

# Bubble Sort

9 1 3 2 4

1 9 3 2 4

1 3 9 2 4

1 3 2 9 4

1 3 2 4 9

1 2 3 4 9

1 2 3 4 9

1 2 3 4 9

1 2 3 4 9

For size 5,

4+3+2+1 comparisions  
and up to  
the same swaps

For size  $n$

$$(n-1) + (n-2) + \dots + 1$$

$$\frac{n \cdot (n-1)}{2} = \frac{1}{2}n^2 - \frac{1}{2}n$$

$$\approx O(n^2)$$

Visually

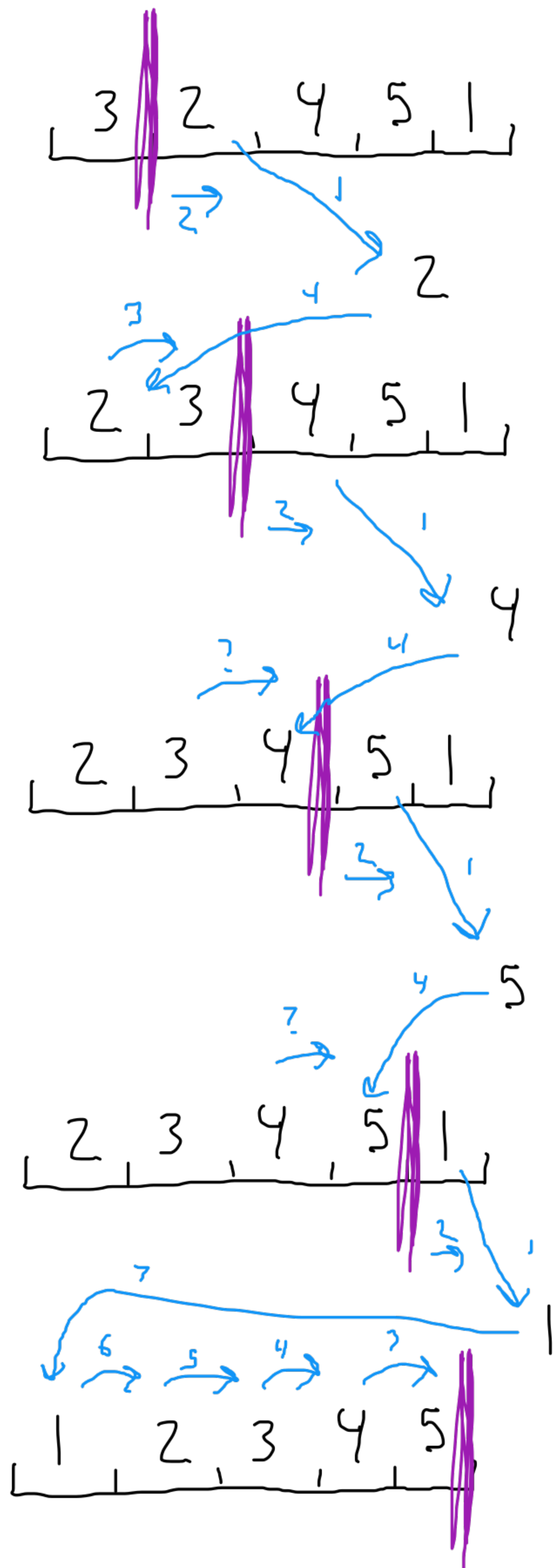


$\approx$  a triangle

$$\frac{(n-1)(n-1)}{2} = O(n^2)$$

This is a stable

# Insertion Sort



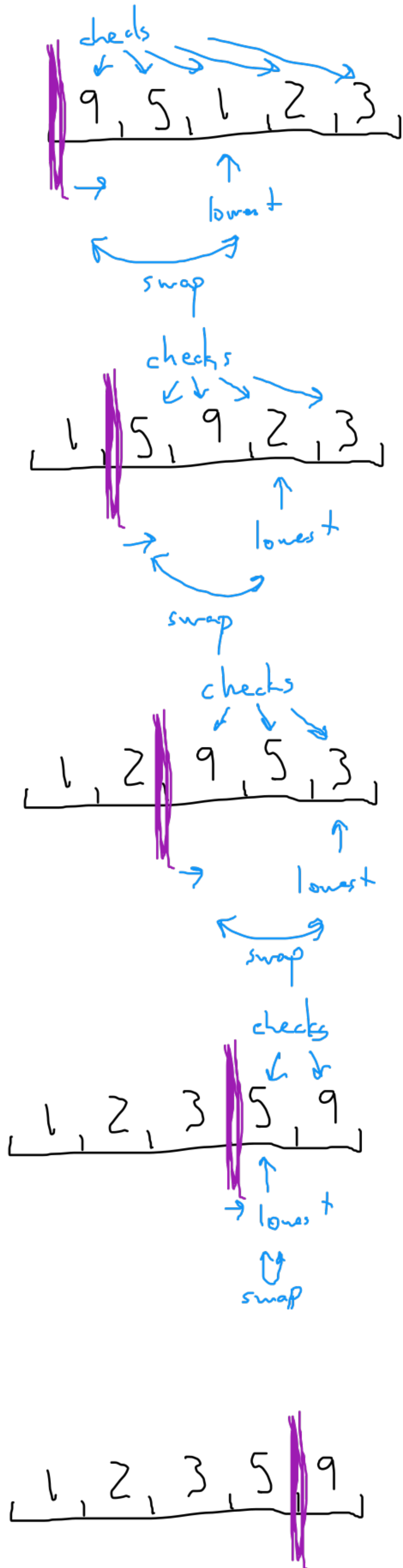
For 5 items,  
we do up to

$$1 + 2 + 3 + 4 = 10 \text{ moves}$$

This is the  
same sequence in  
reverse, so  $O(n^2)$

This is a  
stable sort

# Selection Sort



For 5 items,  
there are 4 swaps

$$O(n)$$

But there are

$$(n-1) + (n-2) + \dots + 1$$

comparisons

$$\text{This is } O(n^2)$$

Due to the large  
swaps, this is  
not a stable sort.