



CS 4104

APPLIED MACHINE LEARNING

Dr. Hashim Yasin

**National University of Computer
and Emerging Sciences,
Faisalabad, Pakistan.**

ARTIFICIAL NEURAL NETWORK



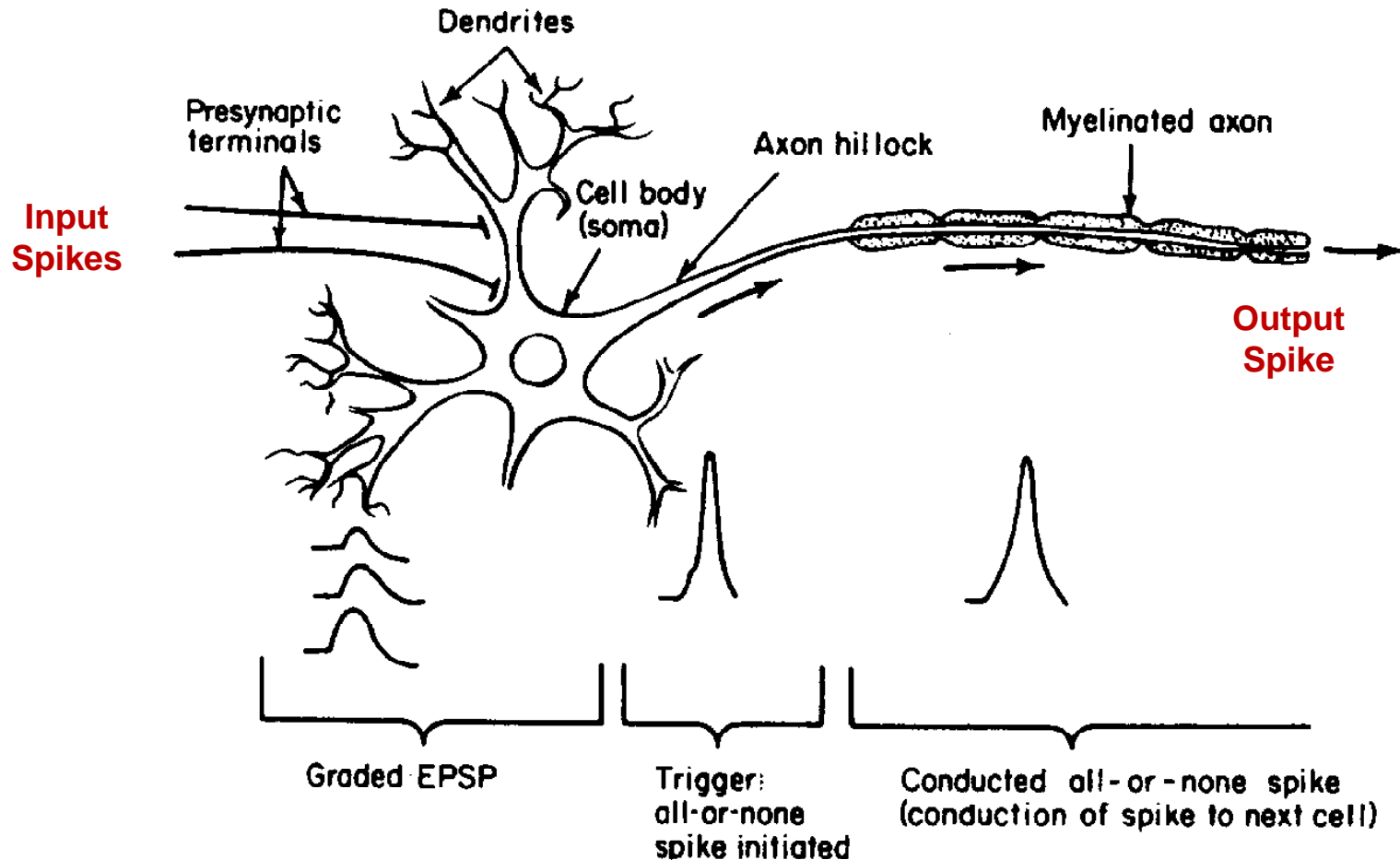
Biological Inspiration

3

- Animals are able to **react adaptively to changes** in their external and internal environment, and they use their **nervous system** to perform these behaviours.
- An *appropriate model/simulation of the nervous system* should be able to produce similar responses and behaviours in artificial systems.

