

Strings

- A string is a sequence of characters
- Examples of strings:
 - Java program
 - HTML document
 - DNA sequence
 - Digitized image
- ♠ An alphabet ∑ is the set of possible characters for a family of strings
- Example of alphabets:
 - ASCII
 - Unicode
 - **(0, 1)**
 - {A, C, G, T}



- Let P be a string of size m
 - A substring P[i..j] of P is the subsequence of P consisting of the characters with ranks between i and j
 - A prefix of P is a substring of the type P[0..i]
 - A suffix of *P* is a substring of the type *P*[*i* ..*m* − 1]
- Given strings T (text) and P (pattern), the pattern matching problem consists of finding a substring of T equal to P
- Applications:
 - Text editors
 - Search engines
 - Biological research

Pattern Matching

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Brute-Force Algorithm



- The brute-force pattern matching algorithm compares the pattern P with the text T for each possible shift of P relative to T, until either
 - a match is found, or
 - all placements of the pattern have been tried
- Brute-force pattern matching runs in time O(nm)
- Example of worst case:
 - $T = aaa \dots ah$
 - P = aaah
 - may occur in images and DNA sequences
 - unlikely in English text

Algorithm BruteForceMatch(T, P)

Input text *T* of size *n* and pattern *P* of size *m*

Output starting index of a substring of *T* equal to *P* or -1 if no such substring exists

