

Statistical Methods for Discrete Response, Time Series, and Panel Data (W271): Lab 2

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1 Report from the Point of View of 1997

1.1 (3 points) Task 0a: Introduction

Climate change is an increasingly pertinent issue for scientists and policymakers alike, as global temperatures rise. It is crucial to understand the underlying reasons for this increase, and its relationship with carbon emissions. This report presents forecasts of this constant increase, and highlights the need to anticipate future impacts of carbon emission reduction efforts.

Geochemist Dr. Charles David Keeling's pioneering work in atmospheric carbon dioxide measurements fundamentally reshaped our understanding of the global carbon cycle and its impact on climate change. In 1958, Keeling initiated a long-term study at the Mauna Loa Observatory, producing the iconic "Keeling Curve," which revealed the steady rise of atmospheric CO₂. His research confirmed that fossil fuel combustion was contributing to increasing CO₂ levels, a discovery with profound social and political consequences. This work also paved the way for further investigations into other greenhouse gases and established benchmarks for testing climate models.

CO₂ is classified as a "greenhouse gas," meaning that it traps heat in the atmosphere and leads to rising global temperatures when in high concentrations. It can be important to track CO₂ levels as rising global temperatures can lead to imbalances in ecosystems and rising water levels that impact both animal and human life. Understanding these trends is essential for assessing the long-term impact of human activities and guiding future policies.

1.2 (3 points) Task 1a: CO₂ data

The current data is gathered from measurements made under Dr. Charles Keeling's study at the Mauna Loa Observatory in Hawaii (Cleaveland, 1993), and part of the R object `co2`. Measurements were taken by a chemical gas analyzer sensor, with detections based on infrared absorption. This data measures monthly CO₂ concentration levels from January 1959 to December 1997. Units are in parts per million of CO₂ (abbreviated as ppmv) using the SIO manometric mole fraction scale. Dr. Keeling initially designed a device to detect CO₂ emitted from limestone near bodies of water. But his measurements revealed a pattern of increasing CO₂ concentrations at the global scale, urging further need to continue tracking the gas (Keeling, 1998). The time series shows a clear upward trend of global CO₂ concentrations from 1959 to 1998, with an average increase in 1.26 CO₂ ppmv and a standard deviation of .51 CO₂ ppmv. Upon inspection of the yearly increases, the bulk of changing CO₂ levels are between 0.75 and 2.0 CO₂ ppmv.

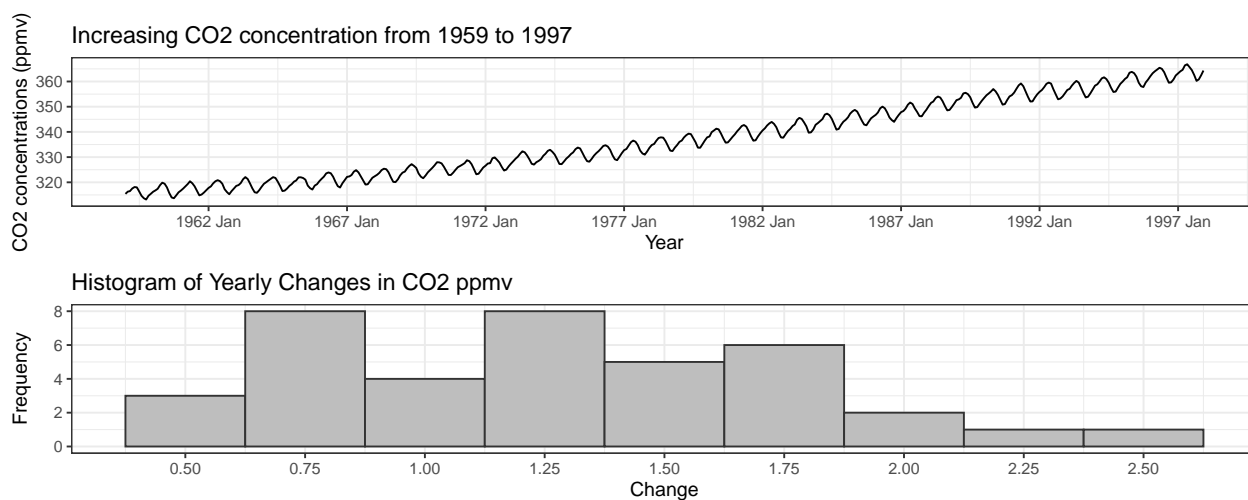


Figure 1: Data source: CO₂ measurements from Mauna Loa Observatory

The time series also shows strong evidence of seasonality corresponding closely with the meteorological seasons

of Autumn, Winter, Spring, and Summer. We now look at the ACF plot and average CO2 concentration for each month to gain further clarity on the seasonality.

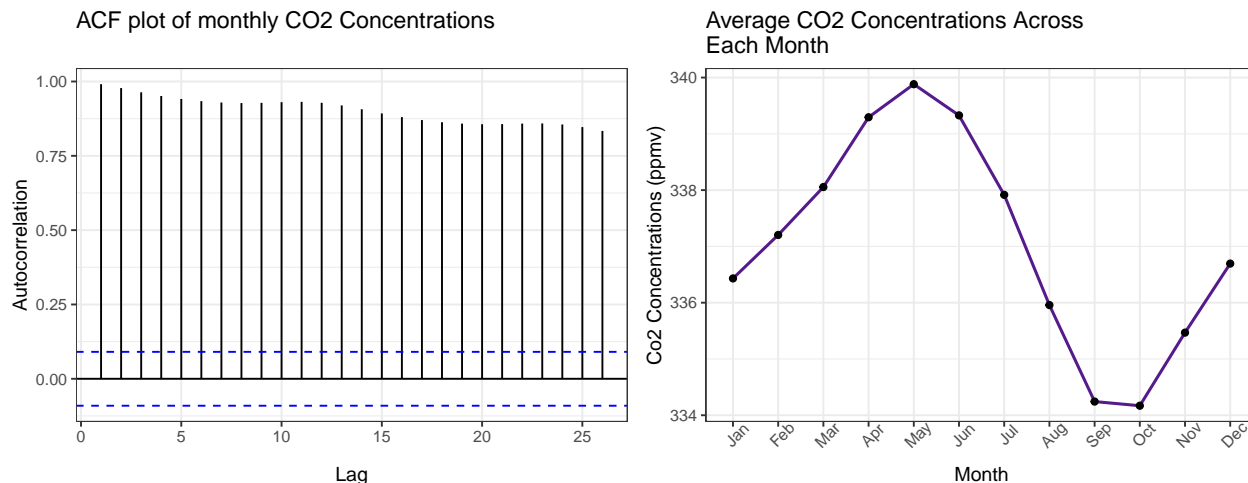


Figure 2: Observing seasonality in CO2 concentration

We see a wave shaped pattern among correlations between the current value and growing lags. Clearer evidence of seasonality is shown when inspecting the monthly average the CO2 ppmv, when averaged across all years in the available data. CO2 concentration peaks at the start of summer, and drops to a low in the fall, before rising again. This is likely due to the organic decomposition of plant life in these seasons (Keeling, 1960).

We now study the time series' stationarity. We first conduct the Augmented Dickey-Fuller (ADF) Test to test the null hypothesis that the time series is not stationary. As seen in the time series plot, we have a clear upward trend, suggesting non-stationarity. This is confirmed by a p-value of 0.2269 yielded by the ADF test, which indicates insufficient evidence to reject the null hypothesis of non-stationarity. To look at stationarity in variance, we fit a yearly CO2 average on the monthly time series, and inspect the residuals from year to year. Although there are slight changes in the variance, they seem to regress to a constant variance over time. Thus, once we account for the yearly increases in CO2 ppmv, there is likely a constant variance over time.

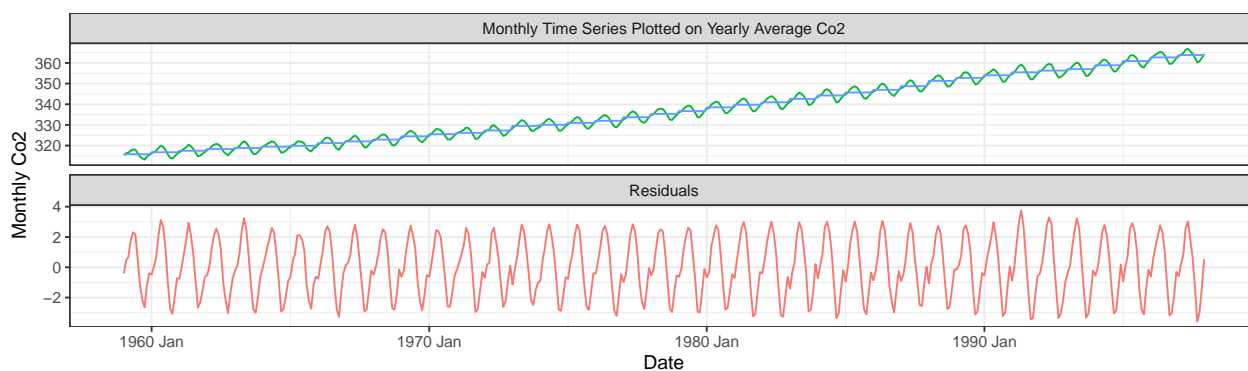


Figure 3: Studying variance over time

1.3 (3 points) Task 2a: Linear time trend model

We now fit a linear time trend model to the `co2` series, and examine the characteristics of the fit and residuals.

