



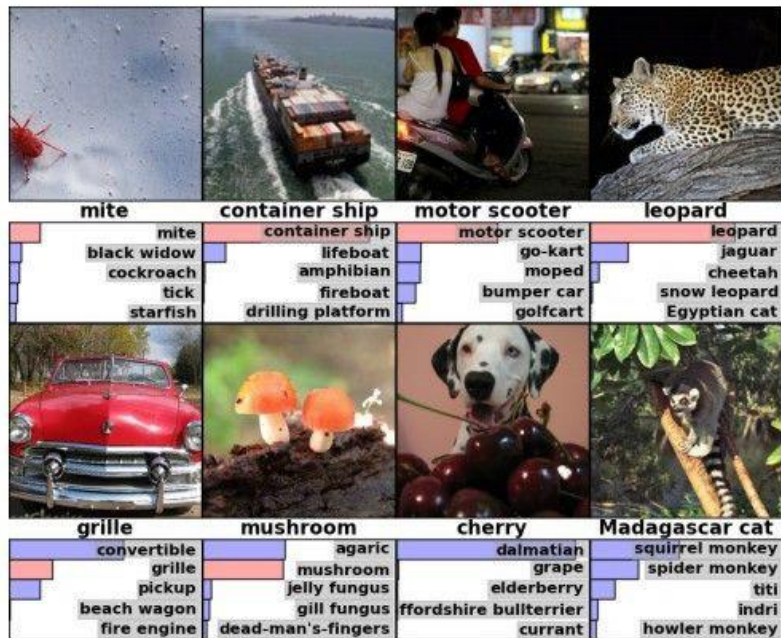
# 11. Convolutional Neural Network

COMP3314  
Machine Learning

Slides adapted from CS231N at Stanford

# ConvNets are everywhere

Classification



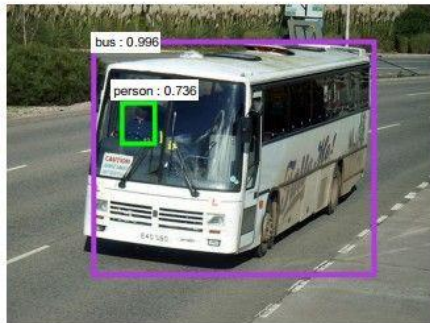
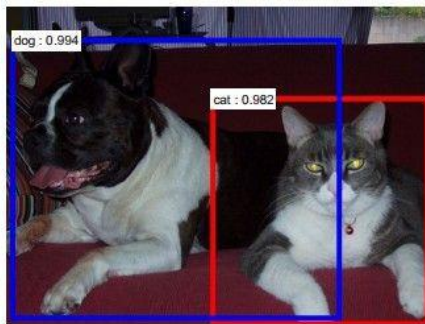
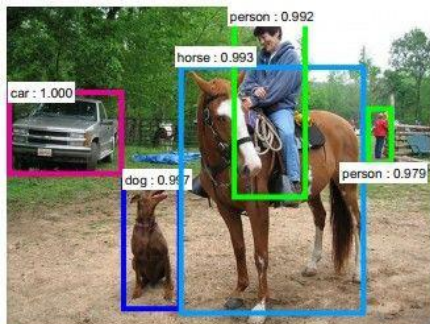
Retrieval



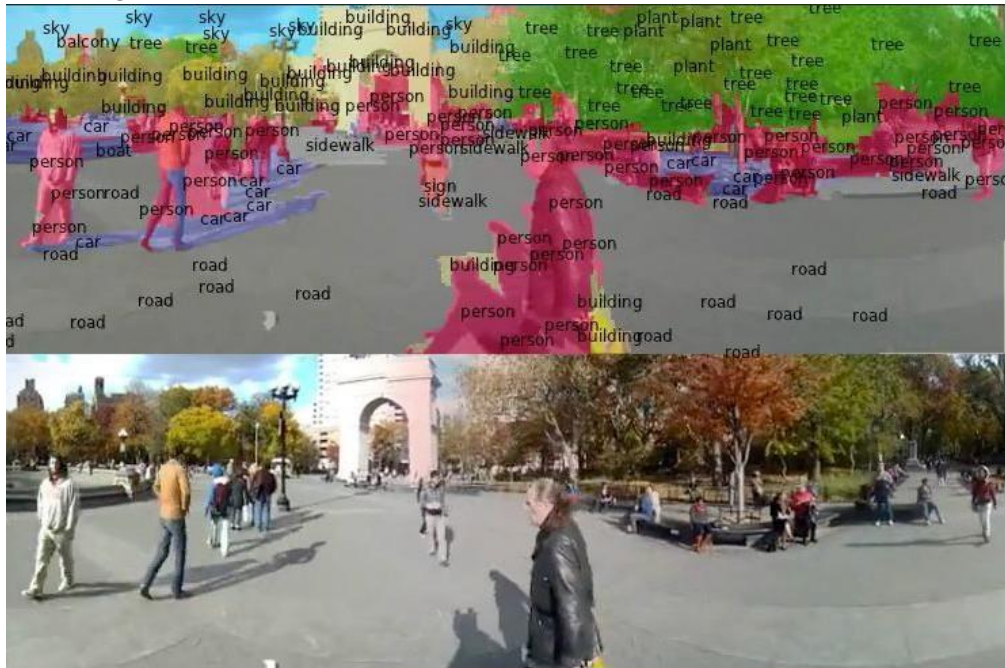
Figures copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

# ConvNets are everywhere

## Detection



## Segmentation



Figures copyright Clement Farabet, 2012.  
Reproduced with permission.

[Farabet et al., 2012]

Figures copyright Shaoqing Ren, Kaiming He, Ross Girshick, Jian Sun, 2015. Reproduced with permission.

[Faster R-CNN: Ren, He, Girshick, Sun 2015]



# ConvNets are everywhere

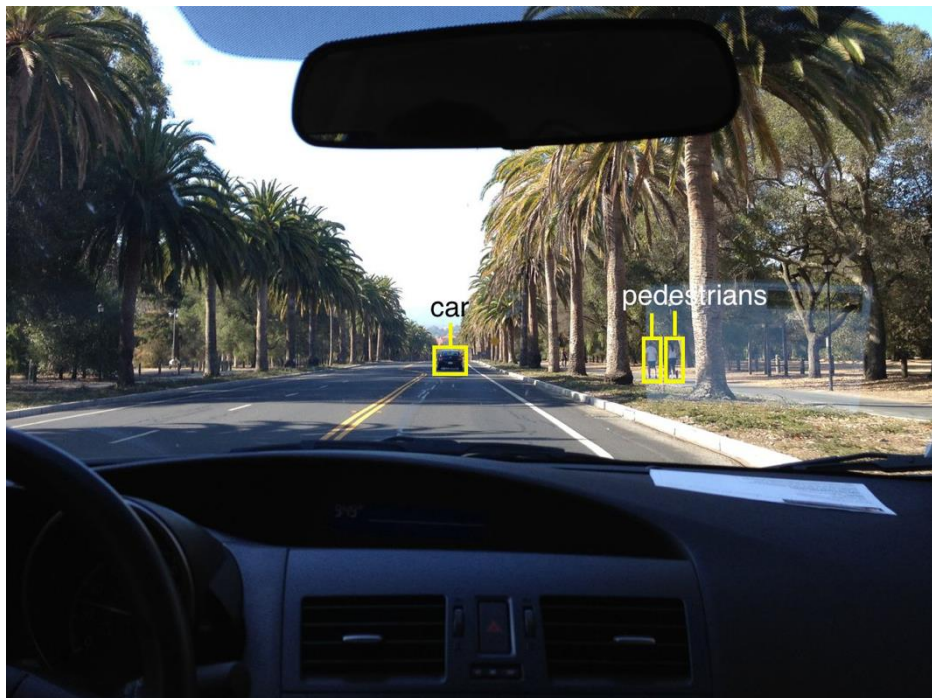


Photo by Lane McIntosh.

self-driving cars

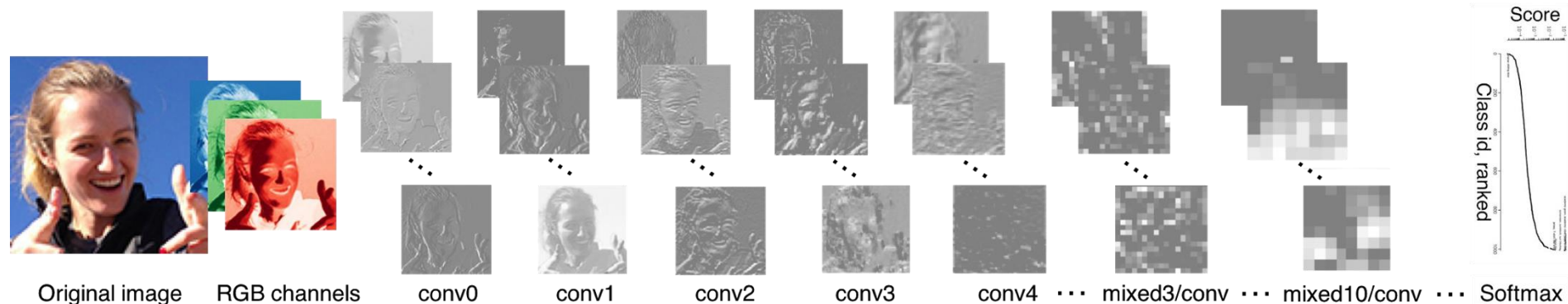


[This image](#) by GBPublic\_PR is licensed under [CC-BY 2.0](#)

## NVIDIA Tesla line

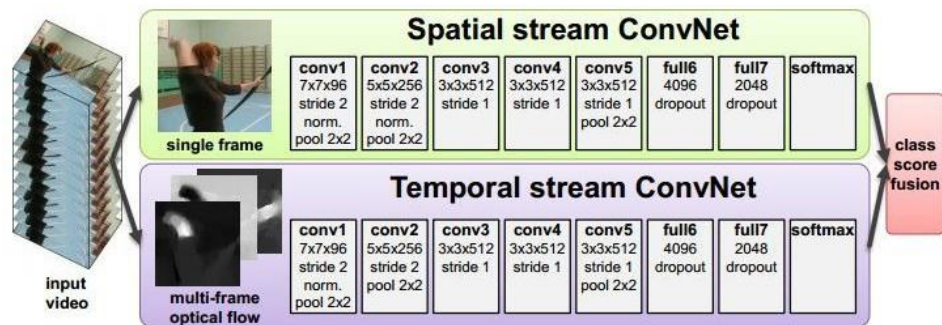
Note that for embedded systems a typical setup would involve NVIDIA Tegras, with integrated GPU and ARM-based CPU cores.

# ConvNets are everywhere



[Taigman et al. 2014]

Activations of [inception-v3 architecture](#) [Szegedy et al. 2015] to image of Emma McIntosh, used with permission. Figure and architecture not from Taigman et al. 2014.



[Simonyan et al. 2014]

Figures copyright Simonyan et al., 2014.  
Reproduced with permission.

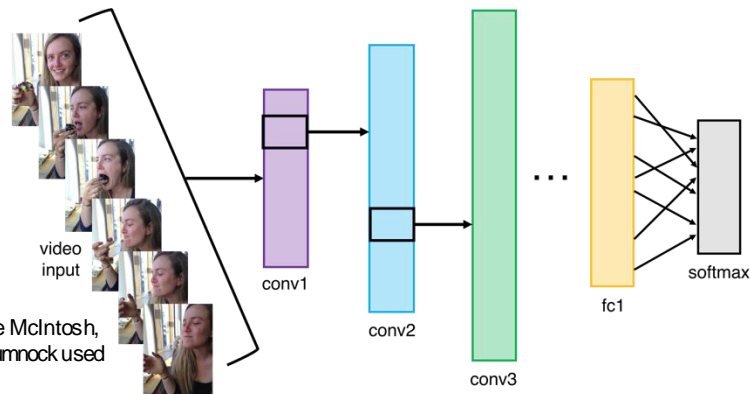


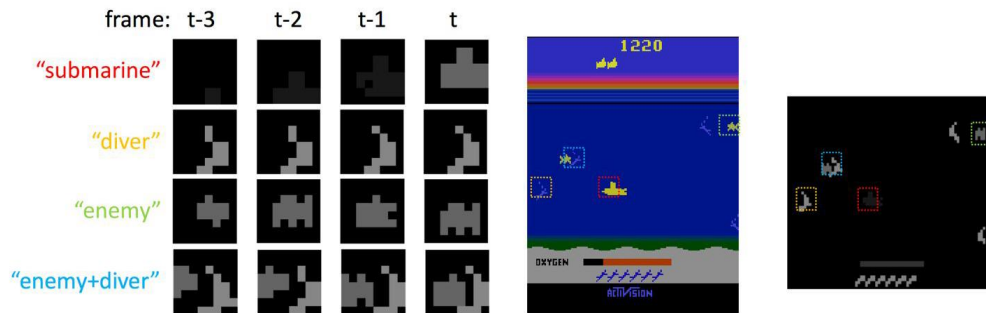
Illustration by Lane McIntosh,  
photos of Katie Cunnock used  
with permission.

# ConvNets are everywhere

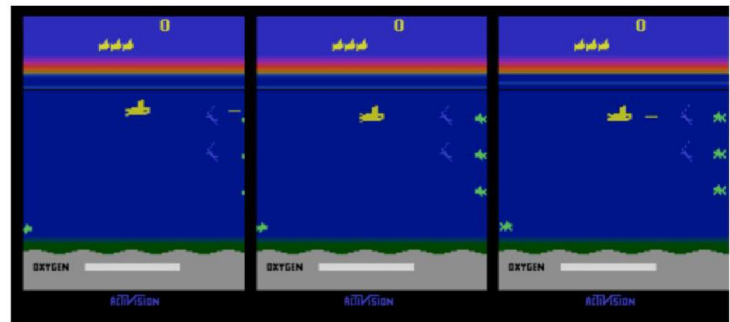


Images are examples of pose estimation, not actually from Toshev & Szegedy 2014. Copyright Lane McIntosh.

[Toshev, Szegedy 2014]



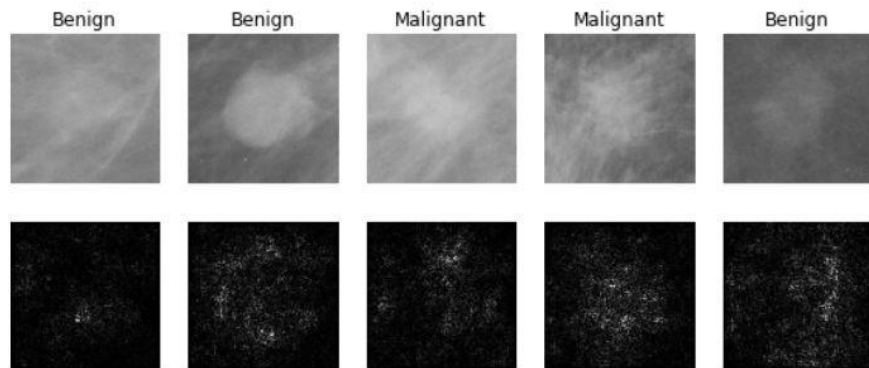
[Guo et al. 2014]



Figures copyright Xiaoxiao Guo, Satinder Singh, Honglak Lee, Richard Lewis, and Xiaoshi Wang, 2014. Reproduced with permission.



# ConvNets are everywhere



[Levy et al. 2016]

Figure copyright Levy et al. 2016.  
Reproduced with permission.



[Dieleman et al. 2014]

From left to right: [public domain by NASA](#), usage [permitted](#) by ESA/Hubble, [public domain by NASA](#), and [public domain](#).

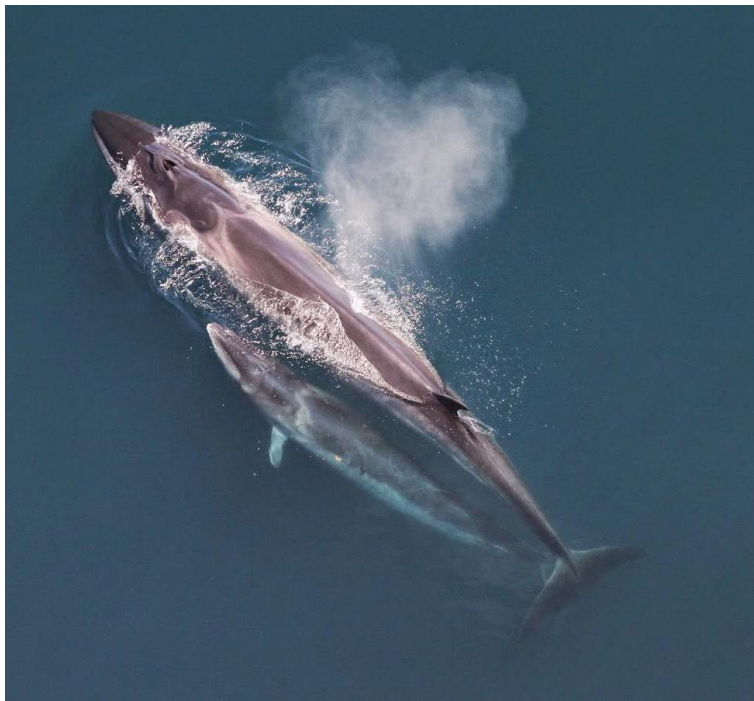


[Sermanet et al. 2011]

[Ciresan et al.]

Photos by Lane McIntosh.

[This image](#) by Christin Khan is in the public domain and originally came from the U.S. NOAA.



*Whale recognition, Kaggle Challenge*

Photo and figure by Lane McIntosh; not actual example from Mnih and Hinton, 2010 paper.



*Mnih and Hinton, 2010*



No errors



*A white teddy bear sitting in the grass*

Minor errors



*A man in a baseball uniform throwing a ball*

Somewhat related



*A woman is holding a cat in her hand*

# Image Captioning

[Vinyals et al., 2015]  
[Karpathy and Fei-Fei, 2015]



*A man riding a wave on top of a surfboard*



*A cat sitting on a suitcase on the floor*

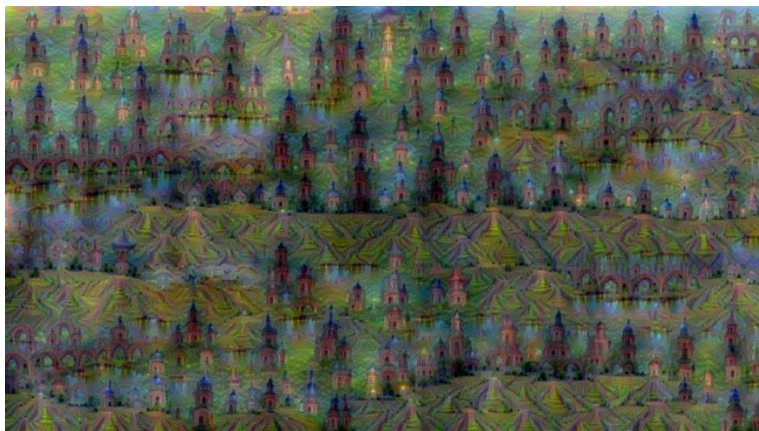
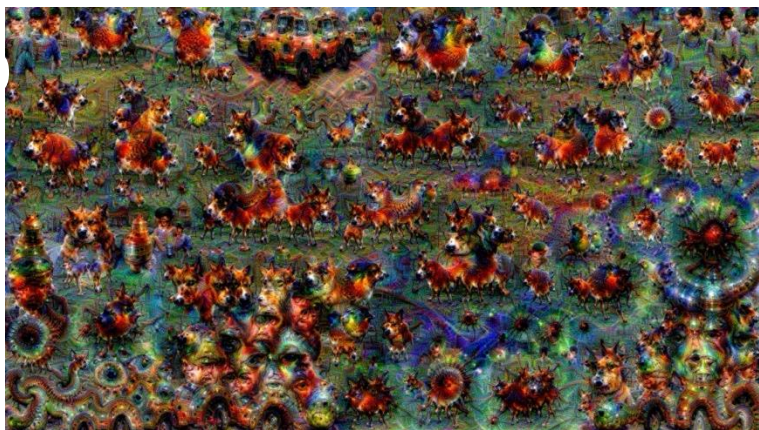


*A woman standing on a beach holding a surfboard*

All images are CC0 Public domain:

<https://pixabay.com/en/luggage-antique-cat-1643010/>  
<https://pixabay.com/en/teddy-plush-bears-cute-teddy-bear-1623436/>  
<https://pixabay.com/en/surf-wave-summer-sport-litoral-1668716/>  
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<https://pixabay.com/en/handstand-lake-meditation-496008/>  
<https://pixabay.com/en/baseball-player-shortstop-infield-1045263/>

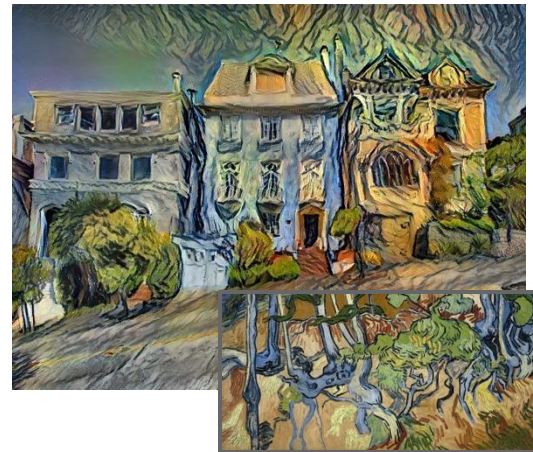
Captions generated by Justin Johnson using [NeuralTalk2](#)



Figures copyright Justin Johnson, 2015. Reproduced with permission. Generated using the Inceptionism approach from a [blog post](#) by Google Research.



[Original image](#) is CC0 public domain  
[Starry Night](#) and [Tree Roots](#) by Van Gogh are in the public domain  
[Bokeh image](#) is in the public domain  
 Stylized images copyright Justin Johnson, 2017;  
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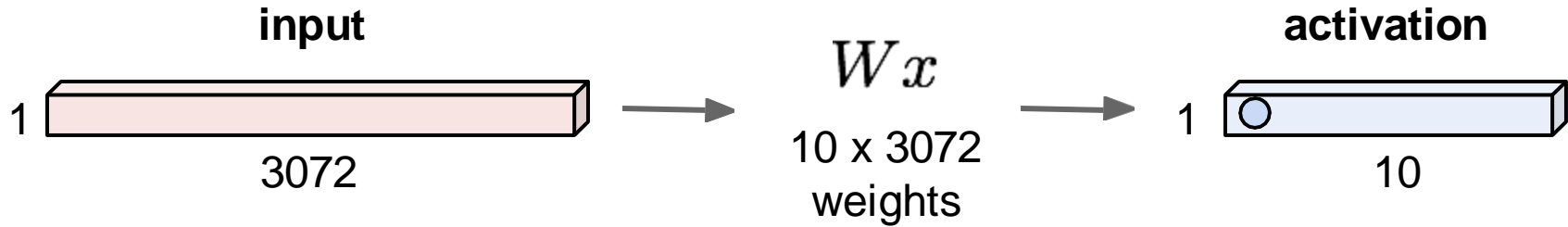
Gatys et al, "Image Style Transfer using Convolutional Neural Networks", CVPR 2016  
 Gatys et al, "Controlling Perceptual Factors in Neural Style Transfer", CVPR 2017

# Convolutional Neural Networks



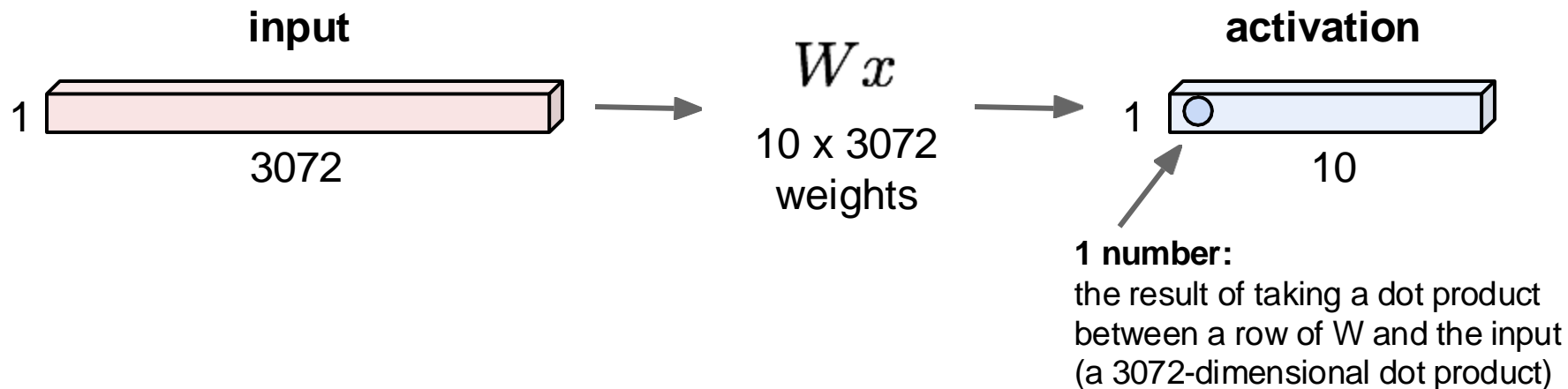
# Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1



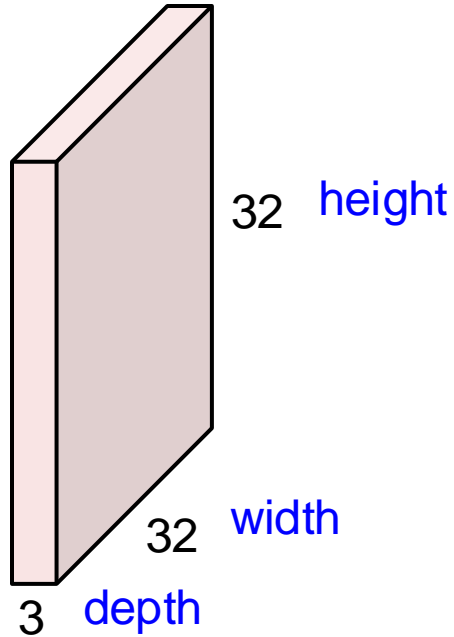
# Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1



# Convolution Layer

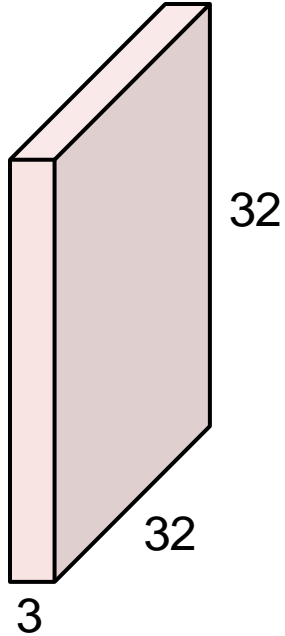
32x32x3 image -> preserve spatial structure





