## **Definition: Mutual Information**

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Let X and Y be random variables. The mutual information I(X;Y) of X and Y is defined as

$$I(X;Y) = H(X) - H(X|Y).$$

Thus, in a sense, mutual information reflects the reduction in uncertainty about X when we learn Y. Verify the following properties of the mutual information:

$$I(X;Y) = H(X) + H(Y) - H(XY)$$
 $I(X;Y) = I(Y;X)$  ("symmetry")
 $I(X;Y) \ge 0$  ("positivity")
 $I(X;Y) = 0 \text{ iff } X \text{ and } Y \text{ are independent}$ 
 $I(X;X) = H(X)$  ("self-information")

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