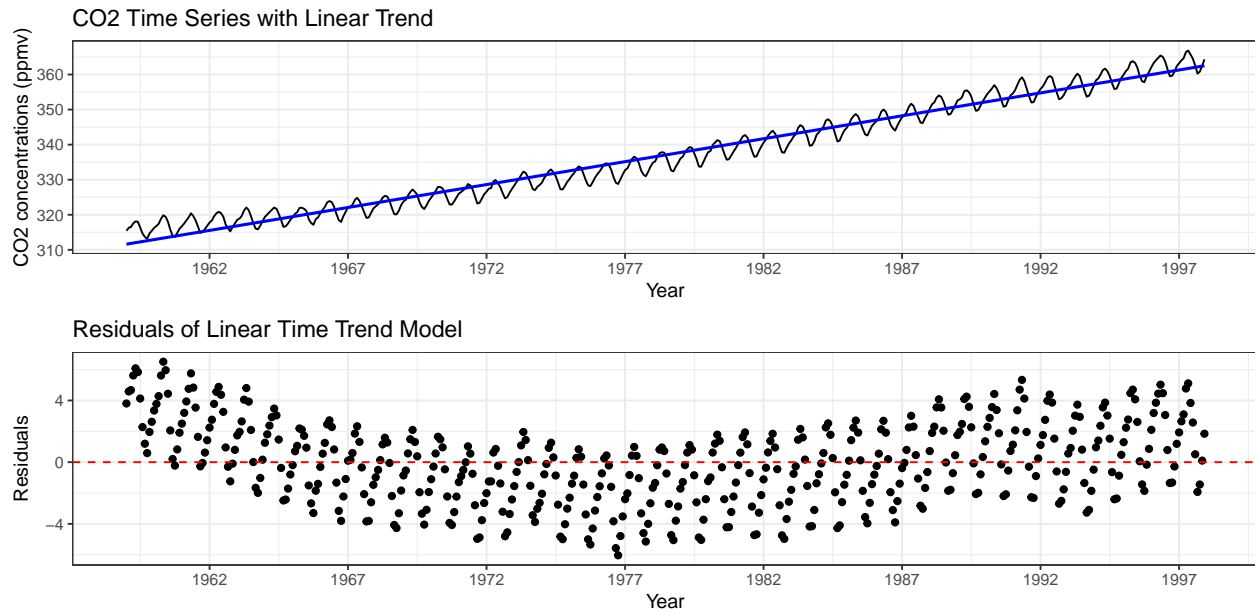


Figure 4: Evaluating a Linear Model

Upon inspection of linear fit, the fitted line appears to be systematically overestimating values at certain points and underestimating values at other points. This indicates that perhaps a higher order polynomial might produce a better fit of the overall trend. The residuals of the linear model also exhibit a cyclical, non-linear pattern, indicating that the model does not capture the seasonality in the data. The overall curve also suggests that the linear model insufficiently captures the overall trend. We now try and assess a quadratic model to see if it better captures the data.

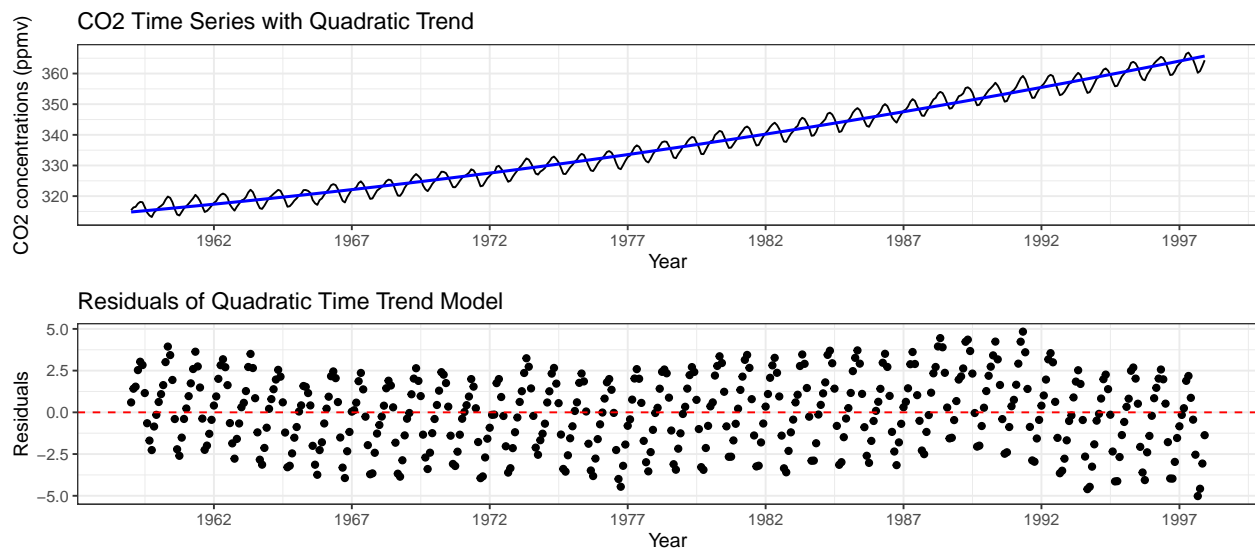


Figure 5: Evaluating a Quadratic Model

The quadratic model's residuals indicate a small reduction in variance, demonstrating a slightly improved fit. However, the cyclical behavior remains, indicating that seasonality is unaccounted for in the model still. There is also an overall non-random trend in the residuals, indicating that the model still may not capture all the structural details. We now fit a polynomial model to the data to see if there is an improved fit.

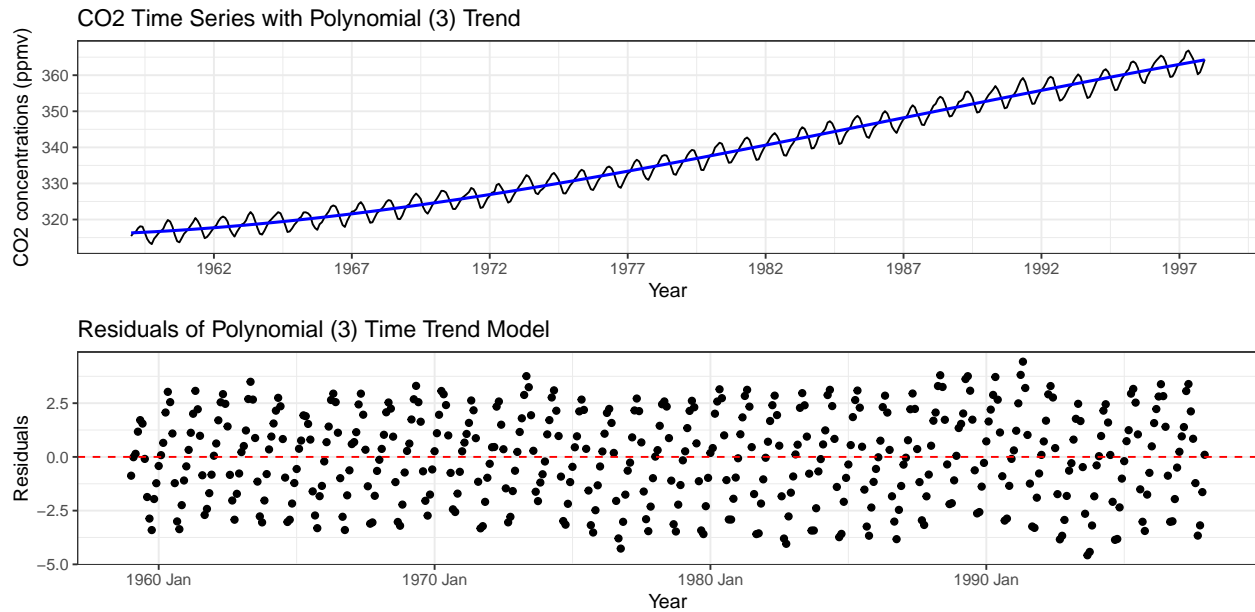


Figure 6: Evaluating a Polynomial (3) Model

The third-order polynomial model demonstrates improved residual behavior compared to quadratic and linear models, although it still doesn't capture the seasonality. We chose to stop at this order to prevent overfitting, as higher-order polynomials showed diminishing returns in model performance.

Apart from transforming the orders of the model, we were interested in data transformations - specifically logarithmic. As such we experimented with a logarithmic dataset to observe the pattern of the data values.