for $i \leftarrow 0$ to n - m

{ test shift *i* of the pattern }

 $i \leftarrow 0$

while $j < m \land T[i+j] = P[j]$

 $j \leftarrow j + 1$

if j = m

return i {match at i}

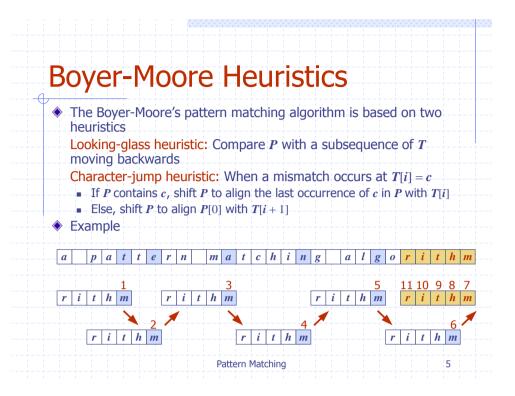
else

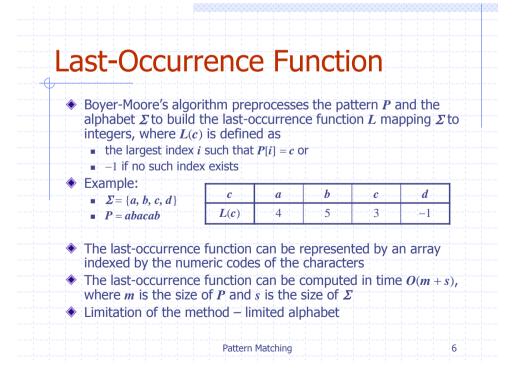
break while loop {mismatch}

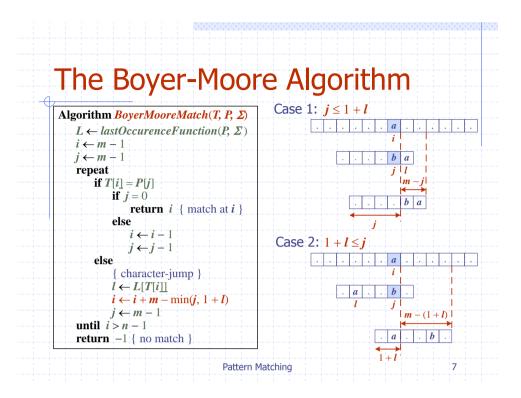
return -1 {no match anywhere}

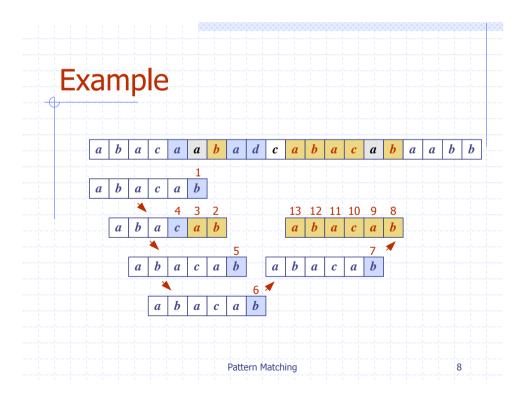
Pattern Matching

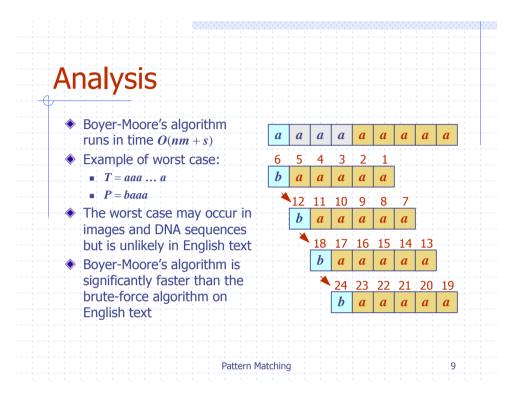
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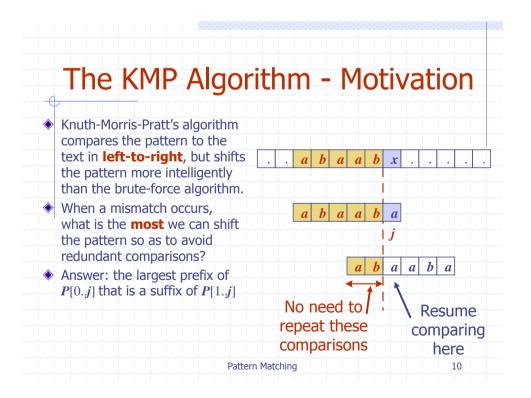


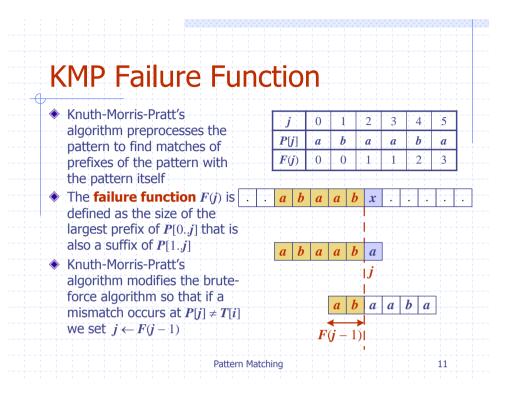


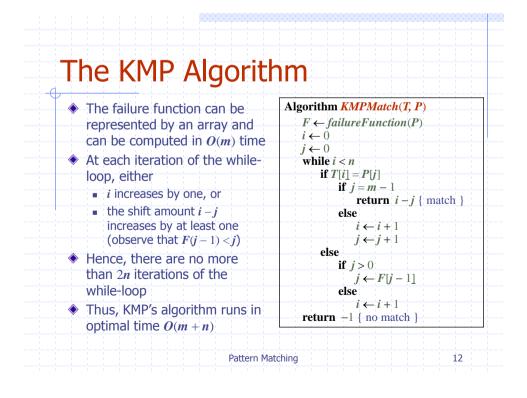












Computing the Failure Function

- ◆ The failure function can be represented by an array and can be computed in O(m) time
- The construction is similar to the KMP algorithm itself
- At each iteration of the whileloop, either
 - *i* increases by one, or
 - the shift amount i j increases by at least one (observe that F(j-1) < j)</p>
- Hence, there are no more than 2m iterations of the while-loop

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Algorithm failure Function (P)

F[0] \leftarrow 0
i \leftarrow 1
j \leftarrow 0
while i < m
if P[i] = P[j]
{we have matched j + 1 chars}
F[i] \leftarrow j + 1
i \leftarrow i + 1
j \leftarrow j + 1
else if j > 0 then
{use failure function to shift P}
j \leftarrow F[j - 1]
else
F[i] \leftarrow 0 \text{ {no match }}
i \leftarrow i + 1
```

Pattern Matching

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