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1 # ----- Imports -----
2 from PIL import Image
3 import numpy as np
4 import math
5 import time
6 from random import randint, sample, uniform, seed
7 from itertools import permutations
8 from datetime import datetime
9
10 seed(datetime.now())
11
12
13 # ----- Usage Method -----
14 # image_compression(image_reading('Dataset/A2.png'), use_genetic_algorithm=True, debug=False)
15
16
17 # ----- Image Reading Function -----
18 def image_reading(file):
19     print("=" * 150)
20     print("=" * 68 + " Image Reading " + "=" * 67)
21     print("=" * 150)
22     print("Image File: " + file)
23     image = Image.open(file).convert("1")
24     print("Image Mode: " + image.mode)
25     (width, height) = image.size
26     print("Image Size (Width*Height): (" + str(width) + "*" + str(height) + ")")
27     image_array = np.asarray(image)
28     print("Binary Image Array:")
29     print(image_array)
30     return image_array
31
32
33 # ----- Image Compression Function -----
34 def image_compression(image_array, use_genetic_algorithm=False, debug=False):
35     start_time = time.time()
36     print("=" * 150)
37     print("=" * 51 + " Image Compression: Constant Area Code Algorithm " + "=" * 50)
38     print("=" * 150)
39     block_widths = divisor_generator(len(image_array[0]))
40     block_heights = divisor_generator(len(image_array))
41     block_sizes = [(width, height) for width in block_widths for height in block_heights]
42     print("# Possible Block Widths: " + str(block_widths))
43     print("# Possible Block Heights: " + str(block_heights))
44     print("# Number of Possible Block Sizes (Width*Height): " + str(len(block_sizes)))
45     if use_genetic_algorithm:
46         max_CR = genetic_algorithm(image_array, block_sizes, debug=debug)
47     else:
48         max_CR = brute_force(image_array, block_sizes, debug=debug)
49     print(" " * 25 + "=" * 100)
50     temp_string = str("# Maximum Compression Ratio: " + str(max_CR['CR']))
51     print(temp_string)
52     print('=' * len(temp_string))
53     CAC(image_array, max_CR['block_width'], max_CR['block_height'], get_result=True, debug=True)
54     print("=" * 150)
55     execution_time = time.time() - start_time
56     print("# Program Execution Time: " + str(execution_time) + " Seconds")
57     print("=" * 150)
58
59
60 # ----- Brute Force Function -----
61 def brute_force(image_array, block_sizes, debug=False):
62     max_CR = {'CR': -1, 'block_width': 0, 'block_height': 0}
63     temp_string = str("# Brute Force (Without Optimization):")
64     print(temp_string)
65     print('=' * len(temp_string))
66     if not debug:
67         print('Processing', end='', flush=True)
68         i = 10
69     for block_width, block_height in block_sizes:
70         if not debug:
71             if i < 150 or i % 150 != 0:
72                 print('.', end='', flush=True)
73             else:
74                 print('\n.', end='', flush=True)
75             i = i + 1
76             if (i - 10) == len(block_sizes):
77                 print()
78         else:
79             if i == 10:
80                 i += 1
81             else:
82                 print(" " * 25 + "-" * 100)
83             CR = CAC(image_array, block_width, block_height, debug=debug)
84             if CR > max_CR['CR']:
85                 max_CR['CR'] = CR
86                 max_CR['block_width'] = block_width
87                 max_CR['block_height'] = block_height
88     return max_CR
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91 # ----- CAC Function -----
92 def CAC(image_array, block_width, block_height, debug=False, get_result=False):
93     image_width = len(image_array[0])
94     image_height = len(image_array)
95     blocks_array = np.asarray(
96         [[get_block_type(image_array, block_width, block_height, x * block_width, y * block_height)
97            for x in range(int(image_width / block_width))] for y in range(int(image_height / block_height))])
98     counter, codes = blocks_counter_encoder(blocks_array)
99     N1 = image_width * image_height
100     N2 = 0
101     for key, value in counter.items():
102         if key == 'M':
103             N2 = N2 + value * (len(codes[key]) + block_width * block_height)
104         else:
105             N2 = N2 + (value * len(codes[key]))
106     CR = N1 / N2
107     if get_result:
108         with open("Result.txt", "w") as result:
109             for h in range(len(blocks_array)):
110                 for w in range(len(blocks_array[0])):
111                     if blocks_array[h][w] == 'M':
112                         result.write(codes['M'])
113                         for hx in range(h * block_height, (h + 1) * block_height):
114                             for wx in range(w * block_width, (w + 1) * block_width):
115                                 result.write(str(int(image_array[hx][wx])))
116                     else:
117                         result.write(codes[blocks_array[h][w]])
118                 result.close()
119     else:
120         open("Result.txt", "w").close()
121     if debug:
122         print("For Block Size (Width*Height): (" + str(block_width) + "*" + str(block_height) + ")")
123         print("Blocks Counter: " + str(counter))
124         print("Blocks Codes: " + str(codes))
125         print("Blocks Array Size (Width*Height): (" + str(len(blocks_array[0])) + "*" + str(len(blocks_array)) + ")")
126         print("Blocks Array:")
127         print(blocks_array)
128         print("Compression Ratio (N1/N2): (" + str(N1) + "/" + str(N2) + ") = " + str(CR))
129         print("Result: Result.txt")
130     return CR
131
132 # ----- Help Functions -----
133 def divisor_generator(n):
134     divisors = []
135     large_divisors = []
136     for i in range(1, int(math.sqrt(n) + 1)):
137         if n % i == 0:
138             divisors.append(i)
139             if i * i != n:
140                 large_divisors.append(int(n / i))
141     return sorted(divisors + large_divisors)
142
143 def get_block_type(image_array, block_width, block_height, w_start, h_start):
144     has_white = False
