# Logic-Based Agents<sup>1</sup>

### LECTURE 1

<sup>&</sup>lt;sup>1</sup>The slides have been prepared using the textbook material available on the web, and the slides of the previous editions of the course by Prof. Luigia Carlucci Aiello

## Summary

- ♦ Logical Agents Russell & Norvig Sect. 7.1–7.4
- ♦ Knowledge Representation
- ♦ Knowledge-based Agents
- ♦ The wumpus world
- Propositional Logic

### Symbol hypothesis

The conputer belongs to a class of artificial systems, symbolic systems...

Symbols can be used to represent structures. ...

A computer is a symbolic system, where symbols are **created**, **modified**, **copied**,...

not a quote, but this is argued in: [H. Simon, The Sciences of the Artificial, 1969, 1994]

## Properties of a good representation

A **representation** is made by a set of symbols, stored on a computer together with algorithms that allow to us to use it in order to solve problems.

♦ Adequacy criteria by McCarthy & Hayes in 1969: metaphysics, epistemology, heuristics

- $\diamondsuit$  language expressive power (ontology)
- ♦ level of abstraction
- ♦ good design (computation)

## Representation language

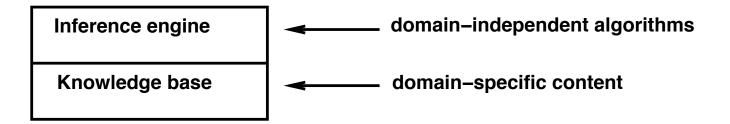
- not a programming language
- not a communication language

Propositional Logic is the basic example:

**Key principle**: syntax – semantics – reasoning

Possibly "visual", but semantically well defined

## Knowledge bases



In a knowledge representation language the set of inferences is defined without referring to the algorithm to compute them.

## Knowledge bases

Knowledge base = set of sentences in a formal language

Declarative approach to building an agent (or other system): TELL it what it needs to know

Then Ask it what to do—answers that follow from the KB

Agents can be viewed at the knowledge level i.e., what they know, regardless of how implemented

Or at the implementation level

i.e., data structures in KB and algorithms that manipulate them

## An example

knowledge base	inference
Rain	
Wind	
if Rain then TakeUmbrella	if $A$ is true and $A \Rightarrow B$
if Wind then WindJacket	then $B$ can be derived
if Rain and WithoutUmbrella	
then Wet	

## From the knowledge base:

Rain??

Wind??

TakeUmbrella??

WindJacket??

Fog??

Wet??

## A simple knowledge-based agent

```
function KB-AGENT( percept) returns an action static: KB, a knowledge base t, a counter, initially 0, indicating time  \text{Tell}(KB, \text{Make-Percept-Sentence}(percept, t)) \\ action \leftarrow \text{Ask}(KB, \text{Make-Action-Query}(t)) \\ \text{Tell}(KB, \text{Make-Action-Sentence}(action, t)) \\ t \leftarrow t+1 \\ \text{return } action
```

## A simple knowledge-based agent

The agent must be able to:

Represent states, actions, etc.

Incorporate new percepts

Update internal representations of the world

Deduce hidden properties of the world

Deduce appropriate actions

## Wumpus World PEAS description

#### **Environment**

Squares adjacent to wumpus are smelly
Squares adjacent to pits are breezy
Glitter iff gold is in the same square
Shooting kills wumpus if you are facing it
Shooting uses up the only arrow
Grabbing picks up gold if in same square
Releasing drops the gold in same square

SS SSS S Stench S		Breeze	PIT
700 700	Breeze	PIT	Breeze
SS SSS S Stench S		Breeze	
START	Breeze /	PIT	Breeze
1	2	3	4

Notice: the world in RN is symmetric (i.e.  $[3,1] \rightarrow [1,3]$ )

