



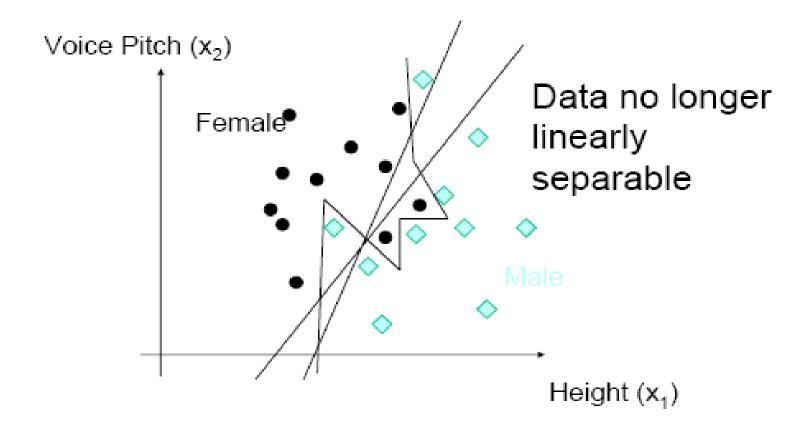
## CS 4104 APPLIED MACHINE LEARNING

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#### MULTILAYER NETWORKS

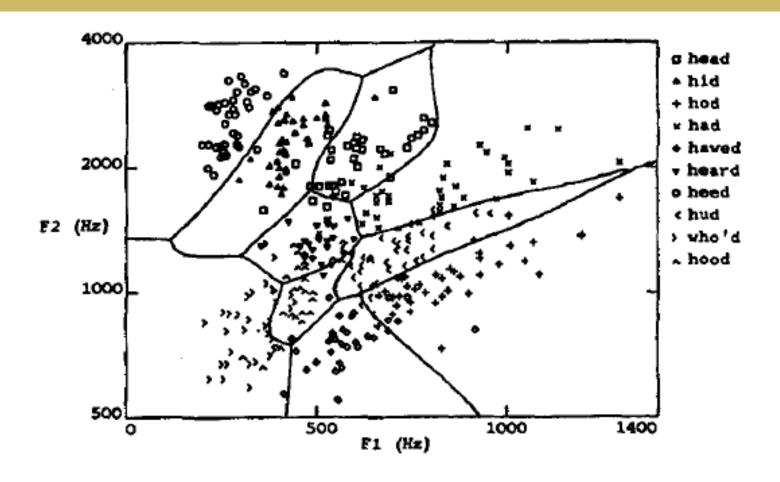


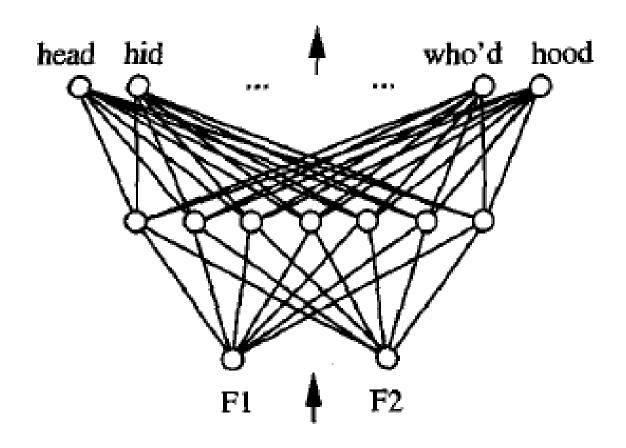
#### What is a good decision boundary?