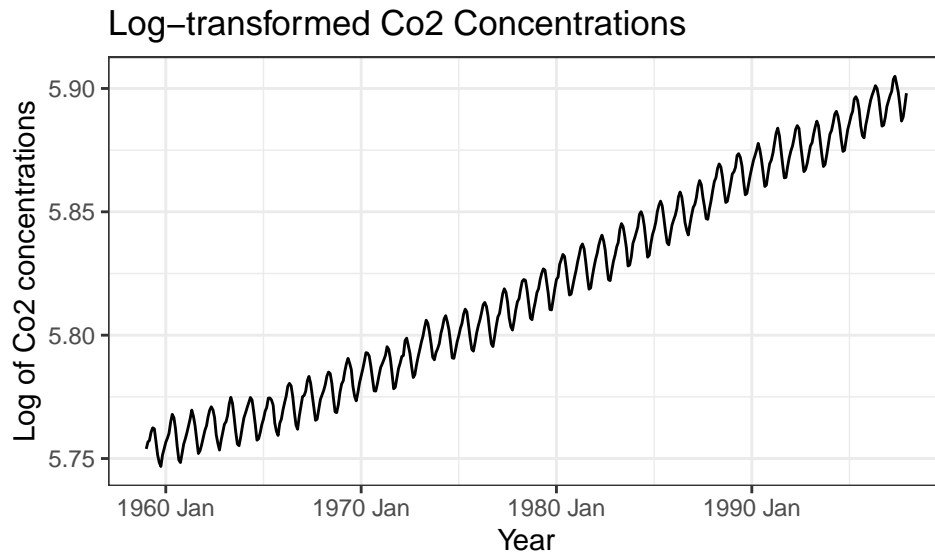


Figure 7: Evaluating effect of taking a log on the series

The logarithmic transformation reduces variance but offers minimal improvement compared to traditional

plotting. This limited impact is likely due to the cyclical nature of the time series, which the transformation does not adequately address. Furthermore, as discussed, the variance of the time series looks about constant over time, indicating that a logarithmic transformation may be unnecessary.

To address the cyclical behavior, we developed another polynomial (3) model that includes each month as a variable, since the average monthly CO2 emissions indicate significant cyclic patterns at the monthly level. By incorporating this variable, we anticipate an improvement in the fit of our time series model. We get the plots below.

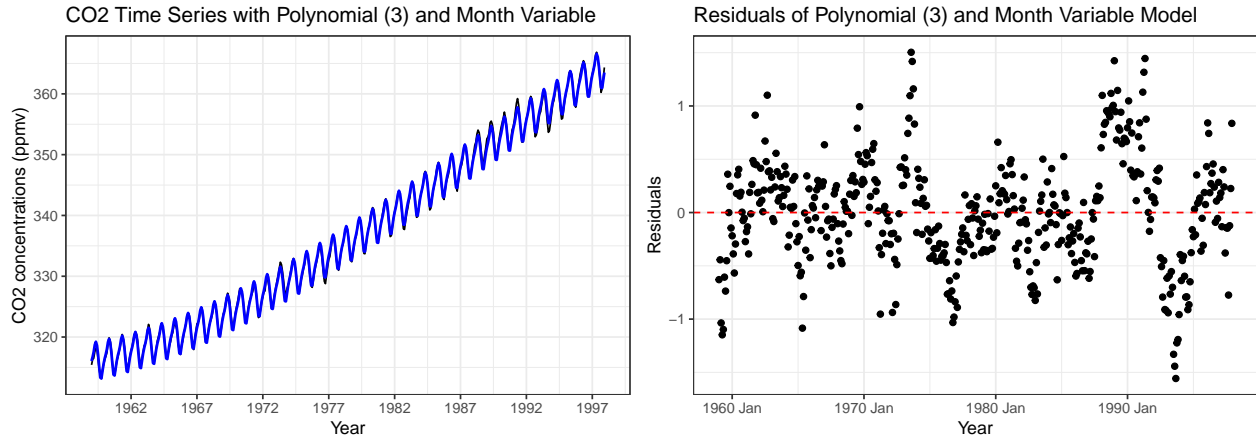


Figure 8: Evaluating a Polynomial (3) with month variable model

As seen above, incorporating the `month` dummy variable further reduced the range of residuals, they now range between 1 and -1, but the residuals still displayed a seasonal pattern. To refine the model, we grouped the months into quarter, to represent the seasons as a categorical variable, `season`.

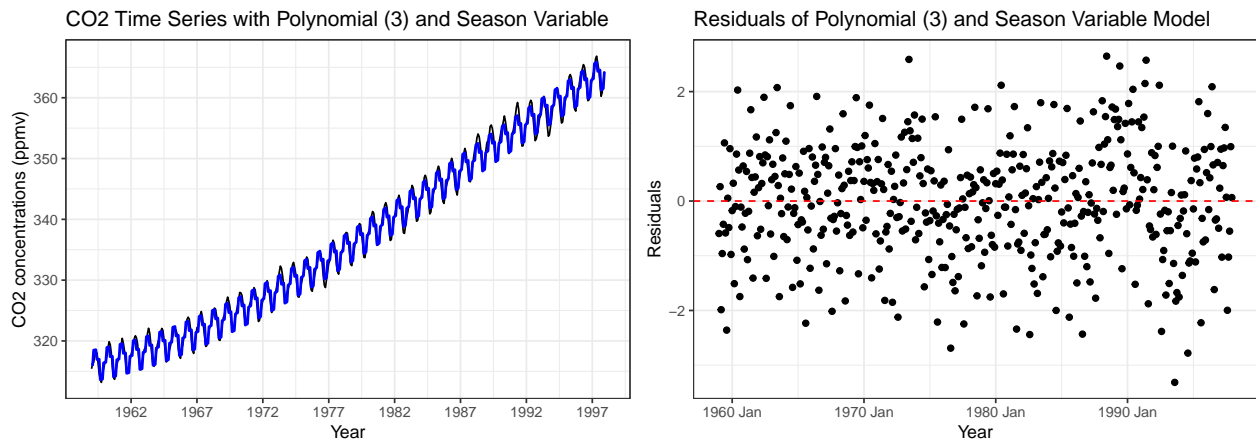


Figure 9: Evaluating a Polynomial (3) with season variable model

We see that using the `season` variable resulted in residuals that most look like a random distribution around the red line centered on zero, when compared to other models tried thus far, though fluctuations increased to between 2 and -2. Still, given that the residuals look like a random distribution, we will accept the larger range of residuals, and proceed to develop a forecast for CO2 emissions through 2020 with this model.

The forecast model using the `season` variable shows decent performance, and predicts for the upward trend to persist but taper off, up to 2020. It also predicts continued annual seasonality. The tapering off is an assumption made implicitly in the model due to it being Polynomial (3), but may not be justified. We will now explore an ARIMA model to see if it will capture the time series' underlying patterns differently.

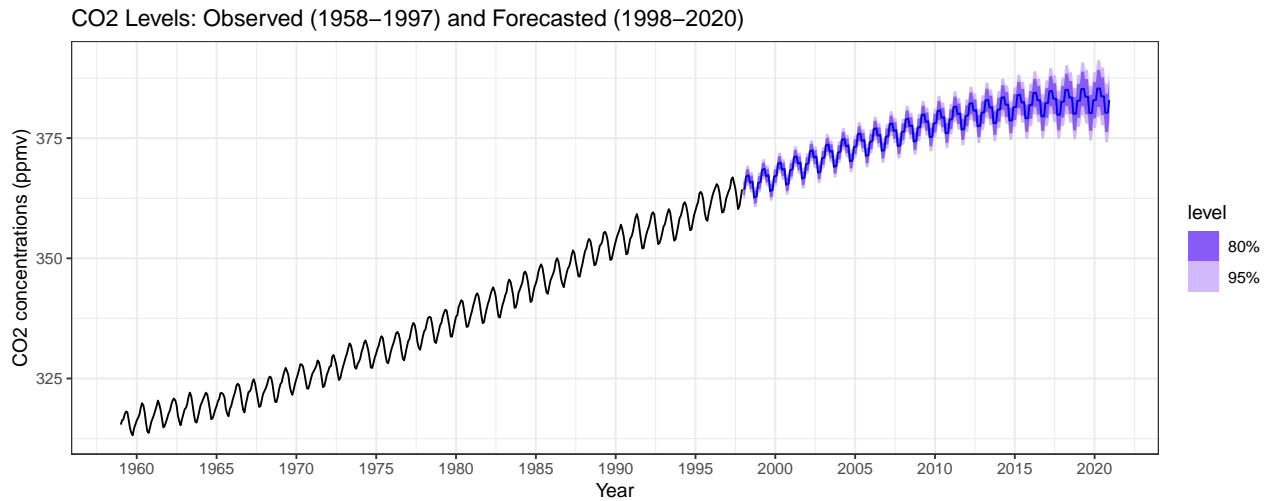


Figure 10: Forecasting CO2 levels up to 2020 using a Polynomial (3) with season variable model

1.4 (3 points) Task 3a: ARIMA times series model

As seen in our EDA, there is non-stationarity. Thus, we will proceed to difference the data to make it stationary, both at the 1st lag followed by the 12th lag to account for seasonality, which is a crucial step before fitting the ARIMA model effectively. We now look at the differenced time series.

