

Leet code: 136.Single Number

Problem statement

Given a **non-empty** array of integers `nums`, every element appears twice except for one. Find that single one.

You must implement a solution with a **linear runtime complexity** and **use only constant extra space**.

Example 1:

Input: `nums = [2,2,1]`

Output: 1

Example 2:

Input: `nums = [4,1,2,1,2]`

Output: 4

Example 3:

Input: `nums = [1]`

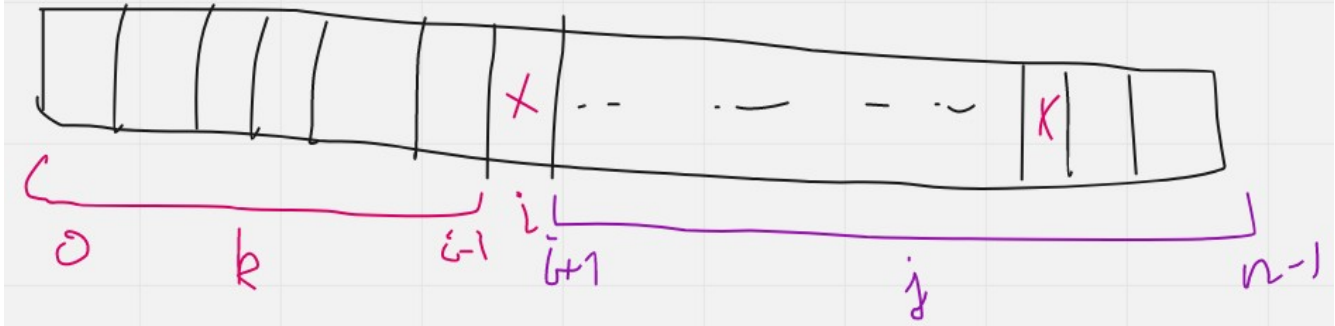
Output: 1

Constraints:

- `1 <= nums.length <= 3 * 104`
- `-3 * 104 <= nums[i] <= 3 * 104`
- Each element in the array appears twice except for one element which appears only once.

Brute force

for every number in the array, check if it exists in the right side of the array **and** in the left side of the array.



C++ >= 11

```
class Solution {
public:
    int singleNumber(vector<int>& nums) {
        int n = nums.size();
        for(int i = 0 ; i < n ; ++i){
            int j = i+1;
            while (j < n && nums[i] != nums[j]) j++;
            int k = i-1;
            while (k >= 0 && nums[i] != nums[k]) k--;

            if (j == n && k == -1) return nums[i];
        }
        return -1;
    }
};
```

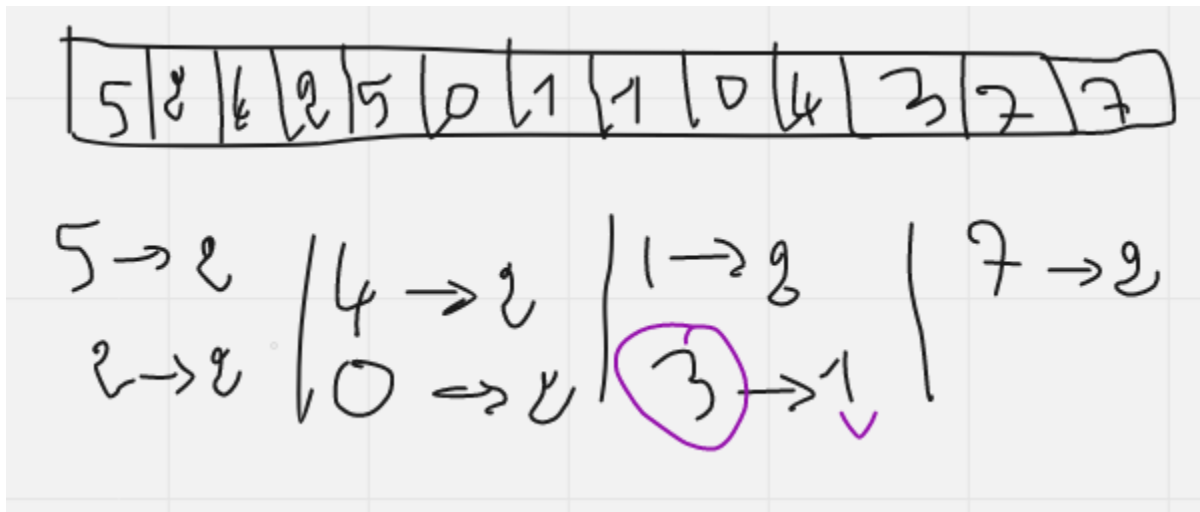
Time complexity: $O(n^2)$

Auxiliary space complexity: $O(1)$

Frequency array

Using a frequency array to **count the occurrence of each number**, then **iterate over that frequency array, if we find a number that appears once, then take it.**