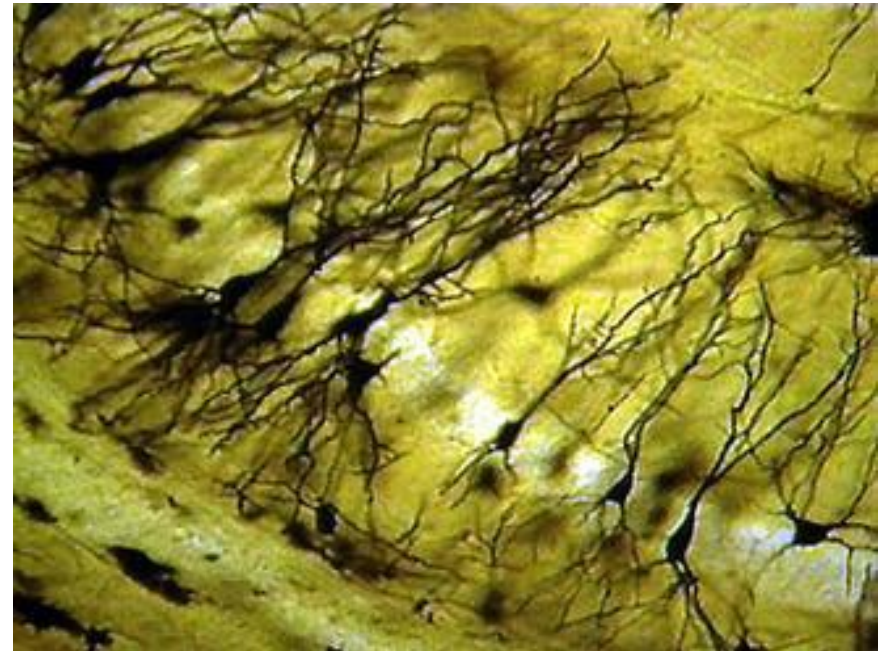
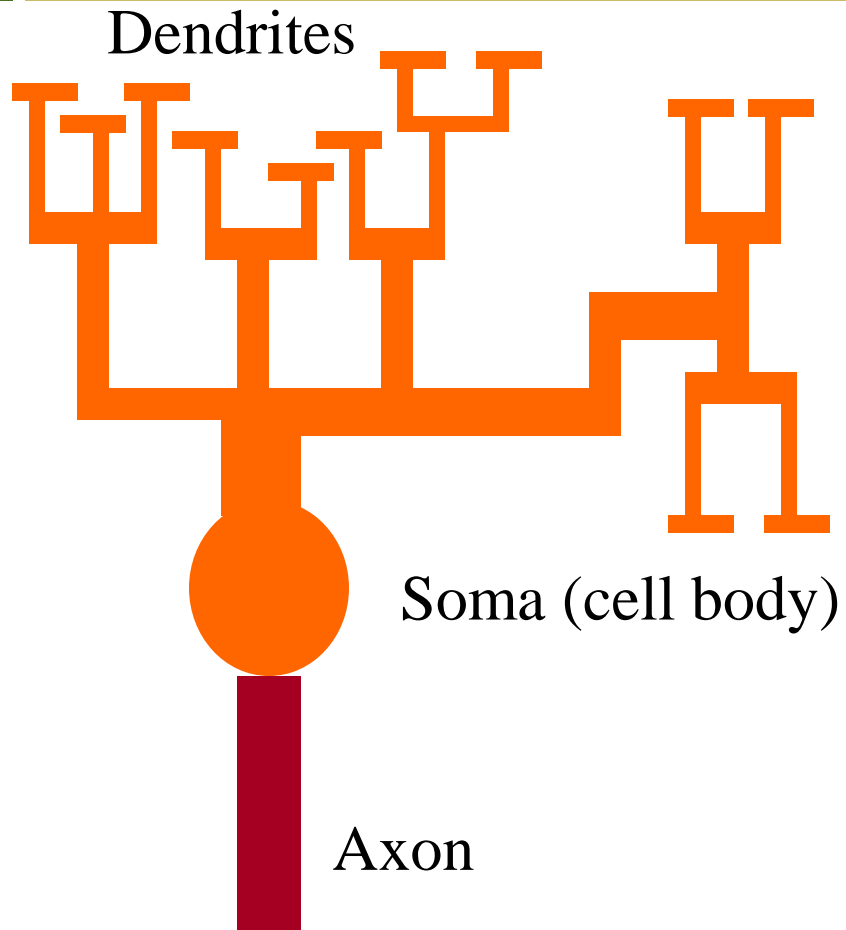
Biological Inspiration

4



Biological Inspiration

5



Biological Inspiration

6

Four Parts of Typical Nerve Cell:

- Dendrites:

accepts the inputs

- Soma:

process the inputs

- Axon:

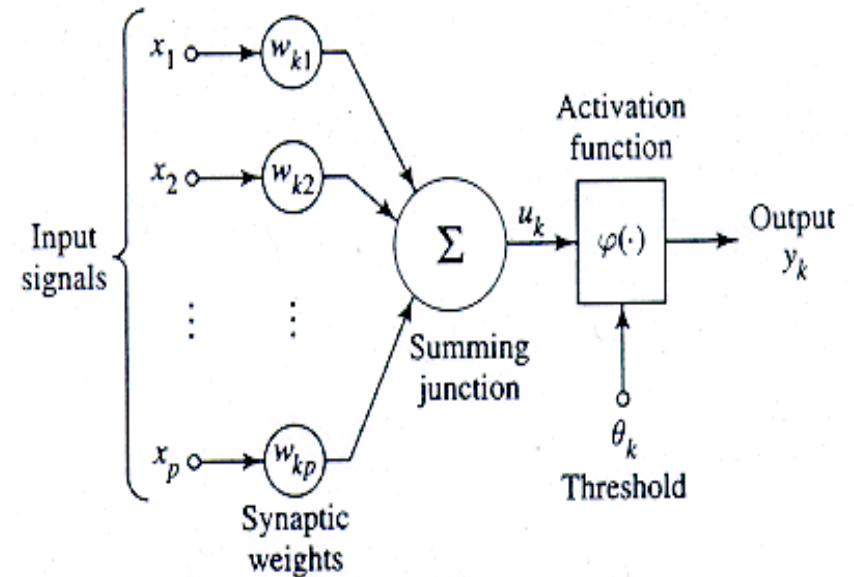
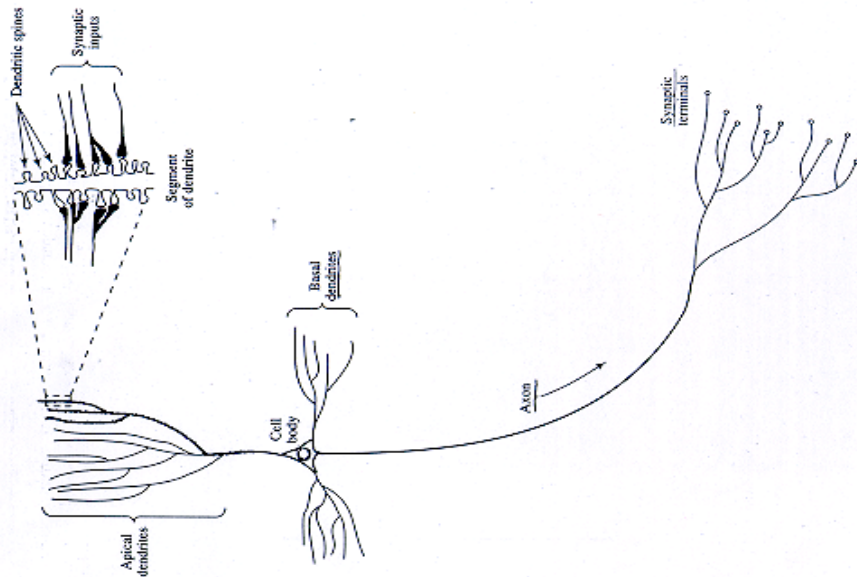
turns the process input into outputs