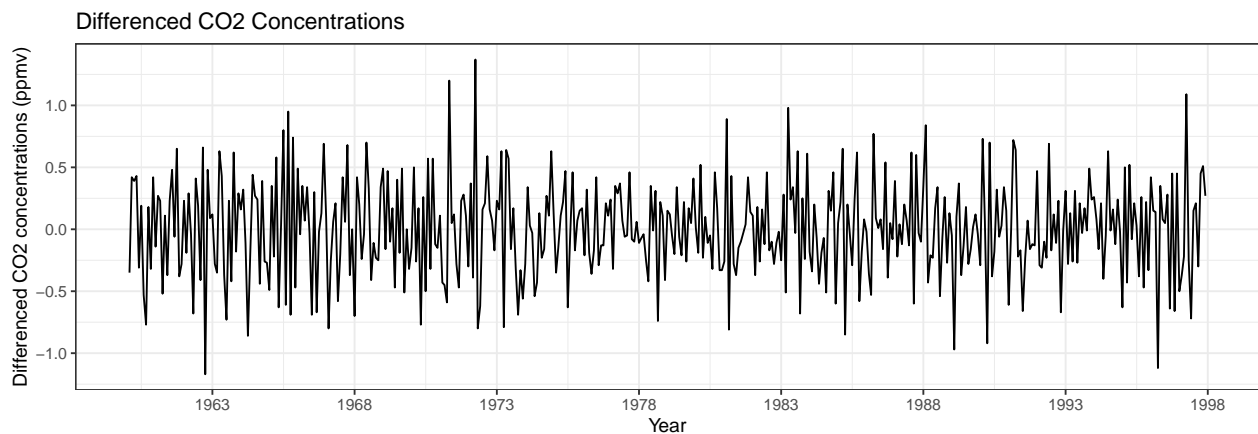


Figure 11: Differenced series looks more stationary in the mean and variance

The plot of the differenced time series does look more stationary in the mean and variance; which is confirmed by a 0.01 p-value yielded from the Augmented Dickey-Fuller Test, indicating sufficient evidence to reject the null hypothesis of non-stationarity. We now look at the ACF and PACF plots of the differenced time series, to inform how we should construct our ARIMA model.

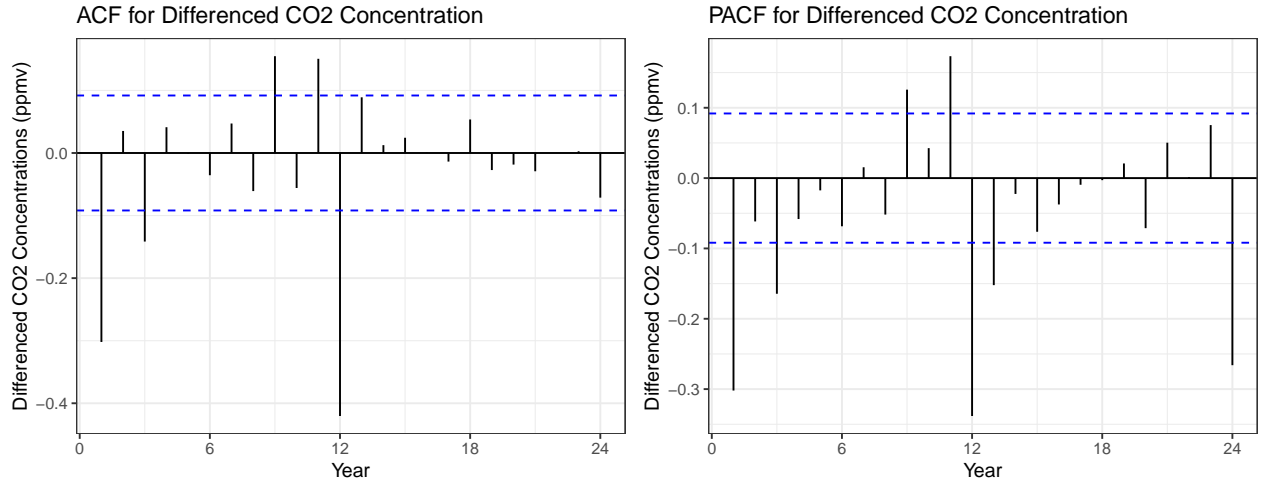


Figure 12: Evaluating ACF and PACF for differenced series

Both ACF and PACF plots show strong auto-correlation with lag 1, and the ACF cutting off strong after lag 1, and the PACF having a significant spike at lag 1, and tapering off a little more. This might indicate that our model has a MA(1) component. The spike at lag 12 in the ACF might also indicate a seasonal MA component.

The ARIMA function behaved as expected, and returned an $\text{ARIMA}(0,1,1)(0,1,1)[12]$ function, with $\text{BIC} = 182.32$. We will now look at the residuals for this model.

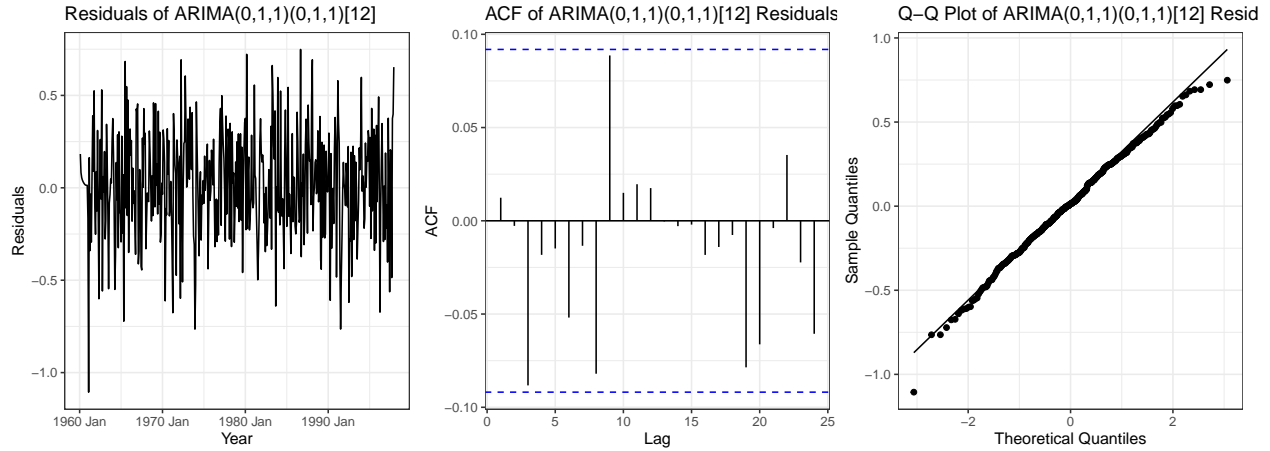


Figure 13: Evaluating $\text{ARIMA}(0,1,1)(0,1,1)[12]$ model

The residuals look random, there are no significant autocorrelations in the ACF, and they closely follow a normal distribution in the Q-Q plot. These all indicate that the model has captured most of the underlying structure of our time series. A Ljung-Box test also yielded a p-value of 0.6733, further confirming that there is insufficient statistical evidence to reject the null hypothesis that there is no autocorrelation. We can proceed with forecasting the time series data through 2022, and note that it does not predict any tapering off of the overall trend.

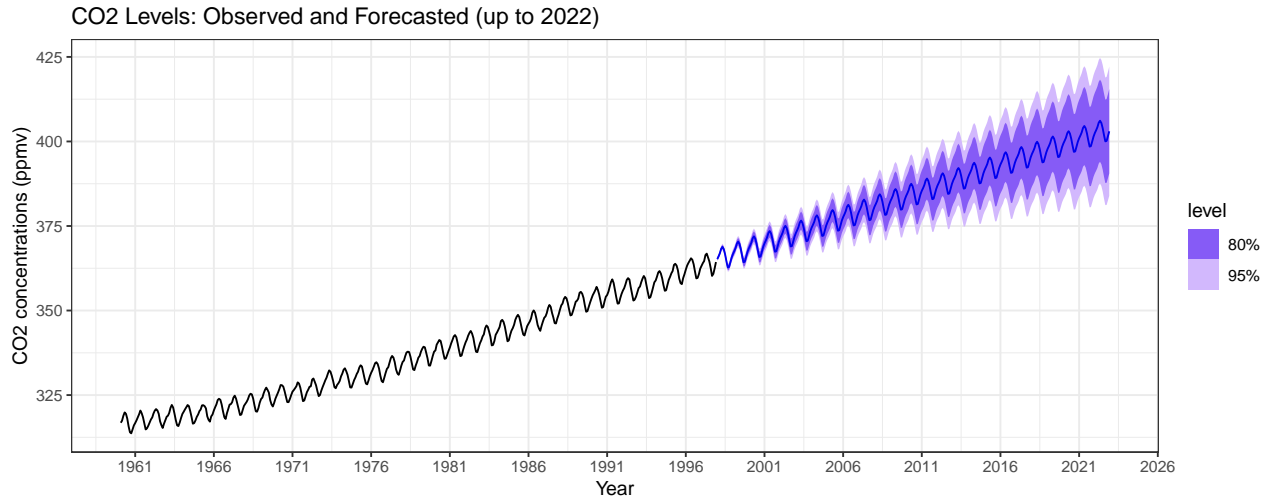


Figure 14: Forecasting up to 2022 using an ARIMA(0,1,1)(0,1,1)[12] model

1.5 (3 points) Task 4a: Forecast atmospheric CO2 growth

We now forecast when atmospheric CO2 is expected to be at 420 ppm and 500 ppm for the first and final times, as seen in the table below.

Table 1: CO2 Levels and Forecasted Times with 80% Confidence Intervals

CO2.Level	First.Month	First.Value	Last.Month	Last.Value
420 ppm	2031 May	420.1 (402.3, 438.0)	2035 Oct	420.4 (399.5, 441.3)
500 ppm	2083 Apr	500.4 (437.9, 562.9)	2085 Dec	500.9 (435.7, 566.2)

Our model also forecasts CO2 levels in the year 2100. Although these forecasts include a standard deviation, but these do not take into account the existing efforts to reduce global greenhouse gases, such as the strong push for electric vehicles to replace gas vehicles. Thus, since these are very human-activity dependent, they are unlikely to be completely reliable without any exogeneous variables. Still, they can give us a sense of the overall trend and CO2 levels, *ceteris paribus*.