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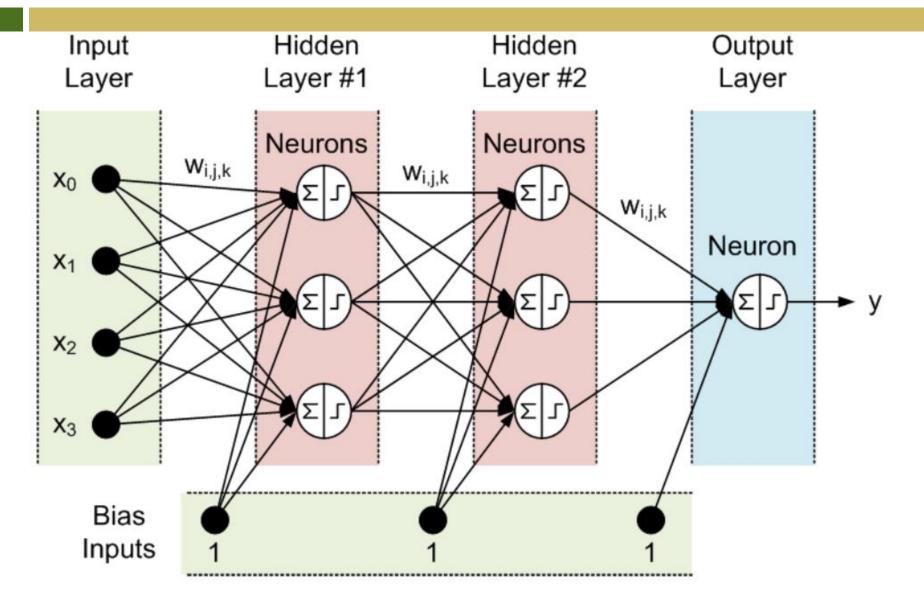
#### **Example:**

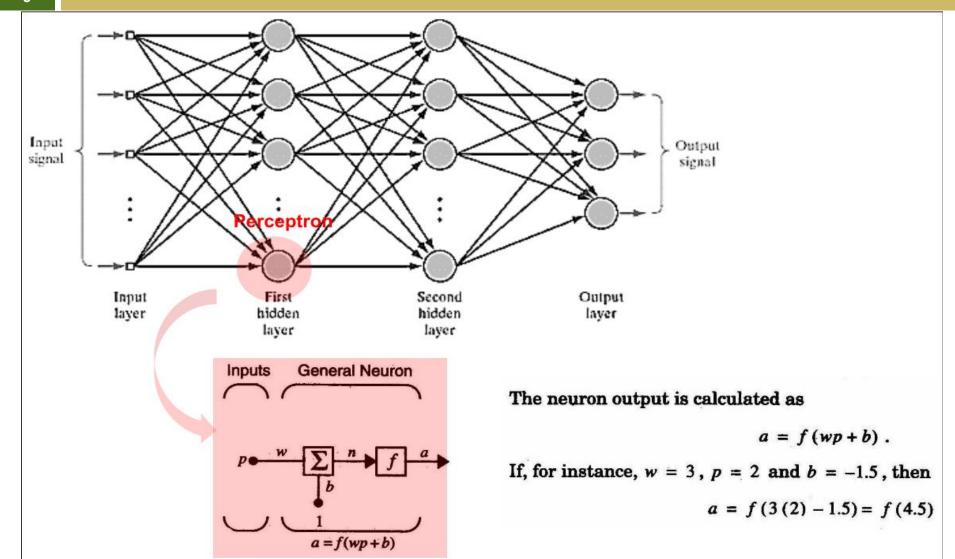
The speech recognition task involves distinguishing among 10 possible vowels, all spoken in the context of "h-d" (i.e., "hid," "had," "head," "hood," etc.).