- Synapses:

the electromechanical contact between the neurons

Biological Inspiration

7



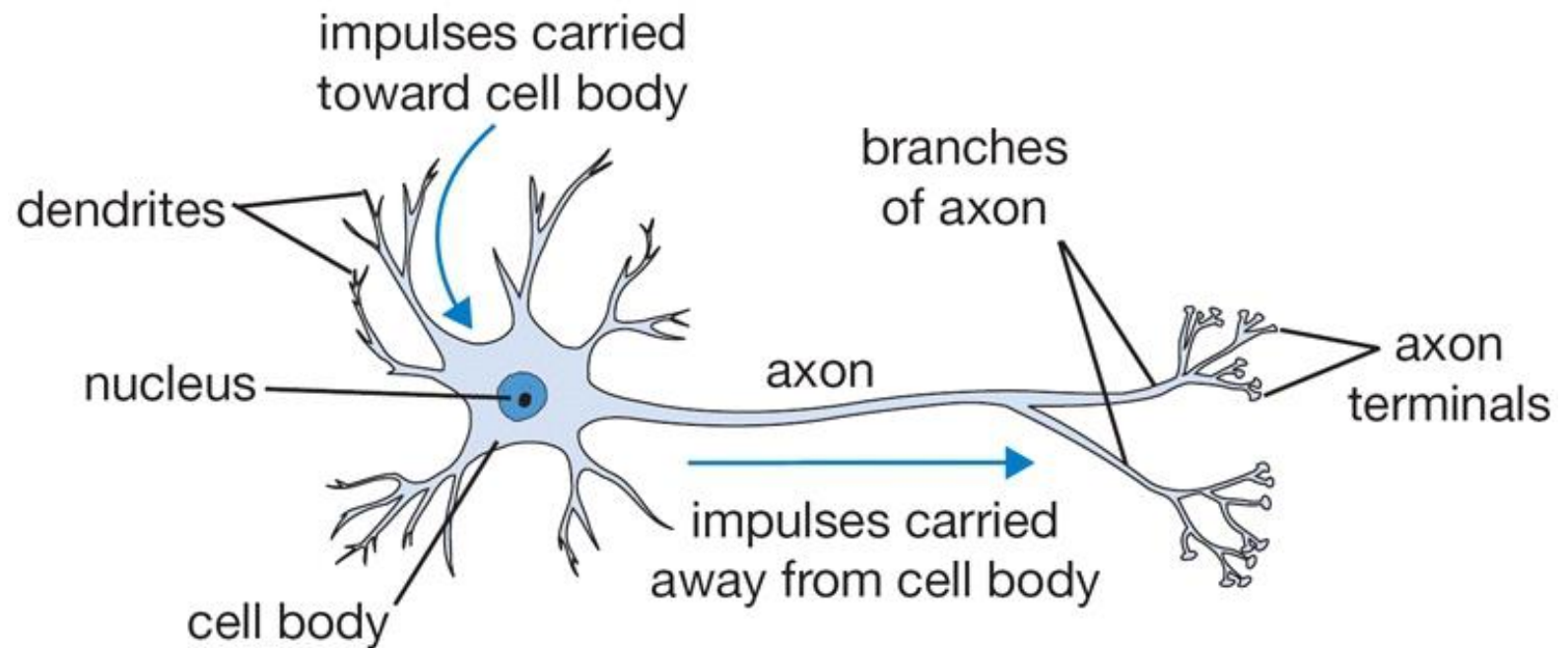
Dendrite

Cell Body

Axon

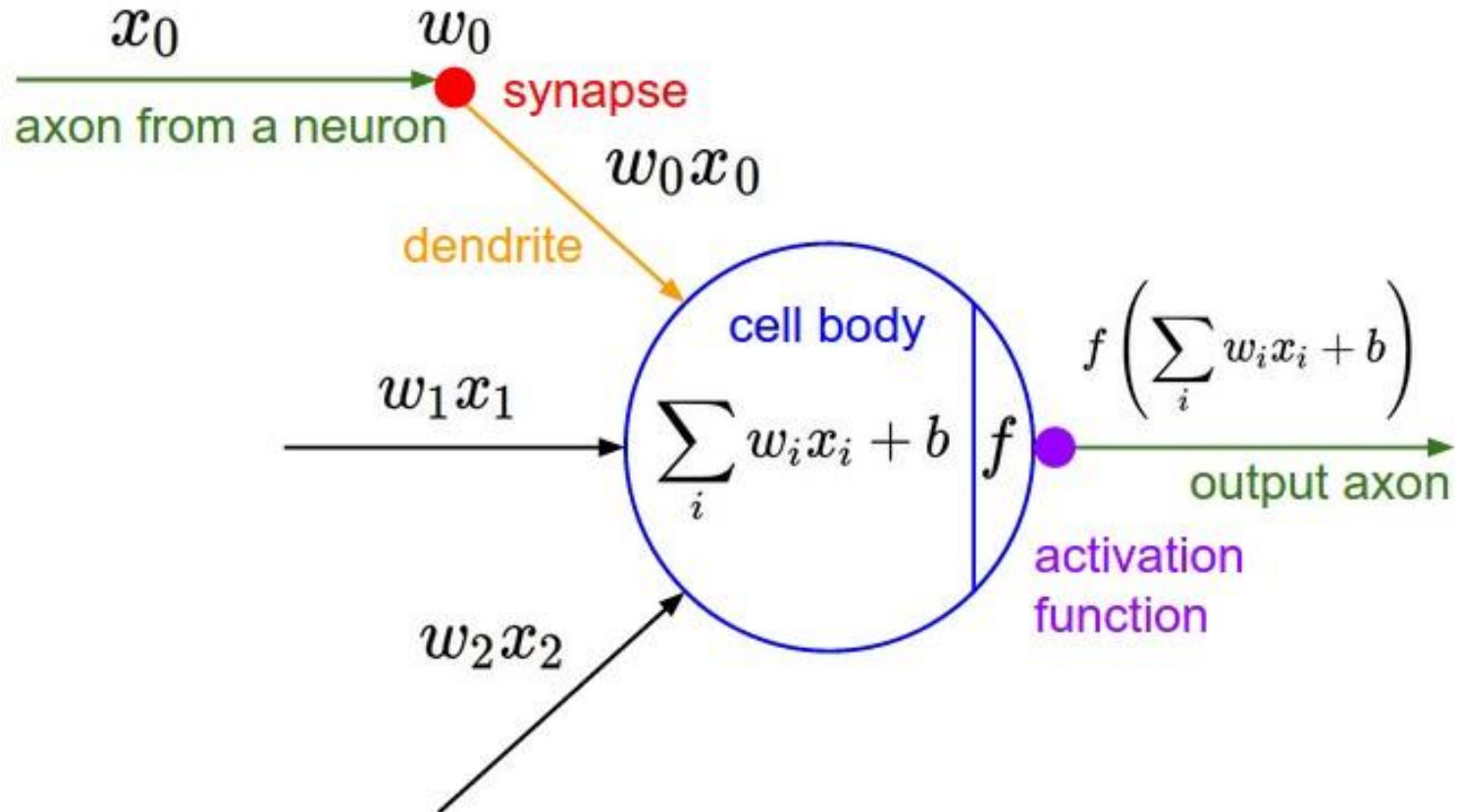
Biological Inspiration

8



Biological Inspiration

9



PERCEPTRON

Perceptron

11

- A simplest type of ANN system is based on a unit called a **perceptron**. A perceptron
 - ▣ takes a **vector of real-valued inputs**,
 - ▣ calculates a linear combination of these inputs,
 - ▣ then **outputs** a 1 if the result is greater than some **threshold** and -1 otherwise.
- More precisely, given inputs x_1 through x_n the output $o(x_1, \dots, x_n)$ computed by the perceptron is

$$o(x_1, \dots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1x_1 + \dots + w_nx_n > 0 \\ -1 & \text{otherwise} \end{cases}$$

Perceptron

12

$$o(x_1, \dots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1x_1 + \dots + w_nx_n > 0 \\ -1 & \text{otherwise} \end{cases}$$

- where each w_i is a real-valued constant, or weight,
 - ▣ that *determines the contribution of input x_i* to the perceptron output.
- The quantity (w_0) is a threshold