# Convolution Layer

32x32x3 image



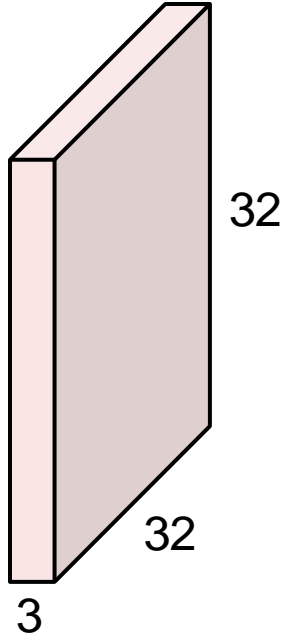
5x5x3 filter



**Convolve** the filter with the image  
i.e. “slide over the image spatially,  
computing dot products”

# Convolution Layer

32x32x3 image



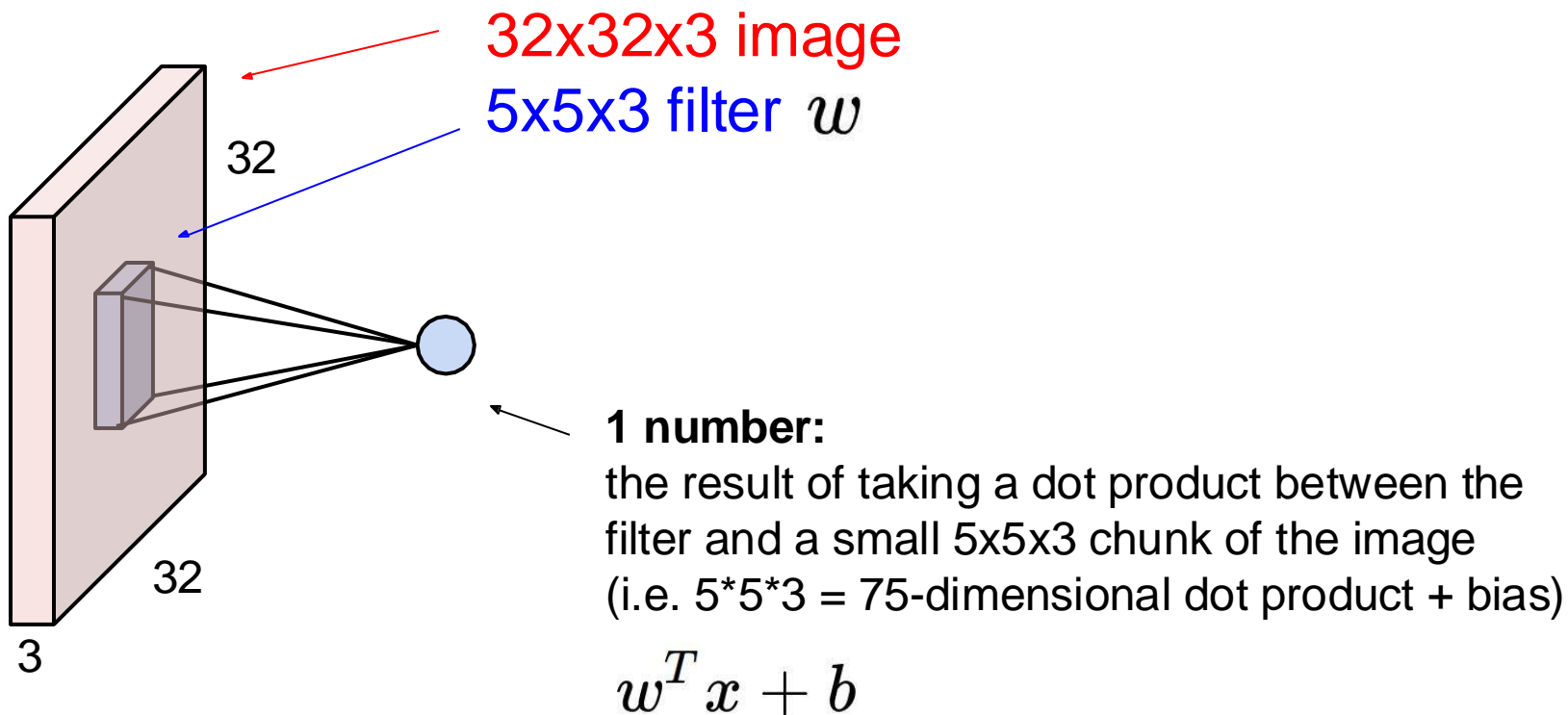
Filters always extend the full depth of the input volume

5x5x3 filter



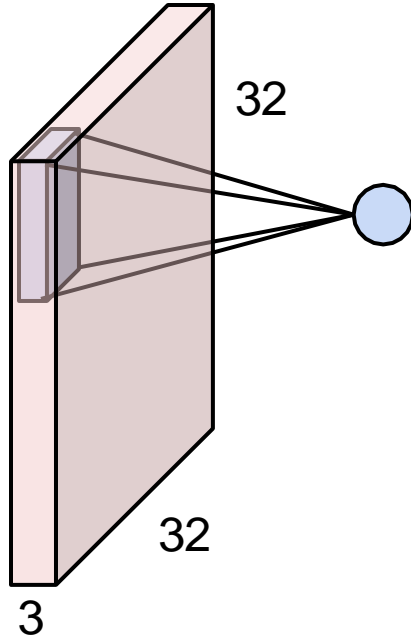
**Convolve** the filter with the image  
i.e. “slide over the image spatially,  
computing dot products”

# Convolution Layer

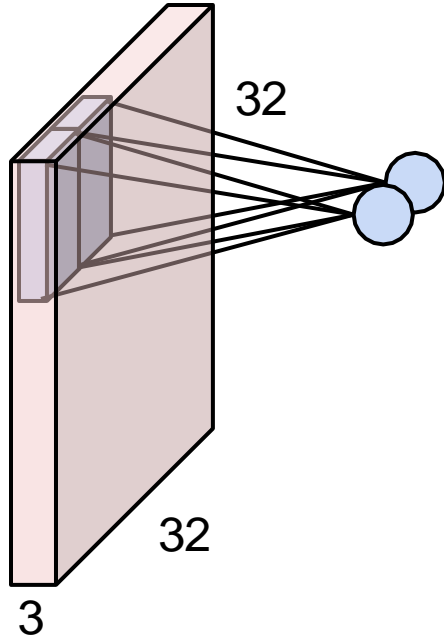




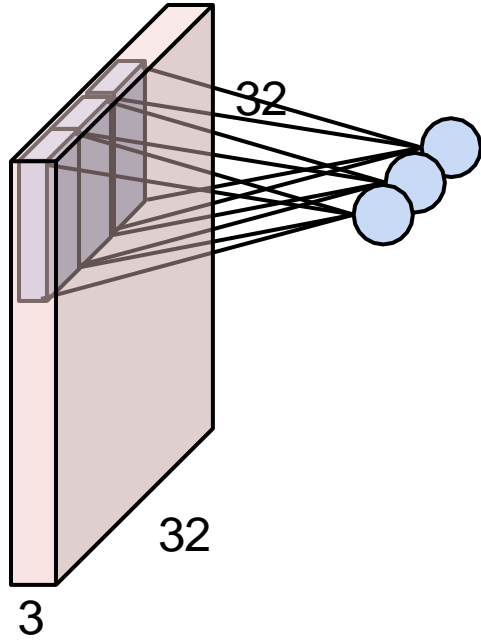
# Convolution Layer



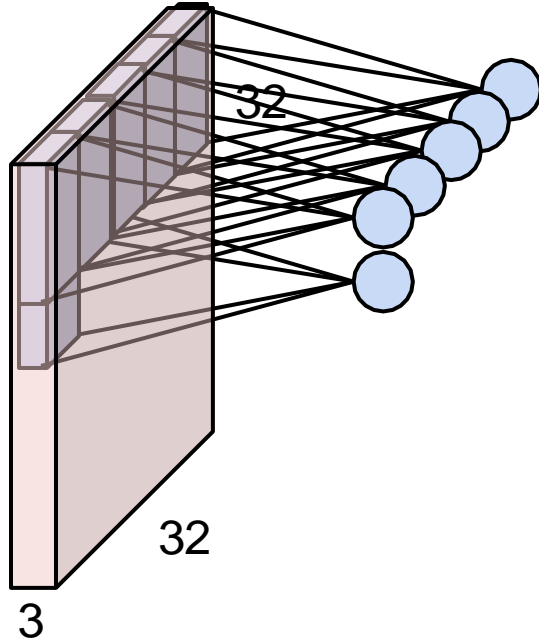
# Convolution Layer



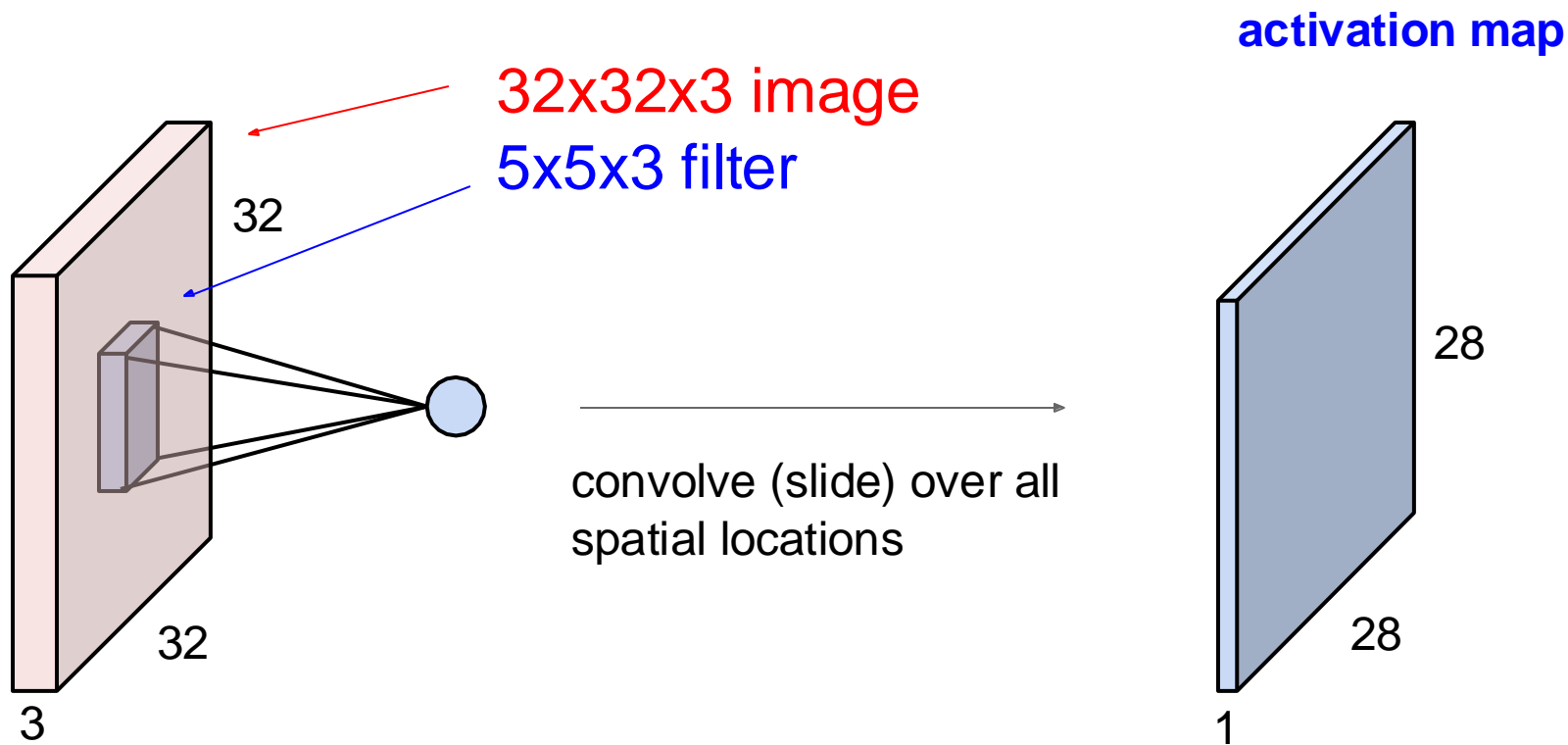
# Convolution Layer



# Convolution Layer



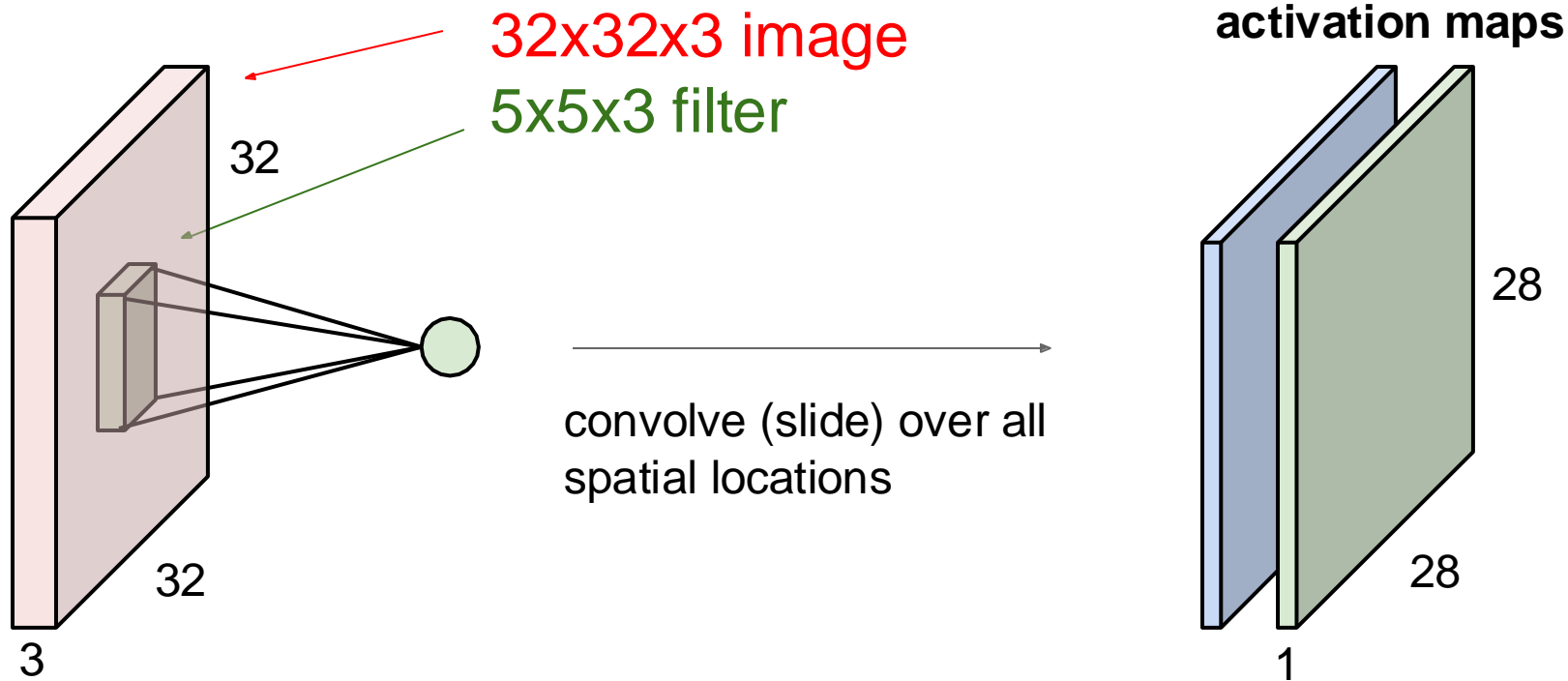
# Convolution Layer





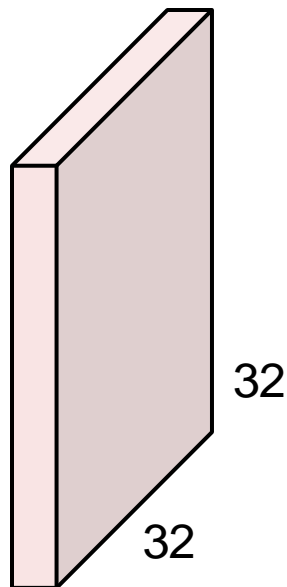
# Convolution Layer

consider a second, **green** filter



# Convolution Layer

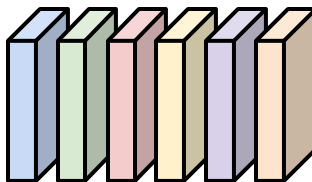
3x32x32 image



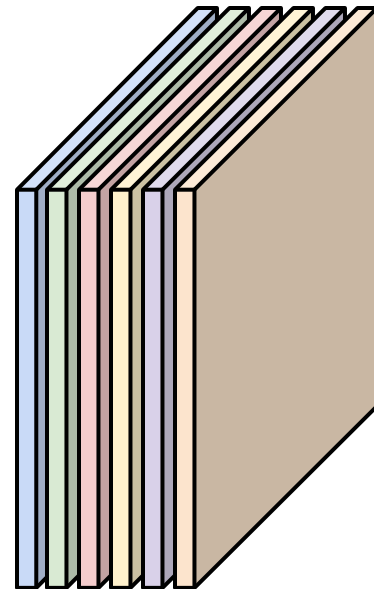
Consider 6 filters,  
each 3x5x5

Convolution  
Layer

6x3x5x5  
filters



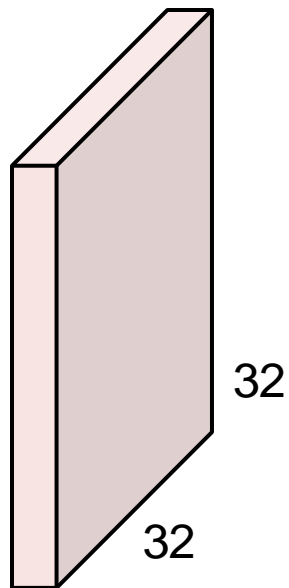
6 activation maps,  
each 1x28x28



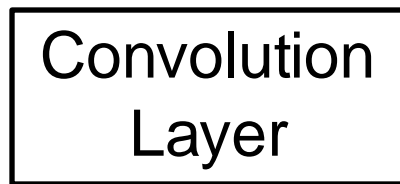
Stack activations to get a  
6x28x28 output feature!

# Convolution Layer

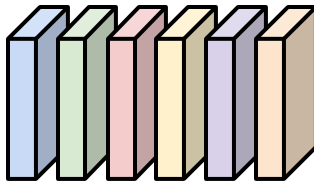
3x32x32 image



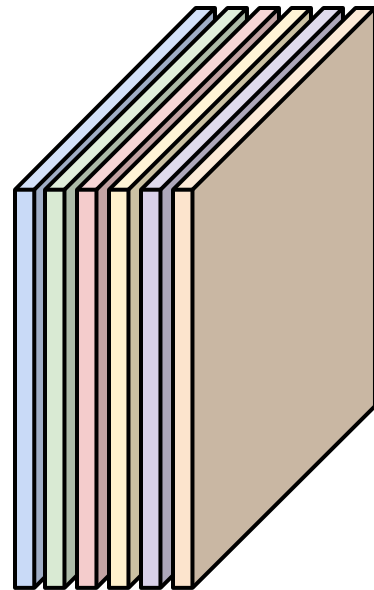
Also 6-dim bias vector:



6x3x5x5  
filters



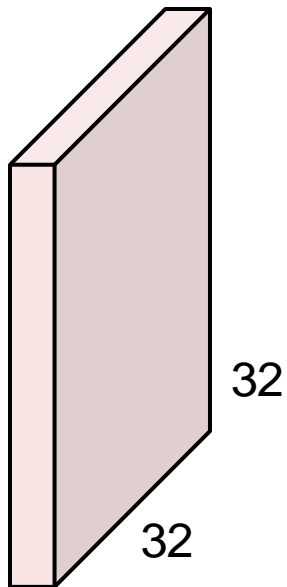
6 activation maps,  
each 1x28x28



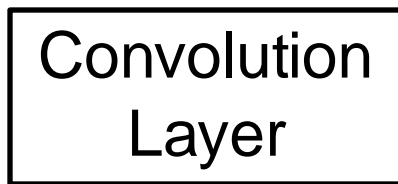
Stack activations to get a  
6x28x28 output feature!

# Convolution Layer

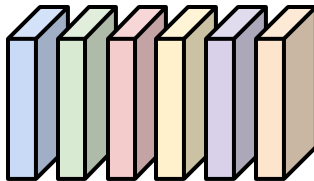
3x32x32 image



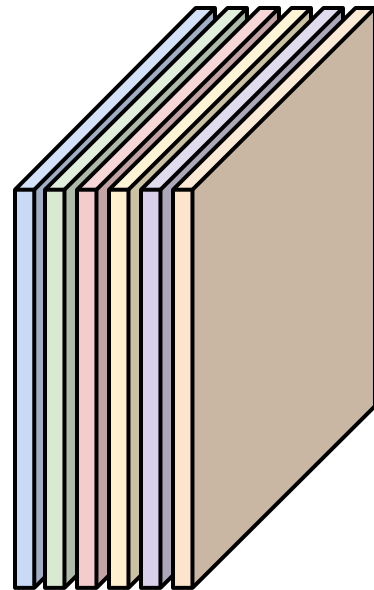
Also 6-dim bias vector:



6x3x5x5 filters



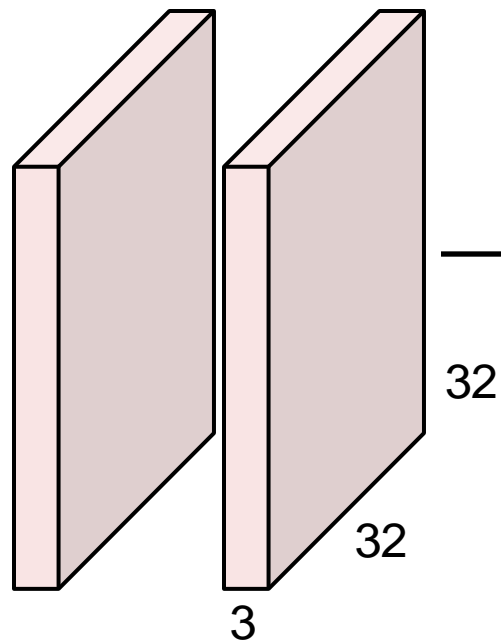
28x28 grid, at each point a 6-dim vector



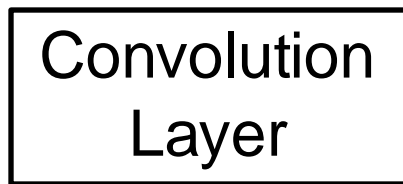
Stack activations to get a 6x28x28 output feature!

# Convolution Layer

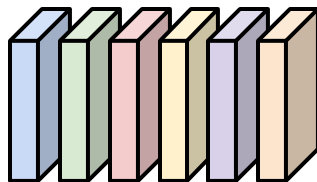
2x3x32x32  
Batch of images



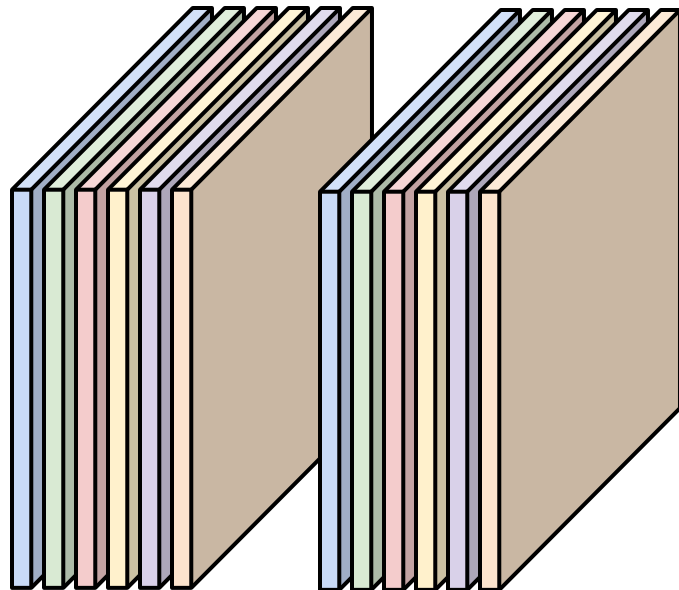
Also 6-dim bias vector:



6x3x5x5  
filters



2x6x28x28  
Batch of outputs





# Convolution Layer

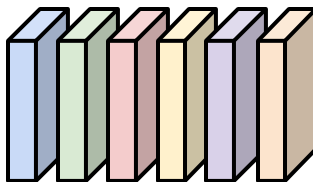
$N \times C_{in} \times H \times W$   
Batch of images

Also  $C_{out}$ -dim bias vector:

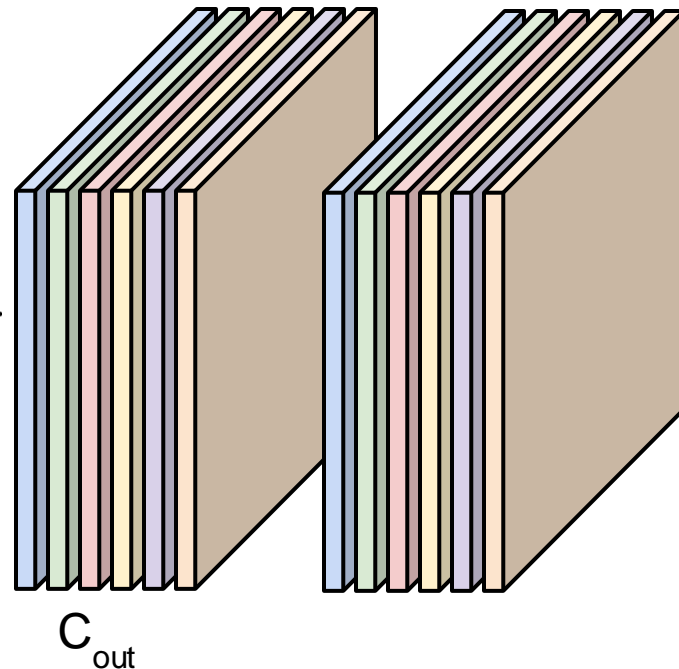


Convolution  
Layer

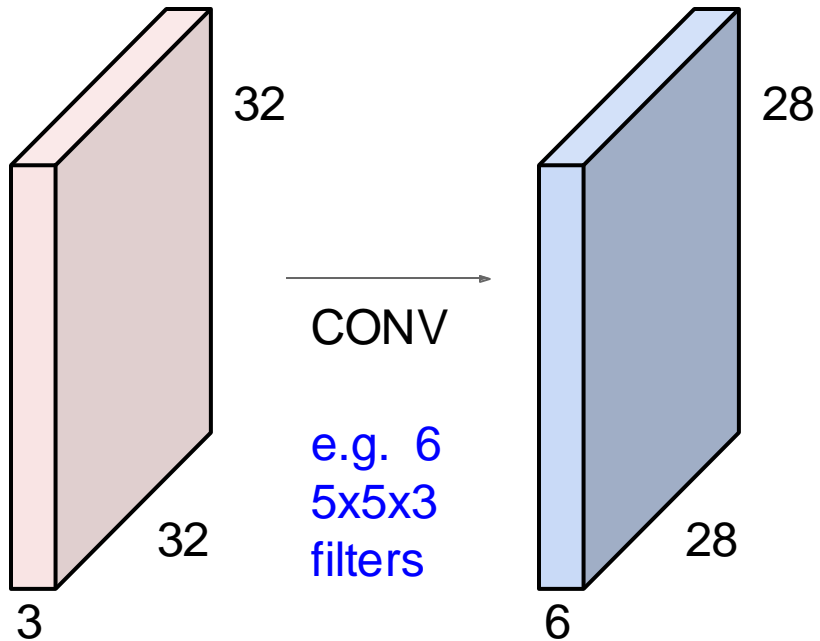
$C_{out} \times C_{in} \times K_w \times K_h$   
filters



