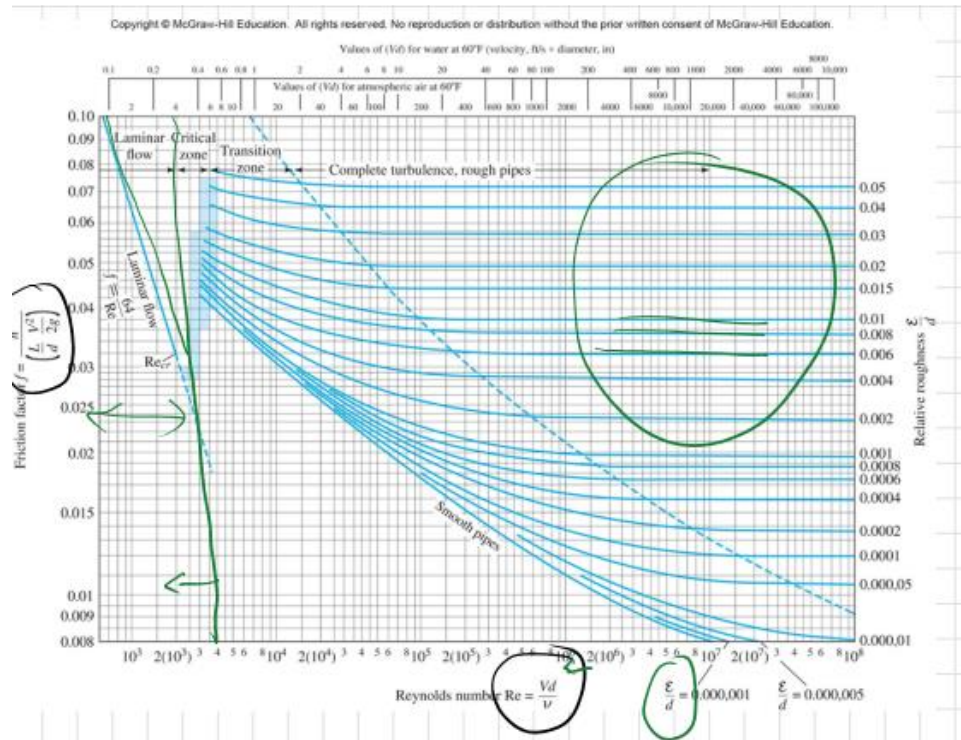
$$We_w \approx 2.3 \times 10^{-4} \rightarrow \text{Surface forces are the King/Queen in } \mu \text{ channel.}$$

So such planning analysis will allow us to plan better; for a large channel surface tension will not be a design/experiment consideration, but for a micro-channel it should be!

- Once data is collected in an experiment, say drag force coefficient for a sphere or a cylinder. Non-dimensional plot, allows a comprehensive representation of data; as seen in figure below, the plots are independent of the fluid used (e.g.,  $\mu, \rho$ ), so it can be for air, water, oil, etc. No more need for 3 plots for air, oil, water...



Also, data interpretation in terms of e.g. forces, with a plot such as the one above can be made in general fashion (e.g. regardless of the type of fluid); see encircled areas in the above plot where an increase in inertial forces leads to reduction of forces on the cylinder or spherical body in any fluid flow ( $C_D \downarrow$ )



How to make non-dimensional groups ( $\pi$ ) or numbers.