 - ▣ the weighted combination of inputs $w_1x_1 + \dots + w_nx_n$ must exceed in order for the perceptron to output a 1.

Perceptron

13

- We may imagine an *additional constant input* $x_0 = 1$, allowing to write the above inequality as,

$$\sum_{i=0}^n w_i x_i > 0$$

or in **vector form** as

$$o(\mathbf{x}) = \begin{cases} 1 & \text{if } \mathbf{w} \cdot \mathbf{x} > 0 \\ -1 & \text{otherwise} \end{cases}$$

$$\mathbf{x} = \vec{x}$$

$$\text{sgn}(y) = \begin{cases} 1 & \text{if } y > 0 \\ -1 & \text{otherwise} \end{cases}$$

Perceptron

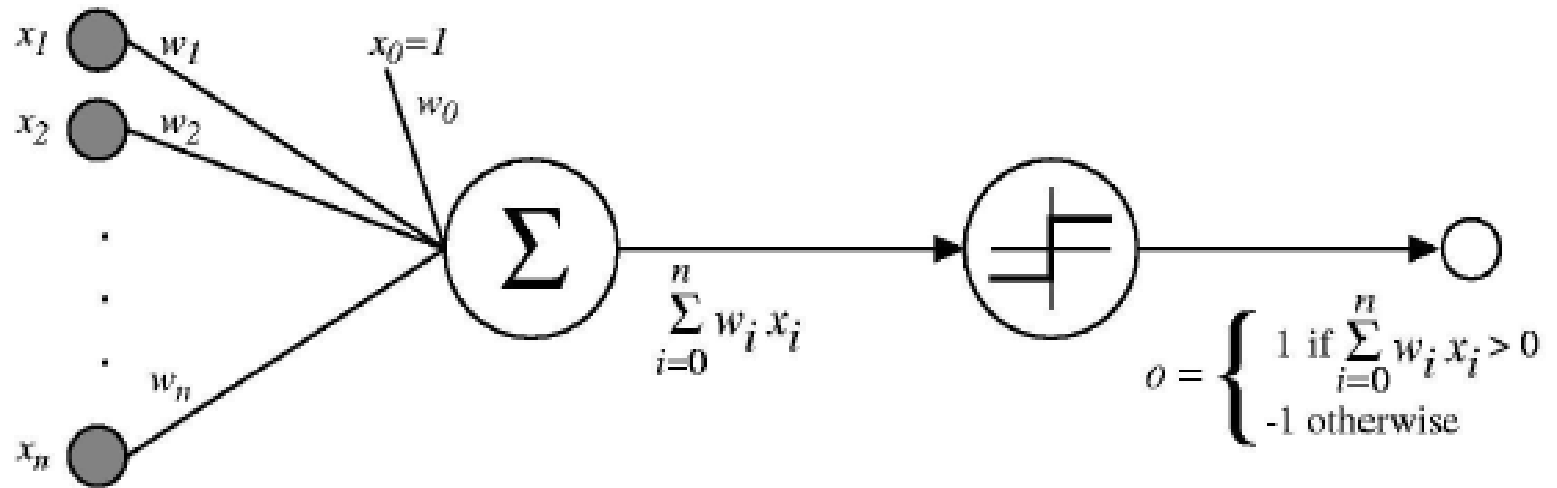
14

- *Learning a perceptron involves choosing values for the weights w_0, \dots, w_n .*
- Therefore, the space H of candidate hypotheses considered in perceptron learning is the *set of all possible real-valued weight vectors*

$$H = \{ \vec{w} \mid \vec{w} \in \mathbb{R}^{(n+1)} \}$$

Perceptron

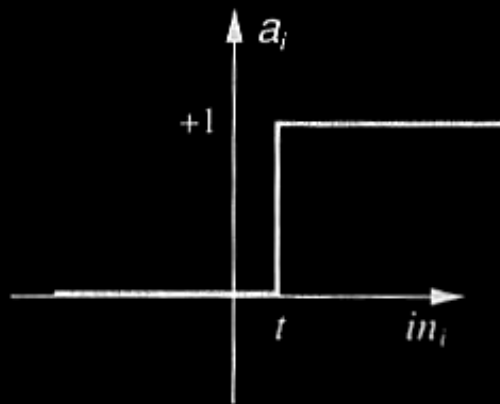
15



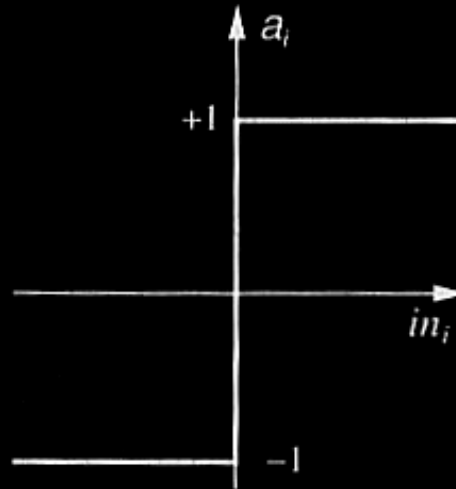
$$o(x_1, \dots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1 x_1 + \dots + w_n x_n > 0 \\ -1 & \text{otherwise.} \end{cases}$$