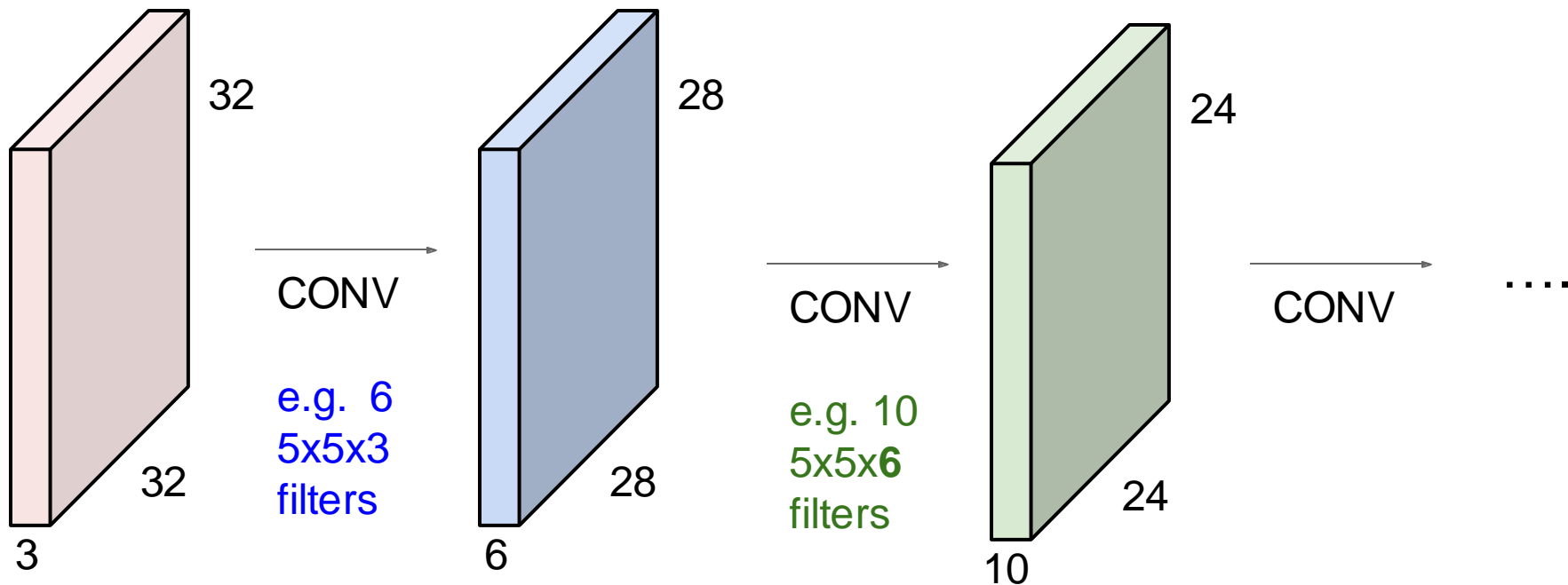
$N \times C_{out} \times H' \times W'$   
Batch of outputs



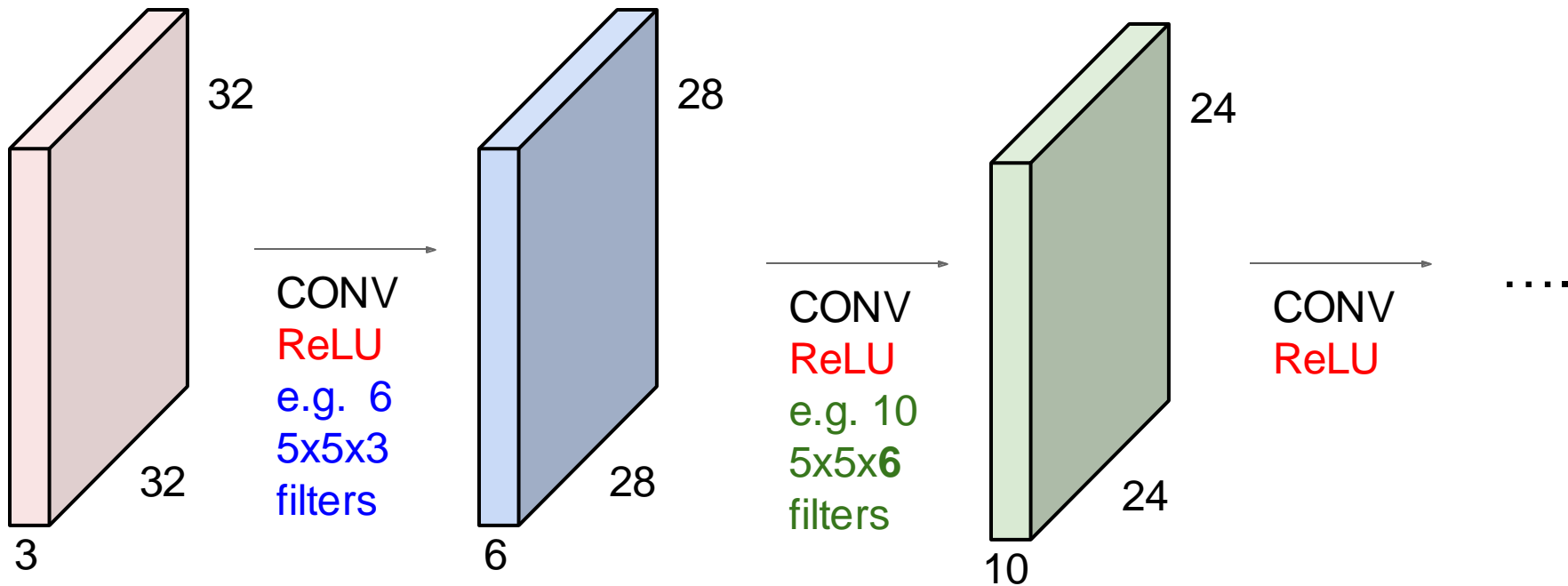
## Preview: ConvNet is a sequence of Convolution Layers



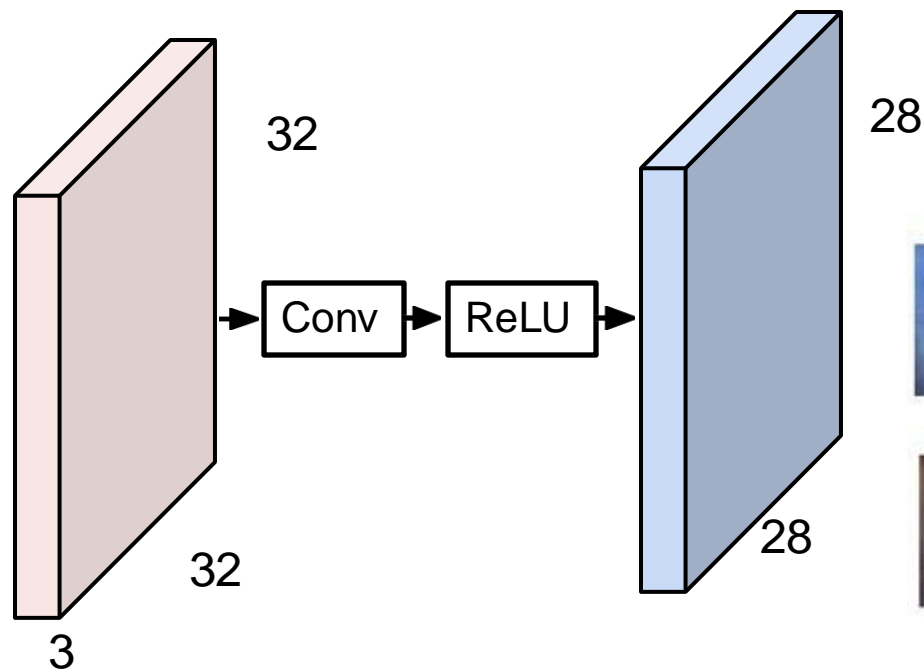
## Preview: ConvNet is a sequence of Convolution Layers



**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions



## Preview: What do convolutional filters learn?

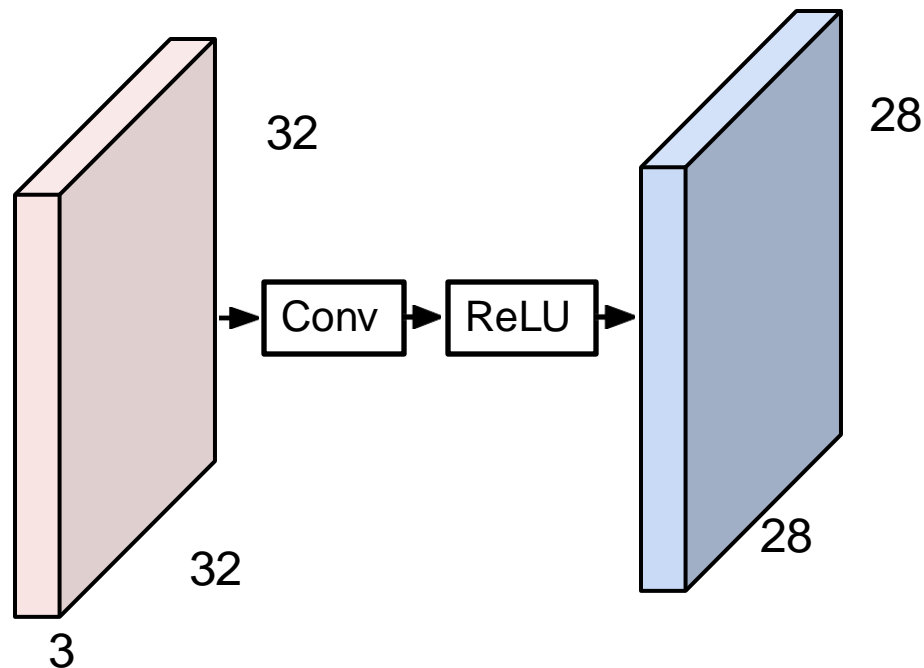


Linear classifier: One template per class





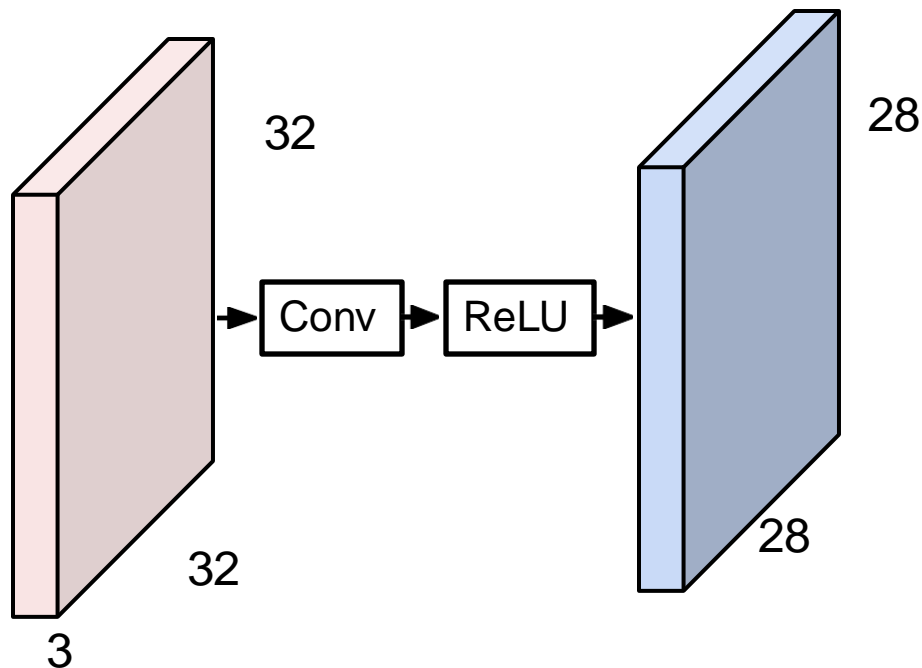
## Preview: What do convolutional filters learn?



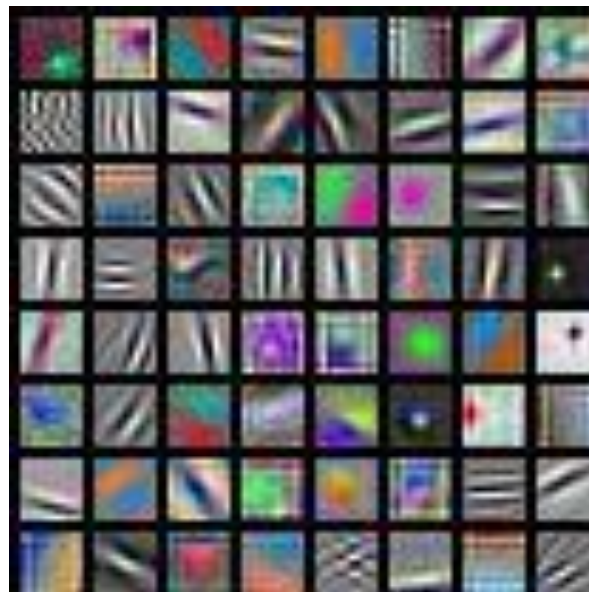
MLP: Bank of whole-image templates



## Preview: What do convolutional filters learn?



First-layer conv filters: local image templates  
(Often learns oriented edges, opposing colors)



AlexNet: 64 filters, each 3x11x11

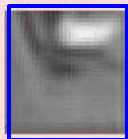


one filter =>  
one activation map



example 5x5 filters  
(32 total)

Activations:



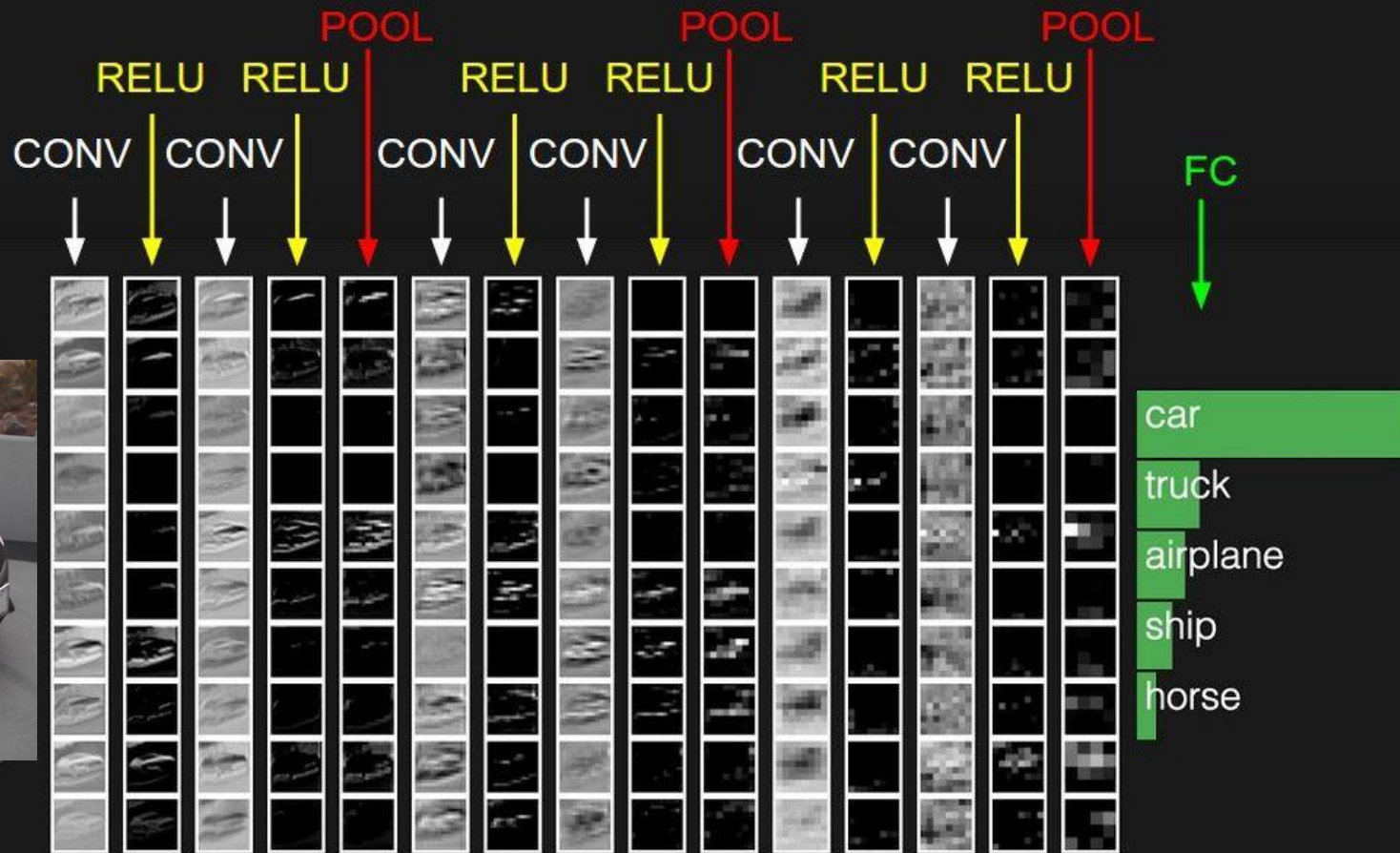
We call the layer convolutional  
because it is related to convolution  
of two signals:

$$f[x,y] * g[x,y] = \sum_{n_1=-\infty}^{\infty} \sum_{n_2=-\infty}^{\infty} f[n_1, n_2] \cdot g[x - n_1, y - n_2]$$

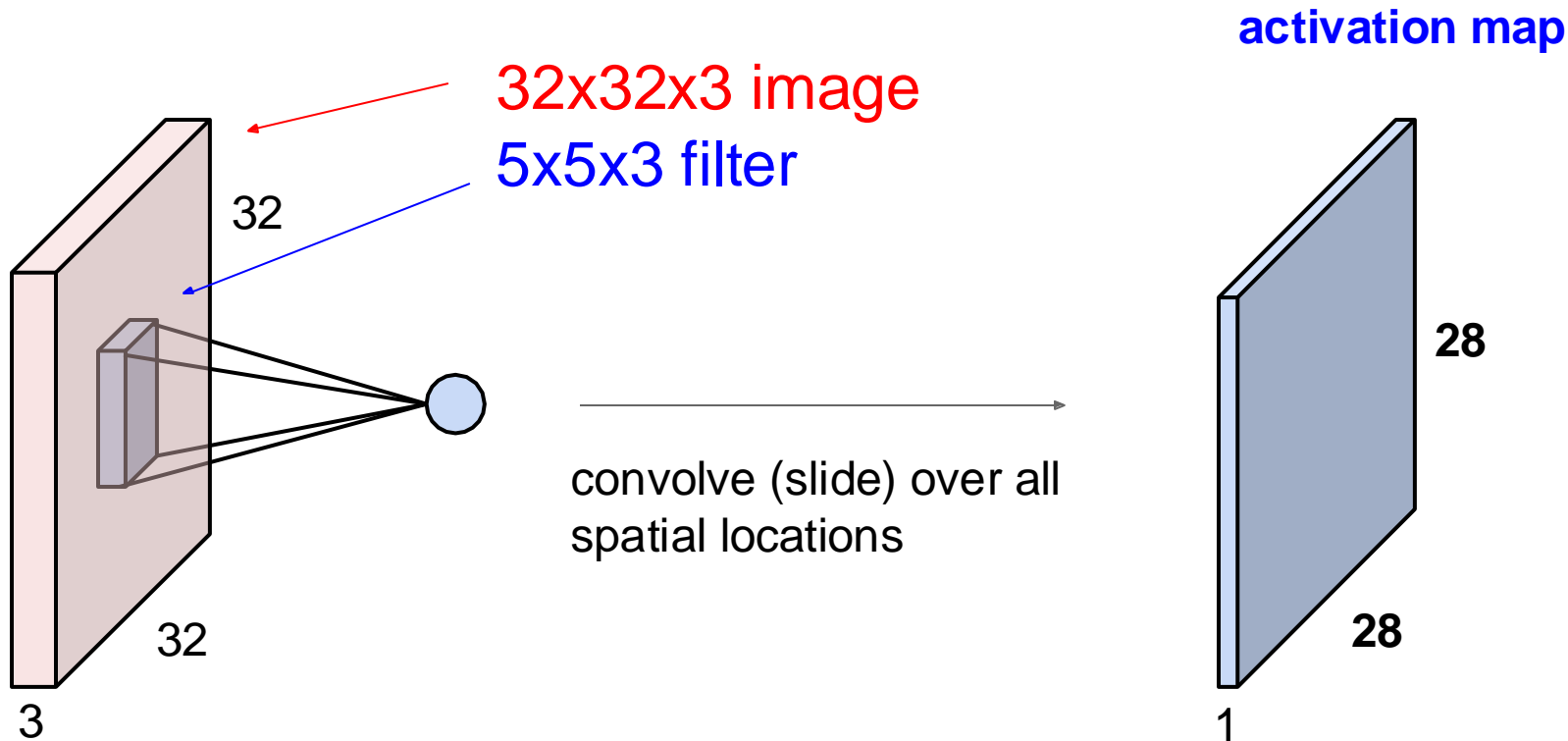


elementwise multiplication and sum of  
a filter and the signal (image)

Figure copyright Andrej Karpathy.

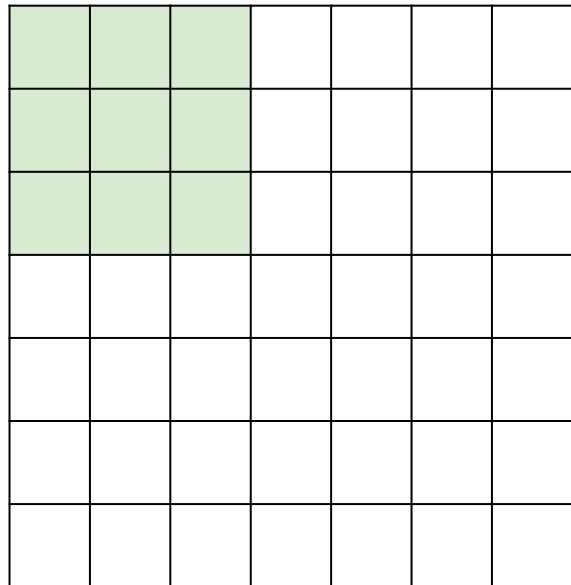


## A closer look at spatial dimensions:



A closer look at spatial dimensions:

7



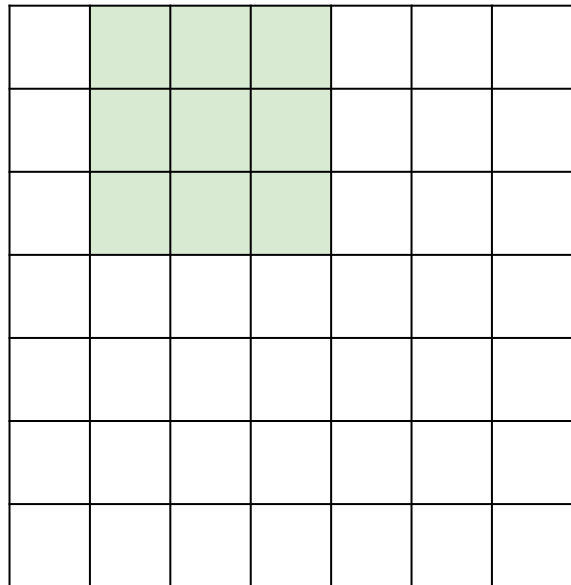
7

7x7 input (spatially)  
assume 3x3 filter



A closer look at spatial dimensions:

7

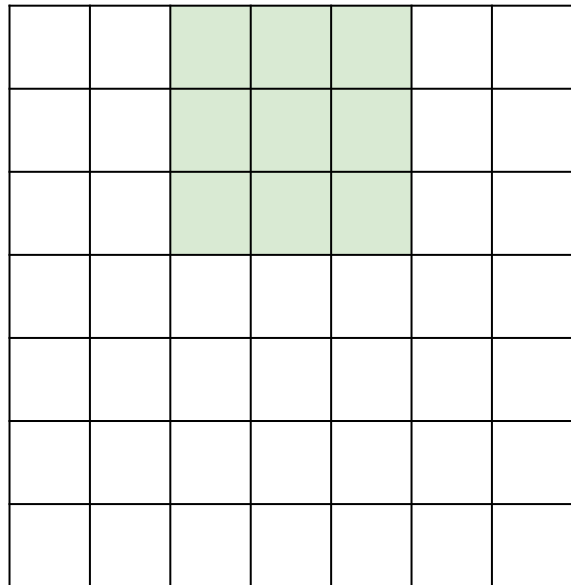


7

7x7 input (spatially)  
assume 3x3 filter

A closer look at spatial dimensions:

7

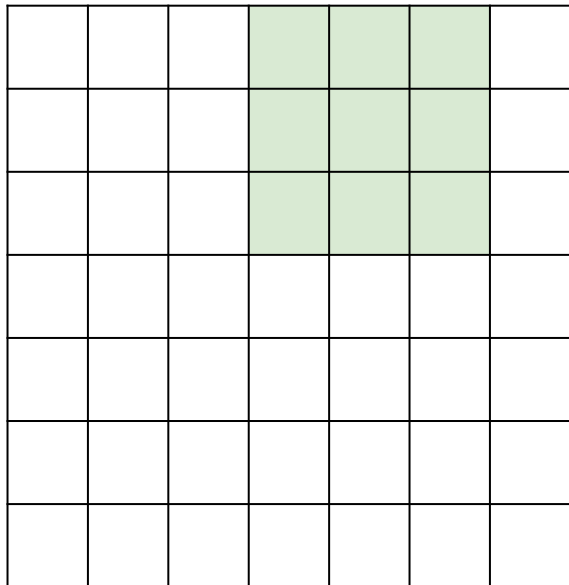


7

7x7 input (spatially)  
assume 3x3 filter

A closer look at spatial dimensions:

7



7

7x7 input (spatially)  
assume 3x3 filter

A closer look at spatial dimensions:

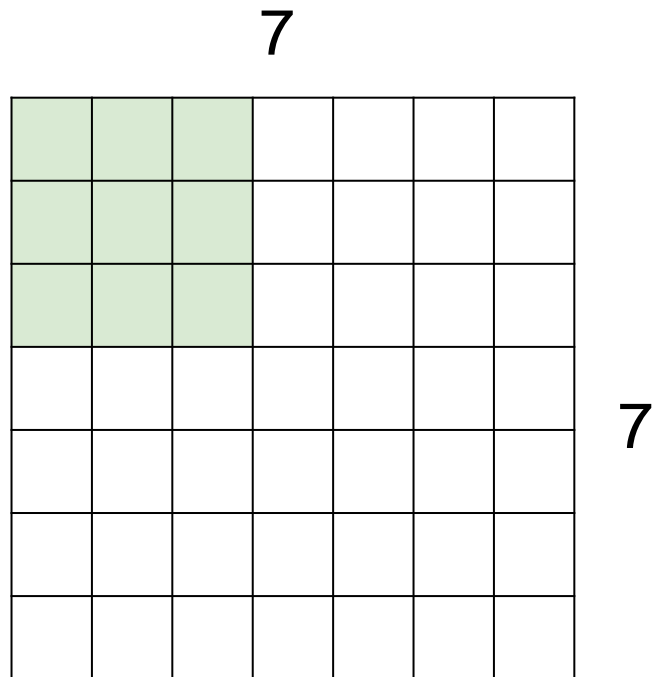
7


7

7x7 input (spatially)  
assume 3x3 filter

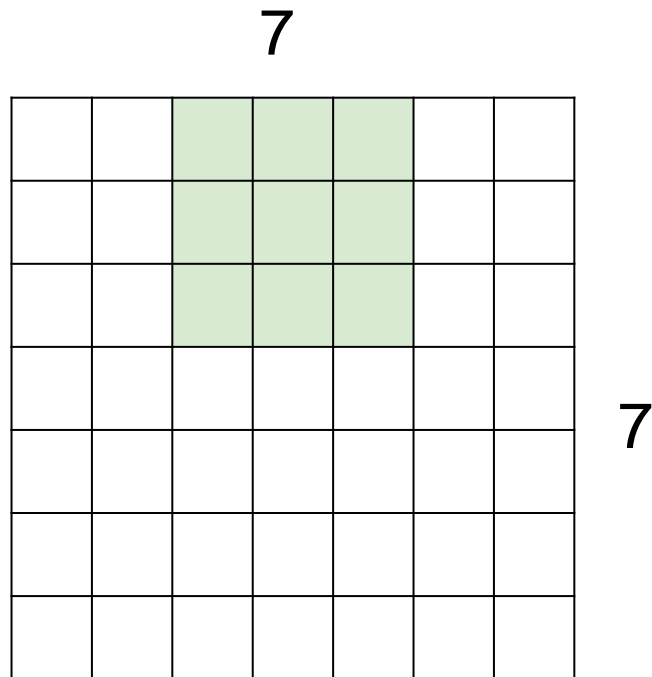
**=> 5x5 output**

A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**

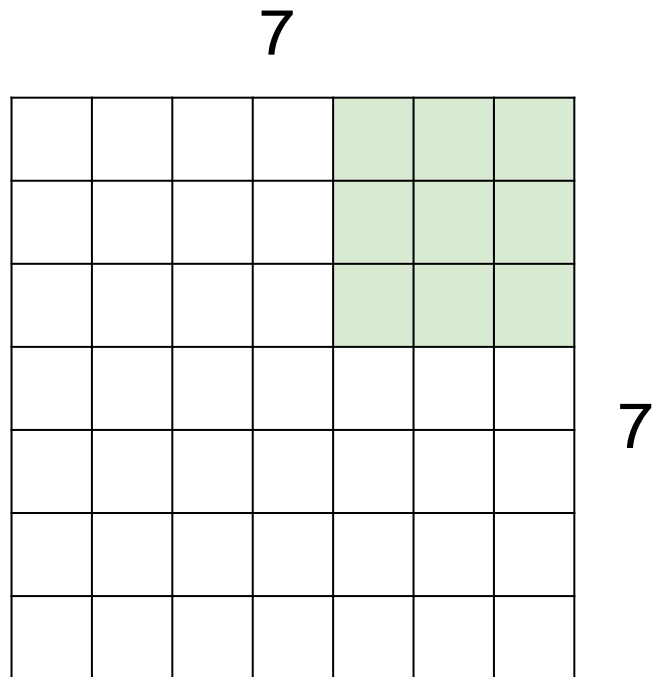
A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**

