Given a binary array nums and an integer goal, return the number of non-empty subarrays with a sum goal.

A **subarray** is a contiguous part of the array.

Example 1:

```
Input: nums = [1,0,1,0,1], goal = 2
Output: 4
Explanation: The 4 subarrays are bolded and underlined below: [\frac{1,0,1}{0},0,1]
[\frac{1,0,1,0}{0},1]
[1,0,1,0,1]
[1,0,\frac{1}{0},0,1]
```

Example 2:

```
Input: nums = [0,0,0,0,0], goal = 0
Output: 15
```

Constraints:

- 1 <= nums.length <= 3 * 104
- nums[i] is either 0 or 1.
- 0 <= goal <= nums.length

Overview

We are given a binary array nums and an integer goal. The task is to find the number of non-empty subarrays in the given binary array where the sum of elements in the subarray equals the specified goal.

Key Observations:

- 1. The array contains only binary values (0 or 1).
- 2. The goal is to find subarrays with a specific sum.
- 3. The subarrays should be non-empty and contiguous.

Consider the given example with nums = [1,0,1,0,1] and goal = 2:

Output: 4

Explanation: The 4 subarrays are **bolded** and <u>underlined</u> below:

[**1,0,1**,0,1]

[**1,0,1,0**,1]

[1,**0,1,0,1**]

[1,0,**1,0,1**]

Note that all these subarrays are contiguous parts of the given array, and the count of such subarrays is the output.

```
Prefix sum+two pointers (at most(goal)-at most(goal-1))
  Time complexity: O(n)
  Space complexity: O(1)
class Solution {
public:
  int numSubarraysWithSum(vector<int>& nums, int goal) {
    int n=nums.size();
    auto at_most=[&](int k)->int{
       int ans=0;
       int l=0,prefix_sum=0;
       // Expand the window from the right
       for(int r=0;r< n;++r){
         prefix_sum+=nums[r];
         // Shrink the window while sum is greater than k
         while(l<=r && prefix_sum>k){
           prefix_sum-=nums[l]; // Update the sum
            1++; // Shrink the window from the left
         }
         // Compute the number of subarrays with sum at most k
         ans+=r-l+1;
       }
       return ans;
     };
    // Illustrated by Venn diagram
    return at_most(goal)-at_most(goal-1);
  }
};
```

```
Prefix sum+two pointers (at least(goal)-at least(goal+1))
  Time complexity: O(n)
  Space complexity: O(1)
class Solution {
public:
  int numSubarraysWithSum(vector<int>& nums, int goal) {
     int n=nums.size();
     auto at_least=[&](int k)->int{
       int ans=0;
       int l=0,prefix_sum=0;
       for(int r=0;r< n;++r){
         prefix_sum+=nums[r];
          while(l<=r && prefix_sum>=k){
            // Compute the number of subarrays with sum at least k
            ans+=n-r;
            prefix_sum-=nums[l];
            <u>l++;</u>
          }
       }
       return ans;
     };
    // Illustrated by Venn diagram
     return at_least(goal)-at_least(goal+1);
  }
};
```

3306. Count of Substrings Containing Every Vowel and K Consonants II

You are given a string word and a **non-negative** integer k.

Return the total number of $\ \$ of word that contain every vowel ('a', 'e', 'i', 'o', and 'u') at least once and exactly k consonants.

Example 1:

Input: word = "aeioqq", k = 1

Output: 0

Explanation:

There is no substring with every vowel.

Example 2:

Input: word = "aeiou", k = 0

Output: 1

Explanation:

The only substring with every vowel and zero consonants is word[0..4], which is "aeiou".

Example 3:

Input: word = "ieaouqqieaouqq", k = 1

Output: 3

Explanation:

The substrings with every vowel and one consonant are:

- word[0..5], which is "ieaouq".
- word[6..11], which is "qieaou".
- word[7..12], which is "ieaouq".

Constraints:

- 5 <= word.length <= 2 * 105
- word consists only of lowercase English letters.
- $0 \le k \le word.length 5$

3306. Count of Substrings Containing Every Vowel and K Consonants II

```
Prefix sums+two pointers+at last(k)-at last(k+1)
  Time compelxity: O(n)
  Space compelxity: O(1)
*/
typedef long long ll;
typedef std::vector<int> vi;
typedef std::vector<vi>vvi;
class Solution {
  public:
    ll countOfSubstrings(std::string word, int k) {
       int n=word.size();
       auto is_vowel=[&](char letter)->bool{
          return letter=='a' || letter=='e' || letter=='i'|| letter=='o' || letter=='u';
       };
       // Funtion to check if we have, in range[l,r], at least one occurence of a vowel, and
       // at least k consonant.
       auto is_possible=[&](int& count_a,
                      int& count_e,
                      int& count i,
                      int& count_o,
                      int& count_u,
                      int& count_cons,
                      int k)->bool{
          return count_a>=1 &&
            count_e>=1 &&
            count i \ge 1 \&\&
            count_o>=1 &&
            count_u>=1 &&
            count_cons>=k;
       };
```

```
// Function to check if we have, in the whole word, at least one occurrence of a vowel, and
       // at least k consonant.
       auto at_least=[&](int k)->ll{
         ll ans=0;
         int l=0;
          int count_a=0,count_e=0,count_i=0,count_o=0,count_u=0,count_cons=0;
          for(int r=0;r< n;++r){
            count_a+=(word[r]=='a');
            count_e+=(word[r]=='e');
            count_i+=(word[r]=='i');
            count_o+=(word[r]=='o');
            count_u+=(word[r]=='u');
            count_cons+=(!is_vowel(word[r]));
            while(is_possible(count_a,count_e,count_i,count_o,count_u,count_cons,k)){
               count_a-=(word[l]=='a');
              count_e-=(word[l]=='e');
               count_i-=(word[l]=='i');
               count_o-=(word[l]=='o');
               count_u-=(word[l]=='u');
               count_cons-=(!is_vowel(word[l]));
               ans+=n-r;
               l++;
            }
          }
         return ans;
       };
       return at_least(k)-at_least(k+1);
};
```