

Part #2:- $(0,0,1)$

forward propagation.

$$n_1 = G[x_1 w_1 + x_2 w_2 + b_1]$$

$$0,0,1 \rightarrow G(0.1) = 0.0996$$

$$1,0,0 \rightarrow G(0.2) = 0.19737$$

$$0,1,0 \rightarrow G(0.2) = 0.19737$$

$$1,1,1 \rightarrow G(0.3) = 0.2913$$

$$n_2 = G[x_1 w_3 + x_2 w_4 + b_2]$$

$$0,0,1 \rightarrow G(0.1) = 0.099$$

$$1,0,0 \rightarrow G(0.2) = 0.19737$$

$$0,1,0 \rightarrow G(0.2) = 0.197$$

$$1,1,1 \rightarrow G(0.3) = 0.2913$$

$$y_{HAT} = G[n_1 w_5 + n_2 w_6 + b_3]$$

$$0,0,1 \rightarrow G(0.1199336) = 0.1193$$

$$1,0,0 \rightarrow G(0.13947506) = 0.1385$$

$$0,1,0 \rightarrow G(0.13946) = 0.3856$$

$$1,1,1 \rightarrow G(0.1582625) = 0.1569$$

$$(0, 0, 1)$$

$$= \frac{1}{2} (1 - 0.11936185)^2$$

$$= 0.3877647756$$

$$(1, 0, 0)$$

$$= \frac{1}{2} (1 - 0.13857763)^2 \Rightarrow 0.37102424$$

$$(0, 1, 0)$$

$$= \frac{1}{2} (0 - 0.3856286)^2$$

$$= 0.07435470857$$

$$(1, 1, 1)$$

$$= \frac{1}{2} (1 - 0.1569543)^2$$

$$= 0.3553630261$$

$$\delta y_{HAT} = y_{HAT} (1 - y_{HAT}) (t_{y_{HAT}} - y_{HAT})$$

$$= 0.11936185 (1 - 0.11936185) (1 - 0.11936185)$$

$$= 0.11936185 (0.88063815) (0.88063815)$$

$$= 0.092567925$$

$$\delta n_1 = n_1 (1 - n_1) w_5 + \delta y_{HAT}$$

$$= (0.099668) (0.900332) (0.1) + 0.092567925$$

$$= 0.101541354$$

$$\delta n_2 = n_2 (1 - n_2) w_6 + \delta y_{HAT}$$

$$= (0.099668) (0.900332) (0.1) + 0.092567925$$

$$= 0.101541354$$

$$w_1 = \Delta w_1 + w_1$$

$$\Delta w_1 = \eta \delta n_1 x_1 = (0.5)(0.16541354)(0) = 0$$

$$w_1 = 0 + 0.1 \Rightarrow \boxed{w_1 = 0.1}$$

$$w_2 = \Delta w_2 + w_2$$

$$\Delta w_2 = \eta \delta n_2 x_2 = (0.5)(0.16541354)(0) = 0$$

$$w_2 = 0 + 0.1 \Rightarrow \boxed{w_2 = 0.1}$$

$$w_3 = \Delta w_3 + w_3$$

$$\Delta w_3 = \eta \delta n_3 x_3 = 0$$

$$w_3 = 0 + 0.1 \Rightarrow \boxed{w_3 = 0.1}$$

$$w_4 = \Delta w_4 + w_4$$

$$\Delta w_4 = \eta \delta n_4 x_4 = 0$$

$$w_4 = \Delta w_4 + w_4 = 0 + 0.1 = \boxed{0.1 = w_4}$$

$$w_5 = w_5 + \Delta w_5$$

$$\Delta w_5 = \eta \delta y_{HAT} n_5 = (0.5)(0.092567925)(0.099668) \\ = 0.004613029$$

$$w_5 = 0.1 + 0.004613029 \Rightarrow \boxed{w_5 = 0.10461303}$$

$$w_6 = \Delta w_6 + w_6$$

$$\Delta w_6 = 0.004613029$$

$$\boxed{w_6 = 0.10461303}$$

Iteration #02.

(0, 0, 1)

$$n_1 = 0.099668$$

$$n_2 = 0.099668$$

$$y_{HAT} = 0.17077132$$

(1,0,0)

$$n_1 = 0.197375$$

$$n_2 = 0.197375$$

$$y_{HAT} = 0.1403684$$

(0,1,0)

$$n_1 = 0.197375$$

$$n_2 = 0.197375$$

$$y_{HAT} = 0.1413019$$

(1,1,1)

$$n_1 = 0.2913126$$

$$n_2 = 0.2913126$$

$$y_{HAT} = 0.1595831$$

Error computation:

$$(0,0,1) \rightarrow \frac{1}{2} (1 - 0.1202)^2 = 0.38696$$

$$(1,0,0) \rightarrow \frac{1}{2} (0 - 0.1403)^2 = 0.009818$$

$$(0,1,0) \rightarrow \frac{1}{2} (0 - 0.14013)^2 = 0.009818$$

$$(1,1,1) \rightarrow \frac{1}{2} (1 - 0.159831)^2 = 0.3529$$

Back Propagation.

$$\delta y_{HAT} = 0.09308068672$$

$$\delta n_1 = 0.000835$$

$$\delta n_2 = 0.000835$$

updating weights:-

$$w_1 = 0.1 \quad , \quad w_2 = 0.1$$

$$w_3 = 0.1 \quad , \quad w_4 = 0.1$$

$$w_5 = 0.1092516129$$

$$w_6 = 0.1092516129$$