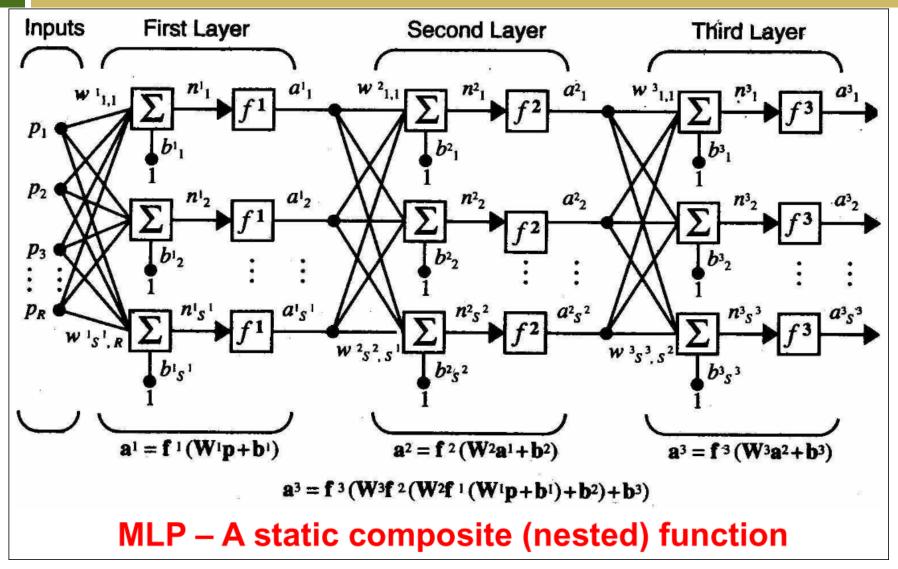


### Multilayer Perceptron Architecture





## Multilayer Network Architecture



The single perceptron can only express <u>linear</u>
 <u>decision surfaces</u>.

The kind of multilayer networks learned by the back propagation algorithm are capable of expressing a rich variety of nonlinear decision surfaces.

- What type of <u>unit</u> shall we use as the basis for constructing multilayer networks?
- □ Can we use the delta/gradient descent learning rule?
  - multi-layers of linear units... multiple layers of cascaded linear units still produce only linear functions, and we prefer networks capable of representing highly nonlinear functions.
- The perceptron unit is another possible choice, is it?
  - its discontinuous threshold makes it undifferentiable and hence unsuitable for gradient descent.

#### **Solution:**

- □ One solution is the sigmoid unit:
  - a unit very much like a perceptron, but based on a smoothed, differentiable threshold function.
- Like the perceptron, the sigmoid unit,
  - first computes a linear combination of its inputs,
  - then applies a threshold to the result. However, the threshold output is a continuous function of its input.

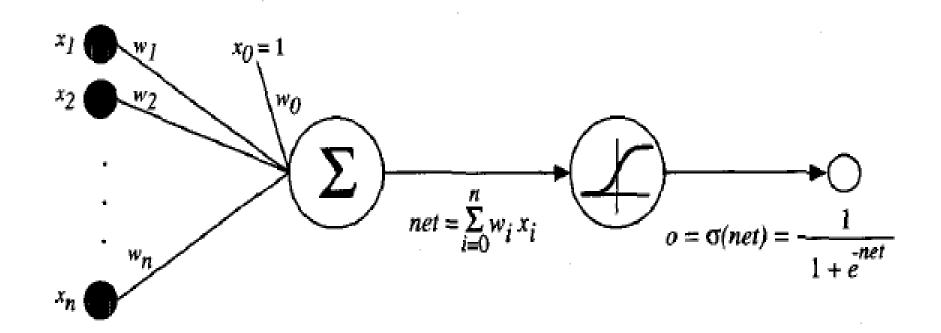
- In case of sigmoid unit, however, the threshold output is a continuous function of its input.
- $\square$  More precisely, the sigmoid unit computes its output o as,

$$o = \sigma(\vec{w} \cdot \vec{x})$$

$$\sigma(y) = \frac{1}{1 + e^{-y}}$$

 $\Box$   $\sigma$  is often called the sigmoid function or, alternatively, the logistic function.

## Sigmoid Threshold Unit



#### Sigmoid Function

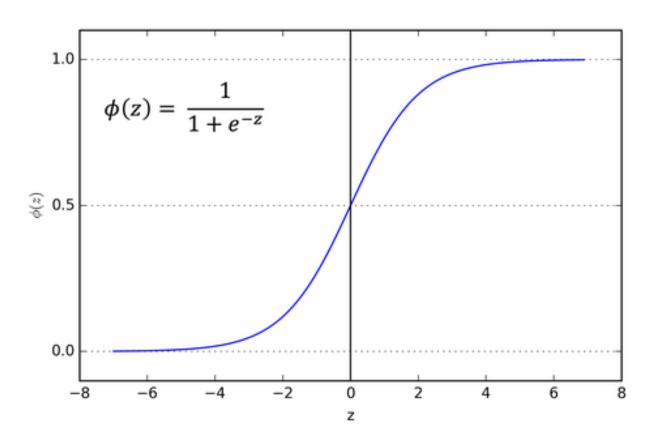
- Sigmoid function maps a very large input domain to a small range of outputs, it is often referred to as the squashing function of the unit.
- The sigmoid function has the <u>useful property</u> that its derivative is easily expressed in terms of its output.