Table 2: CO2 Forecasts in 2100

Date	Value	SD
2100 Jan	523.7	62.8
2100 Feb	524.6	62.9
2100 Mar	525.5	63.0
2100 Apr	526.8	63.0
2100 May	527.4	63.1
2100 Jun	526.7	63.2
2100 Jul	525.2	63.3
2100 Aug	523.1	63.3
2100 Sep	521.3	63.4
2100 Oct	521.4	63.5
2100 Nov	522.8	63.5
2100 Dec	524.2	63.6

2 Report from the Point of View of the Present

2.1 (1 point) Task 0b: Introduction

Following our initial evaluation using Keeling's data from the point of view of 1997, we now seek to re-examine the original study to identify potential deviations in CO₂ level predictions from the point of view of the present, in 2024. Specifically, we aim to discern whether any discrepancies between predicted and actual CO₂ levels since 1997 arise from the inherent limitations of prior models or from changes within the CO₂-generating system itself.

Before 1997, CO₂ data was collected using a chemical gas analyzer that relied on infrared absorption to measure monthly CO₂ concentrations from January 1959 through December 1997. The present data collection approach, however, leverages a newer CO₂ analyzer installed at Mauna Loa, employing Cavity Ring-Down Spectroscopy (CRDS). CRDS determines CO₂ concentration by measuring the rate at which light is absorbed in an optical cavity, rather than the intensity. This method offers significant advantages, as it eliminates dependencies on light intensity and sample path length, providing absolute, highly accurate concentration measurements without frequent recalibration. Furthermore, CRDS is capable of hourly measurements, and its rigorous gas-flushing system ensures each sample's reliability. These improvements in measurement precision and frequency offer researchers enhanced insight into CO₂ trends, facilitating a more robust evaluation of the models' predictive capabilities and any potential systemic changes.

2.2 (3 points) Task 1b: Create a modern data pipeline for Mona Loa CO₂ data.

We created a data pipeline, pulling the most recent weekly data from the Global Monitoring Laboratory page. We now conduct a similar EDA for the updated time series data from Dr. Xin Lan's study of CO₂ atmospheric trends. We first plot the time series data for CO₂ concentrations, and a histogram of the yearly changes.

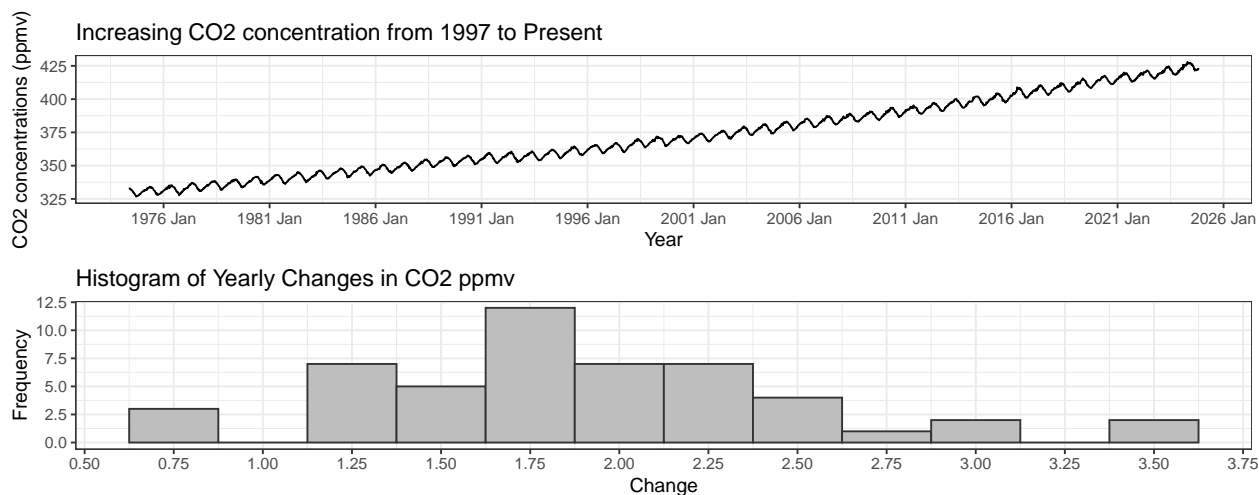


Figure 15: Data source: CO₂ measurements from Mauna Loa Observatory

From 1998 to 2024, the time series continues to show a clear upward trend of global CO₂ concentrations, with an average increase in 1.90 CO₂ ppmv and a standard deviation of .61 CO₂ ppmv. These are larger values than those calculated in 1997, indicating that the time series had a larger average increase and standard deviation from 1998 to present day 2024. The histogram also shows a rightward shift in the distribution, indicating that the annual changes have generally increased.

We now look at the ACF plot and weekly CO₂ concentration across every year to gain further clarity on the seasonality.

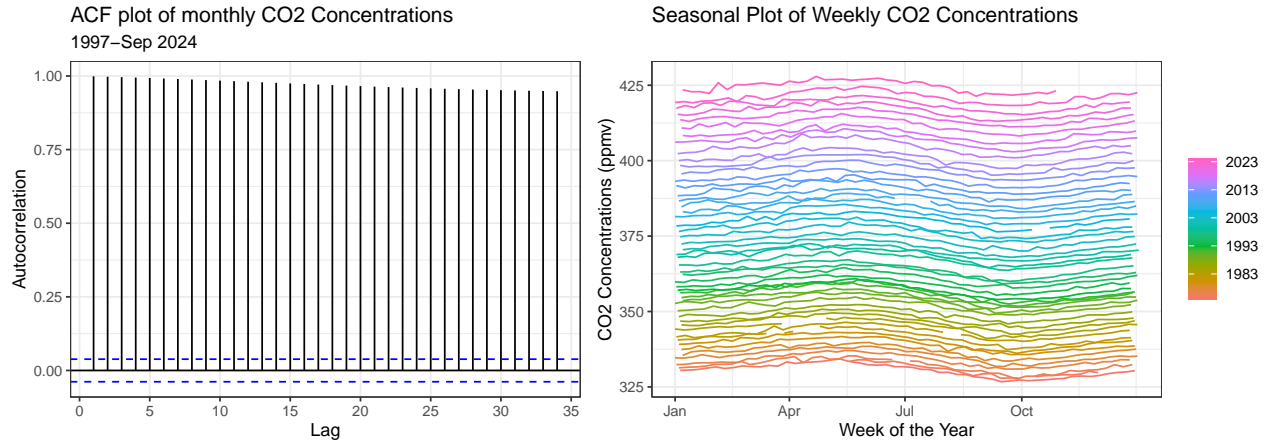


Figure 16: Observing seasonality in CO2 concentration

We see strong persistent autocorrelation for many lags, indicating an overall trend. The time series also shows strong evidence of seasonality corresponding closely with the meteorological seasons: the seasonal plot on the right shows that CO2 concentration peaks at the start of summer, and drops to a low in the fall, before rising again. These observations are consistent with the report from 1997.

We now study the time series' stationarity. We conduct the Augmented Dickey-Fuller (ADF) Test to test the null hypothesis that the time series is not stationary. As seen in the time series plot for `co2`, we have a clear upward trend, suggesting non-stationarity. However, this is *contrasted* by a p-value of 0.01 yielded by the test, which indicates sufficient evidence to reject the null hypothesis of non-stationarity. To look at stationarity in variance, we fit a yearly CO2 average on the monthly time series, and inspect the residuals from year to year. Although there are slight changes in the variance, they seem to regress to a constant variance over time. Thus, once we account for the yearly increases in CO2 ppmv, there is likely a constant variance over time.

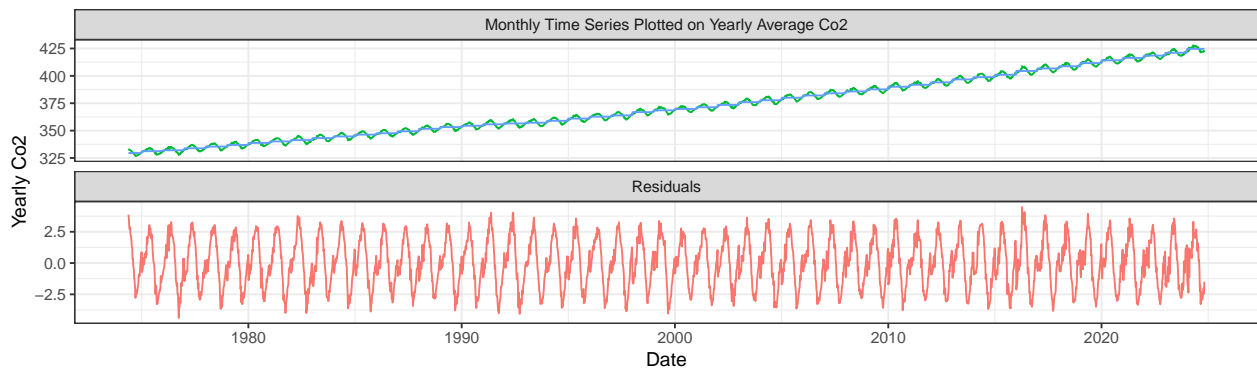


Figure 17: Studying variance over time

The new data collection method and techniques yield similar trends in average CO2 levels across months and years, with no notable deviations from prior patterns. Additionally, the residuals display consistent patterns, indicating that the updated methods align closely with previous data quality and trend behavior. The only detected change was the results of the adf test which found the CO2 values to be stationary.

