Given the string S, return the size of the longest substring containing each vowel an even number of times. That is, 'a', 'e', 'i', 'o', and 'u' must appear an even number of times.

Example 1:

Input: s = "eleetminicoworoep"

Output: 13

Explanation: The longest substring is "leetminicowor" which contains two each of

the vowels: \mathbf{e} , \mathbf{i} and \mathbf{o} and zero of the vowels: \mathbf{a} and \mathbf{u} .

Example 2:

Input: s = "leetcodeisgreat"

Output: 5

Explanation: The longest substring is "leetc" which contains two e's.

Example 3:

Input: s = "bcbcbc"

Output: 6

Explanation: In this case, the given string "bcbcbc" is the longest because all

vowels: \mathbf{a} , \mathbf{e} , \mathbf{i} , \mathbf{o} and \mathbf{u} appear zero times.

Constraints:

- 1 <= s.length <= 5 x 10⁵
- S contains only lowercase English letters.

```
Brute force - TLE
  Time complexity: O(n^2 *(26+n+26)) = O(n^3+2*26.n^2) = O(n^3)
  Space complexity: O(26)=O(1)
*/
class Solution {
  public:
     int findTheLongestSubstring(std::string s) {
        int n=s.size();
        int ans=0;
        for(int left=0;left<n;++left){</pre>
           for(int right=left;right<n;++right){</pre>
             std::vector<int> freq(26,0);
             for(int i=left;i<=right;++i){</pre>
                if(s[i]=='a' \parallel s[i]=='e' \parallel s[i]=='i' \parallel s[i]=='o' \parallel s[i]=='u') freq[s[i]-'a']++;
             }
             int sum=0;
             for(int i=0; i<26;++i){
                freq[i]%=2;
                sum+=freq[i];
              }
             if(sum==0) ans=std::max(ans,right-left+1);
           }
        }
        return ans;
};
```

```
Preprecessing + Brute force - TLE
  Time complexity: O(5n+n+n^2)=O(n^2)
  Space complexity: O(5n)=O(n)
*/
typedef std::vector<int> vi;
typedef std::vector<vi>vvi;
class Solution {
  public:
     int findTheLongestSubstring(std::string s) {
       int n=s.size();
       vvi pre(5,vi(n+1));
       for(int i=1;i<=n;++i){
          pre[0][i]=pre[0][i-1]+int(s[i-1]=='a');
          pre[1][i]=pre[1][i-1]+int(s[i-1]=='e');
          pre[2][i]=pre[2][i-1]+int(s[i-1]=='i');
          pre[3][i]=pre[3][i-1]+int(s[i-1]=='o');
          pre[4][i]=pre[4][i-1]+int(s[i-1]=='u');
       }
       int ans=0;
       for(int left=0;left<n;++left){</pre>
          for(int right=left;right<n;++right){</pre>
            int sum_a=pre[0][right+1]-pre[0][left];
            int sum_e=pre[1][right+1]-pre[1][left];
            int sum_i=pre[2][right+1]-pre[2][left];
            int sum_o=pre[3][right+1]-pre[3][left];
            int sum_u=pre[4][right+1]-pre[4][left];
            if(sum_a%2==0&&sum_e%2==0&&sum_i%2==0&&sum_o%2==0&&sum_u%2==0)
ans=std::max(ans,right-left+1);
          }
       }
       return ans;
};
```

```
Bitmask version 1
  Time complexity: O(32+n)=O(n)
  Space complexity: O(2^5)=O(32)=O(1)
*/
typedef std::vector<int> vi;
typedef std::vector<vi>vvi;
class Solution {
  public:
     int findTheLongestSubstring(std::string s) {
       int n=s.size();
       vi seen(32,INT_MIN);
       seen[0]=-1;
       int mask=0;
       int ans=0;
       for(int i=0;i< n;++i){
          if(s[i]=='a') mask\stackrel{<}{=}(1\stackrel{<}{<}4);
          else if(s[i]=='e') mask^=(1<<3);
          else if(s[i]=='i') mask^=(1<<2);
          else if(s[i]=='o') mask^=(1<<1);
          else if(s[i]=='u') mask\wedge=(1<<0);
          if(seen[mask]!=INT_MIN) ans=std::max(ans,i-seen[mask]);
          else seen[mask]=i;
        }
       return ans;
     }
};
```

```
Bitmask version 2
  Time complexity: O(32+n)=O(n)
  Space complexity: O(2^5)=O(32)=O(1)
*/
typedef std::vector<int> vi;
typedef std::vector<vi>vvi;
class Solution {
  public:
     int findTheLongestSubstring(std::string s) {
       int n=s.size();
       vi seen(32,INT_MIN);
       seen[0]=-1;
       int mask=0;
       int ans=0;
       for(int i=0;i< n;++i){
          if(s[i]=='a') mask^=16;
          else if(s[i]=='e') mask^=8;
          else if(s[i]=='i') mask^=4;
          else if(s[i]=='o') mask^2;
          else if(s[i]=='u') mask^=1;
          if(seen[mask]!=INT_MIN) ans=std::max(ans,i-seen[mask]);
          else seen[mask]=i;
       }
       return ans;
     }
};
```