209. Minimum Size Subarray Sum

Given an array of positive integers nums and a positive integer target, return the **minimal length** of a subarray whose sum is greater than or equal to target. If there is no such subarray, return 0 instead.

Example 1:

```
Input: target = 7, nums = [2,3,1,2,4,3]
Output: 2
Explanation: The subarray [4,3] has the minimal length under the problem constraint.
```

Example 2:

```
Input: target = 4, nums = [1,4,4]
Output: 1
```

Example 3:

```
Input: target = 11, nums = [1,1,1,1,1,1,1,1]
Output: 0
```

Constraints:

- 1 <= target <= 109
- 1 <= nums.length <= 10⁵
- 1 <= nums[i] <= 10⁴

Follow up: If you have figured out the O(n) solution, try coding another solution of which the time complexity is $O(n \log(n))$.

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```
Sliding window
      Time compelxity: O(n)
      Space complexity: O(1)
*/
class Solution {
public:
  int minSubArrayLen(int target, vector<int>& nums) {
    int n=nums.size();
    int l=0,r=0,sum=0,ans=INT_MAX;
    while(r<n){
      sum+=nums[r];
      while(sum>=target){
         sum-=nums[l];
         ans=std::min(ans,r-l+1);
         l++;
       }
       r++;
    return ans==INT_MAX?0:ans;
  }
};
```

Given an integer array nums and an integer k, return *the length of the shortest non- empty subarray of* nums *with a sum of at least* k. If there is no such **subarray**, return -1.

A **subarray** is a **contiguous** part of an array.

Example 1:

```
Input: nums = [1], k = 1
Output: 1
```

Example 2:

```
Input: nums = [1,2], k = 4
Output: -1
```

Example 3:

```
Input: nums = [2,-1,2], k = 3
Output: 3
```

Constraints:

- 1 <= nums.length <= 10⁵
- -10⁵ <= nums[i] <= 10⁵
- 1 <= k <= 10⁹

```
Brute force
  Time complexity: O(n^2)
  Space complexity: O(1)
class Solution {
  public:
     int shortestSubarray(std::vector<int>& nums, int k) {
       int n=nums.size();
       int ans=INT_MAX;
       for (int i=0; i< n; ++i){
          long long s=0;
          int j=i;
          while(j \le n \&\& s \le k){
            s+=nums[j];
            j++;
          if(s>=k) ans=std::min(ans,j-i);
       }
       return (ans != INT_MAX)?ans:-1;
     }
};
```

```
Min heap
  Time complexity: O(nlog n)
  Space complexity: O(n)
*/
typedef std::pair<long long,int> ii;
typedef std::vector<ii>vii;
class Solution {
  public:
     int shortestSubarray(std::vector<int>& nums, int k) {
       int n=nums.size();
       std::priority_queue<ii,vii,std::greater<ii>>> min_heap;
       int ans=INT_MAX;
       long long s=0;
       for (int i=0;i< n;++i){
        s+=nums[i];
        // If s \ge k, minimize the actual length with previous lengths
        if(s>=k) ans=std::min(ans,i+1);
        // Always take the minimum prefix sum before i, trying to hold ps[i]-ps[x] > = k
        while(!min_heap.empty() && s-min_heap.top().first>=k){
          ans=std::min(ans,i-min_heap.top().second);
          min_heap.pop(); // Not need to use this index for incoming indexes
         }
        min_heap.push({s,i});
       return (ans != INT_MAX)?ans:-1;
};
```

```
Monotonic deque
  Time complexity: O(n)
  Space complexity: O(n)
*/
typedef std::pair<long long,int> ii;
typedef std::vector<ii>vii;
class Solution {
  public:
     int shortestSubarray(std::vector<int>& nums, int k) {
       int n=nums.size();
       // Create a deque
       std::deque<ii> q;
       int ans=INT_MAX;
       long long s=0;
       for (int i=0; i< n; ++i){
        s+=nums[i];
        // If s \ge k, minimize the actual length with previous lengths
        if(s>=k) ans=std::min(ans,i+1);
        // Always take the minimum prefix sum before i, trying to hold ps[i]-ps[x] > = k
        while(!q.empty() && s-q.front().first>=k){
          ans=std::min(ans,i-q.front().second);
          q.pop_front();
        // Remove any prefix sum > s, to ensure that the deque stay
        // monotonically increasing
        while(!q.empty() && q.back().first>=s) q.pop_back();
        // Here, we are sure that s is the greatest value
        q.push_back({s,i});
        }
       return (ans != INT_MAX)?ans:-1;
};
```