Perceptron

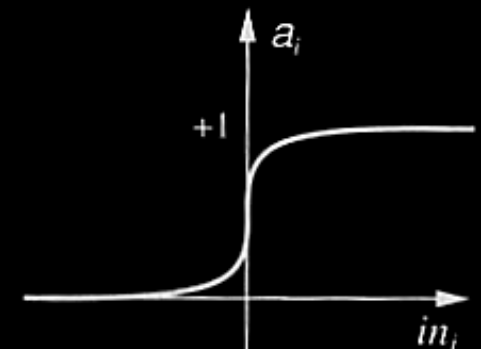
16



(a) Step function



(b) Sign function



(c) Sigmoid function

Figure 19.5 Three different activation functions for units.

$$\text{step}_t(x) = \begin{cases} 1, & \text{if } x \geq t \\ 0, & \text{if } x < t \end{cases} \quad \text{sign}(x) = \begin{cases} +1, & \text{if } x \geq 0 \\ -1, & \text{if } x < 0 \end{cases} \quad \text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

NEURAL NETWORK COMPONENTS



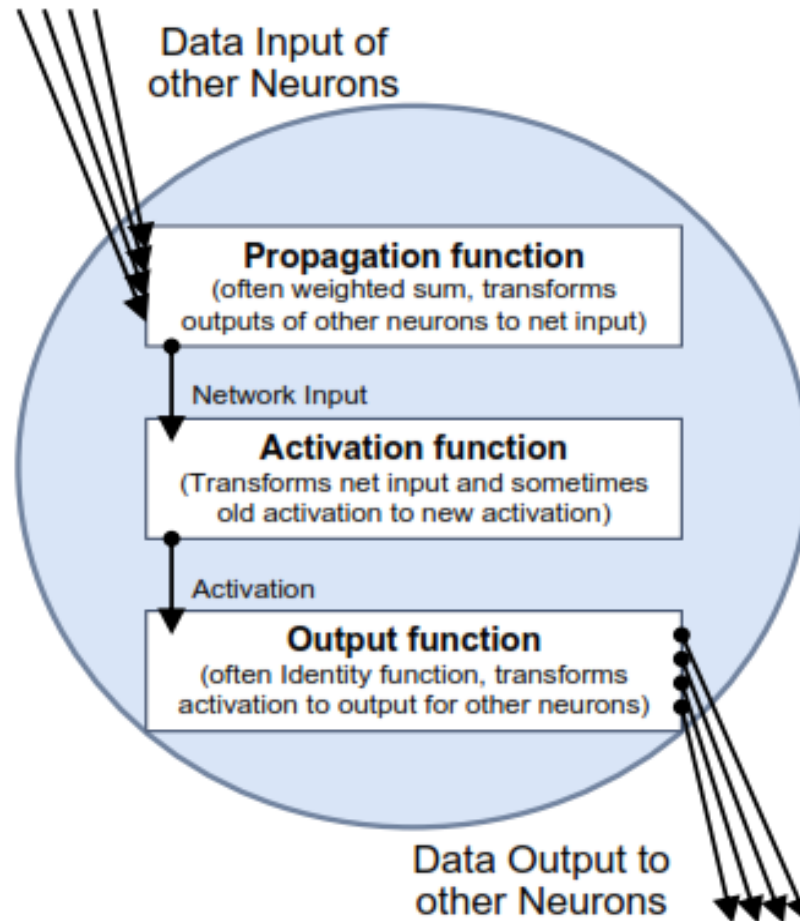
Neural Network Components

18

- A **neural network** is a sorted **triple** (N, V, w) with two sets N, V and a function w ,
 - whereas N is the set of *neurons* and
 - V is a sorted set $\{(i, j) | i, j \in N\}$ whose elements are called **connections** between neuron i and neuron j .
- The function $w : V \rightarrow R$ defines the **weights**, where as $w(i, j)$,
 - The weight of the connection between neuron i and neuron j , is shortly referred to as $w_{i,j}$.


Neural Network Components

19



Input Neuron

20

- An **input neuron** is an **identity neuron**. It exactly forwards the information received.
- Input neuron only forwards data
- Thus, it represents the identity function, which can be indicated by the symbol $/$
- The input neuron is represented by the symbol 

Binary Neuron

21

- **Information processing neurons** process the input information somehow, *i.e.* do not represent the identity function.
- A **binary neuron** sums up all inputs by using the weighted sum as propagation function, which is illustrate by the sigma sign.

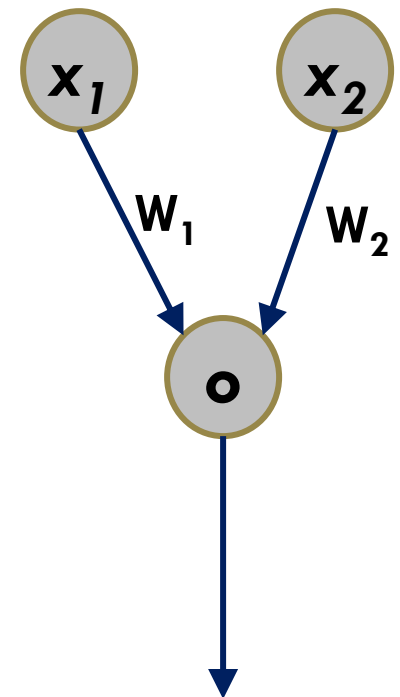
$$\Sigma$$

- The activation function of the neuron is also binary threshold function, which can be illustrated by ⌊