$$\sigma(y) = \frac{1}{1 + e^{-y}}$$

$$\frac{d\sigma(y)}{dy} = \sigma(y) \cdot (1 - \sigma(y))$$

## Sigmoid Function

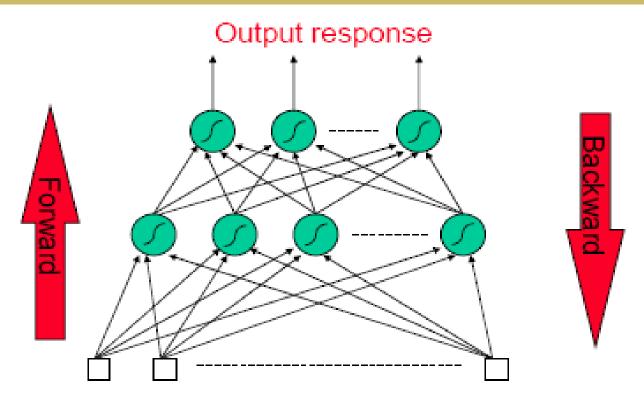
□ Sigmoid function exists between 0 and 1.



# BACK PROPAGATION ALGORITHM

#### The Back Propagation algorithm has two phases:

- Forward pass phase: computes 'functional signal', feed forward propagation of input pattern signals through network
- Backward pass phase: computes 'error signal',
   propagates the error backwards through network
   starting at output units
  - (where the error is the difference between actual and desired output values)



Input patterns

Conceptually: Forward Activity - Backward Error

- The back propagation algorithm learns the weights for a multilayer network,
  - given a network with a fixed set of units and interconnections.
- It employs gradient descent to attempt to minimize the squared error between the network output values and the target values for these outputs.
- □ As we are considering networks with multiple output units, we begin by redefining E to sum the errors over all of the network output units.

$$E(\vec{w}) \equiv \frac{1}{2} \sum_{d \in D} \sum_{k \in outputs} (t_{kd} - o_{kd})^2$$

where **outputs** is the set of output units in the network, and  $t_{kd}$  and  $0_{kd}$  are the target and output values associated with the kth output unit and training example **d**.

#### BACKPROPAGATION(training\_examples, $\eta$ , $n_{in}$ , $n_{out}$ , $n_{hidden}$ )

Each training example is a pair of the form  $\langle \vec{x}, \vec{t} \rangle$ , where  $\vec{x}$  is the vector of network input values, and  $\vec{t}$  is the vector of target network output values.

 $\eta$  is the learning rate (e.g., .05).  $n_{in}$  is the number of network inputs,  $n_{hidden}$  the number of units in the hidden layer, and  $n_{out}$  the number of output units.

The input from unit i into unit j is denoted  $x_{ji}$ , and the weight from unit i to unit j is denoted  $w_{ji}$ .

- Create a feed-forward network with  $n_{in}$  inputs,  $n_{hidden}$  hidden units, and  $n_{out}$  output units.
- Initialize all network weights to small random numbers (e.g., between -.05 and .05).
- Until the termination condition is met, Do

For each  $(\vec{x}, \vec{t})$  in training\_examples, Do

Propagate the input forward through the network:

1. Input the instance  $\vec{x}$  to the network and compute the output  $o_u$  of every unit u in the network.

Propagate the errors backward through the network:

2. For each network output unit k, calculate its error term  $\delta_k$ 

$$\delta_k \leftarrow o_k(1-o_k)(t_k-o_k)$$

3. For each hidden unit h, calculate its error term  $\delta_h$ 

$$\delta_h \leftarrow o_h(1-o_h) \sum_{k \in outputs} w_{kh} \delta_k$$

4. Update each network weight  $w_{ii}$ 

$$w_{ii} \leftarrow w_{ii} + \Delta w_{ii}$$

where

$$\Delta w_{ji} = \eta \, \delta_j \, x_{ji}$$

## Reading Material

- Artificial Intelligence, A Modern Approach
   Stuart J. Russell and Peter Norvig
  - Chapter 18.
- Machine LearningTom M. Mitchell
  - Chapter 4.