2683. Neighboring Bitwise XOR

A **0-indexed** array derived with length n is derived by computing the **bitwise XOR** (\oplus) of adjacent values in a **binary array** original of length n.

Specifically, for each index i in the range [0, n - 1]:

- If i = n 1, then derived[i] = original[i] ⊕ original[0].
- Otherwise, derived[i] = original[i] ⊕ original[i + 1].

Given an array derived, your task is to determine whether there exists a **valid binary array** original that could have formed derived.

Return true if such an array exists or false otherwise.

• A binary array is an array containing only **0**'s and **1**'s

Example 1:

```
Input: derived = [1,1,0]
Output: true
Explanation: A valid original array that gives derived is [0,1,0].
derived[0] = original[0] \oplus original[1] = 0 \oplus 1 = 1
derived[1] = original[1] \oplus original[2] = 1 \oplus 0 = 1
derived[2] = original[2] \oplus original[0] = 0 \oplus 0 = 0
```

Example 2:

```
Input: derived = [1,1]
Output: true
Explanation: A valid original array that gives derived is [0,1].
derived[0] = original[0] @ original[1] = 1
derived[1] = original[1] @ original[0] = 1
```

Example 3:

```
Input: derived = [1,0]
Output: false
Explanation: There is no valid original array that gives derived.
```

Constraints:

- n == derived.length
- 1 <= $n <= 10^5$
- The values in derived are either 0's or 1's

Overview

We are given an integer array derived of length n. This array is formed by taking a binary array original (an array containing only 0s and 1s) and computing the bitwise XOR between adjacent elements in it.

For the last element in derived, the XOR is calculated as: $derived[n-1] = original[n-1] \oplus original[0]$

Our task is to determine if there exists a binary array *original* that could have generated the *derived* array.

To understand how to approach the problem, let's recall some fundamental properties of XOR:

1. Commutativity: $a \oplus b = b \oplus a$

The order in which you XOR two numbers doesn't matter.

2. Associativity: $(a \oplus b) \oplus c = a \oplus (b \oplus c)$

Grouping of *XOR* operations doesn't affect the result.

3. Identity: $a \oplus 0 = a$

XOR with 0 leaves the number unchanged.

4. Self-inverse: $a \oplus a = 0$

XORing a number with itself results in 0.

5. Inversion:

If $a \oplus b = c$, then:

- $a=b\oplus c$
- •
- $b=a\oplus c$

These properties will help us manipulate XOR equations in coming sections to solve the problem.

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```
/*
    Xor properties
    Time complexity: O(n)
    Space complexity: O(1)

*/

class Solution {
    public:
        bool doesValidArrayExist(std::vector<int>& derived){
        int total_xor=0;
        for(auto& e: derived) total_xor^=e;
        return total_xor==0;
    }
};
```

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```
Based on Xor properties: count #1s

Time complexity: O(n)
Space complexity: O(1)

*/

class Solution {
public:
bool does ValidArrayExist(std::vector<int>& derived){
    int s=std::accumulate(derived.begin(),derived.end(),0);
    return s%2==0;
}
};
```