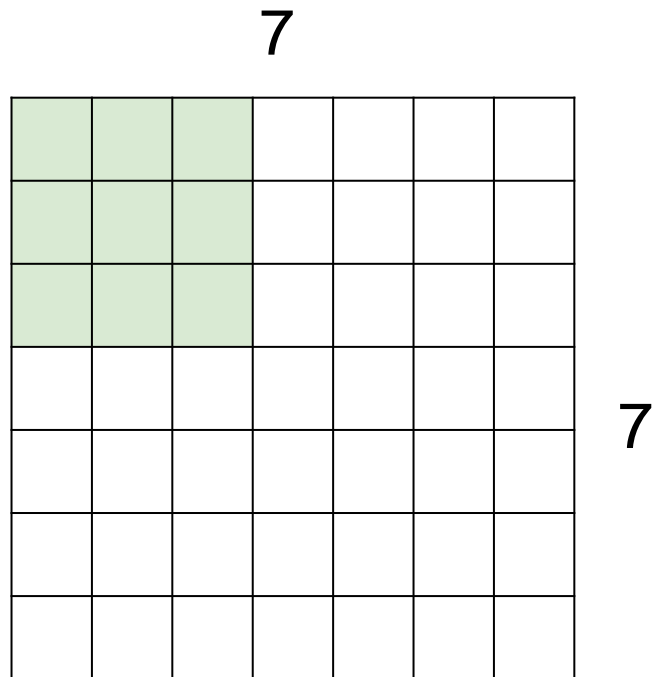


A closer look at spatial dimensions:



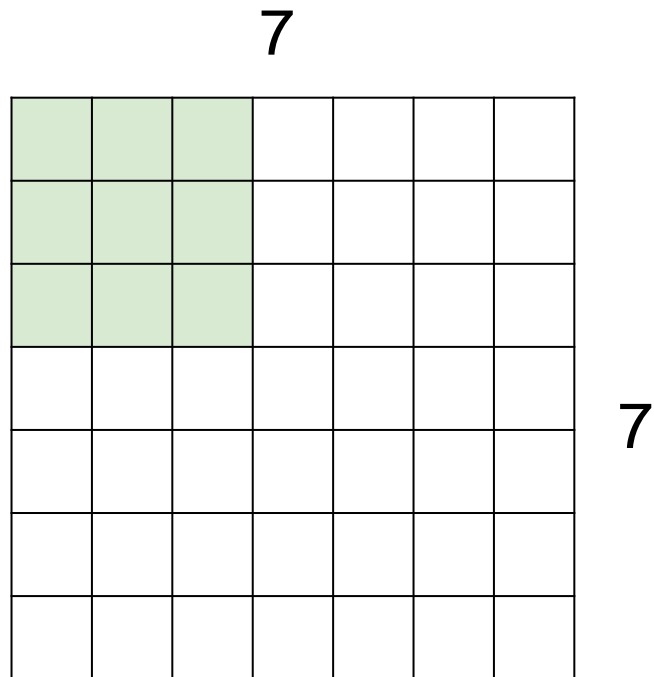
7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**  
**=> 3x3 output!**

A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 3?**

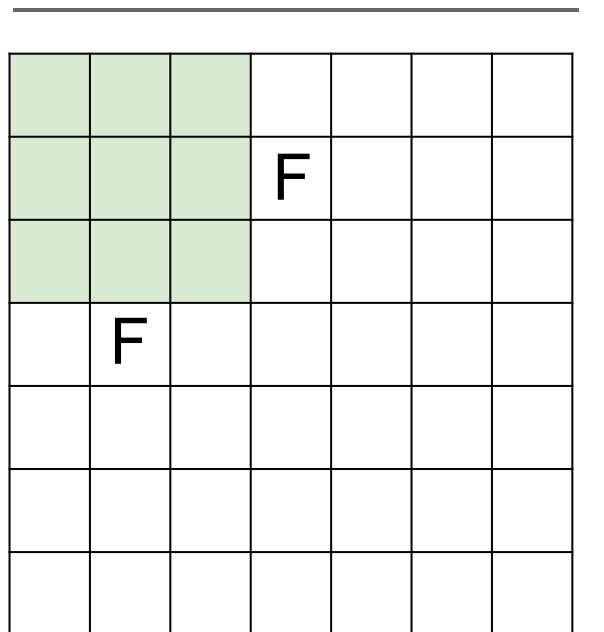
## A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 3?**

**doesn't fit!**  
cannot apply 3x3 filter on  
7x7 input with stride 3.

N



N

Output size:

$$(N - F) / \text{stride} + 1$$

e.g.  $N = 7, F = 3$ :

$$\text{stride } 1 \Rightarrow (7 - 3) / 1 + 1 = 5$$

$$\text{stride } 2 \Rightarrow (7 - 3) / 2 + 1 = 3$$

$$\text{stride } 3 \Rightarrow (7 - 3) / 3 + 1 = 2.33 \therefore \backslash$$

# In practice: Common to zero pad the border

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

(recall:)

$$(N - F) / \text{stride} + 1$$

# In practice: Common to zero pad the border

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

**7x7 output!**

(recall:)

$$(N + 2P - F) / \text{stride} + 1$$

# In practice: Common to zero pad the border

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

**7x7 output!**

in general, common to see CONV layers with stride 1, filters of size  $F \times F$ , and zero-padding with  $(F-1)/2$ . (will preserve size spatially)

e.g.  $F = 3 \Rightarrow$  zero pad with 1

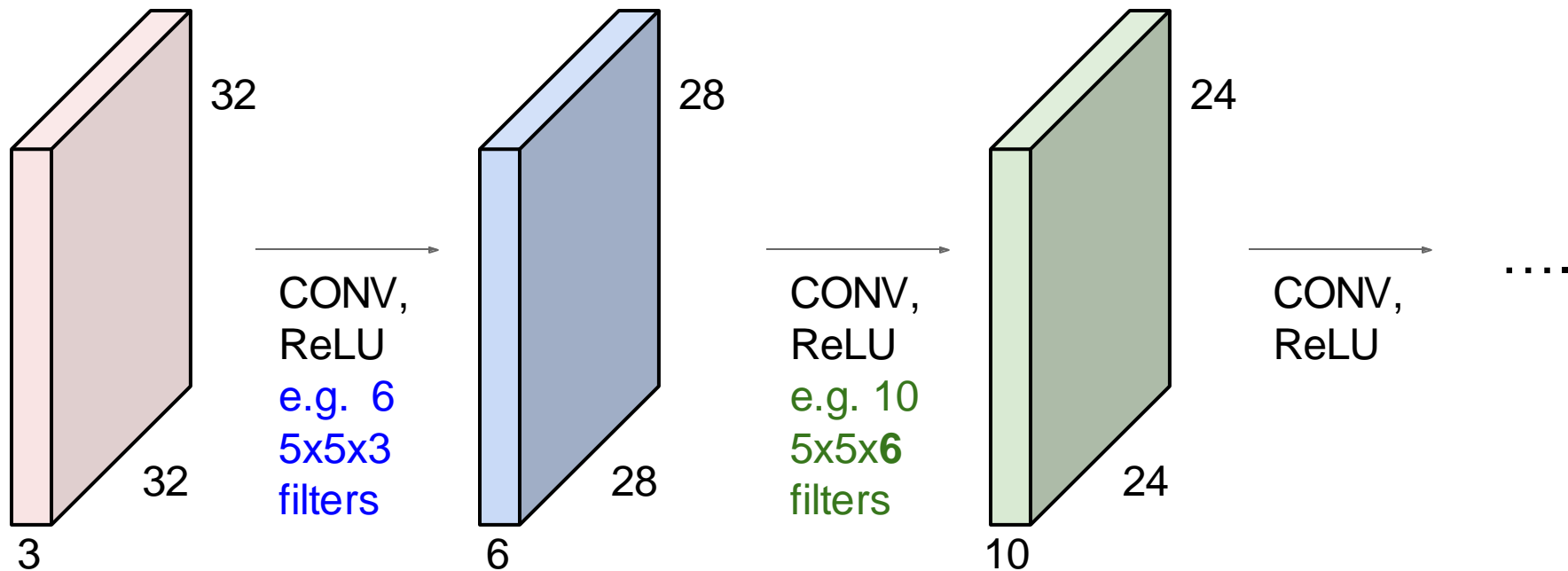
$F = 5 \Rightarrow$  zero pad with 2

$F = 7 \Rightarrow$  zero pad with 3



## Remember back to...

E.g. 32x32 input convolved repeatedly with 5x5 filters shrinks volumes spatially! (32 -> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.

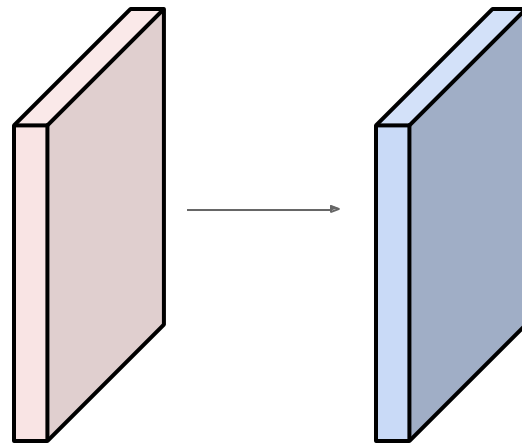


Examples time:

Input volume: **32x32x3**

10 5x5 filters with stride 1, pad 2

Output volume size: ?



Examples time:

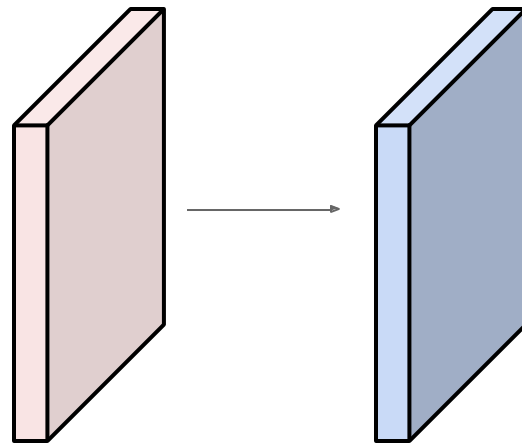
Input volume: **32x32x3**

**10** **5x5** filters with stride **1**, pad **2**

Output volume size:

$(32 + 2 * 2 - 5) / 1 + 1 = 32$  spatially, so

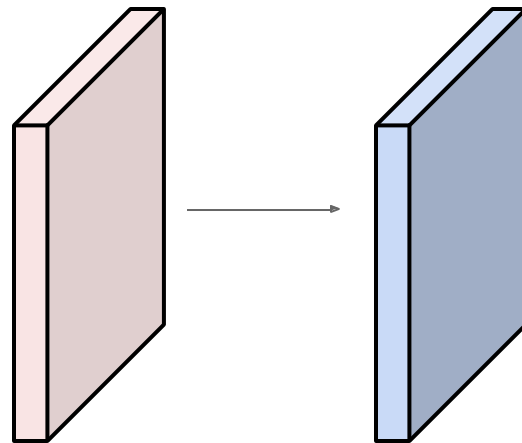
**32x32x10**



Examples time:

Input volume: **32x32x3**

10 5x5 filters with stride 1, pad 2

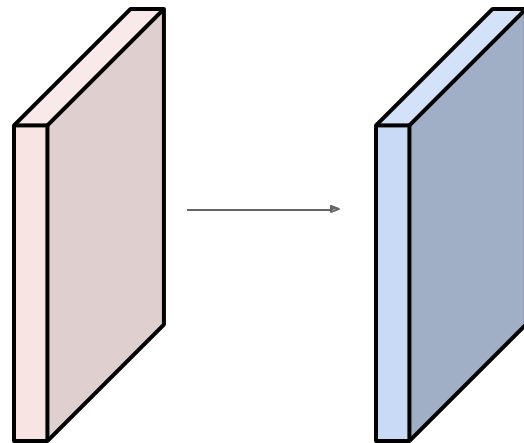


Number of parameters in this layer?

Examples time:

Input volume: **32x32x3**

**10** **5x5** filters with stride 1, pad 2



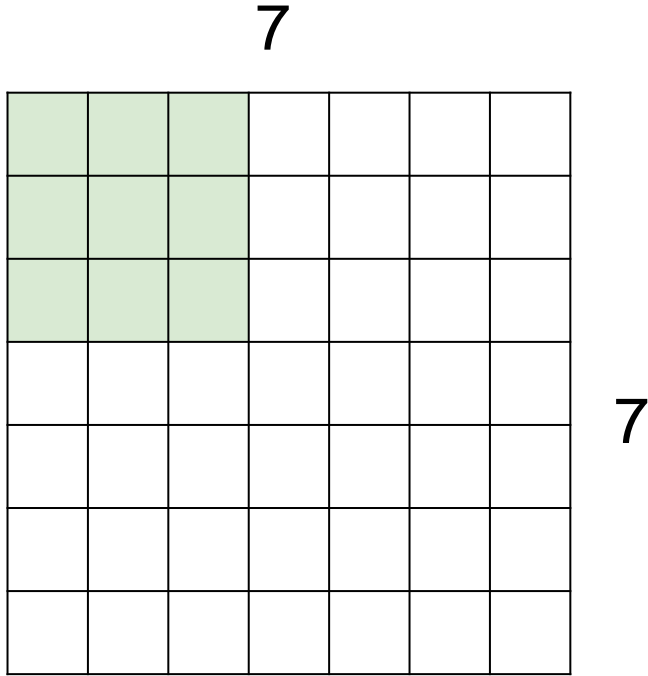
Number of parameters in this layer?

each filter has  $5*5*3 + 1 = 76$  params

(+1 for bias)

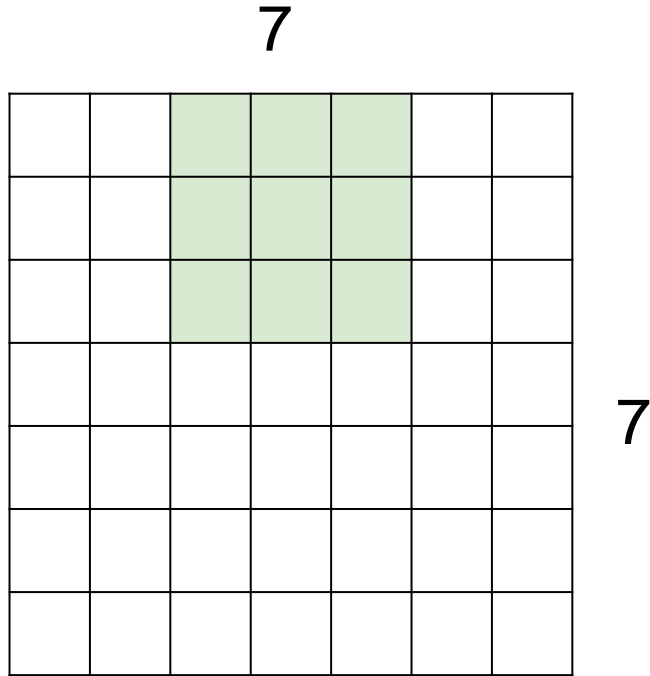
$\Rightarrow 76*10 = 760$

## Solution: **Strided** Convolution



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**

## Solution: **Strided** Convolution



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**

**=> 3x3 output!**

# Convolution layer: summary

Let's assume input is  $W_1 \times H_1 \times C$

Conv layer needs 4 hyperparameters:

- Number of filters **K**
- The filter size **F**
- The stride **S**
- The zero padding **P**

This will produce an output of  $W_2 \times H_2 \times K$   
where:

- $W_2 = (W_1 - F + 2P)/S + 1$
- $H_2 = (H_1 - F + 2P)/S + 1$

Number of parameters:  $F^2CK$  and  $K$  biases



# Convolution layer: summary

Common settings:

Let's assume input is  $W_1 \times H_1 \times C$

Conv layer needs 4 hyperparameters:

- Number of filters **K**
- The filter size **F**
- The stride **S**
- The zero padding **P**

**K** = (powers of 2, e.g. 32, 64, 128, 512)

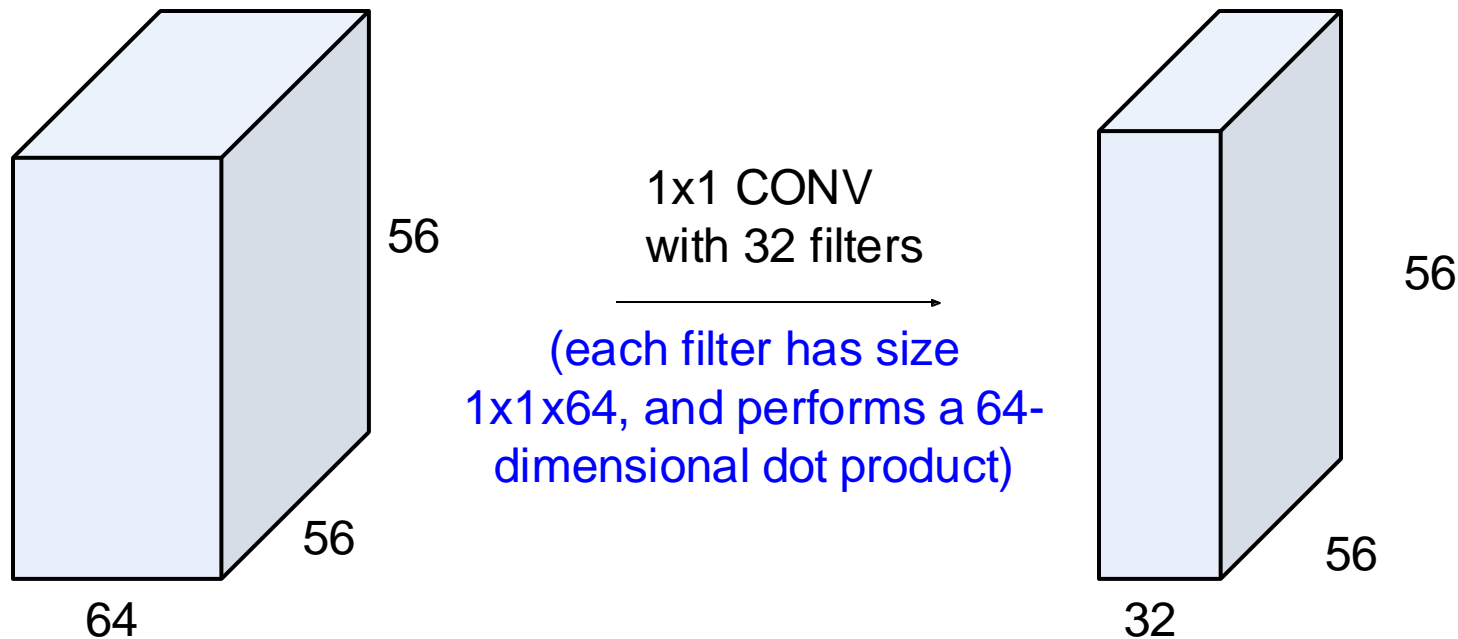
- **F** = 3, **S** = 1, **P** = 1
- **F** = 5, **S** = 1, **P** = 2
- **F** = 1, **S** = 1, **P** = 0

This will produce an output of  $W_2 \times H_2 \times K$   
where:

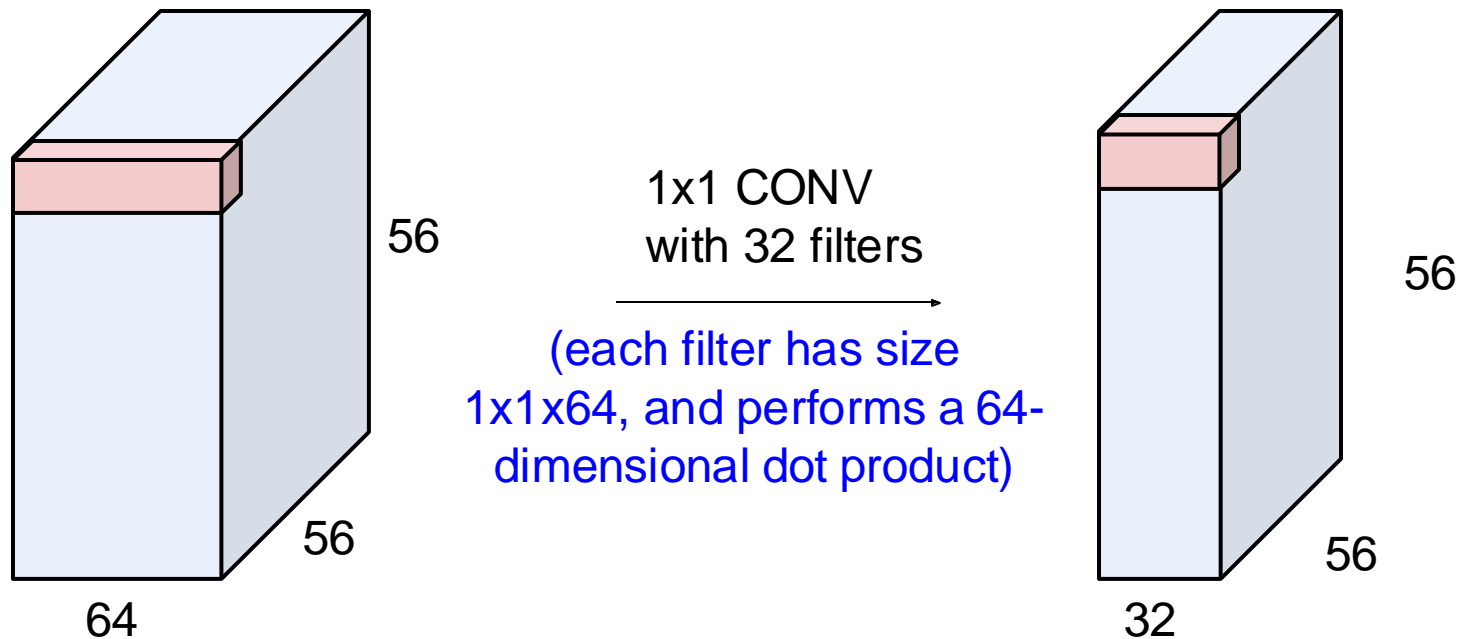
- $W_2 = (W_1 - F + 2P)/S + 1$
- $H_2 = (H_1 - F + 2P)/S + 1$

Number of parameters:  $F^2CK$  and  $K$  biases

(btw, 1x1 convolution layers make perfect sense)



(btw, 1x1 convolution layers make perfect sense)



# Example: CONV layer in PyTorch

## Conv2d

```
CLASS torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1, padding=0, dilation=1, groups=1, bias=True)
```

[SOURCE]

Applies a 2D convolution over an input signal composed of several input planes.

In the simplest case, the output value of the layer with input size  $(N, C_{in}, H, W)$  and output  $(N, C_{out}, H_{out}, W_{out})$  can be precisely described as:

$$\text{out}(N_i, C_{out,j}) = \text{bias}(C_{out,j}) + \sum_{k=0}^{C_{in}-1} \text{weight}(C_{out,j}, k) \star \text{input}(N_i, k)$$

where  $\star$  is the valid 2D **cross-correlation** operator,  $N$  is a batch size,  $C$  denotes a number of channels,  $H$  is a height of input planes in pixels, and  $W$  is width in pixels.

- `stride` controls the stride for the cross-correlation, a single number or a tuple.
- `padding` controls the amount of implicit zero-paddings on both sides for `padding` number of points for each dimension.
- `dilation` controls the spacing between the kernel points; also known as the à trous algorithm. It is harder to describe, but this [link](#) has a nice visualization of what `dilation` does.
- `groups` controls the connections between inputs and outputs. `in_channels` and `out_channels` must both be divisible by `groups`. For example,
  - At `groups=1`, all inputs are convolved to all outputs.
  - At `groups=2`, the operation becomes equivalent to having two conv layers side by side, each seeing half the input channels, and producing half the output channels, and both subsequently concatenated.
  - At `groups= in_channels`, each input channel is convolved with its own set of filters, of size:  $\begin{bmatrix} C_{out} \\ C_{in} \end{bmatrix}$ .

