

## First Lecture

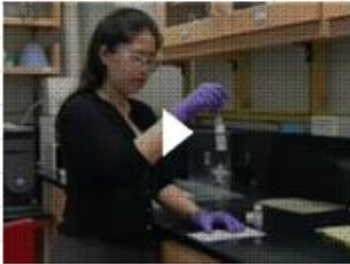
Who is stronger a solid or a fluid?

[Cutting An Anvil In Half With A 60,000 PSI Waterjet - when inside an Anvil? - Scandal](#)



Watch from min 2:10 onwards

[Liquid Bullet-Proof Armour](#)



## Our Goals for Today (lect. 2)

1. Understand shear stress in liquids
2. Viscosity & its temperature and pressure dependance

Before we start... What are we after in Studying Fluid Dynamics?

1. Pressure field/values
2. Velocity Field
  - a. Work
  - b. Forces
  - c. Power
  - d. Losses
    - i. Pressure
    - ii. Drag/resistive force

What is the main difference between a solid and a liquid?

- Fluids do not keep their shape under any stress
- Stems from ability of liquid molecules to move around

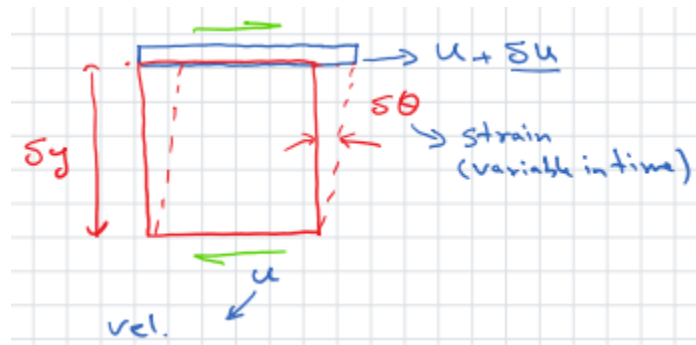
**Aside:** the terms Fluid Dynamics and Fluid Mechanics are used interchangeably in this course and mean largely the same thing

### Solid vs Fluid

A solid can resist a shear stress ( $\tau$ ) by a static deformation, but a fluid cannot!

What happens when a fluid experiences a shear stress?

It flows!



At a given time,  $\delta t$ , The larger the  $\tau$ , the larger will be  $\delta \theta$ , so  $\tau \propto \frac{1}{\delta t}$

$$\therefore \tau \propto \frac{\delta \theta}{\delta t} \quad (1)$$

A constant shear stress, causes a strain ( $\delta \theta$ ) that is changing with time, at a rate of  $\frac{\delta \theta}{\delta t}$ .

$$\text{Eq (1)} \rightarrow \tau = \mu \frac{\delta \theta}{\delta t} \quad (2) \quad \text{Newton's law for viscosity}$$

Where  $\mu$  is the viscosity (proportionality constant)

Viscosity is the resistance of a fluid to motion.

$$\frac{N}{m^2} = \mu \frac{\theta}{s} \rightarrow \mu \text{ unit is } \frac{N \cdot s}{m^2} \text{ or } \frac{kg}{m \cdot s}$$

$$\mu_{\text{water}} = 1 \times 10^{-3} kg/m \cdot s \text{ or } 1 \text{ cP (centi-poise)}$$

$$\mu_{\text{air}} = 1.8 \times 10^{-5} kg/m \cdot s$$

Viscosity is a thermodynamic property, so:  $\mu = \mu(T, P)$

Where  $T$  = temperature and  $P$  = Pressure

$\mu$  changes significantly with temperature.

For gases,

$$\frac{\mu}{\mu_0} = \left(\frac{T}{T_0}\right)^n$$

Known  $\mu_0$  at  $T_0$  (273K)

$n$  is a constant (for air 0.7)

But for liquids,  $\mu$  decreases with temperature

$$\mu \approx ae^{-bT}$$

$a$  and  $b$  are constants that depend on the type of liquid

why different between gas & liquid?

$\mu \propto P$ , and  $P \uparrow$  so does  $\mu$  for all fluids.

If  $\mu$  is divided by fluid density ( $\rho$ ), it is called kinematic viscosity ( $\nu$ ).

$$\nu = \frac{\mu}{\rho} \left(\frac{m^2}{s}\right)$$

For water  $\nu = 1 \text{ cSt}$  or  $1 \times 10^{-6} \frac{m^2}{s}$

In fluid mechanics, we're not interested in strain rate (unlike solid mechanics), but care about velocity distribution within the fluid. Let's see how we can match strain to velocity.