## Wumpus World PEAS description

### Performance measure

gold +1000, death -1000-1 per step, -10 for using the arrow

#### Sensors

Stench, Breeze, Glitter, Bump, Cry

#### **Actuators**

Left turn, Right turn, Forward, Grab, Release, Shoot

## Wumpus world characterization

Observable?? No—only local perception

<u>Deterministic??</u> Yes—outcomes exactly specified

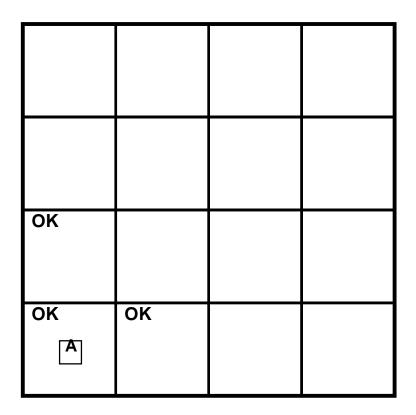
Episodic?? No—sequential at the level of actions

Static?? Yes—Wumpus and Pits do not move

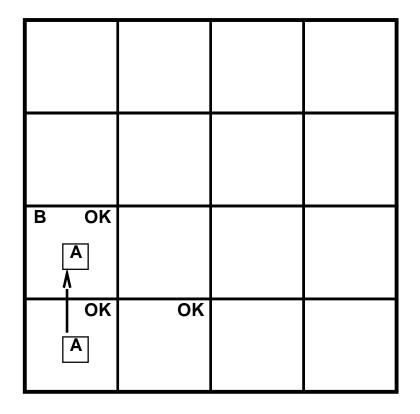
Discrete?? Yes

Single-agent?? Yes—Wumpus is essentially a natural feature

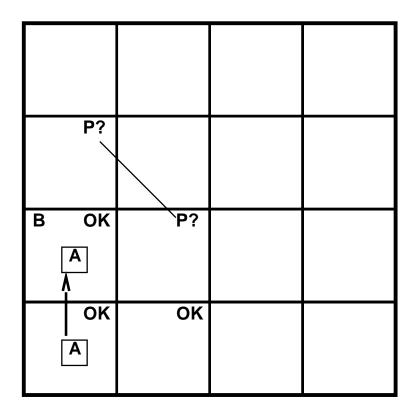
Sensors: [None, None, None, None, None]



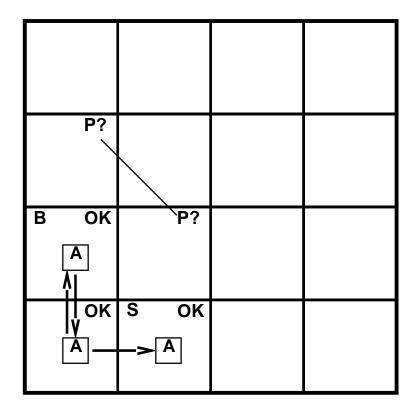
Sensors: [None, Breeze, None, None, None]



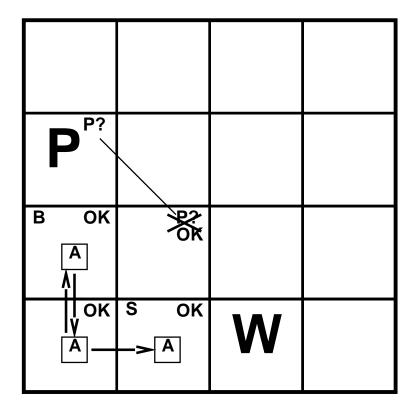
Squares adjacent to pits are breezy

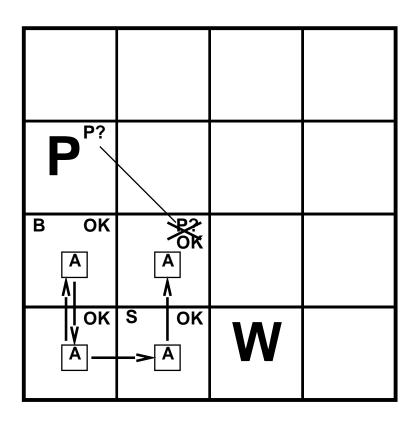


Sensors: [Stench, None, None, None, None]