Single-Layer Perceptron

22

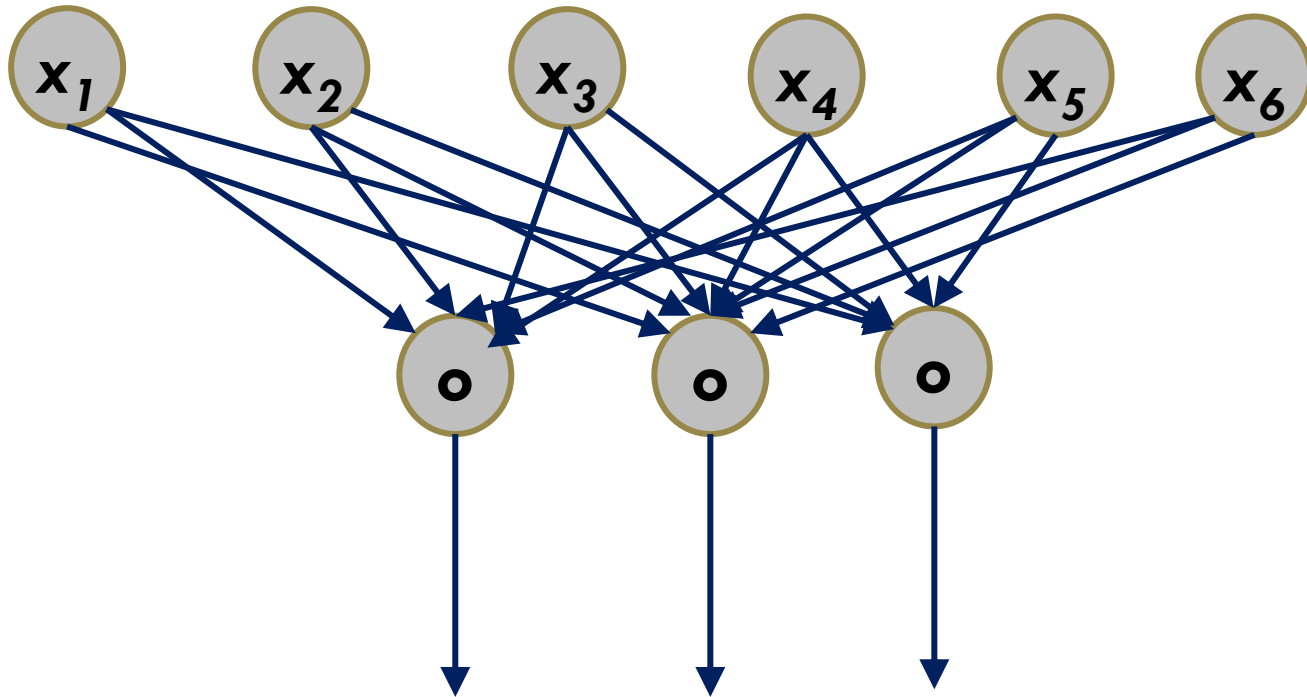
- A **Single-layer perceptron (SLP)** is a perceptron having only one variable-weight layer and one layer of output neurons.
- The technical view of an SLP with two input neurons and one output neuron is shown in the figure.
- The network returns the output by means of the arrow leaving the network.



Single-Layer Perceptron

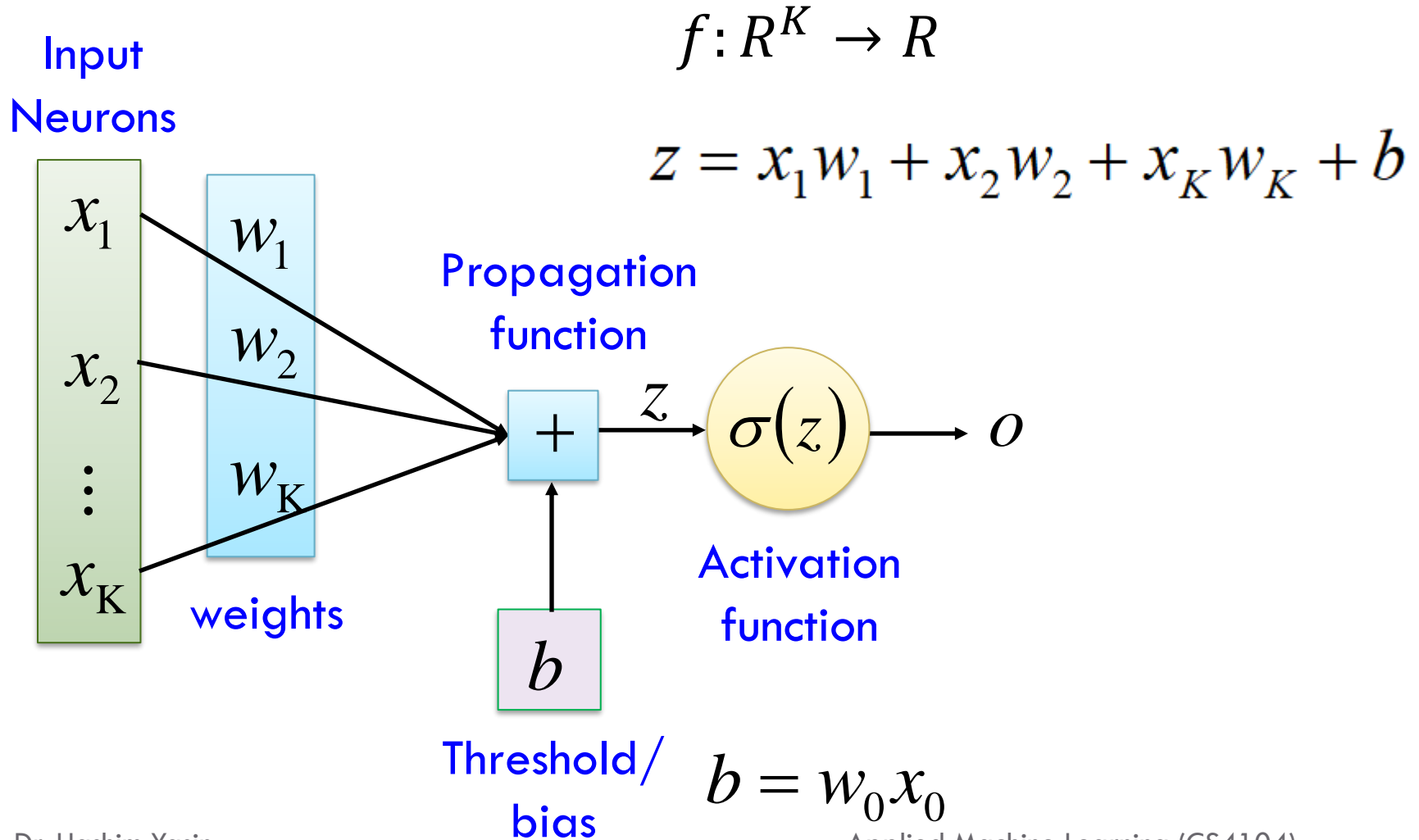
23

- A **Single-layer perceptron (SLP)** with several output neurons.



