

1 Enumerating Arrangements of k items from n objects.

Tips for solving: Look at the simplest cases and try to work out the pseudo code for a recursive algorithm. Some of the functions defined can give clues as to what is to be done.

```
/* Consider all arrangements of k items
   from n objects. For n=3,k=2, they
   are 12,21,13,31,23,32. The number
   of such arrangements is
    $P_k = n(n-1) \cdots (n-k+2)(n-k+1)$ .
   Below is a program which when given n,k
   as input, prints all arrangements of k
   items from n objects. */
```

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>
typedef int** PermList;

int count_arrangements(int n, int k) {
    // Problem 1 a.) write a recursive
    // function logic here in one line to
    // compute the number of all arrangements
    // of k items from n objects. (2 marks)
}
```

```
PermList create_perm_list(int n,
                           int k) {
    int fn = count_arrangements(n, k);
    PermList pl = malloc(fn * sizeof(int *));
    for(int i = 0; i < fn; i++) {
        pl[i] = malloc(n * sizeof(int));
    }
    return pl;
}
```

```
void destroy_perm_list(PermList pl,
                       int n, int k) {
    int fn = count_arrangements(n, k);
    for (int i = 0; i < fn; i++) {
        free(pl[i]);
    }
    free(pl);
}
```

```
// given a 'small_row' of size 'size'
// copies it to 'big_row' which has size
// 'size+1'. Also sets the last position
// in 'big_row' to 'e'
```

```
void insert_and_copy(int* small_row, int size,
                     int e, int* big_row) {
    for (int i = 0; i < size; i++) {
        big_row[i] = small_row[i];
    }
    big_row[size] = e;
}
```

```
// checks if 'e' is in the 'row' of size 'size'
bool find(int e, int* row, int size) {
    for(int i = 0; i < size; i++) {
        if (row[i] == e) {
            return true;
        }
    }
    return false;
}
```

```
// find the numbers from {1,...,n}
// that are not in 'row' which is of size 'k'
// and puts them in 'elements'
void find_elements_not_in_row(int* row, int n,
                              int k,
                              int* elements) {
    int c = 0;
    for (int i = 0; i < n; i++) {
        if (find(i+1, row, k) == false) {
            elements[c++] = i+1;
        }
    }
}
```

```
PermList enumerate_arrangements(
    int n, int k) {
    PermList B = create_perm_list(n,k);
    if (k == 1) {
        // Problem 1 b.) write code here for base
        // case of recursively building list 'B'
        // of all arrangements of k=1 items
        // from {1,...,n}. (3 marks)
    } else {
        // Problem 1 c.) write code here for
        // recursively building list 'B' of all
        // arrangements of k items from
        // {1,...,n}. (5 marks)
    }
    return B;
}
```

```
void print_perm_list(PermList pl,
                     int n, int k) {
    int fn = count_arrangements(n, k);
    for(int i = 0; i < fn; i++) {
        for (int j = 0; j < k; j++) {
            printf("%d ", pl[i][j]);
        }
        printf("\n");
    }
}
```

```
int main() {
    int n = 10;
    int k = 5;
    print_perm_list(
        enumerate_arrangements(n, k), n, k);
    return 0;
}
```

2 Banking on Structs

```

1  /* Build a program for managing a bank.
2     There should be a database of bank
3     accounts and transactions. We should
4     be able to add new accounts,
5     new transactions (credit/debit) and
6     compute the balance of a account */
7  #include <stdio.h>
8  #include <string.h>
9
10 typedef enum AccountType {
11     Savings,
12     Current
13 } AccountType;
14
15 typedef enum TransactionType {
16     Credit,
17     Debit
18 } TransactionType;
19
20 typedef struct Transaction {
21     TransactionType type;
22     struct BankAccount* account;
23     int amount;
24 } Transaction;
25
26 typedef struct BankAccount {
27     char name[100];
28     int pin;
29     AccountType type;
30     // passbook is an array of transactions
31     // pointers to avoid taking too much memory
32     struct Transaction* passbook[1000];
33     int transactions_count;
34 } BankAccount;
35
36 typedef struct BankDatabase {
37     BankAccount accounts[1000];
38     Transaction transactions[10000];
39     int accounts_count;
40     int transactions_count;
41 } BankDatabase;
42
43 // compute the total amount of money
44 // with the bank amoung all the accounts
45 int compute_money_with_bank(
46     BankDatabase* db) {
47     int sum = 0;
48     for(int i = 0;
49         i < db->transactions_count; i++) {
50         switch(db->transactions[i].type) {
51             case Credit:
52                 sum += db->transactions[i].amount;
53                 break;
54             case Debit:
55                 sum -= db->transactions[i].amount;
56                 break;
57         }
58     }
59     return sum;
60 }

```

```

61 int compute_balance(BankAccount* acc) {
62     // Problem 2 a.) fill in the code to
63     // find the balance of the account
64     // 'acc'. (3 marks)
65 }
66
67 BankAccount* add_bank_account(char* name,
68     int pin, AccountType type,
69     BankDatabase* db) {
70     // Problem 2 b.) fill in the code to add
71     // a new account 'acc' to the bank
72     // database 'db'. The function should
73     // also return a pointer to the bank
74     // account created in 'db'. (3 marks)
75 }
76
77 Transaction* add_transaction(
78     TransactionType type,
79     BankAccount *account,
80     int amount, BankDatabase* db) {
81     // Problem 2 c.) Fill in the code for
82     // adding a transaction to the system.
83     // The logic should be written such
84     // that the all the other functions in
85     // this program continue to work
86     // correctly. (4 marks)
87 }
88
89 int main() {
90     BankDatabase db;
91     db.accounts_count = db.transactions_count = 0;
92     BankAccount acc = { .pin = 1234,
93         .transactions_count = 0};
94     strcpy(acc.name, "Ivan");
95     BankAccount* acc_ptr = add_bank_account(
96         acc.name, acc.pin, acc.type, &db);
97     add_transaction(Credit, acc_ptr, 10000, &db);
98     add_transaction(Debit, acc_ptr, 2000, &db);
99     add_transaction(Credit, acc_ptr, 5000, &db);
100
101     // should print 13000
102     printf("Account balance is %d\n",
103         compute_balance(acc_ptr));
104
105     BankAccount acc2 = { .pin = 6897,
106         .transactions_count = 0};
107     strcpy(acc2.name, "Jake");
108     BankAccount* acc_ptr2 = add_bank_account(
109         acc2.name, acc2.pin, acc2.type, &db);
110     add_transaction(Credit, acc_ptr2, 100000, &db);
111     add_transaction(Debit, acc_ptr2, 20000, &db);
112     add_transaction(Credit, acc_ptr2, 50000, &db);
113
114     // should print 130000
115     printf("Account balance is %d\n",
116         compute_balance(acc_ptr2));
117
118     // should print 143000
119     printf("Total Money with bank is %d\n",
120         compute_money_with_bank(&db));
121 }
122
123
124
125
126

```