

# Assignment 1

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## question

Using the factor theorem show that  $x-2$  is a factor of  $x^3 + x^2 - 4x - 4$ . hence factorise the polynomial completely

roots are

$$\frac{-b \pm \sqrt{b^2 - 4 \times a \times c}}{2 \times a}$$

## solution:

By the factor theorem if  $f(a) = 0$ , then  $x - a$  will be factor of  $f(x)$

here  $b = 3, a = 1, c = 2$

so roots would be

let the given polynomial be  $f(x)$

$$\frac{-3 \pm \sqrt{3^2 - 4 \times 1 \times 2}}{2 \times 1}$$

$$f(x) = x^3 + x^2 - 4x - 4 \quad (1)$$

$$f(2) = 2^3 + 2^2 - 4 \times 2 - 4 \quad (2)$$

$$\implies f(2) = 0$$

$$(3) \quad \text{so other two factors are}$$

$x + 1$  and  $x + 2$

the final factors are

so,  $x-2$  is a factor of  $f(x)$ , now to factorise  $f(x)$

$x + 1, x - 2$  and  $x + 2$

$$(x^3 + x^2 - 4x - 4) \div (x - 2) = x^2 + 3x + 2 \quad f(x) = (x + 1) \times (x - 2) \times (x + 2)$$

$$\begin{array}{r} x^3 + x^2 - 4x - 4 \\ - x^3 + 2x^2 \\ \hline 3x^2 - 4x \\ - 3x^2 + 6x \\ \hline 2x - 4 \\ - 2x + 4 \\ \hline 0 \end{array}$$

we get  $x^2 + 3x + 2$

which is a quadratic expression so we can factorise it further by finding its roots