The parameters `kernel_size`, `stride`, `padding`, `dilation` can either be:

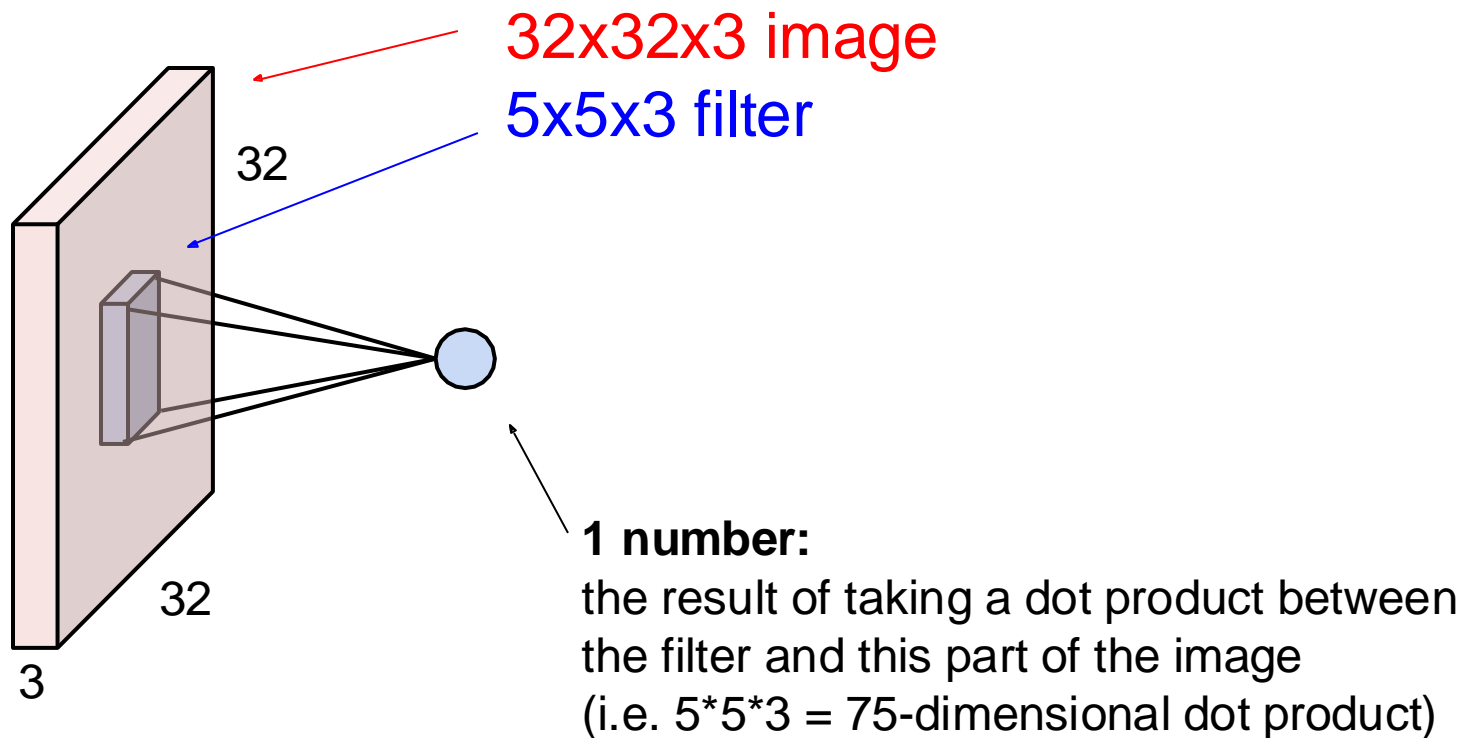
- a single `int` – in which case the same value is used for the height and width dimension
- a `tuple` of two ints – in which case, the first `int` is used for the height dimension, and the second `int` for the width dimension

Conv layer needs 4 hyperparameters:

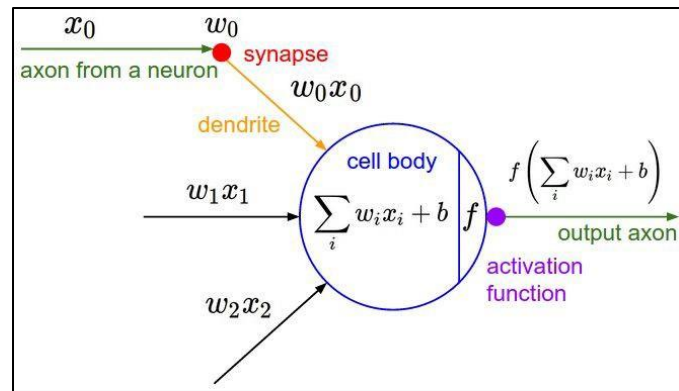
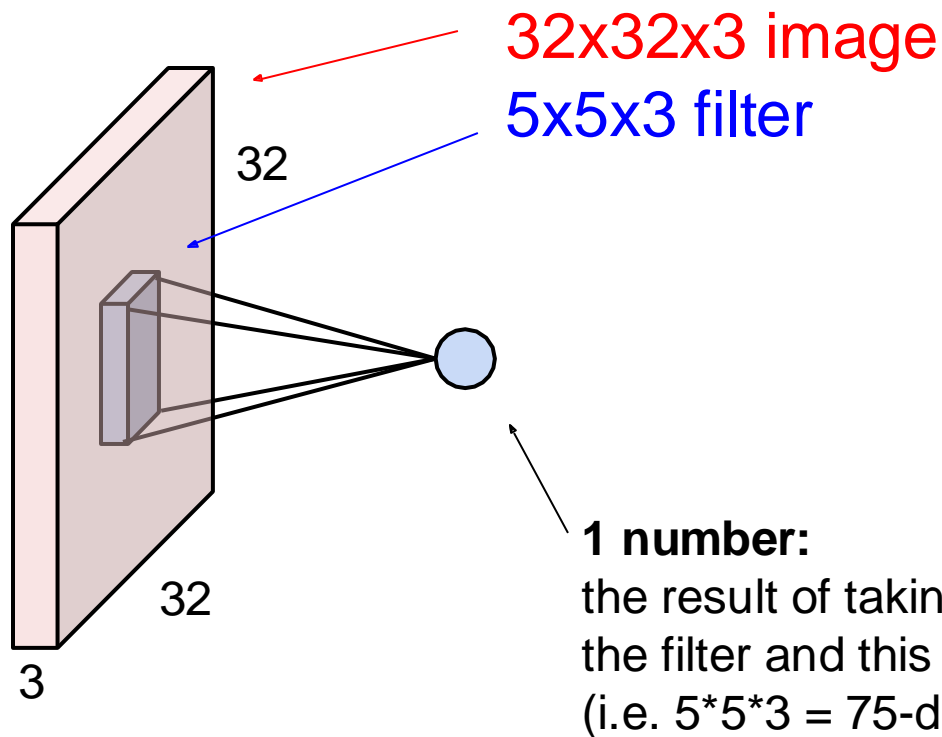
- Number of filters K
- The filter size F
- The stride S
- The zero padding P

[PyTorch](#) is licensed under [BSD 3-clause](#).

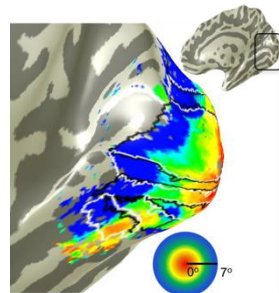
# The brain/neuron view of CONV Layer



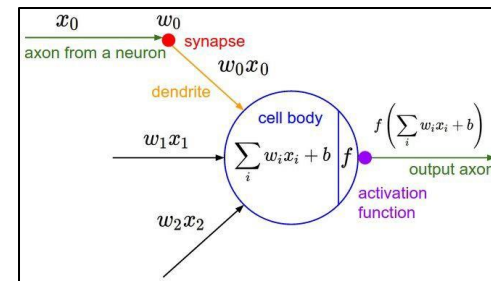
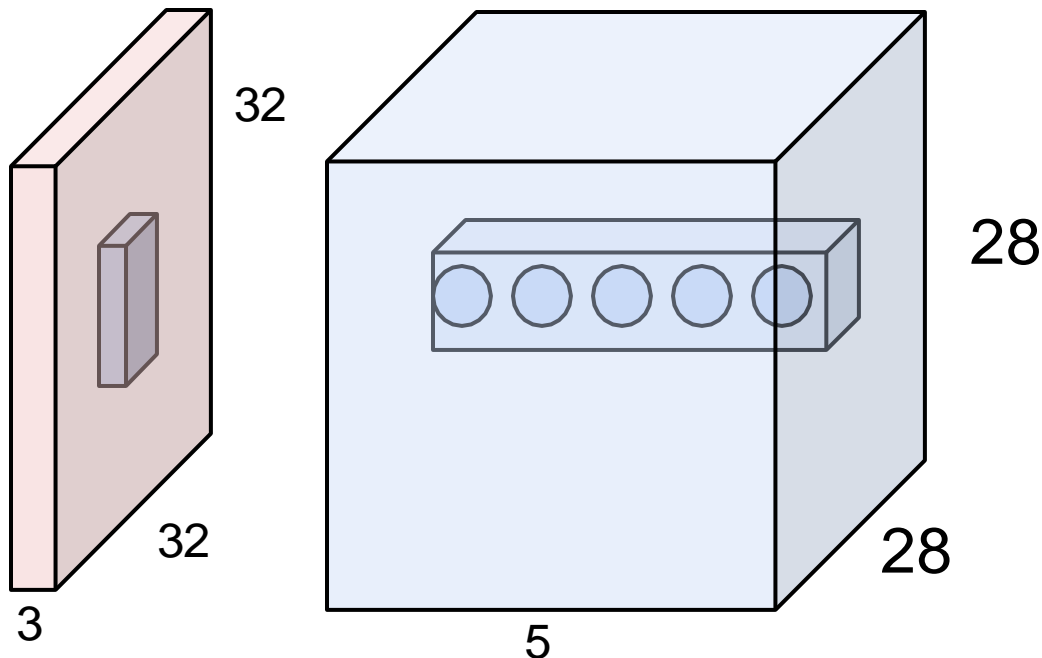
# The brain/neuron view of CONV Layer



It's just a neuron with local connectivity...



# The brain/neuron view of CONV Layer



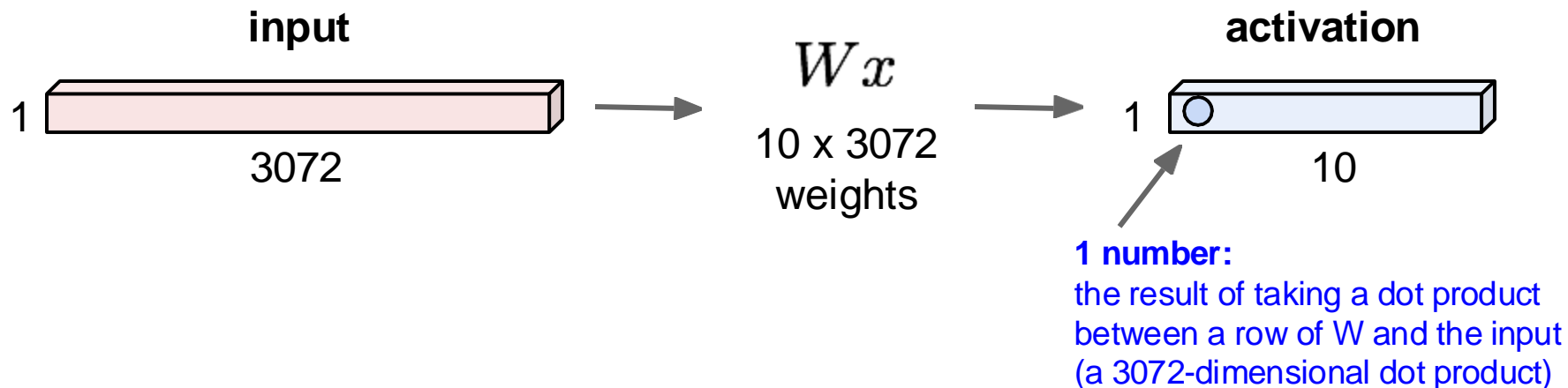
E.g. with 5 filters,  
CONV layer consists of  
neurons arranged in a 3D grid  
(28x28x5)

There will be 5 different  
neurons all looking at the same  
region in the input volume

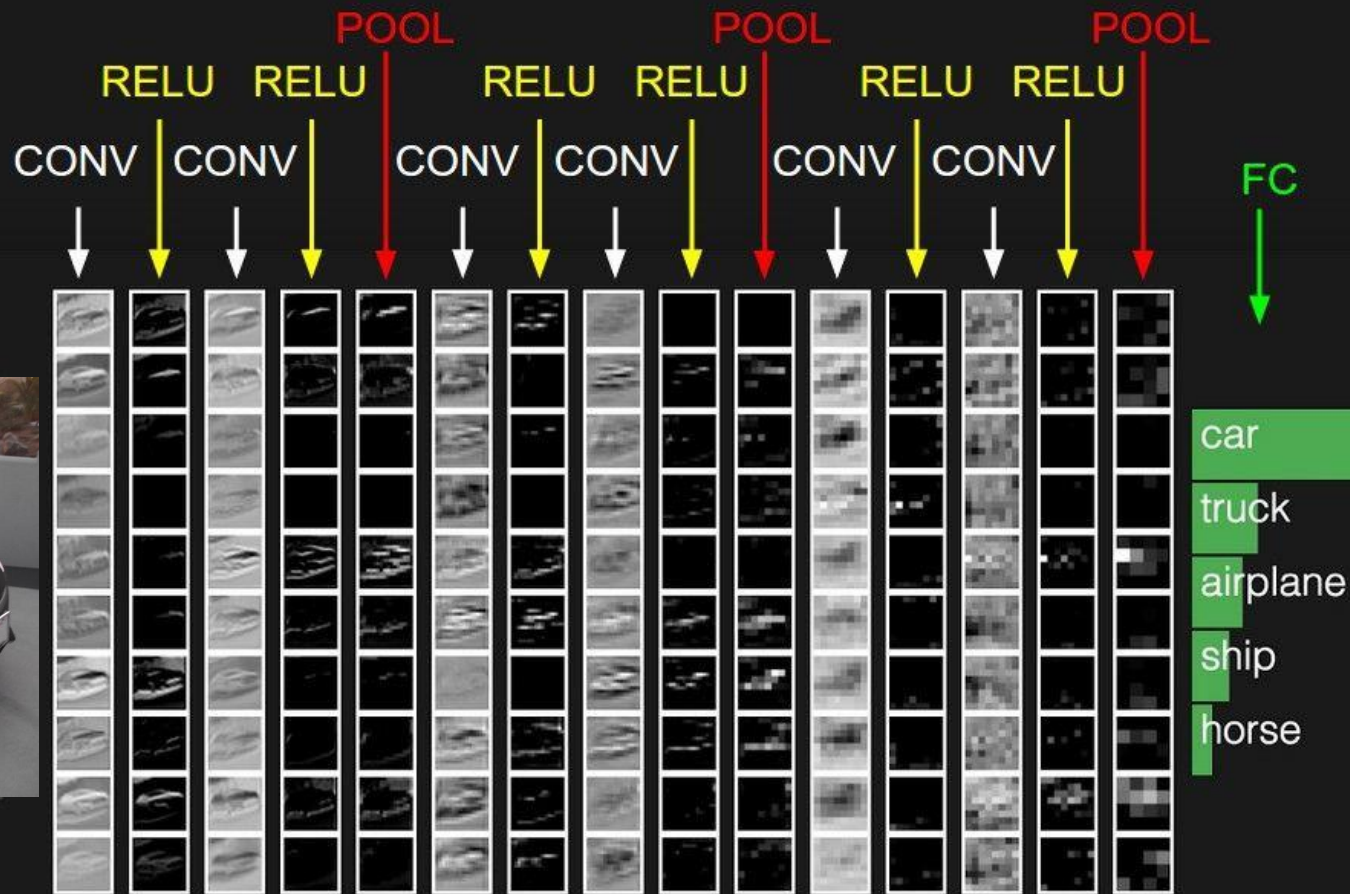
# Reminder: Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1

Each neuron  
looks at the full  
input volume

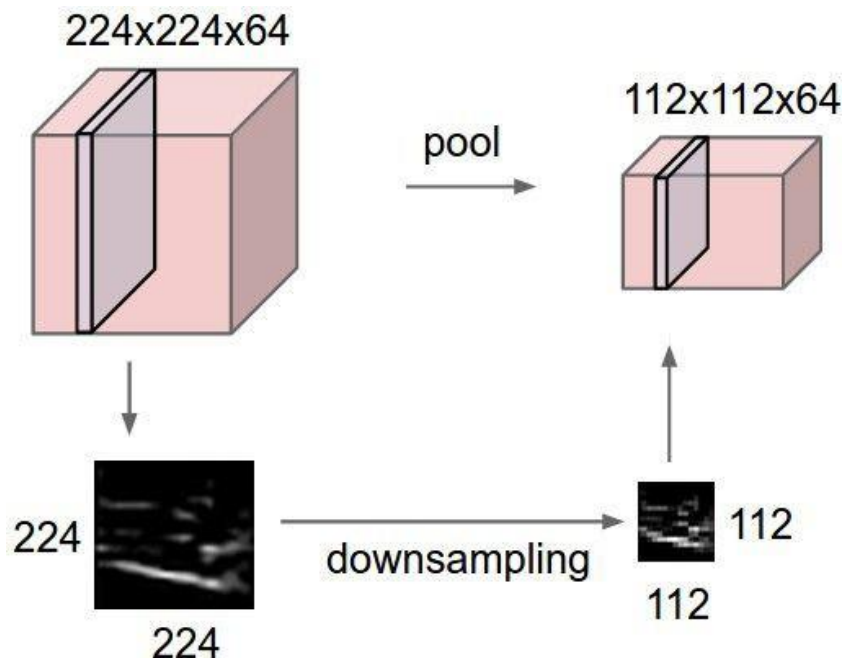




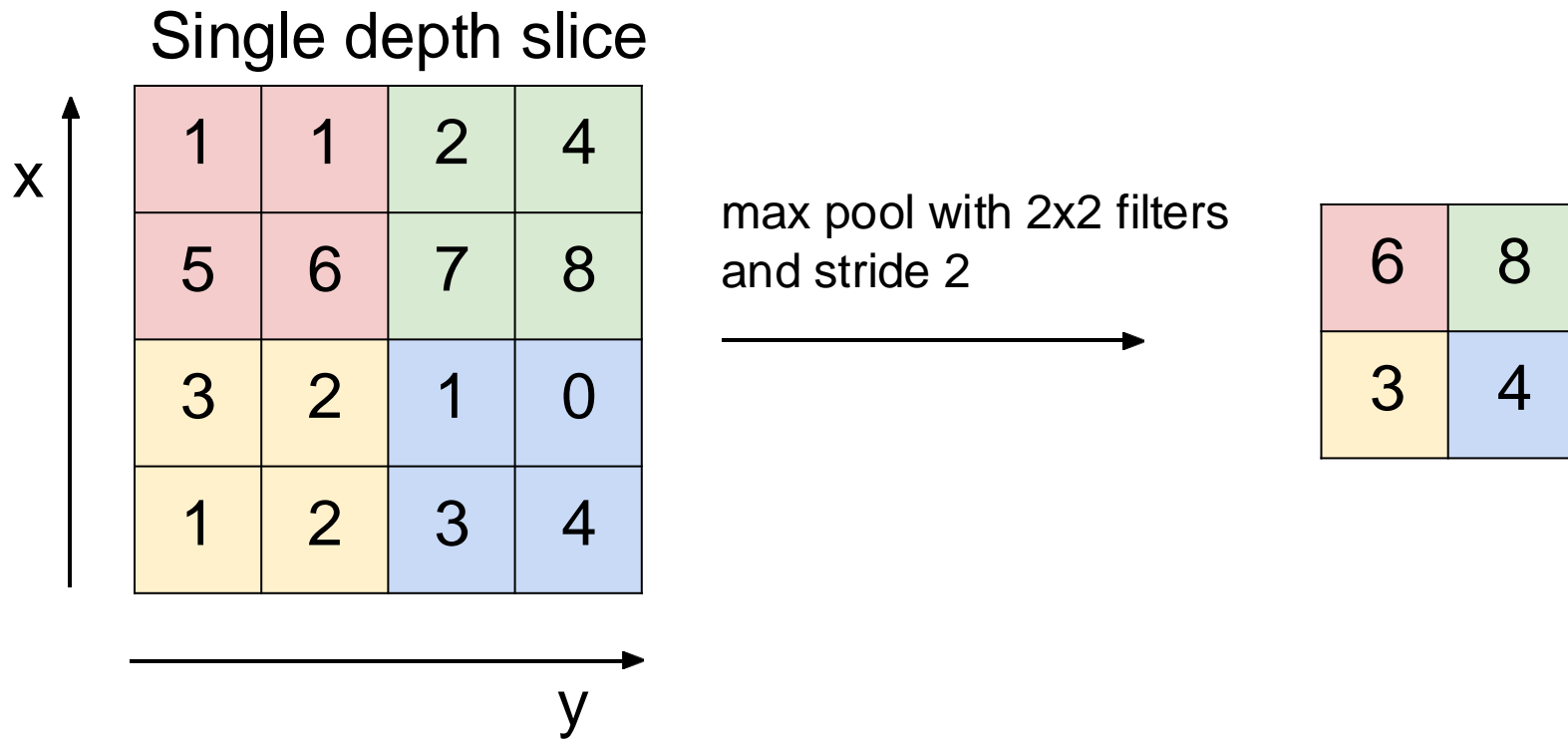


# Pooling layer

- makes the representations smaller and more manageable
- operates over each activation map independently



# MAX POOLING



# MAX POOLING

Single depth slice

x ↑

1	1	2	4
5	6	7	8
3	2	1	0
1	2	3	4

→ y

max pool with 2x2 filters  
and stride 2



6	8
3	4

- No learnable parameters
- Introduces spatial invariance

# Pooling layer: summary

Let's assume input is  $W_1 \times H_1 \times C$

Conv layer needs 2 hyperparameters:

- The spatial extent **F**
- The stride **S**

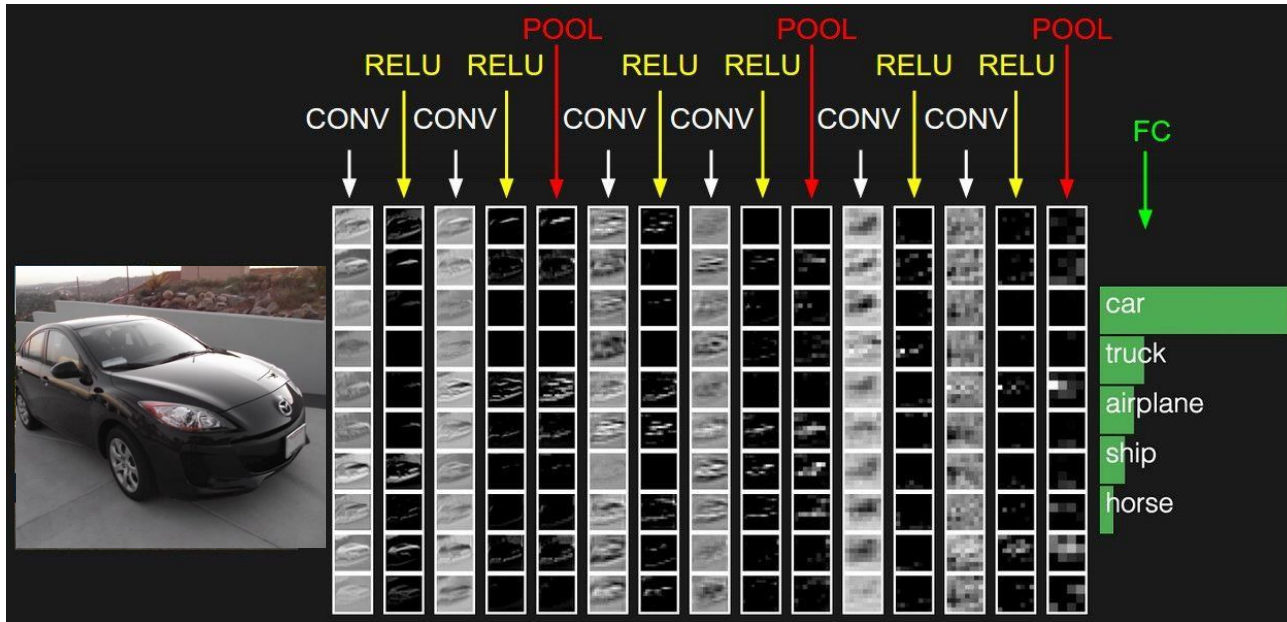
This will produce an output of  $W_2 \times H_2 \times C$  where:

- $W_2 = (W_1 - F) / S + 1$
- $H_2 = (H_1 - F) / S + 1$

Number of parameters: 0

# Fully Connected Layer (FC layer)

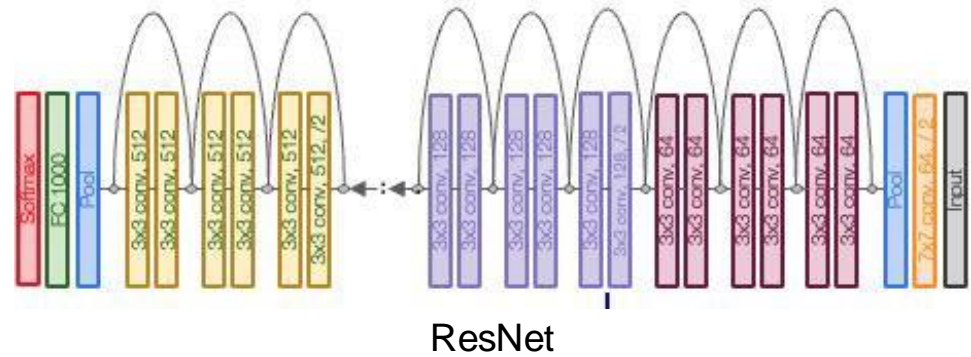
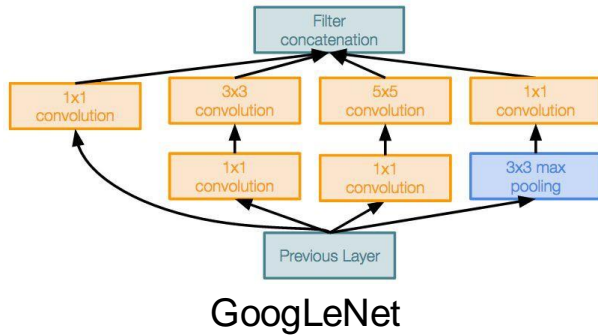
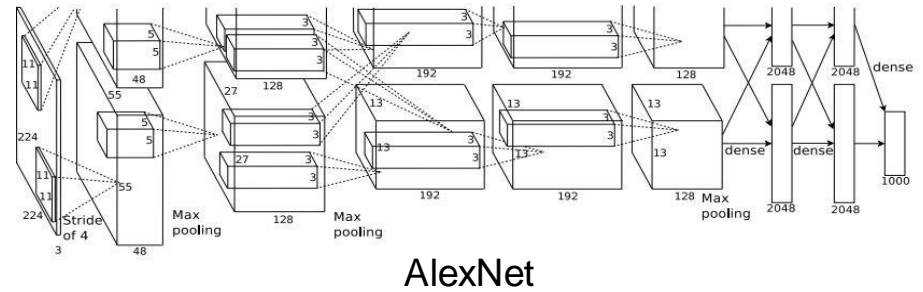
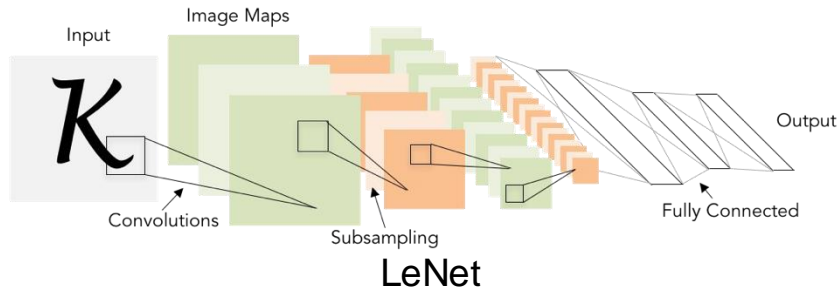
- Contains neurons that connect to the entire input volume, as in ordinary Neural Networks



# Summary

- ConvNets stack CONV, POOL, FC layers
- Trend towards smaller filters and deeper architectures
- Trend towards getting rid of POOL/FC layers (just CONV)
- Historically architectures looked like  
 **$[(\text{CONV-RELU})^N \text{- POOL?}]^M \text{- (FC-RELU)}^K, \text{SOFTMAX}$**   
where N is usually up to ~5, M is large,  $0 \leq K \leq 2$ .
- But recent advances such as ResNet/GoogLeNet have challenged this paradigm