145     has_black = False
146     for w in range(w_start, w_start + block_width):
147         for h in range(h_start, h_start + block_height):
148             if image_array[h][w]:
149                 has_white = True
150             else:
151                 has_black = True
152             if has_white and has_black:
153                 return 'M'
154     if has_white:
155         return 'W'
156     elif has_black:
157         return 'B'
158
159 def blocks_counter_encoder(blocks_array):
160     unique, counts = np.unique(blocks_array, return_counts=True)
161     counter = dict(zip(unique, counts))
162     codes = counter.copy()
163     max_count = max(counter, key=counter.get)
164     codes[max_count] = '0'
165     i = 0
166     for key, value in counter.items():
167         if key is not max_count:
168             if len(counter) == 2:
169                 codes[key] = '1'
170             elif len(counter) == 3:
171                 if i == 0:
172                     codes[key] = '01'
173                     i = i + 1
174                 elif i == 1:
175                     codes[key] = '11'
176     return counter, codes
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182 # ----- Genetic Algorithm Function -----
183 def genetic_algorithm(image_array, block_sizes, delta_error=10 ** -5, least_number_of_generations=5, debug=False):
184     max_CR = {'CR': -1, 'block_width': 0, 'block_height': 0}
185     temp_string = str("# Genetic Algorithm (Optimization):")
186     print(temp_string)
187     print('=' * len(temp_string))
188     multiplicat = uniform((3 / len(block_sizes)), 0.1)
189     if len(block_sizes) < 30:
190         multiplicat = (3 / len(block_sizes))
191     if multiplicat <= 1:
192         population_size = randint(3, int(len(block_sizes) * multiplicat))
193     else:
194         population_size = len(block_sizes)
195     least_number_of_mating_pools = population_size
196     for X in range(population_size):
197         if population_size <= (X + len(list(permutations([None] * X, 2)))):
198             least_number_of_mating_pools = X
199             break
200     number_of_mating_pools = randint(least_number_of_mating_pools, population_size)
201     print("Least Number of Generations: " + str(least_number_of_generations))
202     print("Δ Error of Convergence: " + str(delta_error))
203     print("Population Size [3->" + str(int(len(block_sizes) * multiplicat)) + "]: " + str(population_size))
204     print("Number of Mating Pools [" + str(least_number_of_mating_pools) + "->" + str(population_size) + "]: " +
205           str(number_of_mating_pools))
206     print("Mutation Percentage {0%,50%,100%}: 50%")
207     if not debug:
208         print('Processing', end='', flush=True)
209     i = 10
210     generations_counter = 0
211     new_populations = []
212     random_indexes = sample(range(len(block_sizes)), population_size)
213     for i in range(population_size):
214         new_populations += [block_sizes[random_indexes[i]]]
215     condition = True
216     while condition:
217         if not debug:
218             if i < 150 or i % 150 != 0:
219                 print('*', end='', flush=True)
220             else:
221                 print('\n*', end='', flush=True)
222             i = i + 1
223         else:
224             if i == 10:
225                 i += 1
226             else:
227                 print(" " * 25 + "-" * 100)
228             last_max_CR = max_CR.copy()
229             generations_counter += 1
230             populations = new_populations.copy()
231             populations_with_fitnesses = [(CAC(image_array, width, height), width, height) for width, height in populations]
232             populations_with_fitnesses.sort(reverse=True)
233             max_CR['CR'] = populations_with_fitnesses[0][0]
234             max_CR['block_width'] = populations_with_fitnesses[0][1]
235             max_CR['block_height'] = populations_with_fitnesses[0][2]
236             mating_pools = []
237             for i in range(number_of_mating_pools):
238                 mating_pools += [(populations_with_fitnesses[i][1], populations_with_fitnesses[i][2])]
239             possible_offsprings = [(X1, Y2) for (X1, Y1), (X2, Y2) in list(permutations(mating_pools, 2))]
240             offsprings = []
241             random_indexes = sample(range(len(possible_offsprings)), population_size - number_of_mating_pools)
242             for i in range(population_size - number_of_mating_pools):
243                 offsprings += [possible_offsprings[random_indexes[i]]]
244             mutants = offsprings.copy()
245             for i in range(len(mutants)):
246                 index = randint(0, 1)
247                 temp_mutant = list(mutants[i])
248                 temp_mutant[index] = block_sizes[randint(0, len(block_sizes) - 1)][index]
249                 mutants[i] = tuple(temp_mutant)
250
251             new_populations = mating_pools + mutants
252             condition = (generations_counter < least_number_of_generations) or (
253                 (max_CR['CR'] - last_max_CR['CR']) > delta_error)
254             if debug:
255                 temp_string = "Generation: (" + str(generations_counter) + ")"
256                 print(temp_string)
257                 print('-' * len(temp_string))
258                 print("Populations (BlockWidth,BlockHeight): " + str(populations))
259                 print("Sorted Populations with Fitnesses (CR,BlockWidth,BlockHeight): " + str(populations_with_fitnesses))
260                 print("Mating Pools (BlockWidth,BlockHeight): " + str(mating_pools))
261                 print("Offsprings (BlockWidth,BlockHeight): " + str(offsprings))
262                 print("Mutants (BlockWidth,BlockHeight): " + str(mutants))
263                 print("Best Compression Ratio: " + str(max_CR['CR']))
264             if (not debug) and (i < 150 or i % 150 != 0):
265                 print()
266             return max_CR
267
268
269 if __name__ == "__main__":
270     image_compression(image_reading('Dataset/A2.png'), use_genetic_algorithm=True, debug=False)

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