2.3 (1 point) Task 2b: Compare linear model forecasts against realized CO2

We now compare the Polynomial (3) with `season` variable's forecasts with the realized CO2 levels.

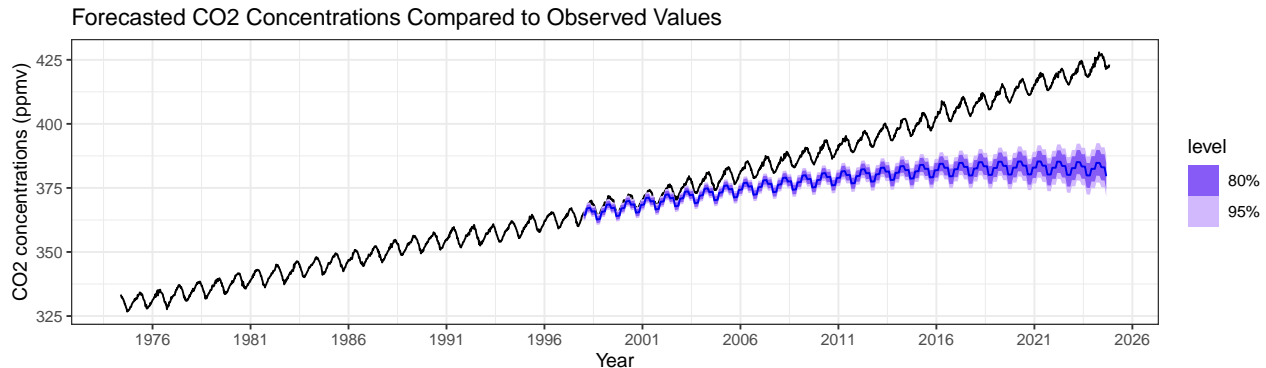


Figure 18: Forecasted with a Polynomial (3) with Season Variable Model

We see a clear mismatch in predictions from the plot above. The model had predicted a declining trend of CO2 concentrations, but actual concentrations seemed to increase fairly linearly. The declining trend was modeled with an expected curvilinear relationship with CO2 concentrations over time, as this fit better when looking at the time period between the 1950s and 1990s. However, the assumption of a the trend to taper off as suggested by the Polynomial (3) model is a strong, possibly unjustified one. Whether human-led efforts to reduce carbon emissions or efforts to restrict policy against reducing carbon emissions are sufficient to slow the trend requires further study and justification.

2.4 (1 point) Task 3b: Compare ARIMA models forecasts against realized CO2

We now compare the ARIMA(0,1,1)(0,1,1)[12] model's forecasts against the realized CO2 levels.

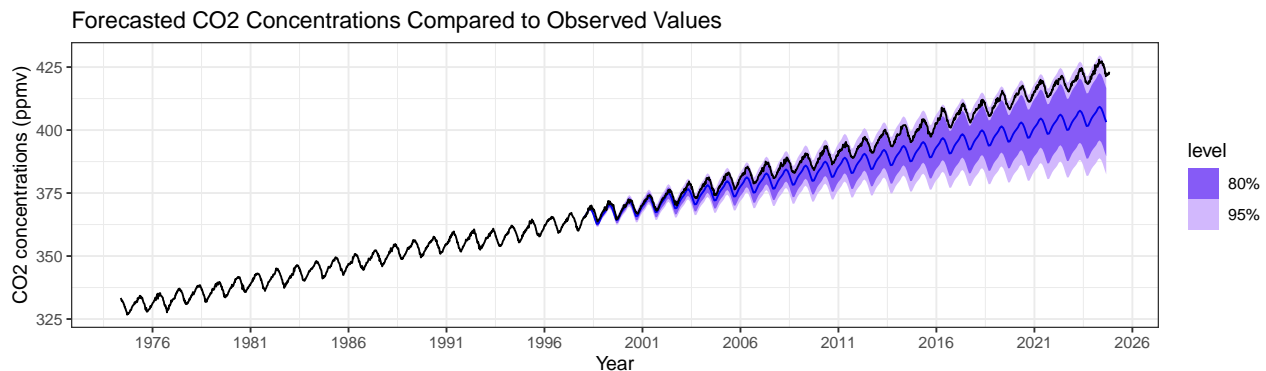


Figure 19: Forecasted with a ARIMA(0,1,1)(0,1,1)[12] Model

The ARIMA model, while closer in trend to the observed values than the curvilinear model, still underestimates the increases in global CO2 concentrations. The yearly fluctuations match better than the previous forecast and in the short-term the forecast performs well, but within 5 years the forecast diverges from actual concentrations and by 2020 we see concentrations of ~12.5 Co2 ppmv higher than anticipated. By 2024, the observed values are barely at the tail end of the 95% confidence interval, and look unlikely to stay within the confidence interval should the forecast continue.

2.5 (3 points) Task 4b: Evaluate the performance of 1997 linear and ARIMA models

Before, we expected that we would reach 420 ppmv around May of 2031, but the first date we past this threshold was in December of 2022. In other words, our predictions were nearly a decade off course. This may imply a more concerning trajectory for negative environmental outcomes than previously anticipated.

We now use the weekly data to generate a month-average series from 1997 to present-day 2024, and compare the overall forecasting performance of both the Polynomial (3) with `season` variable model, and the ARIMA model.

We do this by first comparing the Mean Absolute Error (MAE) and Root Mean Squared Error (RMSE) of each forecasting model, and conduct a significance test to formally compare the differences. We see that the polynomial season model has an MAE of ~ 15.8 , while the ARIMA model has lower MAE of ~ 7.3 . Similarly, we see that the polynomial season model has a higher RMSE of ~ 19.9 , while the ARIMA model has lower RMSE of ~ 8.9 . That the ARIMA model has lower errors suggests that it is a better fitting forecasting model. Finally, we conducted the Diebold-Mariano Test, which tests for differences in forecast errors, returns a significant p-value of less than $2.2e-16$, allowing us to reject the null hypothesis that the two forecasts have the same forecast accuracy.

2.6 (4 points) Task 5b: Train best models on present data

We now seasonally adjust the weekly data, and split both seasonally-adjusted (SA) and non-seasonally-adjusted (NSA) series into training and test sets, using the last two years (Oct 2022- Sep 2024) of observations as the test sets. We also use spline interpolation for 18 missing values. We obtain the decomposition in the plots below.

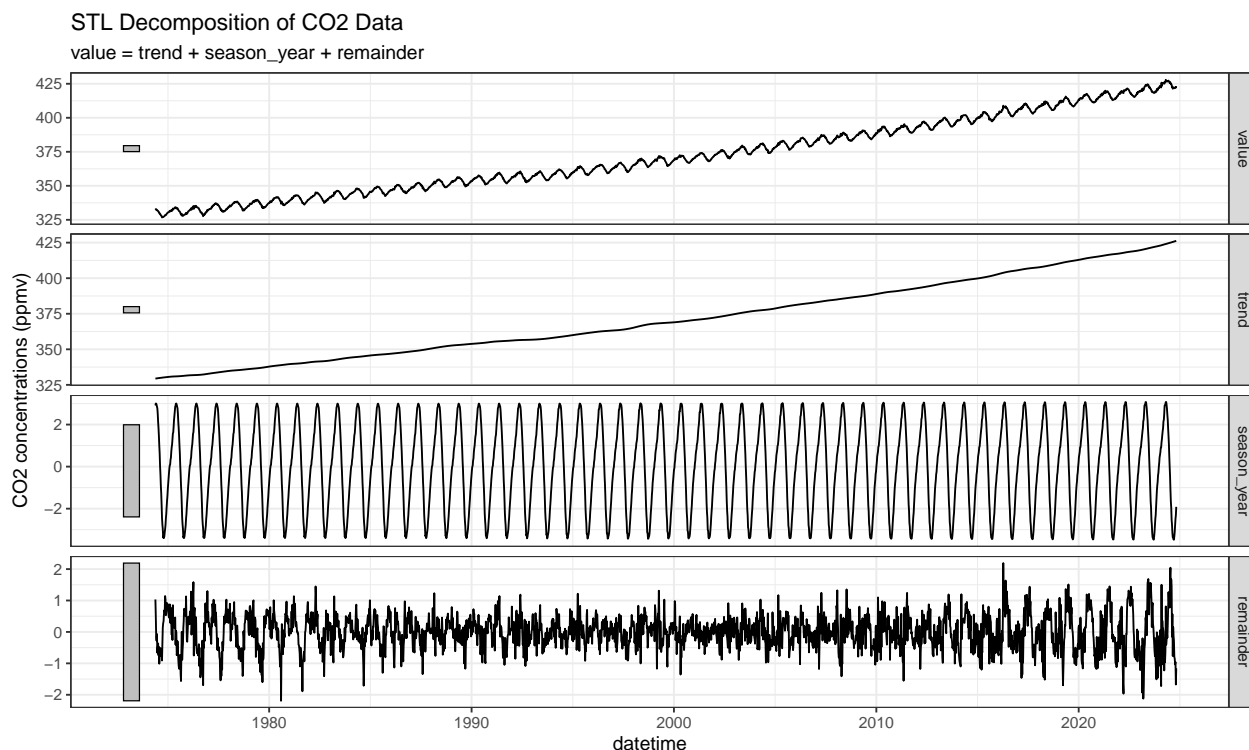


Figure 20: Clear seasonality and trend seen from decomposition

We now look at the ACFs and PACFs of the SA and NSA training data, with a difference of 1 and 52 to account for the overall trend and annual seasonality, to consider what ARIMA models we can fit to it.