# CNN Architectures





# Today: CNN Architectures

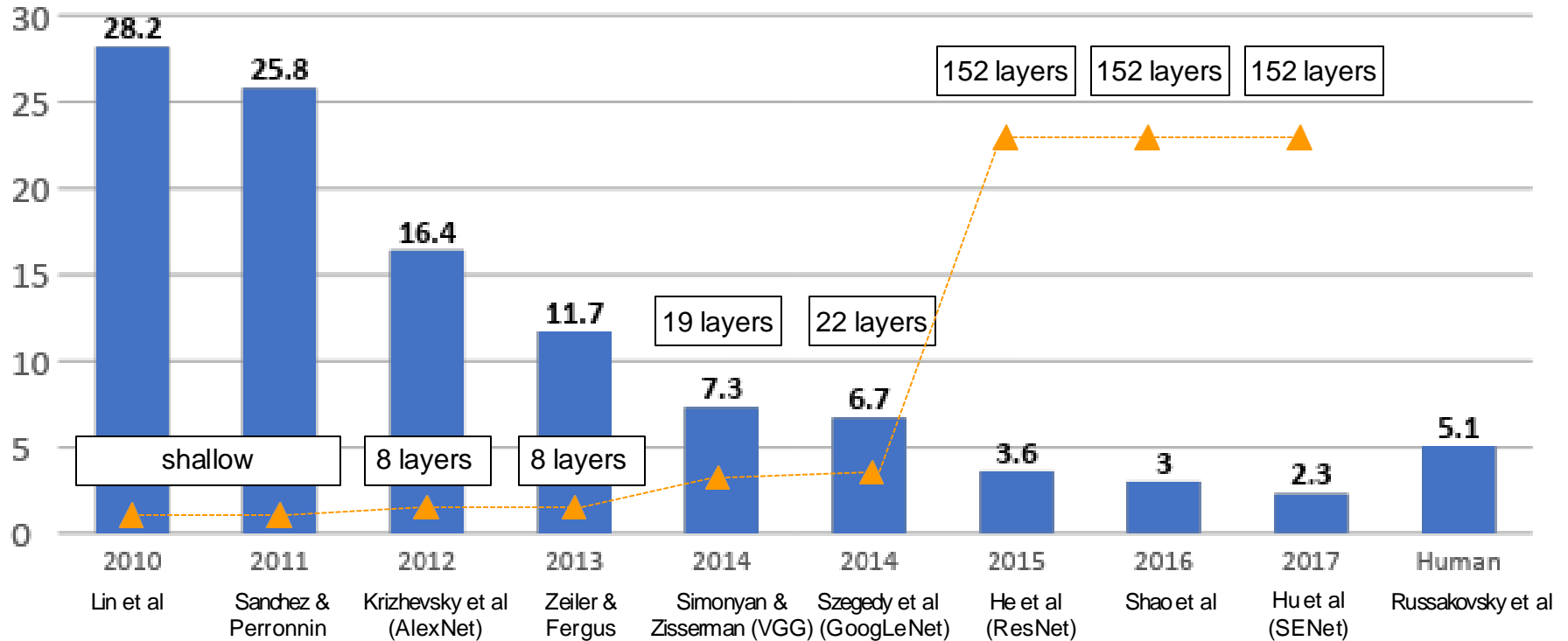
## Case Studies

- AlexNet
- VGG
- ResNet

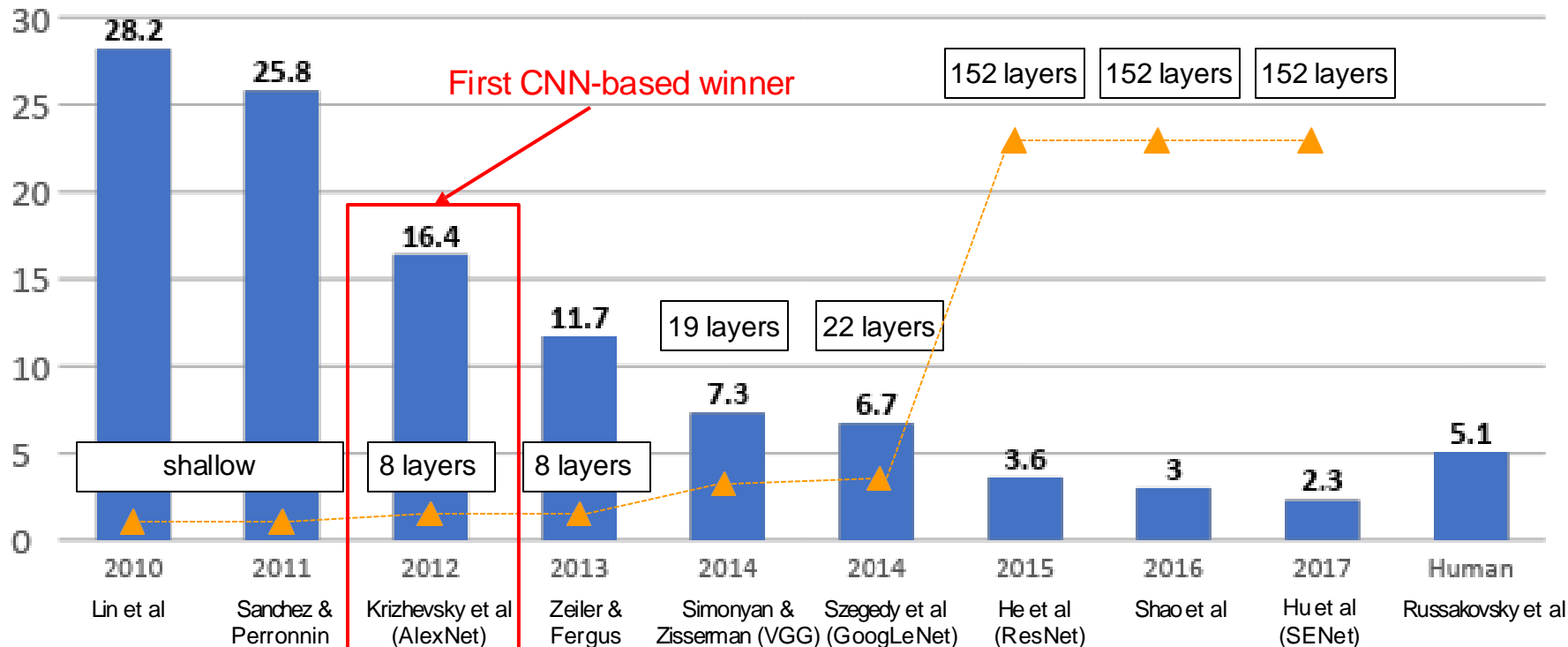
## Also.....

- GoogLeNet
- ZFNet
- SENet
- Wide ResNet
- ResNeXT
- DenseNet
- MobileNets
- NASNet
- EfficientNet

# ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners



# ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners



# Case Study: AlexNet

[Krizhevsky et al. 2012]

## Architecture:

CONV1

MAX POOL1

NORM1

CONV2

MAX POOL2

NORM2

CONV3

CONV4

CONV5

Max POOL3

FC6

FC7

FC8

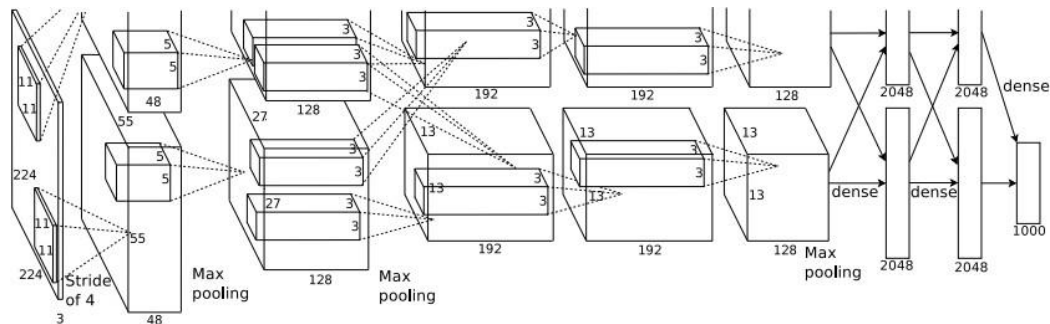
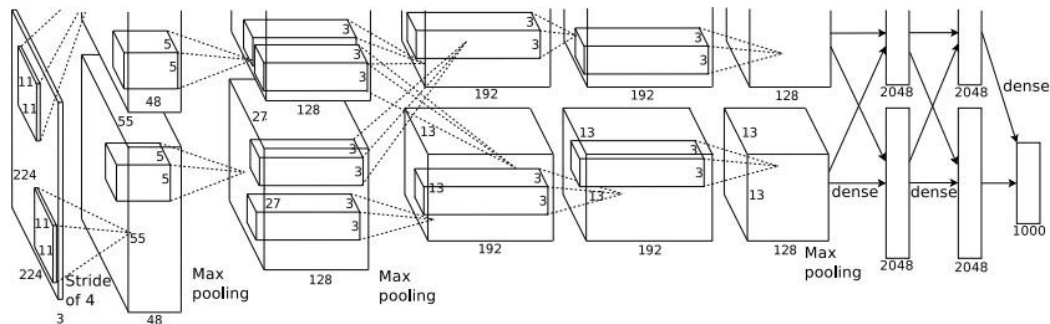


Figure copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

**First layer (CONV1):** 96 11x11 filters applied at stride 4

=>

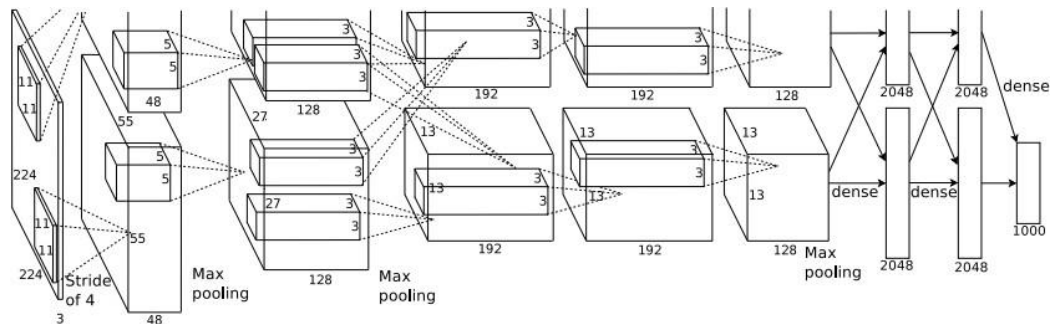
Q: what is the output volume size? Hint:  $(227-11)/4+1 = 55$

$$W' = (W - F + 2P) / S + 1$$

Figure copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

**First layer (CONV1):** 96 11x11 filters applied at stride 4

=>

Output volume **[55x55x96]**

$$W' = (W - F + 2P) / S + 1$$

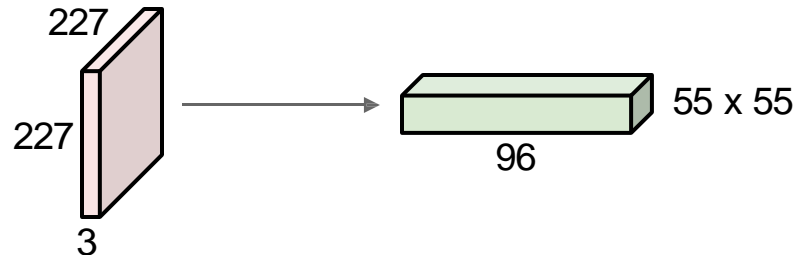
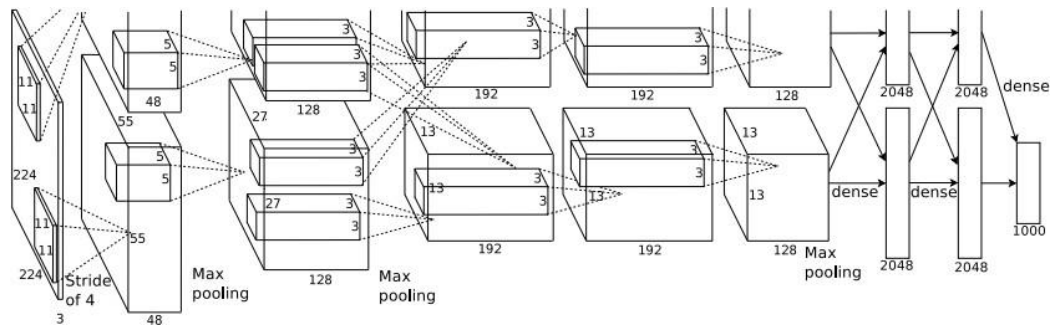


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# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

**First layer (CONV1):** 96 11x11 filters applied at stride 4

=>

Output volume **[55x55x96]**

Q: What is the total number of parameters in this layer?

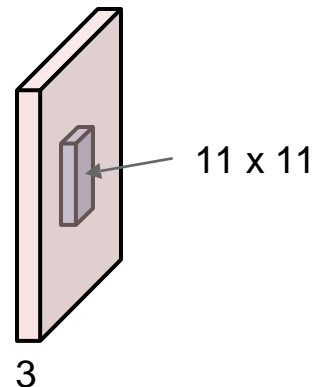
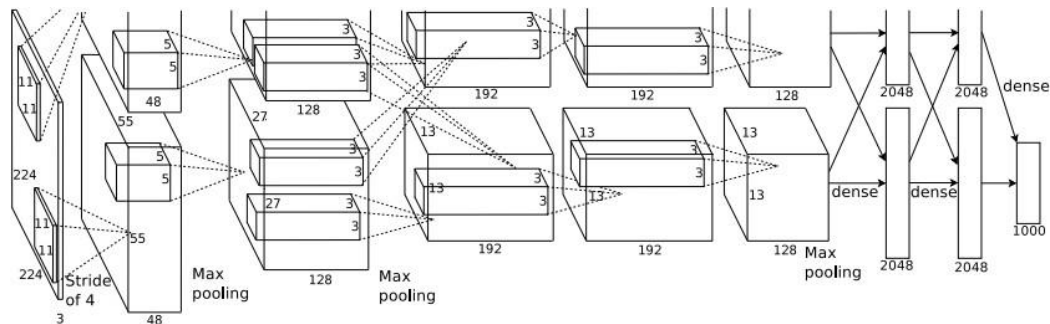


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# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

**First layer (CONV1):** 96 11x11 filters applied at stride 4

=>

Output volume **[55x55x96]**

Parameters:  $(11 \cdot 11 \cdot 3 + 1) \cdot 96 = \mathbf{35K}$

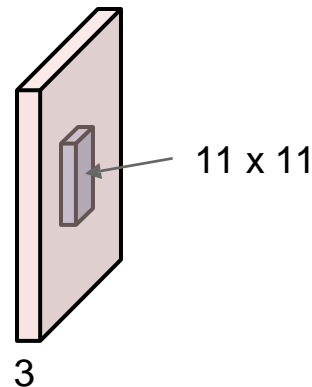
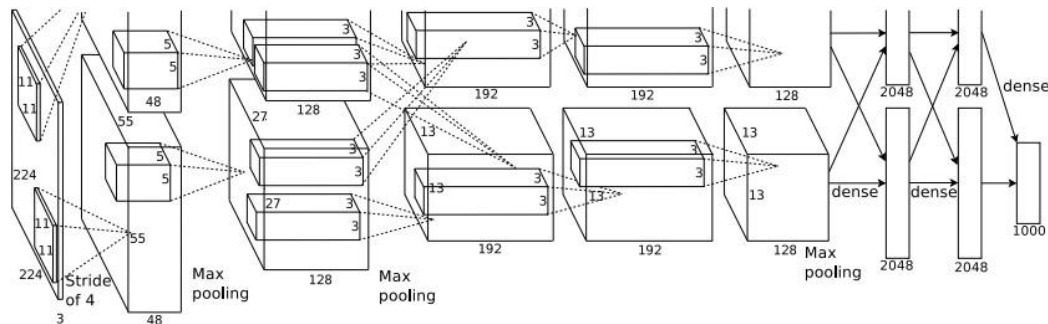


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# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

After CONV1: 55x55x96

$$W' = (W - F + 2P) / S + 1$$

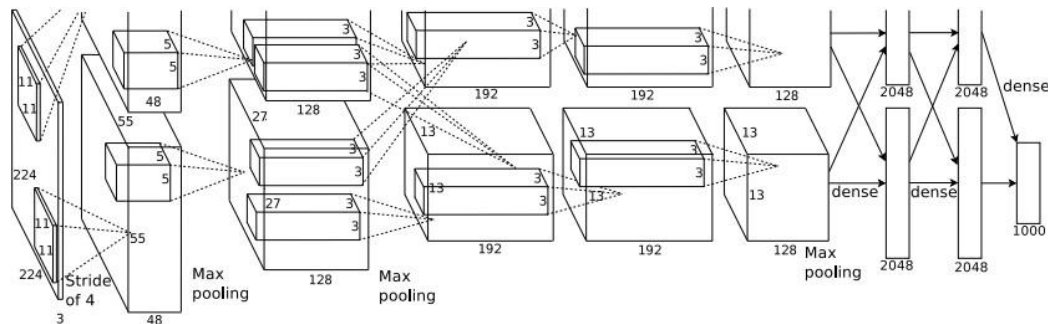
**Second layer (POOL1):** 3x3 filters applied at stride 2

Q: what is the output volume size? Hint:  $(55-3)/2+1 = 27$

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# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

After CONV1: 55x55x96

**Second layer (POOL1):** 3x3 filters applied at stride 2

Output volume: 27x27x96

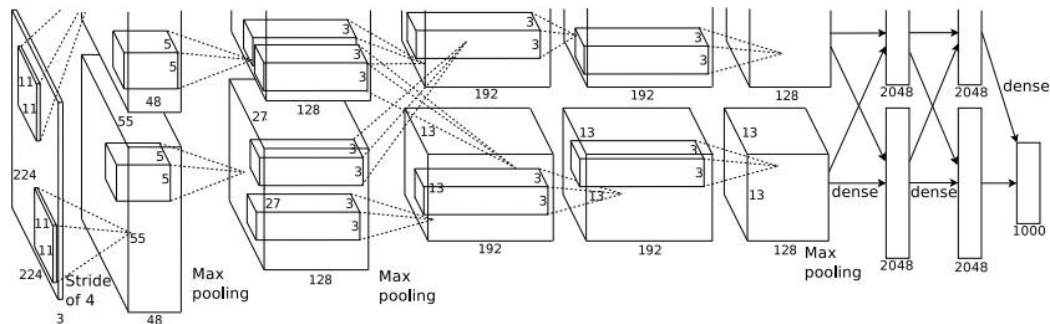
Q: what is the number of parameters in this layer?

$$W' = (W - F + 2P) / S + 1$$

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# Case Study: AlexNet

[Krizhevsky et al. 2012]



Input: 227x227x3 images

After CONV1: 55x55x96

**Second layer (POOL1):** 3x3 filters applied at stride 2

Output volume: 27x27x96

Parameters: 0!

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# Case Study: AlexNet

[Krizhevsky et al. 2012]

Input: 227x227x3 images

After CONV1: 55x55x96

After POOL1: 27x27x96

...

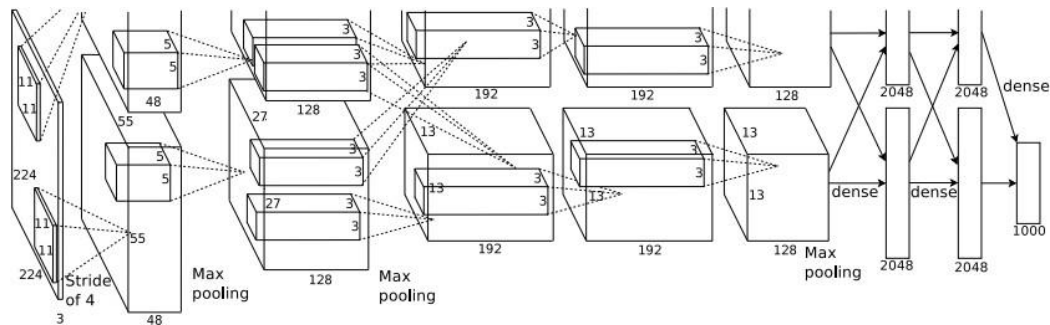


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# Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] **CONV1**: 96 11x11 filters at stride 4, pad 0

[27x27x96] **MAX POOL1**: 3x3 filters at stride 2

[27x27x96] **NORM1**: Normalization layer

[27x27x256] **CONV2**: 256 5x5 filters at stride 1, pad 2

[13x13x256] **MAX POOL2**: 3x3 filters at stride 2

[13x13x256] **NORM2**: Normalization layer

[13x13x384] **CONV3**: 384 3x3 filters at stride 1, pad 1

[13x13x384] **CONV4**: 384 3x3 filters at stride 1, pad 1

[13x13x256] **CONV5**: 256 3x3 filters at stride 1, pad 1

[6x6x256] **MAX POOL3**: 3x3 filters at stride 2

[4096] **FC6**: 4096 neurons

[4096] **FC7**: 4096 neurons

[1000] **FC8**: 1000 neurons (class scores)

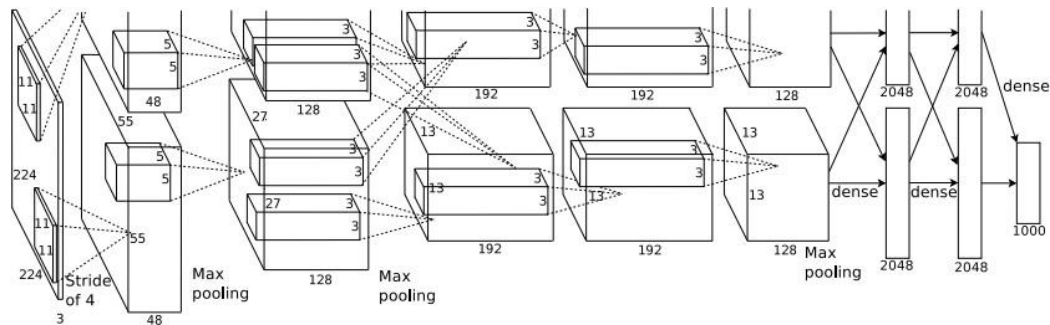


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# Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] **CONV1**: 96 11x11 filters at stride 4, pad 0

[27x27x96] **MAX POOL1**: 3x3 filters at stride 2

[27x27x96] **NORM1**: Normalization layer

[27x27x256] **CONV2**: 256 5x5 filters at stride 1, pad 2

[13x13x256] **MAX POOL2**: 3x3 filters at stride 2

[13x13x256] **NORM2**: Normalization layer

[13x13x384] **CONV3**: 384 3x3 filters at stride 1, pad 1

[13x13x384] **CONV4**: 384 3x3 filters at stride 1, pad 1

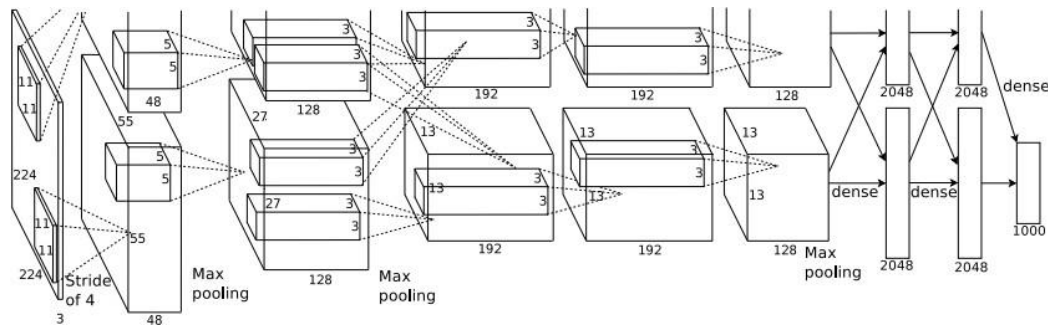
[13x13x256] **CONV5**: 256 3x3 filters at stride 1, pad 1

[6x6x256] **MAX POOL3**: 3x3 filters at stride 2

[4096] **FC6**: 4096 neurons

[4096] **FC7**: 4096 neurons

[1000] **FC8**: 1000 neurons (class scores)

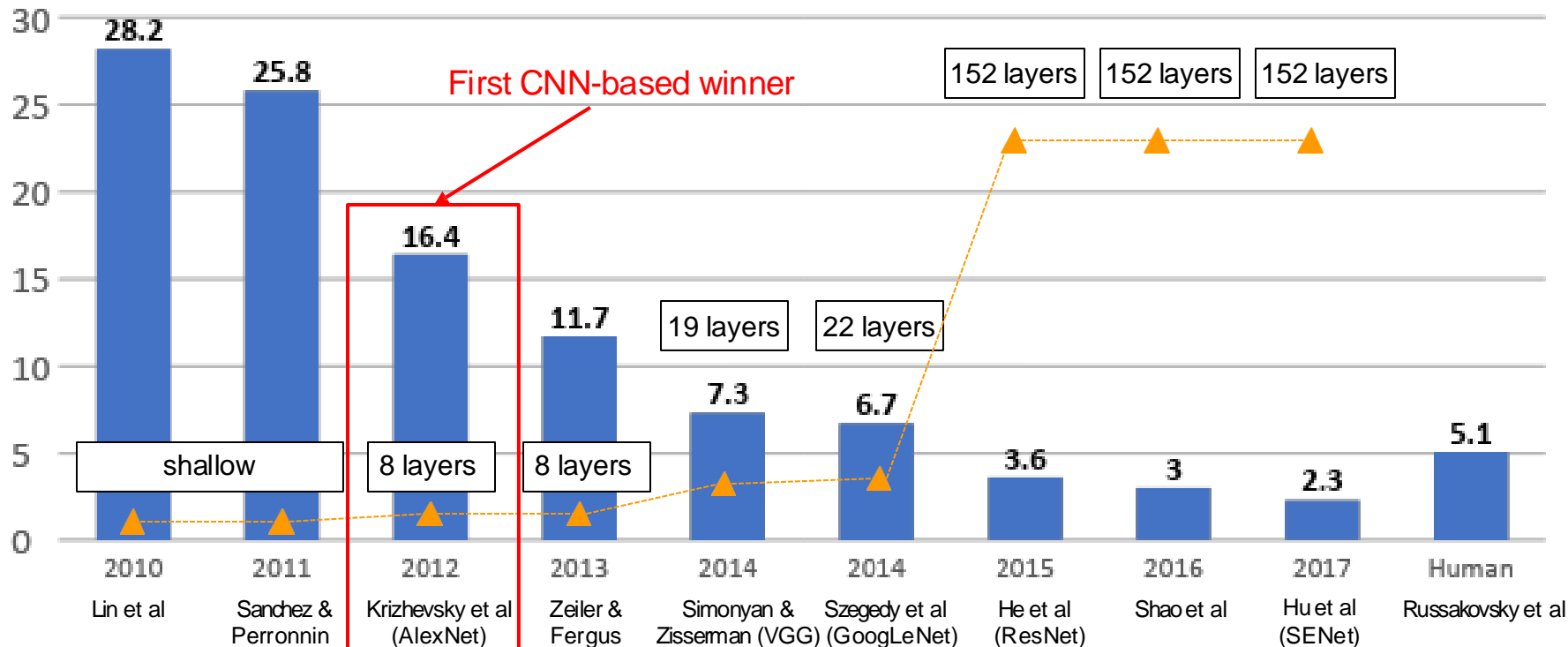


## Details/Retrospectives:

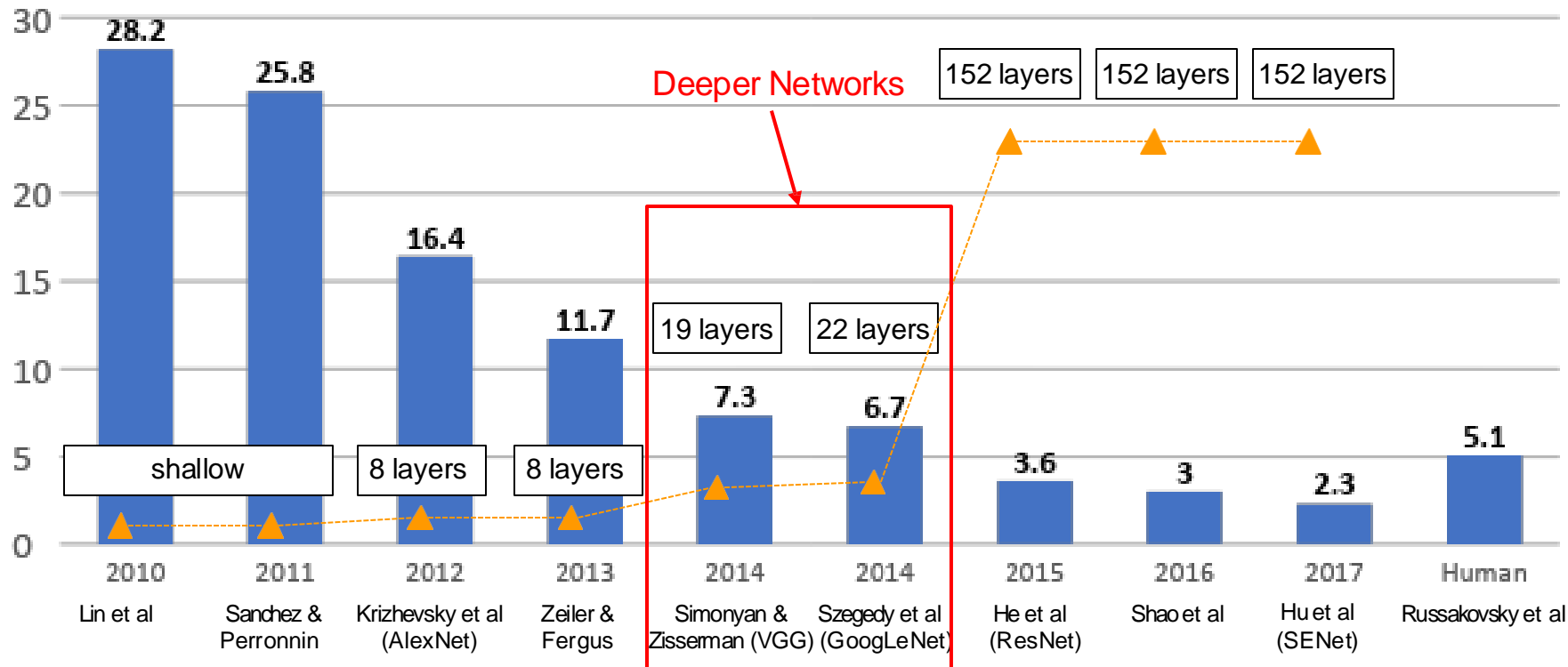
- first use of ReLU
- used LRN layers (not common anymore)
- heavy data augmentation
- dropout 0.5
- batch size 128
- SGD Momentum 0.9
- Learning rate 1e-2, reduced by 10 manually when val accuracy plateaus
- L2 weight decay 5e-4
- 7 CNN ensemble: 18.2% -> 15.4%