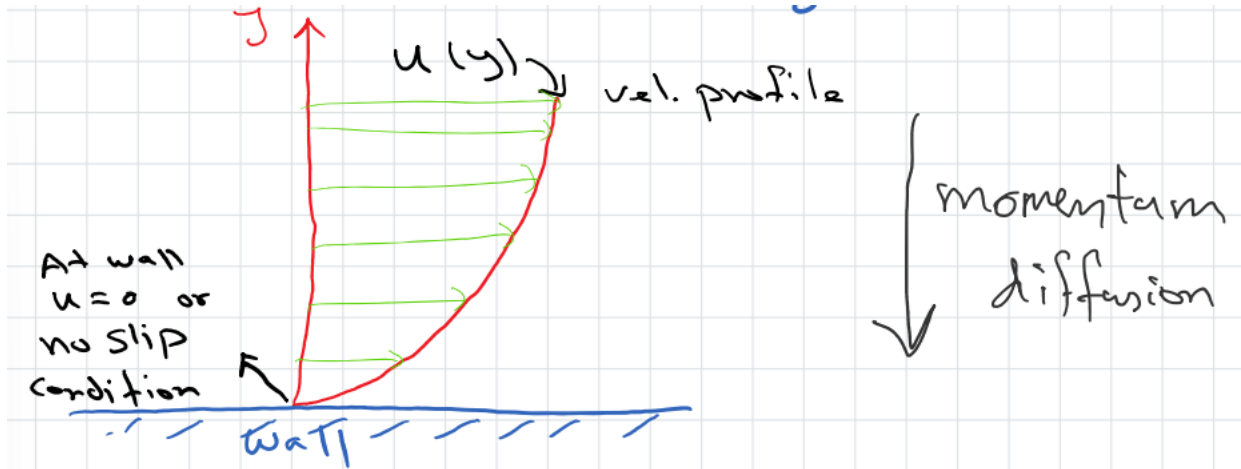
$$\tan \delta \theta = \frac{\delta x}{\delta y} \rightarrow (\text{for small strains \& elements}) \delta \theta = \frac{\delta x}{\delta y}$$

$$\delta x = \delta u \delta t \rightarrow \delta \theta = \frac{\delta u \delta t}{\delta y}$$

$$\frac{\delta \theta}{\delta t} = \frac{\delta u}{\delta y} (3)$$

From Eqs. (2 & 3):

$$\tau = \mu \frac{\delta u}{\delta y} \quad (4)$$



$$\delta_m \mu \equiv \text{momentum}$$

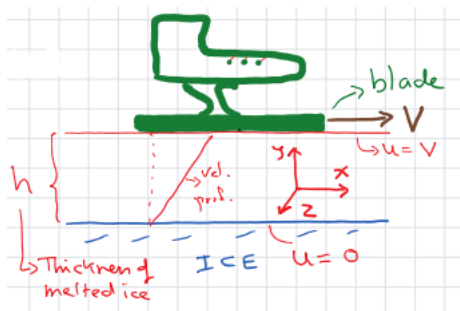
$$q = k \frac{dT}{dx}$$

$$\tau = -\mu \frac{dv}{dy}$$

$$\dot{m} = D \frac{ds}{dx}$$

Example: Skating on ICE!

Let's assume ice between skate and surface is melted. What is the relative profile within the liquid film?

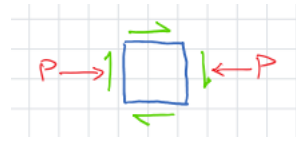


Assumption:

1 – The flow is one dimensional in x-direction, i.e.  $u(x) = u(z) = 0$ ,  $u(y) \neq 0$

2 – no pressure variation in x direction

Let's consider force balance over a fluid element



From force balance  $\frac{du}{dy} = \frac{\tau}{\mu}$

$$du = \frac{\tau}{\mu} dy \rightarrow \int du = \int \frac{\tau}{\mu} dy$$

If the person is not accelerating, then  $\tau$  is a constant,  $\mu$  is a constant (water), then the integral can be solved as:

$$u = a + \frac{\tau}{\mu} y$$

B.C.

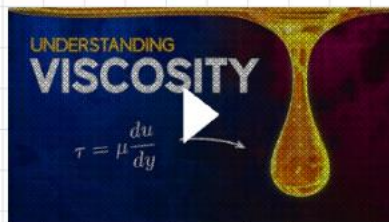
at  $y = 0 \rightarrow u = 0 \rightarrow a = 0$

at  $y = h \rightarrow u = v \rightarrow v = 0 + \frac{\tau}{\mu} h \rightarrow \frac{\tau}{\mu} = \frac{v}{h}$

$u = \frac{v}{h} y$  (linear velocity profile)

Summary for today's lecture

A good video to watch for the review of materials in this lecture  
[Understanding Viscosity](#)



1. Viscosity change with T&P
2. Intermolecular forces is the origin of viscosity
3. Difference between solid & liquid in terms of strain
4. Proportionality between velocity & shear stress

## Our Goals for Today (lect. 3)

1. Non-Newtonian Fluids
2. Various ways to study fluid dynamics

## Newtonian vs Non-Newtonian Fluid