Example:



C++ >= 11

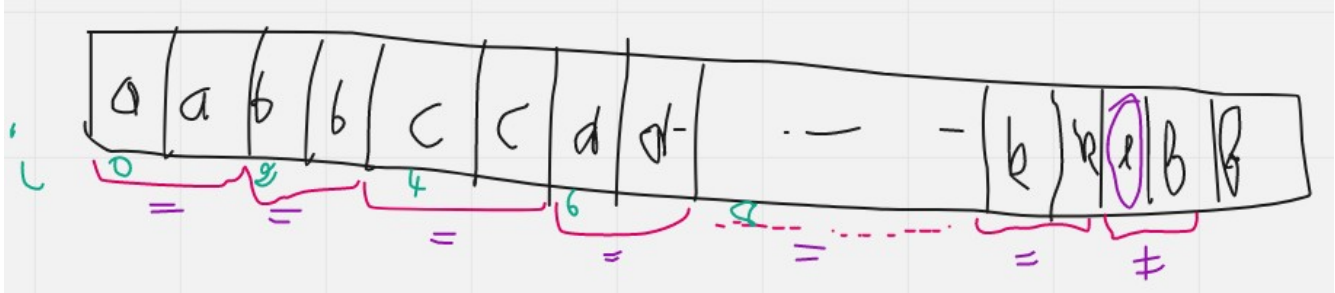
```
class Solution {
public:
    int singleNumber(vector<int>& nums) {
        unordered_map<int, int> f;
        for(auto x: nums){
            f[x]++;
        }
        for (auto x: f){
            if (x.second == 1) return x.first;
        }
        return -1;
    }
};
```

Time complexity: $O(n)$

Auxiliary space complexity: $O(n)$

Sorting

Sort the array, and check the numbers every two adjacent numbers, if we find two numbers not equal we take the first one.



C++ >= 11

```
class Solution {
public:
    int singleNumber(vector<int>& nums) {
        int n = nums.size();
        sort(nums.begin(), nums.end());
        int i = 0;
        while (i < n-1 && nums[i] == nums[i+1]) i += 2;
        if (i <= n-1) return nums[i];
        return -1;
    }
};
```

Time complexity: $O(n \log n) + O(n)$

Auxiliary space complexity: $O(1)$

Xor

Properties

https://en.wikipedia.org/wiki/Exclusive_or#Properties

$$0 \oplus 0 = 0$$

$$a \oplus a = 0$$

$$a \oplus 0 = a$$

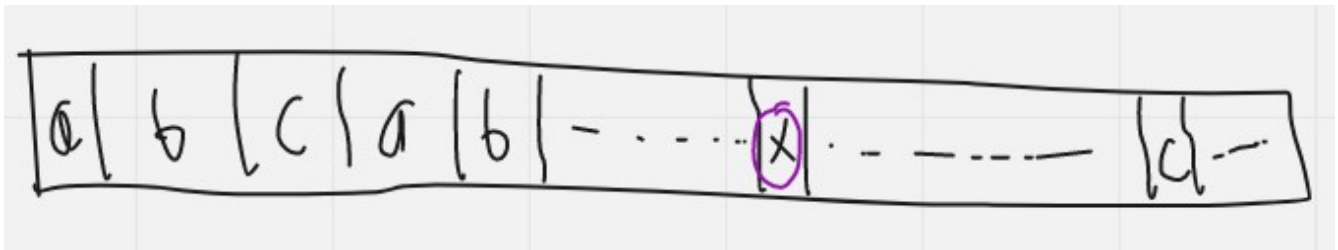
$$a \oplus b = b \oplus a$$

$$a \oplus (b \oplus c) = (a \oplus b) \oplus c$$

$$a \oplus (b \oplus a) = a \oplus (a \oplus b) = (a \oplus a) \oplus b = 0 \oplus b = b$$

Main idea of the solution

Every element in the array appears twice except one.



We can write:

$$(a \oplus a) \oplus (b \oplus b) \oplus (c \oplus c) \oplus \dots \oplus x = 0 \oplus 0 \oplus 0 \oplus \dots \oplus x = 0 \oplus x = x$$

C++ >= 11

```
class Solution {
public:
    int singleNumber(vector<int>& nums) {
        int ans = 0;
        for(auto x: nums){
            ans ^= x;
        }
        return ans;
    }
};
```

Time complexity: $O(n)$

Space complexity: $O(1)$