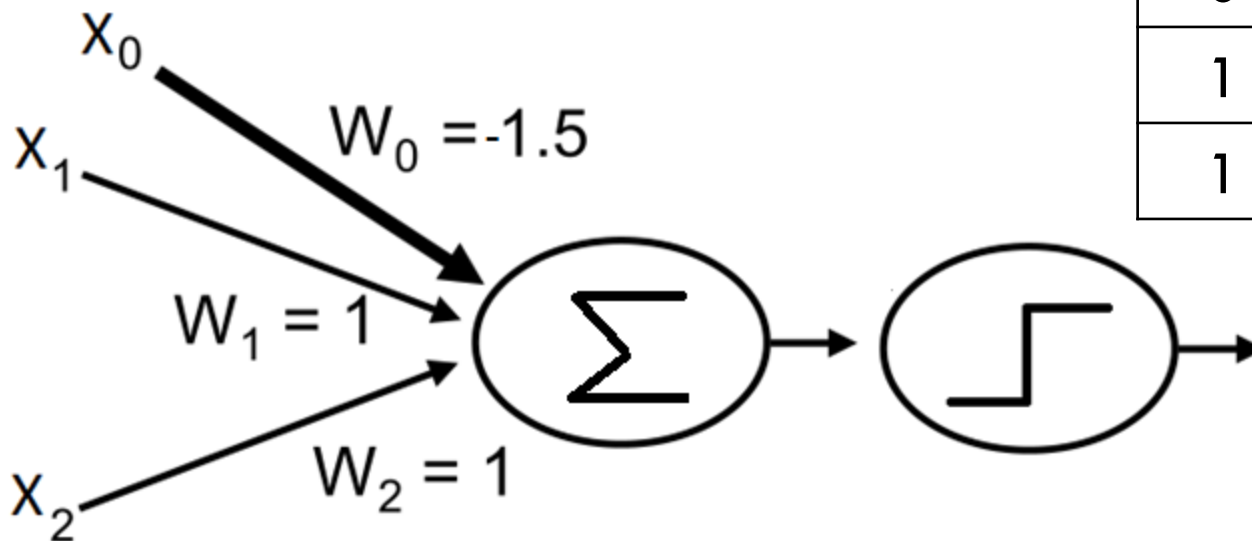
Neural Network Components

24



AND Function

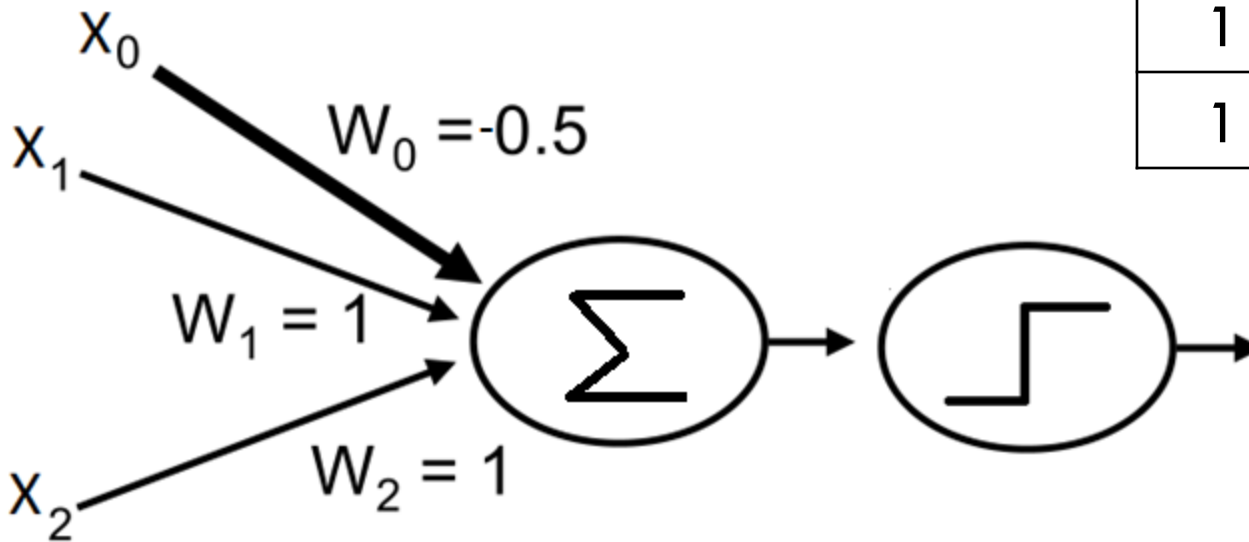
25



X_1	X_2	Y
0	0	0
0	1	0
1	0	0
1	1	1

OR Function

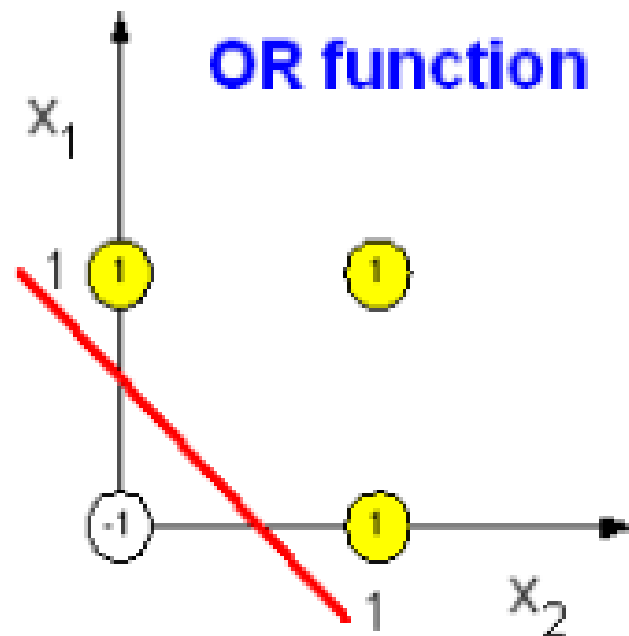
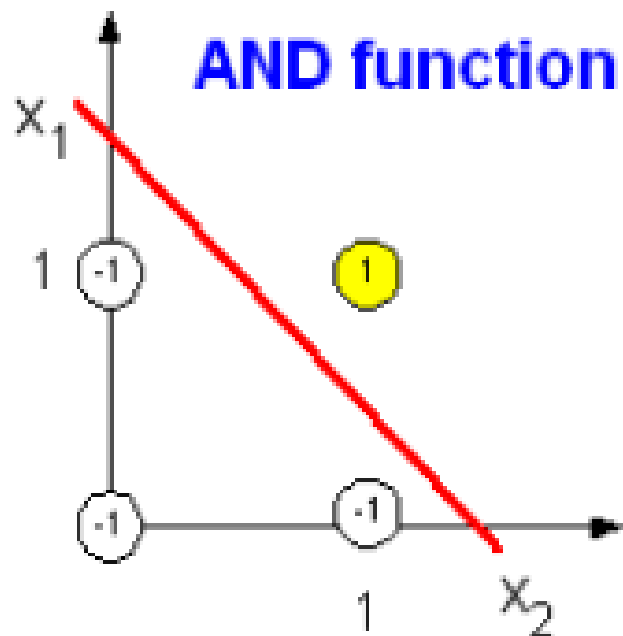
26



x_1	x_2	Y
0	0	0
0	1	1
1	0	1
1	1	1

AND OR Functions

27



PERCEPTRON TRAINING RULE



Perceptron Training Rule

29

- **How to learn the weights for a single perceptron.**
 - Begin with random weights,
 - Iteratively apply the perceptron to each training example,
 - **Modifying the perceptron weights** whenever it misclassifies an example.
 - This process is repeated, iterating through the training examples as many times as needed until the perceptron classifies all training examples correctly.
 - Weights are modified at each step according to the perceptron training rule.

Perceptron Training Rule

30

- The **perceptron training rule**, which revises the weight w_i associated with input x_i according to the rule:

$$w_i \leftarrow w_i + \Delta w_i$$

where

$$\Delta w_i = \eta(t - o)x_i$$

Where:

- t is target value
- o is perceptron output
- η is small constant (e.g., 0.1) called *learning rate*

Perceptron Training Rule

31

- The weight changes Δw_{ij} need to be applied repeatedly ... for each weight w_{ij} in the network, and for each training pattern in the training set.
- One pass through all the weights for the whole training set is called one **epoch** of training
- Eventually, usually after many epochs, when all the network outputs match the targets for all the training patterns,
