## MPDL Base Station Sleep Control Algorithm and Variables

### Algorithm 1: MPDL Base Station Sleep Control

#### Inputs:

- Initial network state:  $X(0) = \{x_1(0), x_2(0), \dots, x_N(0)\}$  (loads of all base stations).
- Arrival probabilities:  $v_i$  for each base station i.
- Departure probabilities:  $w_i$  for each base station i.
- Light sleep threshold L.
- Deep sleep decision function  $J(u_i, u_j)$ .

#### Steps:

- 1. Initialization:
  - Set the initial state t = 1 and X(0).
- 2. For each time step t = 1 to T:
  - $\bullet$  Randomly generate a parameter c between 0 and 1.
- 3. Determine User Activity Based on c:
  - If  $\sum_{k=1}^{i-1} v_k < c \le \sum_{k=1}^{i} v_k$  (A user arrives at base station i):
    - Case 1: If  $u_i(t-1) = 0$  (base station is empty):
      - \* Find max  $J(1, u_i(t-1))$ , where  $j \in K(i)$  (neighboring base stations).
      - \* If  $\max J(1, u_i(t-1)) > 0$ :
        - · Increment  $u_i(t+1) = u_i(t) + 1$  (neighbor takes the user).
      - \* Else:
        - · Set  $u_i(t) = 1$  (base station becomes active).
    - Case 2: If  $u_i(t-1) + 1 > U_{\text{max}}$  (load exceeds capacity):
      - \* Find neighboring base stations  $\{j|u_i(t-1)=0\}.$
      - st Distribute load among base station i and its neighbors:

$$u_i(t) = u_j(t) = \frac{u_i(t-1)+1}{k+1}$$
, where k is the number of neighbors.

- Case 3: If  $u_i(t-1) + 1 \le U_{\text{max}}$ :
  - \* Increment  $u_i(t) = u_i(t-1) + 1$ .
- If  $\sum_{k=1}^{n} v_k + \sum_{k=1}^{i-1} w_k < c \le \sum_{k=1}^{n} v_k + \sum_{k=1}^{i} w_k$  (A user departs from base station i):
  - Case 1: If the base station transitions to deep sleep:
    - \* Find  $\max J(u_i(t-1) 1, u_i(t-1))$ , where  $j \in K(i)$ .
    - \* Distribute load among neighbors or wake up base station j.
- If no user activity: (User remains stationary)
  - Retain the same state X(t+1) = X(t).

#### 4. Evaluate Sleep Transitions:

- If  $\rho_i(t) < L$  (light sleep threshold) and delay  $D(\rho_i)$  is acceptable:
  - Transition base station i to light sleep.
- If  $\max J(u_i,u_j)>0$  and neighbors can take the load:
  - Transition base station i to deep sleep.

#### 5. Update Network State:

• Adjust states X(t+1) based on user activity and base station transitions.

# Variables and Formulas

Variable	Description	How to Find It
X(t)	Network state at time $t$ , represented as	Update using user arrival $(v_i)$ and departure
	$\{x_1(t), x_2(t),, x_N(t)\},$ where $x_i(t)$ is the load	$(w_i)$ .
	of base station $i$ .	
$v_i$	Probability of a user arriving at base station $i$ .	Typically modeled using a Poisson process.
$w_i$	Probability of a user leaving base station $i$ .	Derived from user behavior or historical data.
$J(u_i,u_j)$	Decision function for deep sleep transition.	$J(u_i, u_j) = P(u_i) + P(u_j) - P(u_i + u_j) -$
		$w_{i,j}(u_i)$ , where $P(u)$ is power consumption.
$ ho_i$	Load of base station i, defined as $\rho_i = \frac{u_i}{U_{\text{max}}}$ .	Calculate using $u_i$ , the number of users, and
	- Hox	$U_{\rm max}$ , the base station's maximum capacity.
P(u)	Power consumption of the base station.	Different formulas for normal, light sleep, and
		deep sleep states:
		$P(u) = \begin{cases} \frac{u}{U_{\text{max}}} P_t + P_0 & \text{if active} \\ P_{\text{doze}} + F_m E_s & \text{if light sleep} \\ 0 & \text{if deep sleep} \end{cases}$
$F_m$	Frequency of entering the doze state in light sleep.	$F_m = \frac{(U_{\text{max}} - u)(1 - \Gamma_V)}{U_{\text{max}}V}.$ $\Gamma_V = e^{-p\mu V}, \text{ where } p \text{ is the probability of a}$
$\Gamma_V$	Probability that there is no queue at the end of a	
	doze window.	request in a time slot, $\mu$ is service rate, and $V$
		is the doze window.
L	Light sleep threshold for base station $i$ .	$L = -\frac{\ln\left(1 - \frac{V(P_0 - P_{\text{doze}})}{E_s}\right)}{Vp}.$
$w_{i,j}(u_i)$	Transition cost when moving users from base station	Typically a constant or function of user mo-
	i  to  j.	bility.