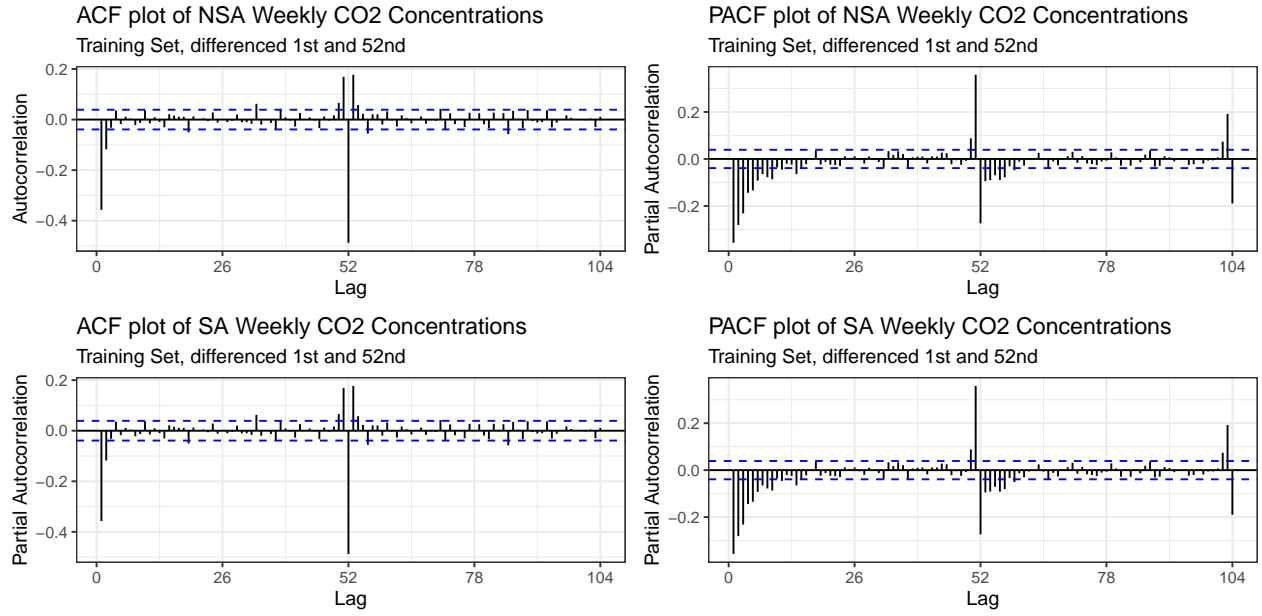


Figure 21: EDA on training and test sets

We note that the NSA ACF shows a sharp tapering off, while the PACF tapers off more slowly. This indicates perhaps a MA model might be more suitable. We also still see spikes at the 52th lags, indicating we could perhaps add an AR seasonal component. Still, we will let the `ARIMA` function choose a model for us. For the SA data, since it was already de-trended and we also see a tapering ACF and sharply dropping PACF, we will simply let the `ARIMA` function pick the best model. We get the tables below.

Table 3: NSA ARIMA Model Results

Model	AICc	BIC	LogLik
Auto: ARIMA(0,1,3)(2,1,0)[52]	3333.341	3368.181	-1660.653

Table 4: SA ARIMA Model Results

Model	AICc	BIC	LogLik
Auto: ARIMA(4,1,1)	2855.181	2895.969	-1420.568

Now we assess the residuals for the NSA model ARIMA(0,1,3)(2,1,0)[52]. We get the following plots.

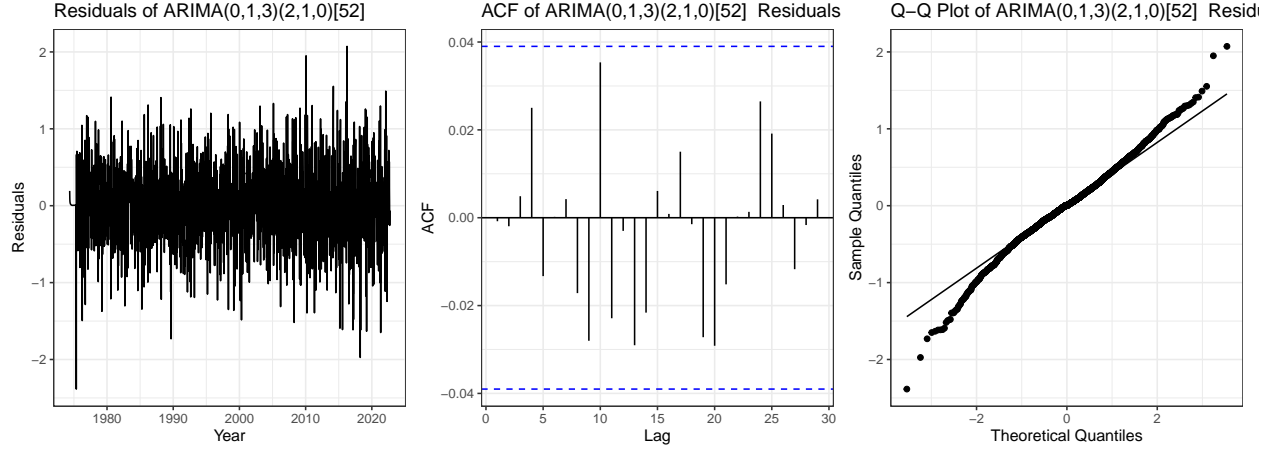


Figure 22: Evaluating ARIMA model for NSA data

The residuals mostly look like white noise, and the q-q plot is moderately close to a normal distribution. A Ljung Box Test on the residuals yielded a p-value of 0.1173, indicating insufficient evidence to reject the null-hypothesis that there is no auto-correlation. We are good with this model; we also note that it is a different model than that when trained on only data up to 1997. This could hint at inherent changes within the CO₂-generating system itself. We now proceed to assess the residuals for the SA data.

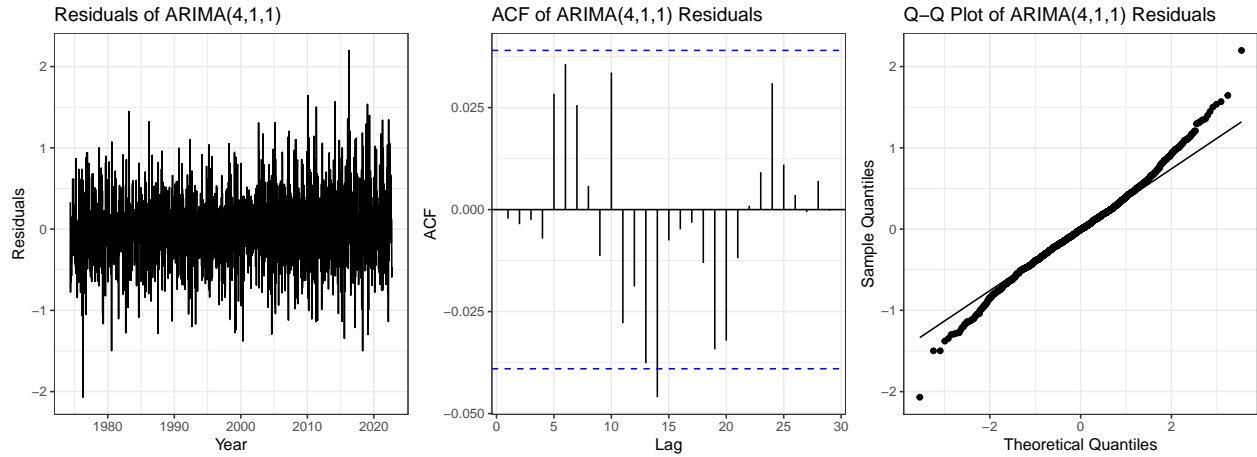


Figure 23: Evaluating ARIMA model for SA data

We can see that the residuals for the SA data do not look like white noise, and a Ljung-Box test yielded a p-value of $\sim 1.087e-09$, indicating sufficient evidence to reject the null-hypothesis that there is no auto-correlation in the residuals. We tried other models like an ARIMA(0,1,4) from studying the ACF and PACF plots, but it did not improve the results. Nonetheless, we now look at the forecasts of these two models on our test data. We now look at both the fit of our models on the actual data, as well as the forecasts for both models.