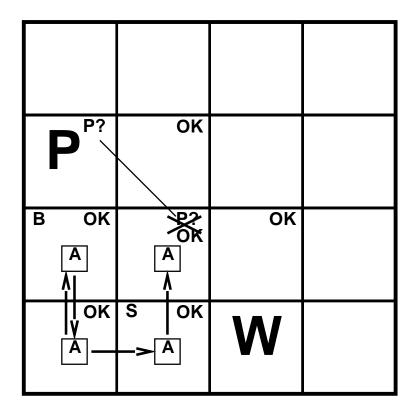


Squares adjacent to wumpus are smelly

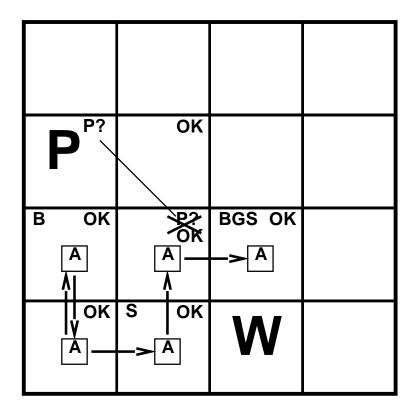




Sensors: [None, None, None, None, None]



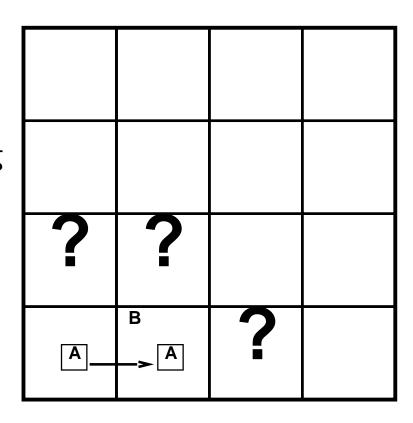
Sensors: [None, None, Glitter, None, None]



## Entailment in the wumpus world

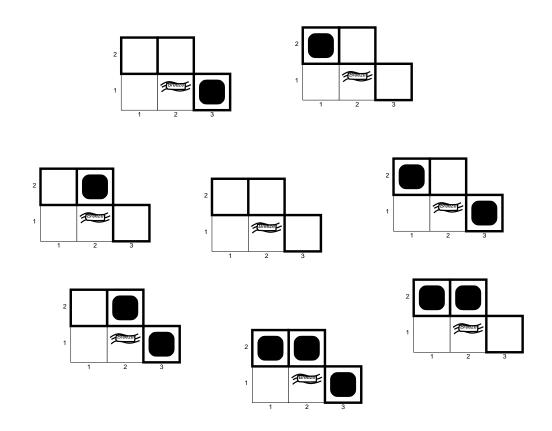
Situation after detecting nothing in [1,1], moving right, breeze in [2,1]

Consider possible cases for ?s assuming only pits

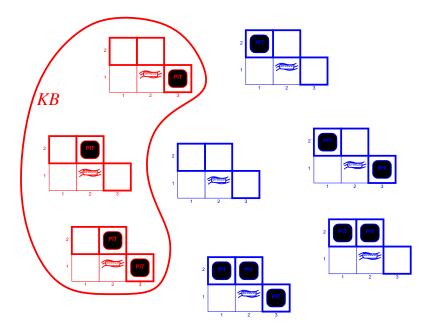


3 Boolean choices  $\Rightarrow$  8 possible cases

# Wumpus possible worlds

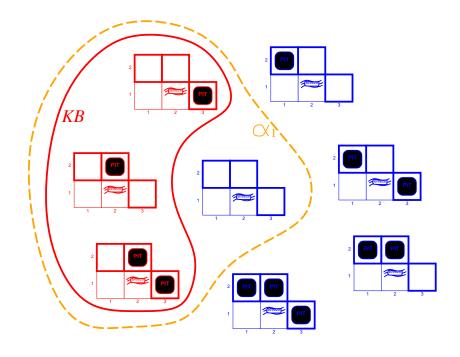


## Wumpus models



KB = wumpus-world rules + observation B[1,1] and B[1,2]  $\mathbf{models} =$  possible worlds that are "coherent with KB