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# ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners



# ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

Small filters, Deeper networks

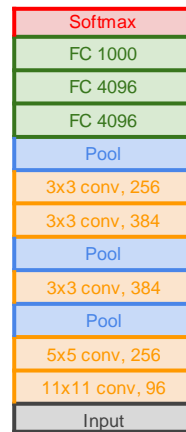
8 layers (AlexNet)

-> 16 - 19 layers (VGG16Net)

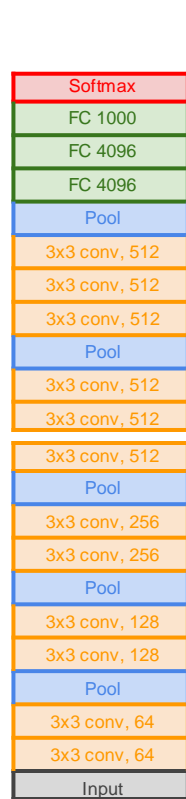
Only 3x3 CONV stride 1, pad 1  
and 2x2 MAX POOL stride 2

11.7% top 5 error in ILSVRC'13  
(ZFNet)

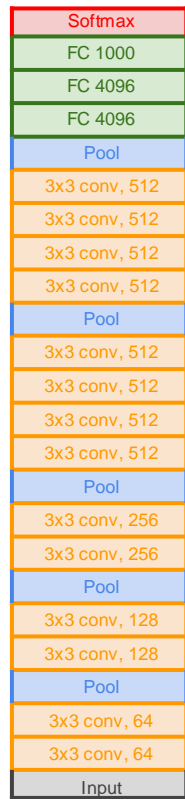
-> 7.3% top 5 error in ILSVRC'14



AlexNet



VGG16

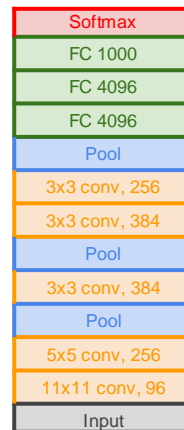


VGG19

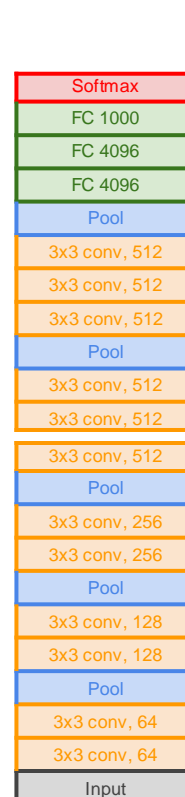
# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

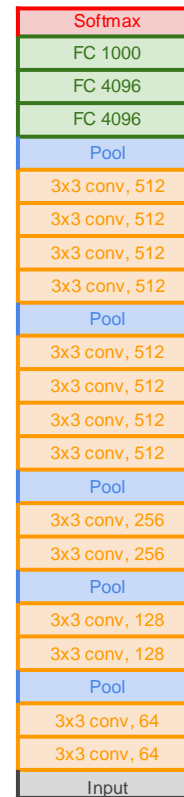
Q: Why use smaller filters? (3x3 conv)



AlexNet



VGG16



VGG19

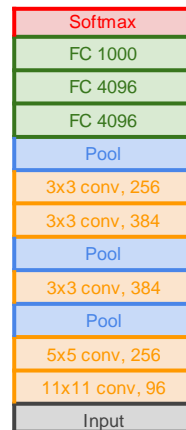
# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

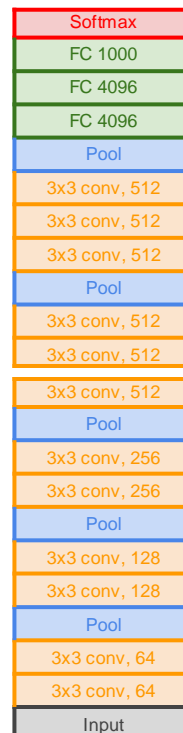
Q: Why use smaller filters? (3x3 conv)

Stack of three 3x3 conv (stride 1) layers has same **effective receptive field** as one 7x7 conv layer

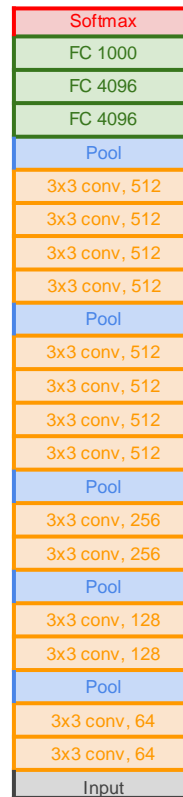
Q: What is the effective receptive field of three 3x3 conv (stride 1) layers?



AlexNet



VGG16

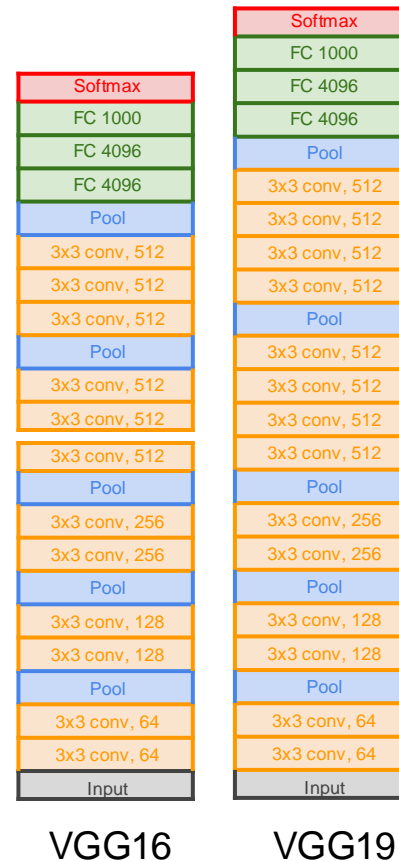
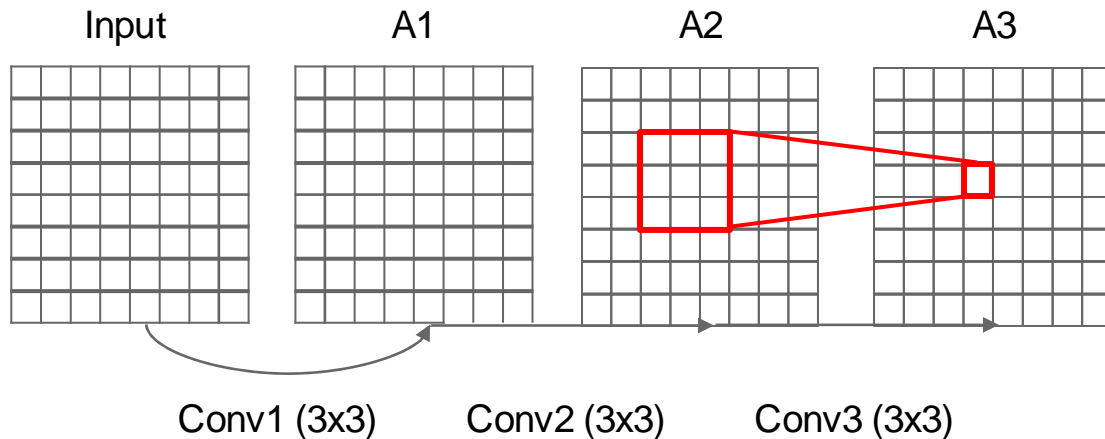


VGG19

# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

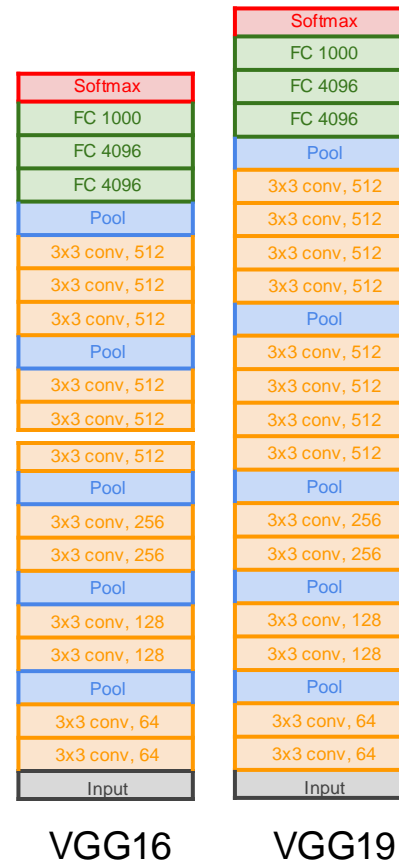
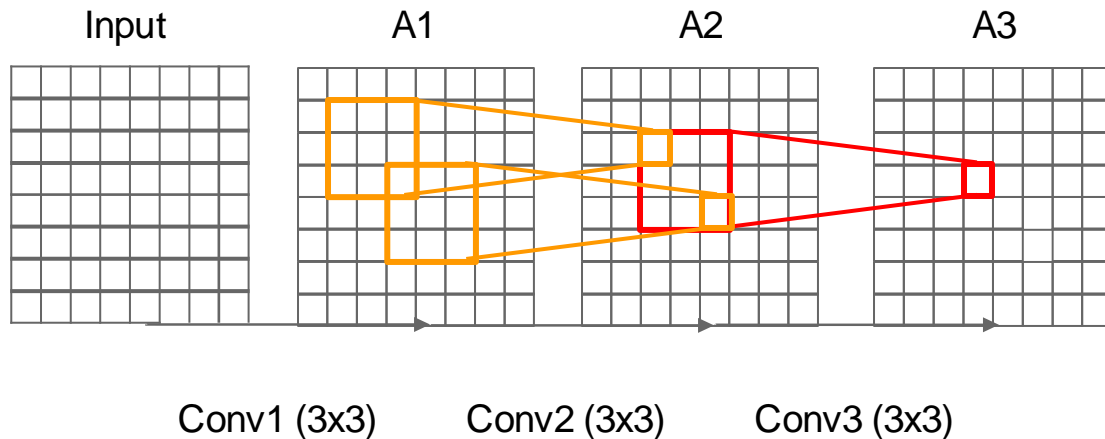
Q: What is the effective receptive field of three 3x3 conv (stride 1) layers?



# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

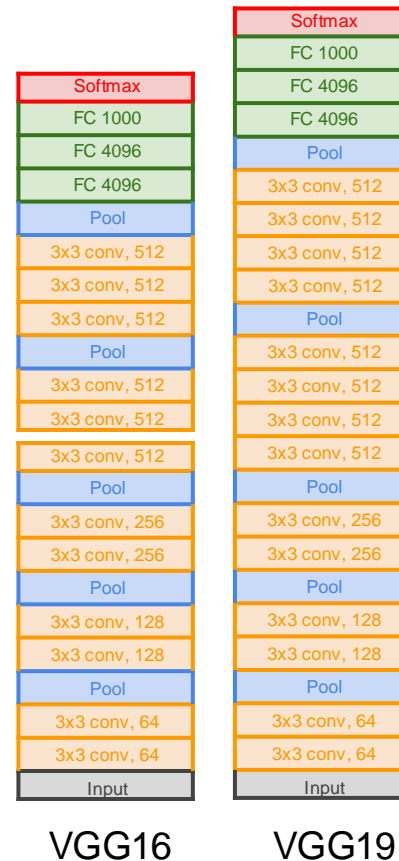
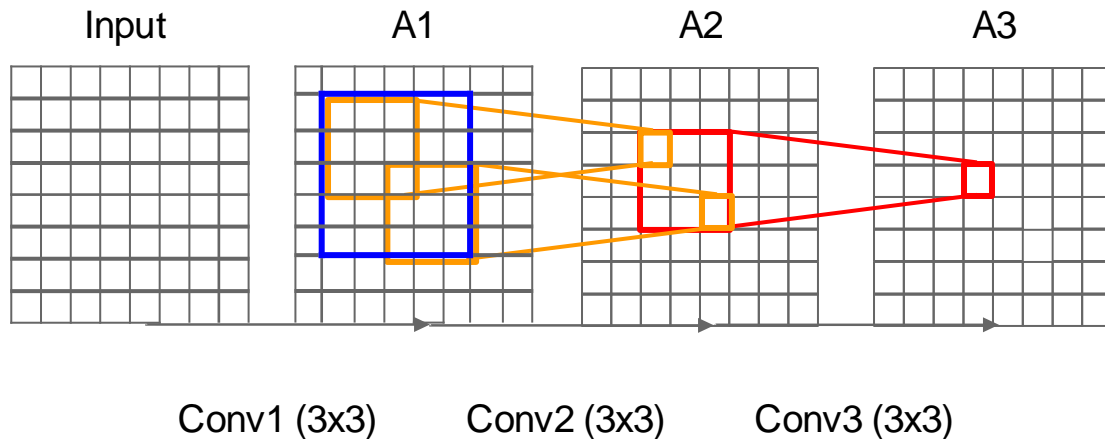
Q: What is the effective receptive field of three 3x3 conv (stride 1) layers?



# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

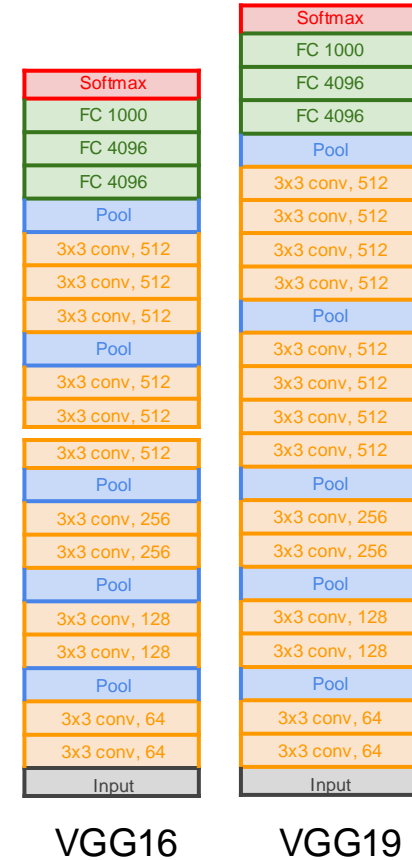
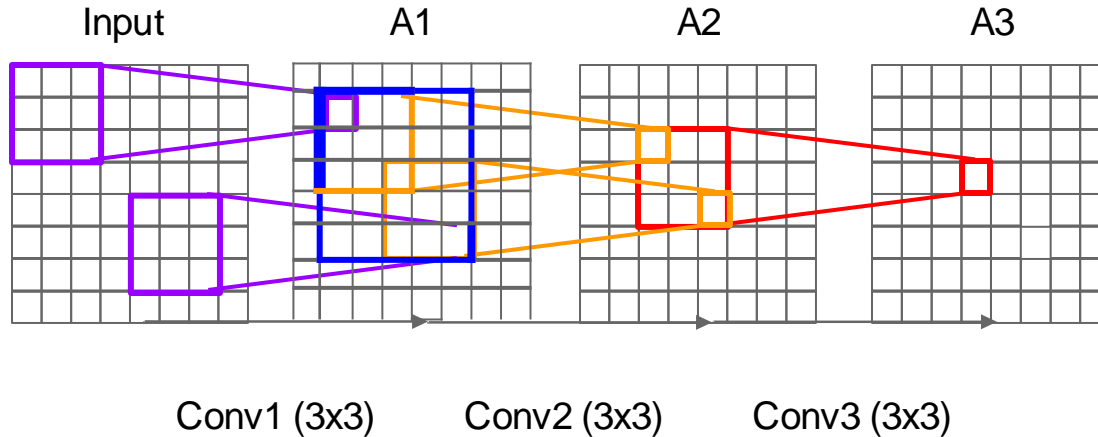
Q: What is the effective receptive field of three 3x3 conv (stride 1) layers?



# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

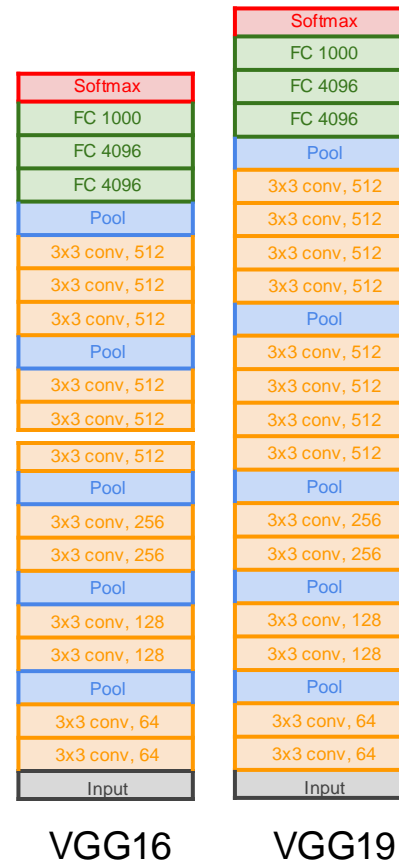
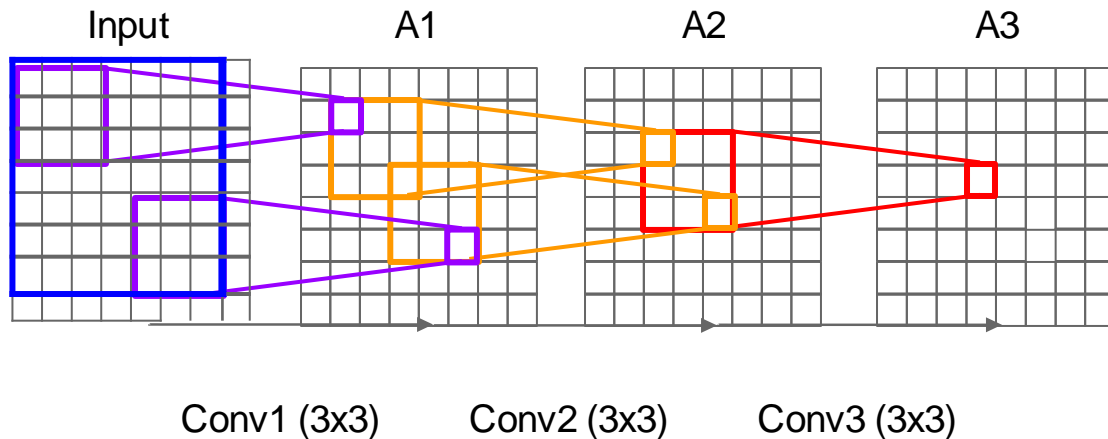
Q: What is the effective receptive field of three 3x3 conv (stride 1) layers?



# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

Q: What is the effective receptive field of three 3x3 conv (stride 1) layers?





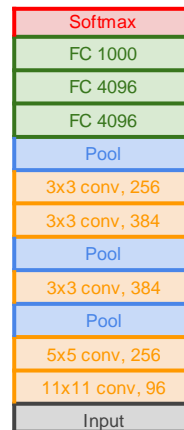
# Case Study: VGGNet

[Simonyan and Zisserman, 2014]

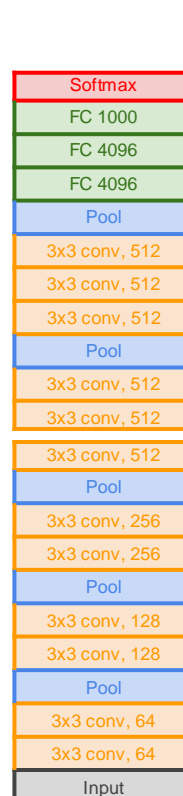
Q: Why use smaller filters? (3x3 conv)

Stack of three 3x3 conv (stride 1) layers has same **effective receptive field** as one 7x7 conv layer

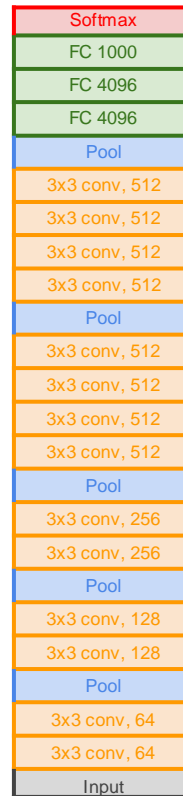
[7x7]



AlexNet



VGG16



VGG19

# Case Study: VGGNet

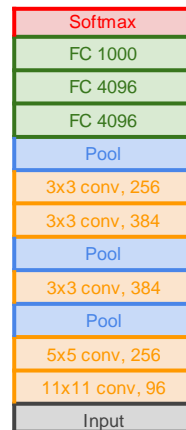
[Simonyan and Zisserman, 2014]

Q: Why use smaller filters? (3x3 conv)

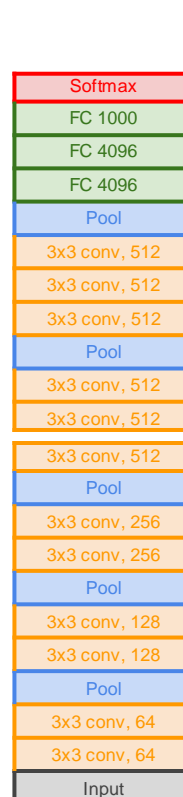
Stack of three 3x3 conv (stride 1) layers has same **effective receptive field** as one 7x7 conv layer

But deeper, more non-linearities

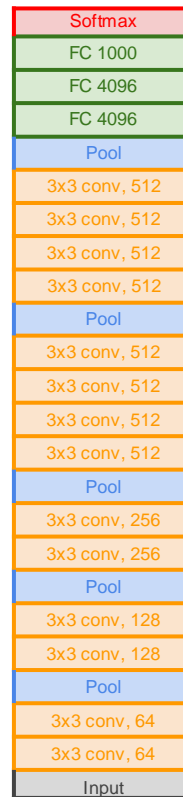
And fewer parameters:  $3 * (3^2 C^2)$  vs.  $7^2 C^2$  for C channels per layer



AlexNet

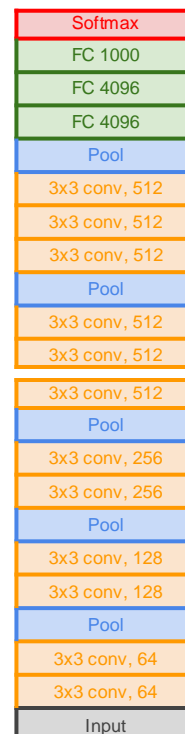


VGG16



VGG19

INPUT: [224x224x3]      memory:  $224*224*3=150\text{K}$       params: 0      (not counting biases)  
 CONV3-64: [224x224x64]      memory:  $224*224*64=3.2\text{M}$       params:  $(3*3*3)*64 = 1,728$   
 CONV3-64: [224x224x64]      memory:  $224*224*64=3.2\text{M}$       params:  $(3*3*64)*64 = 36,864$   
 POOL2: [112x112x64]      memory:  $112*112*64=800\text{K}$       params: 0  
 CONV3-128: [112x112x128]      memory:  $112*112*128=1.6\text{M}$       params:  $(3*3*64)*128 = 73,728$   
 CONV3-128: [112x112x128]      memory:  $112*112*128=1.6\text{M}$       params:  $(3*3*128)*128 = 147,456$   
 POOL2: [56x56x128]      memory:  $56*56*128=400\text{K}$       params: 0  
 CONV3-256: [56x56x256]      memory:  $56*56*256=800\text{K}$       params:  $(3*3*128)*256 = 294,912$   
 CONV3-256: [56x56x256]      memory:  $56*56*256=800\text{K}$       params:  $(3*3*256)*256 = 589,824$   
 CONV3-256: [56x56x256]      memory:  $56*56*256=800\text{K}$       params:  $(3*3*256)*256 = 589,824$   
 POOL2: [28x28x256]      memory:  $28*28*256=200\text{K}$       params: 0  
 CONV3-512: [28x28x512]      memory:  $28*28*512=400\text{K}$       params:  $(3*3*256)*512 = 1,179,648$   
 CONV3-512: [28x28x512]      memory:  $28*28*512=400\text{K}$       params:  $(3*3*512)*512 = 2,359,296$   
 CONV3-512: [28x28x512]      memory:  $28*28*512=400\text{K}$       params:  $(3*3*512)*512 = 2,359,296$   
 POOL2: [14x14x512]      memory:  $14*14*512=100\text{K}$       params: 0  
 CONV3-512: [14x14x512]      memory:  $14*14*512=100\text{K}$       params:  $(3*3*512)*512 = 2,359,296$   
 CONV3-512: [14x14x512]      memory:  $14*14*512=100\text{K}$       params:  $(3*3*512)*512 = 2,359,296$   
 CONV3-512: [14x14x512]      memory:  $14*14*512=100\text{K}$       params:  $(3*3*512)*512 = 2,359,296$   
 POOL2: [7x7x512]      memory:  $7*7*512=25\text{K}$       params: 0  
 FC: [1x1x4096]      memory: 4096      params:  $7*7*512*4096 = 102,760,448$   
 FC: [1x1x4096]      memory: 4096      params:  $4096*4096 = 16,777,216$   
 FC: [1x1x1000]      memory: 1000      params:  $4096*1000 = 4,096,000$

