2523. Closest Prime Numbers in Range

Given two positive integers left and right, find the two integers num1 and num2 such that:

- left <= num1 < num2 <= right .
- Both num1 and num2 are.
- num2 num1 is the **minimum** amongst all other pairs satisfying the above conditions.

Return the positive integer array ans = [num1, num2]. If there are multiple pairs satisfying these conditions, return the one with the **smallest** num1 value. If no such numbers exist, return [-1, -1].

Example 1:

Input: left = 10, right = 19

Output: [11,13]

Explanation: The prime numbers between 10 and 19 are 11, 13, 17, and 19.

The closest gap between any pair is 2, which can be achieved by [11,13] or [17,19].

Since 11 is smaller than 17, we return the first pair.

Example 2:

Input: left = 4, right = 6

Output: [-1,-1]

Explanation: There exists only one prime number in the given range, so the

conditions cannot be satisfied.

Constraints:

• $1 \le \text{left} \le \text{right} \le 10^6$

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```
Sieve of Eratosthenes: store all primes numbers
  Time complexity: O(\text{right.log}(\log(\sqrt{\text{right}})) + (\text{right-left}) + m)
  Space complexity: O(\text{right} + m)
                                            ○ Runtime
                                                                                        @ Memory
*/
                                            154 ms | Beats 68.52%
                                                                                        168.24 MB | Beats 9.44%
class Solution {
  public:
     std::vector<int> closestPrimes(int left, int right) {
       // Build Sieve of Eratosthenes's array
       // TC: O(\text{right.log}(\log(\sqrt{\text{right}})))
       // SC: O(right)
        std::vector<int> is_prime(right+1,true);
        is_prime[0]=is_prime[1]=false;
        for(int i=2;i*i<=right;++i){
          if(is_prime[i]){
             for(int j=i*i;j<=right;j+=i) is_prime[j]=false;</pre>
          }
        }
        // Store all primes numbers in range[left,right]
        // TC: O(right-left)
        // SC: O(m)
        std::vector<int> primes;
        for(int i=left;i<=right;++i){</pre>
          if(is_prime[i]) primes.push_back(i);
        }
```

```
// Get the two closest prime numbers in range [left,right]
       // TC: O(m)
       // SC: O(1)
       // Get the primes size
       int m=primes.size();
       // if size<2, means there is no pair
       if(m<2) return {-1,-1};
       int diff=INT_MAX; // Track the minimum difference
       int prime1,prime2; // Track pair of the two closest primes numbers
       // Iterate all over primes numbers found in range[left,right]
       for(int i=0;i<m-1;++i){
         // If their difference is less than the minimum difference found so far
          if(primes[i+1]-primes[i]<diff){</pre>
            diff=primes[i+1]-primes[i]; // Minimize the difference
            // Update the answer
            prime1=primes[i];
            prime2=primes[i+1];
          }
       }
       return{prime1,prime2};
};
```

2523. Closest Prime Numbers in Range

```
Sieve of Eratosthenes: Track pair of the two adjacent prime numbers
  Time complexity: O(\text{right.log}(\log(\sqrt{\text{right}})) + (\text{right-left}))
  Space complexity: O(right)
*/
                                                                              158.87 MB | Beats 16.67%
                                     87 ms | Beats 80.74% 🞳
class Solution {
  public:
     std::vector<int> closestPrimes(int left, int right) {
        // Build Sieve of Eratosthenes's array
        // TC: O(\text{right.log}(\log(\sqrt{\text{right}})))
        // SC: O(right)
        std::vector<int> is_prime(right+1,true);
        is_prime[0]=is_prime[1]=false;
        for(int i=2;i*i<=right;++i){</pre>
           if(is_prime[i]){
             for(int j=i*i;j<=right;j+=i) is_prime[j]=false;</pre>
           }
        }
```

```
// Get the two first smallest prime number
  // TC: O(right))
  // SC: O(1)
  int diff=INT_MAX; // To minimize the difference
  int prev_prime=-1,next_prime=-1; // Track the two adjacent primes numbers
  int prime1=-1,prime2=-1; // Track the two primes numbers with minimum difference
  for(int cur num=left;cur num<=right;++cur num){</pre>
    // If current number is not prime, pass the next number
    if(!is_prime[cur_num]) continue;
    // If current number is prime:
    // If we still don't have the previous prime number and the
    // the current number will be the previous prime number
    if(prev_prime==-1) prev_prime=cur_num;
    // If we still don't have the next prime number that immediately
    // follows the previous prime number
    // the current number will be the next prime number
    else if(next_prime==-1) next_prime=cur_num;
    // Once we have both the two adjacent prime numbers
    if(next_prime!=-1 && prev_prime!=-1){
      // If difference between the two adjacent prime numbers is less or equal than 2
      // This is the minimum difference that we can have
       int d=next_prime-prev_prime;
       if(d<=2) return {prev_prime,next_prime};</pre>
      // If their difference is less than minimal difference found so far
       if(d<diff){
         diff=d; // Minimize the difference
         // Update the answer
         prime1=prev_prime;
         prime2=next_prime;
       }
       // Pass to the two next adjacent prime numbers
       prev_prime=next_prime;
       next_prime=-1;
    }
  return {prime1,prime2};
}};
```