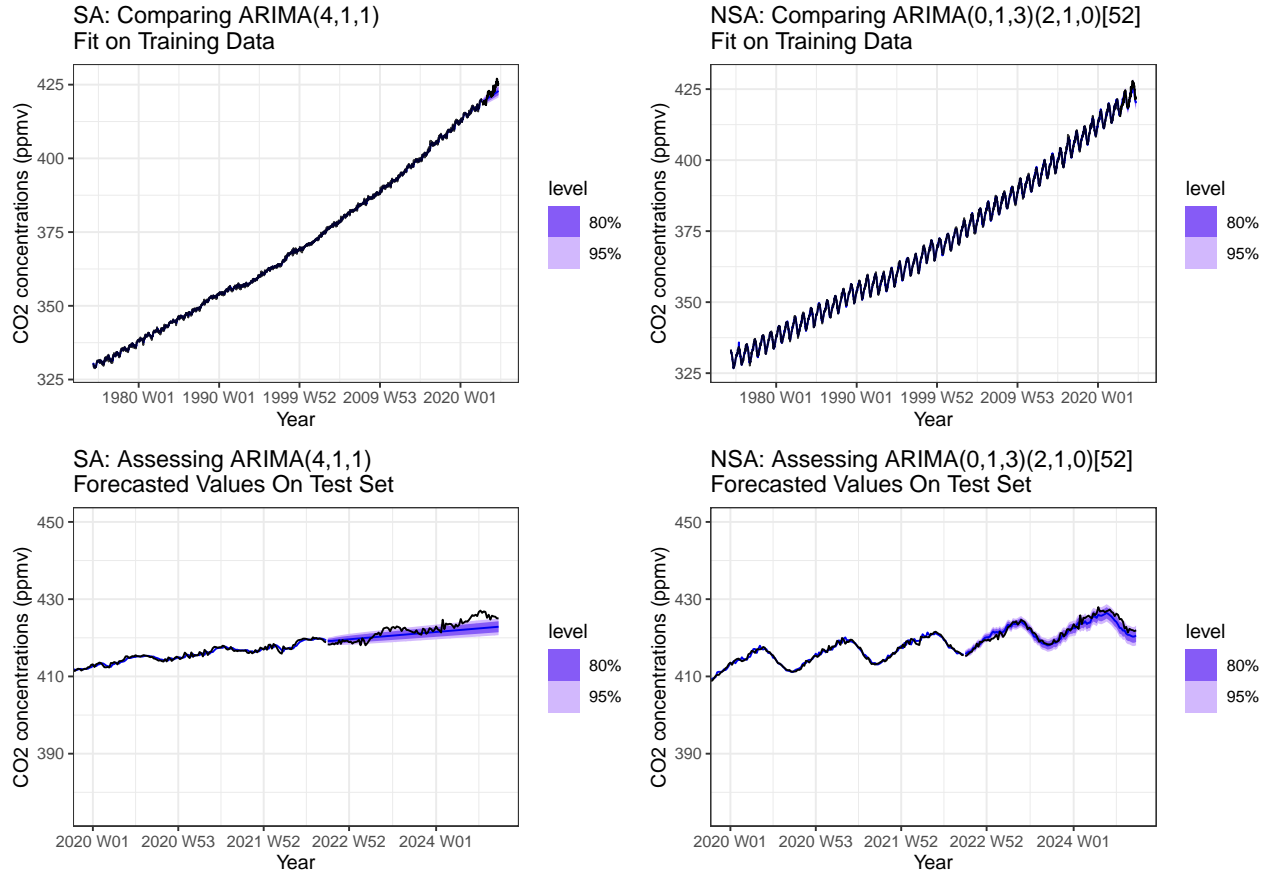


Figure 24: Assessing ARIMA Models on NSA and SA data

We can see that our models' fitted values in blue are extremely close to the actual values plotted in black in the top two plots. For the forecasts, both models 95% confidence intervals in blue included the actual data in black. However, the NSA model seemed to provide a closer fit to the actual data. We now compare both the RMSE and MAE of both models to assess the fits more quantitatively.

Table 5: Comparison of NSA and SA Models on Training and Test Sets

Metric	NSA.ARIMA.Model	SA.ARIMA.Model
RMSE (Training)	0.4687543	0.4248209
MAE (Training)	0.3551191	0.3248854
RMSE (Test)	1.0395081	1.8245332
MAE (Test)	0.8368190	1.4596259

As we see from the table above, the SA model outperformed the NSA model on the training set in both RMSE and MAE metrics, but the NSA model outperformed the SA model on the test set, indicating that the NSA model of $ARIMA(0,1,3)(2,1,0)[52]$ generalizes better. Given that our SA ARIMA model can be improved, we now fit a polynomial time-trend model for the SA series and compare it with the SA ARIMA model.

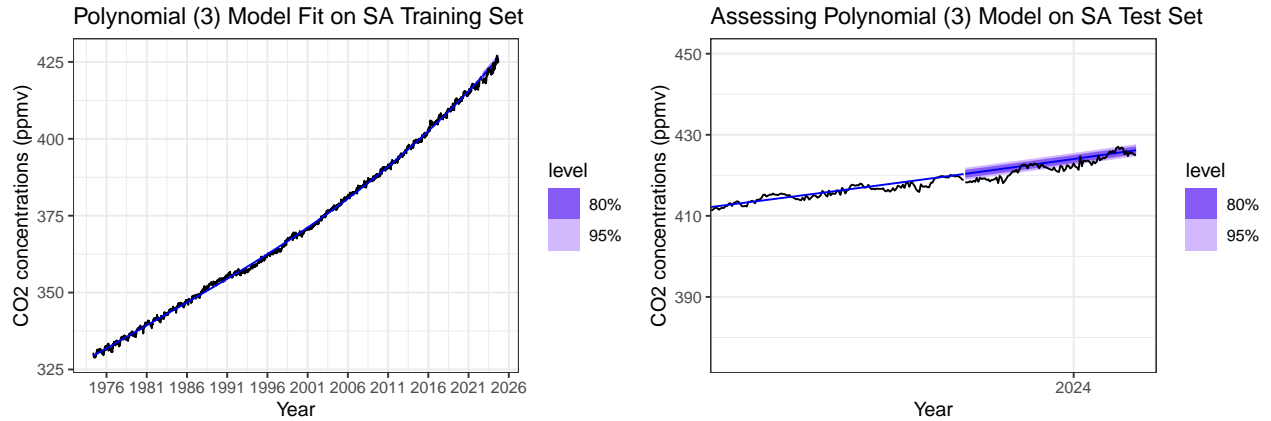


Figure 25: Assessing Polynomial (3) Model on SA data

We can see that Polynomial (3) model seems to fit the overall trend decently, although it does not perform so well on the forecast, with the actual data out of the 95% confidence interval. Interestingly, the Polynomial (3) model yielded a RMSE and MAE of 0.756 and 0.616 respectively for the training set, and a RMSE and MAE of 1.61 and 1.38 respectively for the test set. This means that although the SA ARIMA model outperformed the Polynomial (3) model on the training sets, the Polynomial (3) model did better with a lower RMSE and MAE on the test set.

2.7 (3 points) Task Part 6b: How bad could it get?

With the non-seasonally adjusted data series, we now generate predictions for when atmospheric CO2 is expected to be at 420 ppm and 500 ppm levels for the first and final times. We also generate a prediction for atmospheric CO2 levels in the year 2122.

Table 6: CO2 Levels and Forecasted Times ARIMA NSA with 80% Confidence Intervals

CO2.Level	First.Month	First.Value	Last.Month	Last.Value
420 ppm	2022 Dec	420.1 (419.3, 421.0)	2024 Sep	420.8 (419.1, 422.5)
500 ppm	2056 Feb	500.2 (448.5, 551.9)	2058 Aug	500.8 (443.3, 558.4)

Using the non-seasonally adjusted model, the table above presents projections for when atmospheric CO2 concentrations are anticipated to reach 420 ppm and 500 ppm levels, both for the first occurrence and the final plateau. This provides insights into the timeline of CO2 concentration milestones based on current trends, though it does not factor in potential mitigation efforts.

We now forecast for CO2 levels up to the year 2122 in following table, including the standard deviation. However, these projections do not account for current global initiatives aimed at reducing greenhouse gases, such as the transition from gas-powered vehicles to electric vehicles as part of the drive toward net-zero emissions. Given that CO2 levels are heavily influenced by human activities and policy changes, these forecasts are unlikely to be highly accurate over such a long horizon.

Table 7: CO2 Forecasts in 2122

Date	Value	SD
2122 W01	655.9	199.5
2122 W02	656.0	199.6
2122 W03	656.3	199.6
2122 W04	656.5	199.7
2122 W05	656.2	199.8
2122 W06	655.9	199.8
2122 W07	655.6	199.9
2122 W08	655.1	199.9
2122 W09	654.6	200.0
2122 W10	654.1	200.0
2122 W11	653.4	200.1
2122 W12	652.7	200.2
2122 W13	652.6	200.2
2122 W14	652.0	200.3
2122 W15	652.0	200.3
2122 W16	651.2	200.4
2122 W17	651.0	200.4
2122 W18	650.9	200.5
2122 W19	650.6	200.5
2122 W20	650.4	200.6
2122 W21	650.4	200.7
2122 W22	650.7	200.7
2122 W23	650.9	200.8
2122 W24	651.3	200.8
2122 W25	651.1	200.9
2122 W26	651.4	201.0
2122 W27	652.2	201.0
2122 W28	652.1	201.1
2122 W29	652.9	201.1
2122 W30	653.3	201.2
2122 W31	653.1	201.2
2122 W32	653.6	201.3
2122 W33	654.4	201.4
2122 W34	654.7	201.4
2122 W35	654.8	201.5
2122 W36	655.0	201.5
2122 W37	654.9	201.6
2122 W38	655.9	201.6
2122 W39	656.4	201.7
2122 W40	655.9	201.8
2122 W41	656.4	201.8
2122 W42	656.2	201.9
2122 W43	656.6	201.9
2122 W44	655.9	202.0
2122 W45	656.2	202.0
2122 W46	656.3	202.1
2122 W47	657.5	202.2
2122 W48	657.9	202.2
2122 W49	657.8	202.3
2122 W50	657.6	202.3
2122 W51	658.2	202.4
2122 W52	658.1	202.4
2122 W53	658.2	202.5