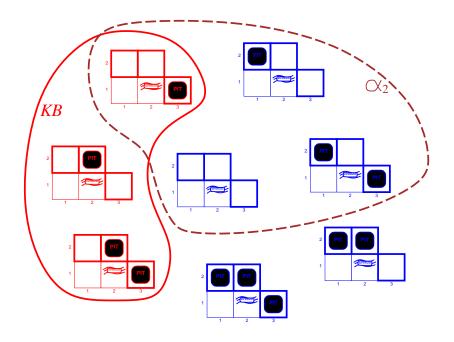
# Inference by model checking



KB as before and  $\alpha_1 =$  "[1,2] is safe"?  $KB \models \alpha_1$ 

$$KB \models \alpha_1$$

# Inference by model checking



KB as before and  $\alpha_2=$  "[2,2] is safe"?  $KB\not\models\alpha_2$ 

### Logic in general

Logics are formal languages for representing information such that conclusions can be drawn

Syntax defines the legal sentences in the language

Semantics define the "meaning" of sentences; i.e., define truth of a sentence in a world

E.g., the language of arithmetic

 $x + 2 \ge y$  is a sentence; x2 + y > i is not a sentence

 $x + 2 \ge y$  is true iff number x + 2 is no less than number y

 $x+2 \ge y$  is true in a world where x=7, y=1

 $x+2 \ge y$  is false in a world where x=0, y=6

### Entailment

Entailment means that one thing *follows from* another:

$$KB \models \alpha$$

Knowledge base KB entails sentence  $\alpha$  if and only if  $\alpha$  is true in all worlds where KB is true

E.g., the KB with "the Giants won" and "the Reds won" entails "Either the Giants won or the Reds won"

E.g., 
$$x + y = 4$$
 entails  $4 = x + y$ 

Entailment is a relationship between sentences (i.e., *syntax*) that is based on *semantics* 

Note: brains process *syntax* (of some sort)

### Models

Logicians typically think in terms of models, which are formally structured worlds with respect to which truth can be evaluated

We say m is a model of a sentence  $\alpha$  if  $\alpha$  is true in m

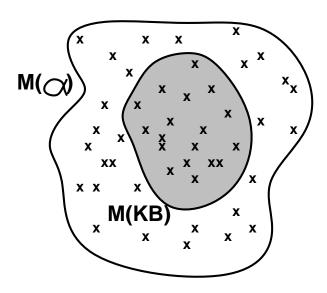
 $M(\alpha)$  is the set of all models of  $\alpha$ 

Then  $KB \models \alpha$  if and only if  $M(KB) \subseteq M(\alpha)$ 

NOTE: Russell and Norvig overload the term **model** by using it also for interpretation structures

# Models: example

E.g. KB = Giants won and Reds won  $\alpha = \text{Giants won}$ 



## Model Checking

The knowledge that is entailed by a KB can be computed by:

$$KB \models \alpha$$

can be derived by building models and checking whether:

$$M(KB) \subseteq M(\alpha)$$

This approach is referred to as model checking

### **Deduction**

Another way of computing the knowledge entailed by a KB is by a deduction procedure (proof):

$$KB \vdash_i \alpha$$

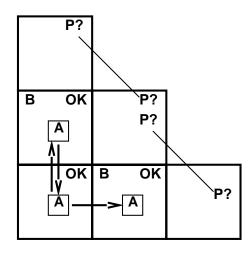
denotes that  $\alpha$  can be derived from KB by procedure i

Deduction works on formulae by applying inference rules.

Note: the term inference is used for any procedure that can compute logical entailment.

## Sometimes there is no certainty

Breeze in (1,2) and (2,1)  $\Rightarrow$  no safe actions



Assuming pits uniformly distributed, (2,2) has pit w/ prob 0.86, vs. 0.31

## Sometimes you can only try

Smell in (1,1)

 $\Rightarrow$  cannot move

Can use a strategy of coercion:

shoot straight ahead

wumpus was there  $\Rightarrow$  dead  $\Rightarrow$  safe

wumpus wasn't there  $\Rightarrow$  safe