 - all the Δw_{ij} will be zero and the process of training will cease.
 - We then say that the training process has **converged** to a solution

Perceptron Training Rule

32

Example:

- The training rule **will increase w** , if $(t - o)$, η and x_i **are all positive**.

- if $x_i = 0.8$, $\eta = 0.1$, $t = 1$, and $o = -1$, then the weight update will be

$$\Delta w_i = \eta(t - o)x_i = 0.1(1 - (-1))0.8 = 0.16.$$

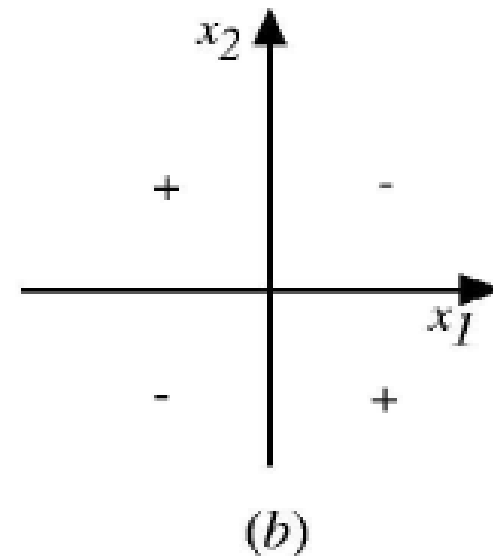
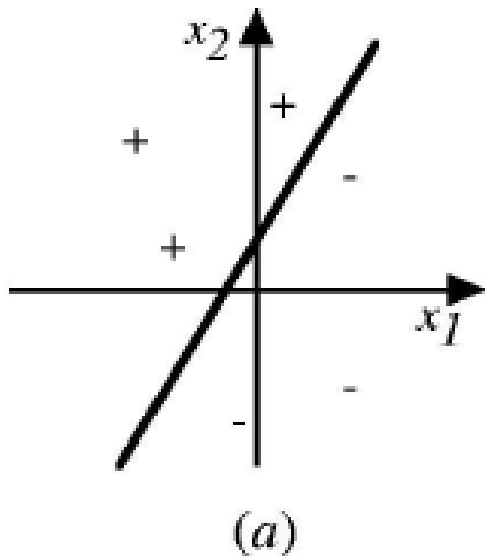
- On the other hand,

- if $x_i = 0.8$, $\eta = 0.1$, $t = -1$ and $o = 1$, then weights associated with positive x_i will be decreased rather than increased.

$$\Delta w_i = \eta(t - o)x_i = 0.1(-1 - (1))0.8 = -0.16.$$

Perceptron

33



The **decision surface** represented by a **two-input perceptron x_1 and x_2** .
(a) A set of training examples and the decision surface of a perceptron that classifies them correctly. (b) A set of training examples that is not linearly separable.

Perceptron Training Rule

34

- The **perceptron rule** finds a successful weight vector when the training examples are **linearly separable**,
- It fails to converge if the examples are **not linearly separable**.
- The solution is ... **Delta Rule** also known as **(Widrow-Hoff Rule)**

Delta Rule

- use ***gradient descent*** to search the hypothesis space of possible weight vectors to find the weights that best fit the training examples.

Reading Material

35

- **Artificial Intelligence, A Modern Approach**

Stuart J. Russell and Peter Norvig

- ▣ Chapter 18.

- **Machine Learning**

Tom M. Mitchell

- ▣ Chapter 4.

