

# Logarithms

Throughout the course, we will be working heavily with the **logarithm function**. Familiarize yourself with its definition, and make sure you are able to manipulate expressions and solve equations involving logarithms.

## Convention

We will write  $\log(x)$  for the base-2 logarithm of  $x$ . That is,  $\log x = \frac{\ln(x)}{\ln(2)}$ .

In particular, you should know the following facts:

$$\begin{aligned}\log(1) &= 0. \text{ For } 0 < x < 1 \text{ it holds that } \log(x) < 0, \text{ and for } x > 1, \text{ we have that } \log(x) > 0. \\ \log(2) &= 1. \\ \log(2^x) &= x. \\ 2^{\log(x)} &= x. \\ \log(x \cdot y) &= \log(x) + \log(y). \\ \log\left(\frac{x}{y}\right) &= \log(x) - \log(y). \\ \log(x^y) &= y \cdot \log(x). \\ x^{\log(y)} &= y^{\log(x)}.\end{aligned}$$

- The logarithm function is only defined on  $\mathbb{R}_+$ .
- The logarithm function is strictly increasing:  $\log(x) > \log(y)$  whenever  $x > y$ .
- $\log(x + y)$  and  $\log(x - y)$  do not generally have a simpler form.