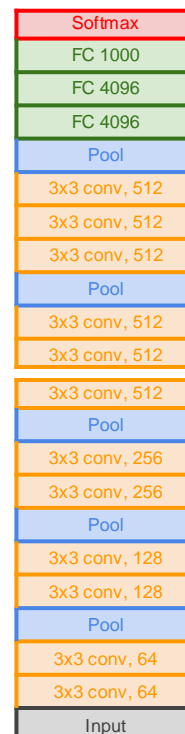


VGG16

INPUT: [224x224x3]      memory:  $224*224*3=150\text{K}$     params: 0      (not counting biases)  
 CONV3-64: [224x224x64]    memory:  $224*224*64=3.2\text{M}$     params:  $(3*3*3)*64 = 1,728$   
 CONV3-64: [224x224x64]    memory:  $224*224*64=3.2\text{M}$     params:  $(3*3*64)*64 = 36,864$   
 POOL2: [112x112x64]    memory:  $112*112*64=800\text{K}$     params: 0  
 CONV3-128: [112x112x128]    memory:  $112*112*128=1.6\text{M}$     params:  $(3*3*64)*128 = 73,728$   
 CONV3-128: [112x112x128]    memory:  $112*112*128=1.6\text{M}$     params:  $(3*3*128)*128 = 147,456$   
 POOL2: [56x56x128]    memory:  $56*56*128=400\text{K}$     params: 0  
 CONV3-256: [56x56x256]    memory:  $56*56*256=800\text{K}$     params:  $(3*3*128)*256 = 294,912$   
 CONV3-256: [56x56x256]    memory:  $56*56*256=800\text{K}$     params:  $(3*3*256)*256 = 589,824$   
 CONV3-256: [56x56x256]    memory:  $56*56*256=800\text{K}$     params:  $(3*3*256)*256 = 589,824$   
 POOL2: [28x28x256]    memory:  $28*28*256=200\text{K}$     params: 0  
 CONV3-512: [28x28x512]    memory:  $28*28*512=400\text{K}$     params:  $(3*3*256)*512 = 1,179,648$   
 CONV3-512: [28x28x512]    memory:  $28*28*512=400\text{K}$     params:  $(3*3*512)*512 = 2,359,296$   
 CONV3-512: [28x28x512]    memory:  $28*28*512=400\text{K}$     params:  $(3*3*512)*512 = 2,359,296$   
 POOL2: [14x14x512]    memory:  $14*14*512=100\text{K}$     params: 0  
 CONV3-512: [14x14x512]    memory:  $14*14*512=100\text{K}$     params:  $(3*3*512)*512 = 2,359,296$   
 CONV3-512: [14x14x512]    memory:  $14*14*512=100\text{K}$     params:  $(3*3*512)*512 = 2,359,296$   
 CONV3-512: [14x14x512]    memory:  $14*14*512=100\text{K}$     params:  $(3*3*512)*512 = 2,359,296$   
 POOL2: [7x7x512]    memory:  $7*7*512=25\text{K}$     params: 0  
 FC: [1x1x4096]    memory: 4096    params:  $7*7*512*4096 = 102,760,448$   
 FC: [1x1x4096]    memory: 4096    params:  $4096*4096 = 16,777,216$   
 FC: [1x1x1000]    memory: 1000    params:  $4096*1000 = 4,096,000$

**TOTAL memory:**  $24\text{M} * 4 \text{ bytes} \sim 96\text{MB}$  / image (for a forward pass)

**TOTAL params:** 138M parameters



VGG16

INPUT: [224x224x3] memory:  $224*224*3=150\text{K}$  params: 0 (not counting biases)

CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*3)*64 = 1,728$

CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*64)*64 = 36,864$

POOL2: [112x112x64] memory:  $112*112*64=800\text{K}$  params: 0

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*64)*128 = 73,728$

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*128)*128 = 147,456$

POOL2: [56x56x128] memory:  $56*56*128=400\text{K}$  params: 0

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*128)*256 = 294,912$

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*256)*256 = 589,824$

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*256)*256 = 589,824$

POOL2: [28x28x256] memory:  $28*28*256=200\text{K}$  params: 0

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*256)*512 = 1,179,648$

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [14x14x512] memory:  $14*14*512=100\text{K}$  params: 0

CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [7x7x512] memory:  $7*7*512=25\text{K}$  params: 0

FC: [1x1x4096] memory: 4096 params:  $7*7*512*4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params:  $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params:  $4096*1000 = 4,096,000$

**TOTAL memory:**  $24\text{M} * 4 \text{ bytes} \sim 96\text{MB}$  / image (only forward!  $\sim 2$  for bwd)

**TOTAL params:** 138M parameters

Note:

Most memory is in  
early CONV

Most params are  
in late FC

INPUT: [224x224x3] memory:  $224*224*3=150\text{K}$  params: 0 (not counting biases)

CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*3)*64 = 1,728$

CONV3-64: [224x224x64] memory:  $224*224*64=3.2\text{M}$  params:  $(3*3*64)*64 = 36,864$

POOL2: [112x112x64] memory:  $112*112*64=800\text{K}$  params: 0

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*64)*128 = 73,728$

CONV3-128: [112x112x128] memory:  $112*112*128=1.6\text{M}$  params:  $(3*3*128)*128 = 147,456$

POOL2: [56x56x128] memory:  $56*56*128=400\text{K}$  params: 0

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*128)*256 = 294,912$

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*256)*256 = 589,824$

CONV3-256: [56x56x256] memory:  $56*56*256=800\text{K}$  params:  $(3*3*256)*256 = 589,824$

POOL2: [28x28x256] memory:  $28*28*256=200\text{K}$  params: 0

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*256)*512 = 1,179,648$

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [28x28x512] memory:  $28*28*512=400\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [14x14x512] memory:  $14*14*512=100\text{K}$  params: 0

CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [14x14x512] memory:  $14*14*512=100\text{K}$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [7x7x512] memory:  $7*7*512=25\text{K}$  params: 0

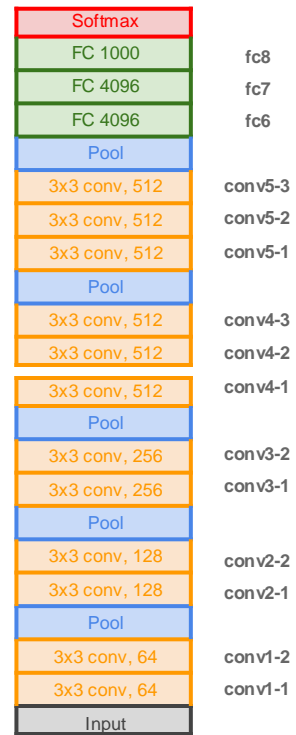
FC: [1x1x4096] memory: 4096 params:  $7*7*512*4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params:  $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params:  $4096*1000 = 4,096,000$

**TOTAL memory:**  $24\text{M} * 4 \text{ bytes} \sim 96\text{MB}$  / image (only forward!  $\sim 2$  for bwd)

**TOTAL params:** 138M parameters



VGG16

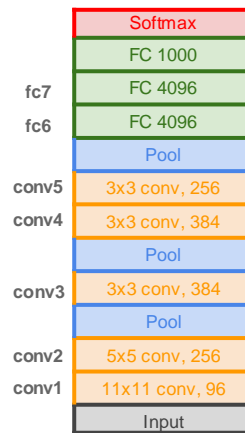
Common names

# Case Study: VGGNet

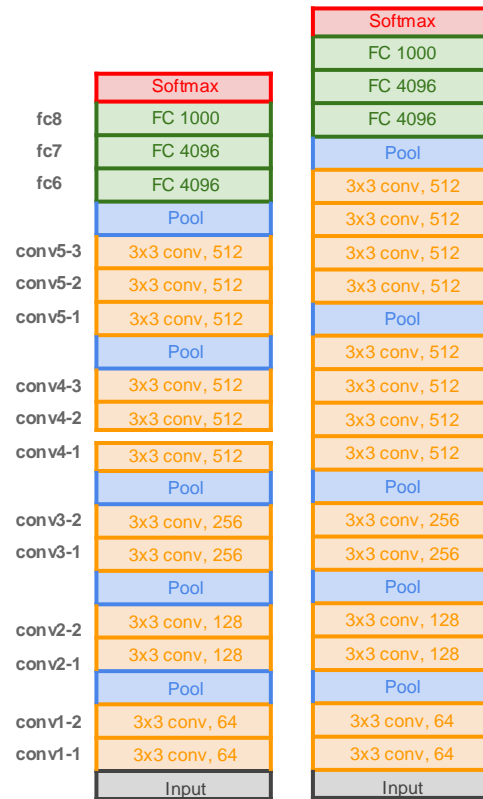
[Simonyan and Zisserman, 2014]

## Details:

- ILSVRC'14 2nd in classification, 1st in localization
- Similar training procedure as Krizhevsky 2012
- No Local Response Normalisation (LRN)
- Use VGG16 or VGG19 (VGG19 only slightly better, more memory)
- Use ensembles for best results
- FC7 features generalize well to other tasks



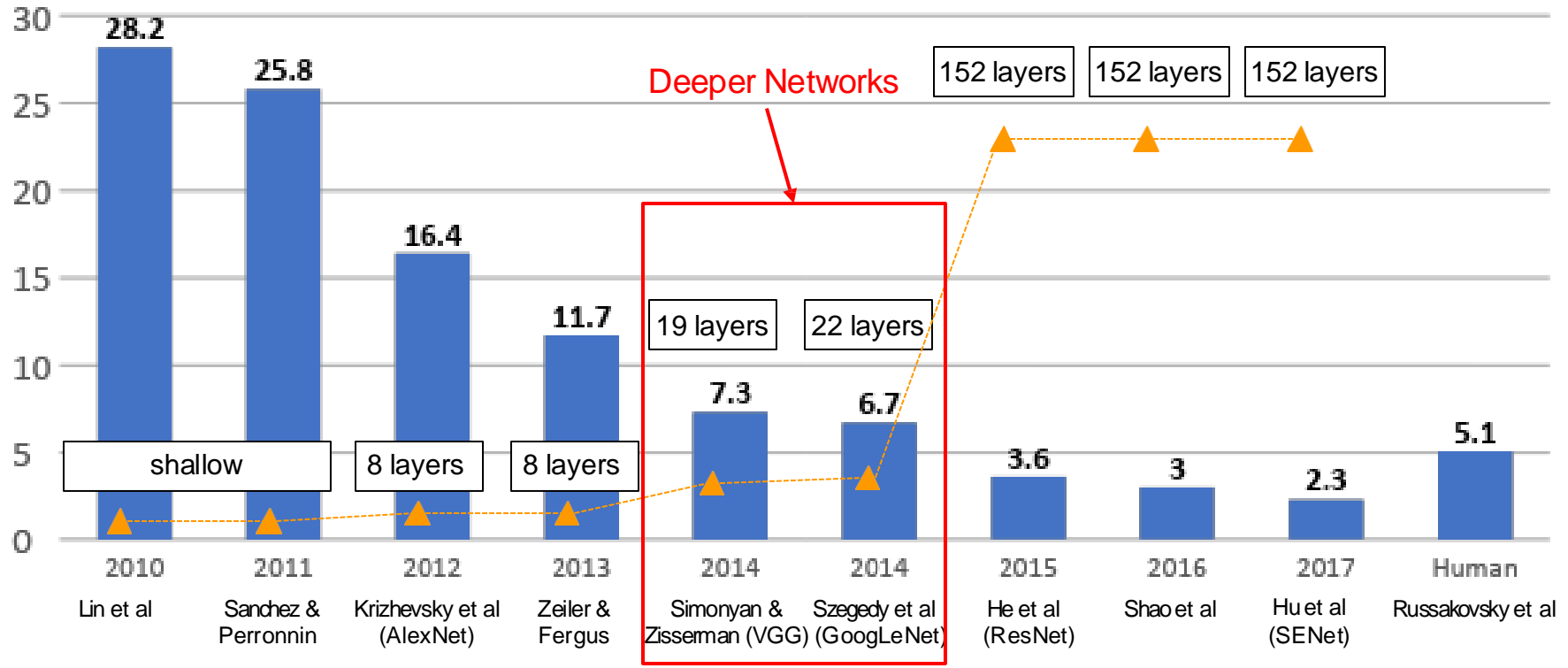
AlexNet



VGG16

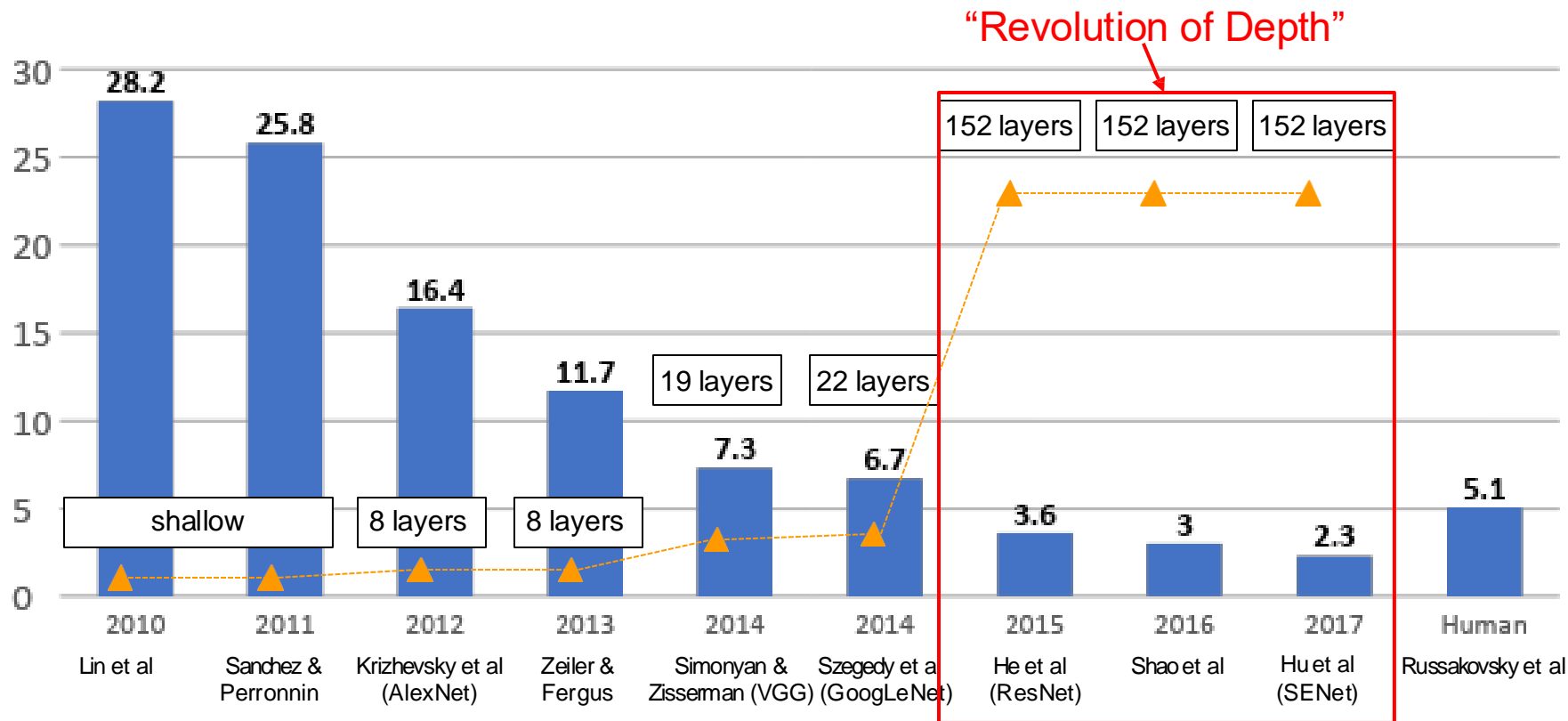
VGG19

# ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





# ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners

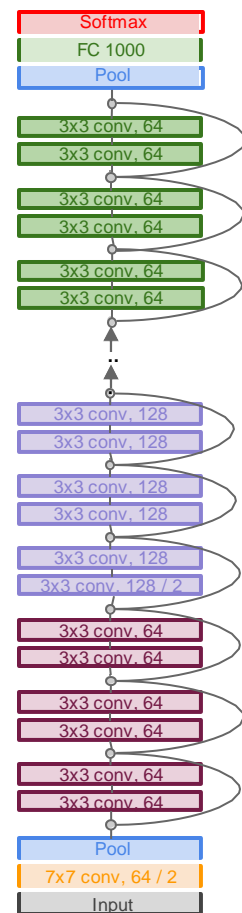
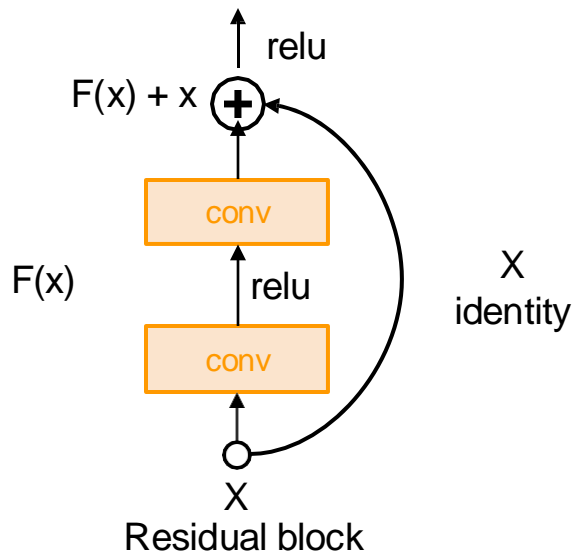


# Case Study: ResNet

[He et al., 2015]

Very deep networks using residual connections

- 152-layer model for ImageNet
- ILSVRC'15 classification winner (3.57% top 5 error)
- Swept all classification and detection competitions in ILSVRC'15 and COCO'15!



# Case Study: ResNet

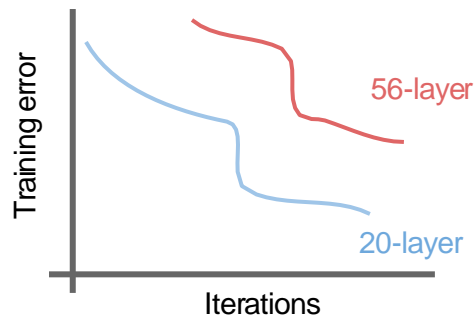
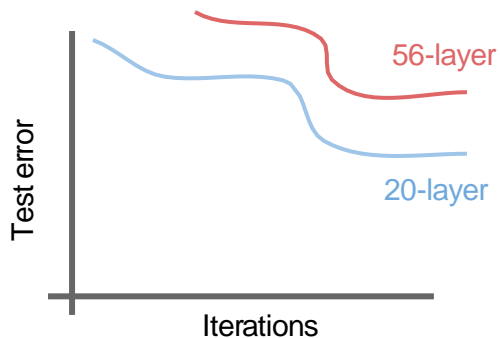
*[He et al., 2015]*

What happens when we continue stacking deeper layers on a “plain” convolutional neural network?

# Case Study: ResNet

*[He et al., 2015]*

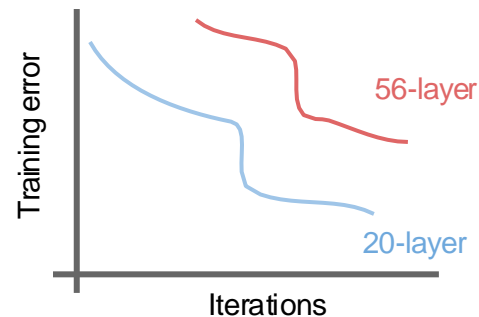
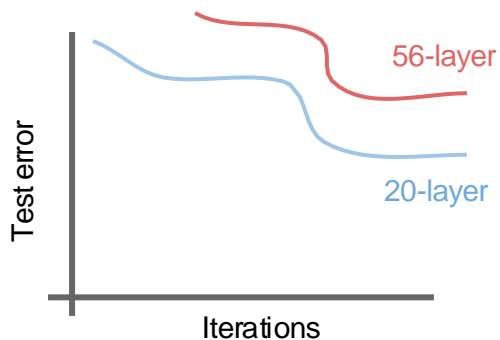
What happens when we continue stacking deeper layers on a “plain” convolutional neural network?



# Case Study: ResNet

[He et al., 2015]

What happens when we continue stacking deeper layers on a “plain” convolutional neural network?



56-layer model performs worse on both test and training error

-> The deeper model performs worse, but it's **not caused by overfitting!**

# Case Study: ResNet

*[He et al., 2015]*

Fact: Deep models have more representation power (more parameters) than shallower models.

Hypothesis: the problem is an *optimization* problem,  
**deeper models are harder to optimize**

# Case Study: ResNet

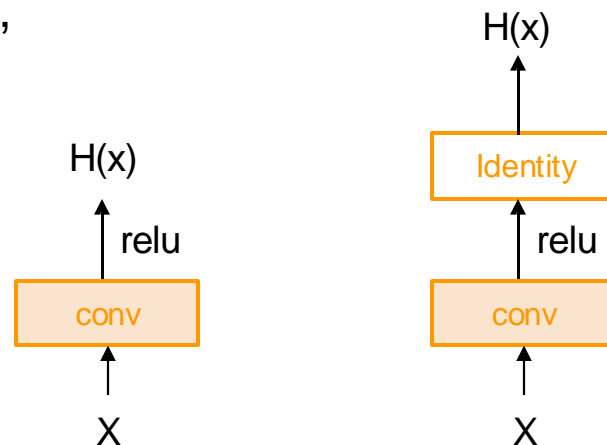
[He et al., 2015]

Fact: Deep models have more representation power (more parameters) than shallower models.

Hypothesis: the problem is an *optimization* problem, deeper models are harder to optimize

What should the deeper model learn to be at least as good as the shallower model?

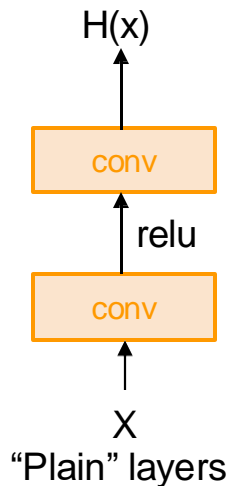
A solution by construction is copying the learned layers from the shallower model and setting additional layers to identity mapping.



# Case Study: ResNet

*[He et al., 2015]*

Solution: Use network layers to fit a residual mapping instead of directly trying to fit a desired underlying mapping

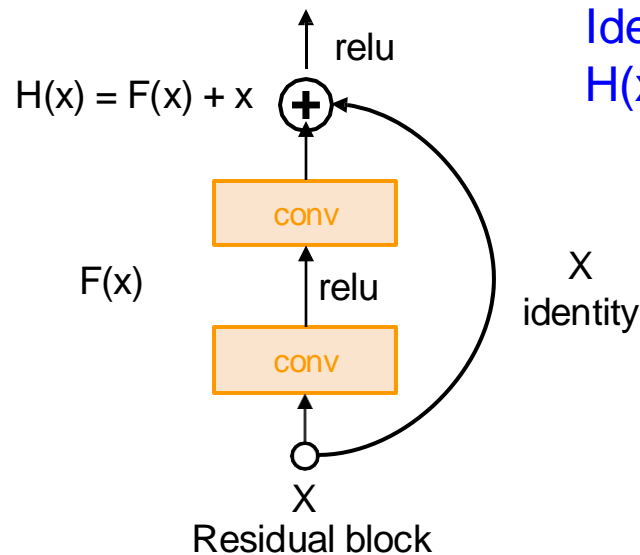
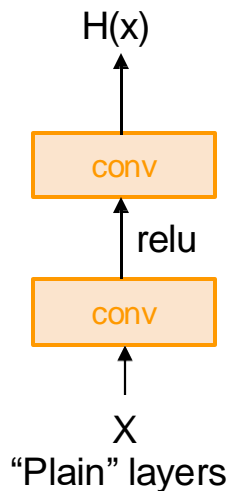




# Case Study: ResNet

[He et al., 2015]

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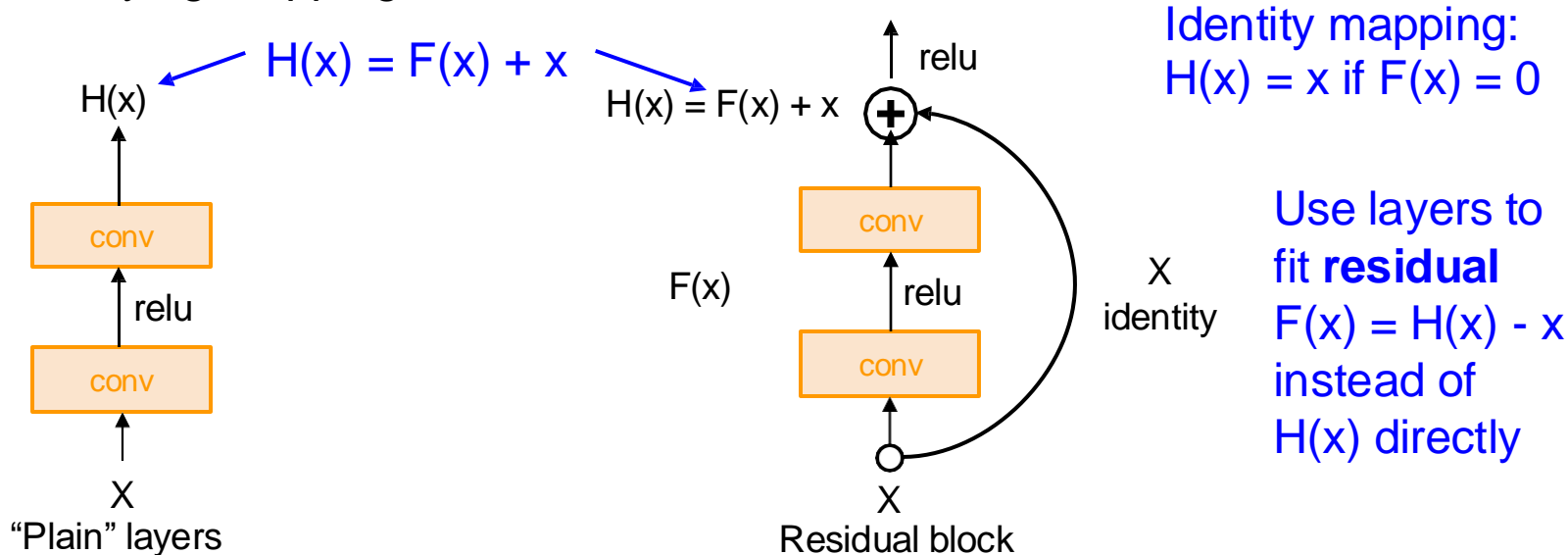


Identity mapping:  
 $H(x) = x$  if  $F(x) = 0$

# Case Study: ResNet

[He et al., 2015]

Solution: Use network layers to fit a residual mapping instead of directly trying to fit a desired underlying mapping

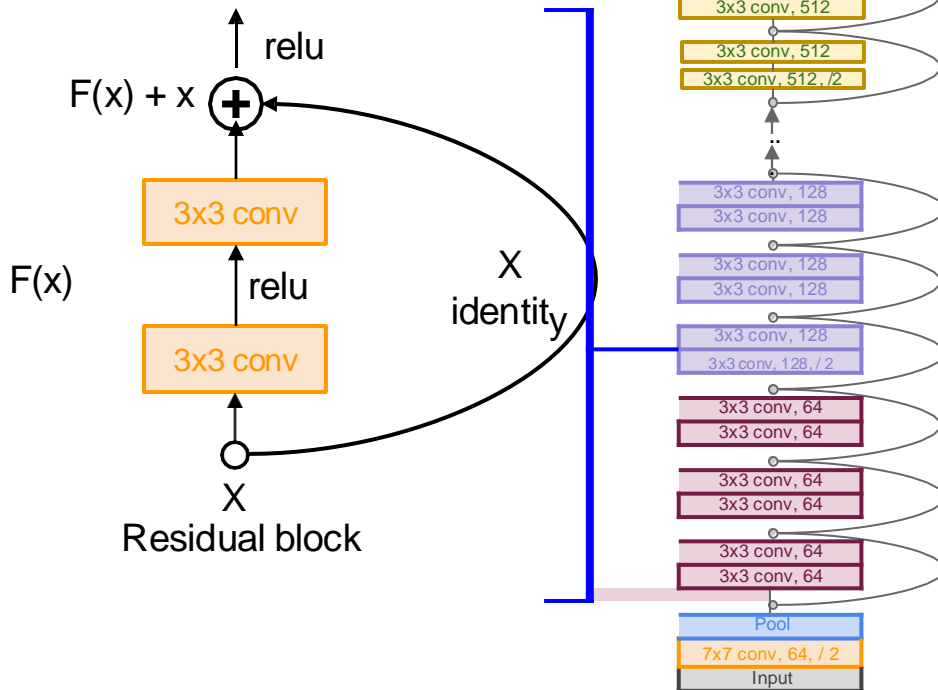


# Case Study: ResNet

[He et al., 2015]

Full ResNet architecture:

- Stack residual blocks
- Every residual block has two 3x3 conv layers

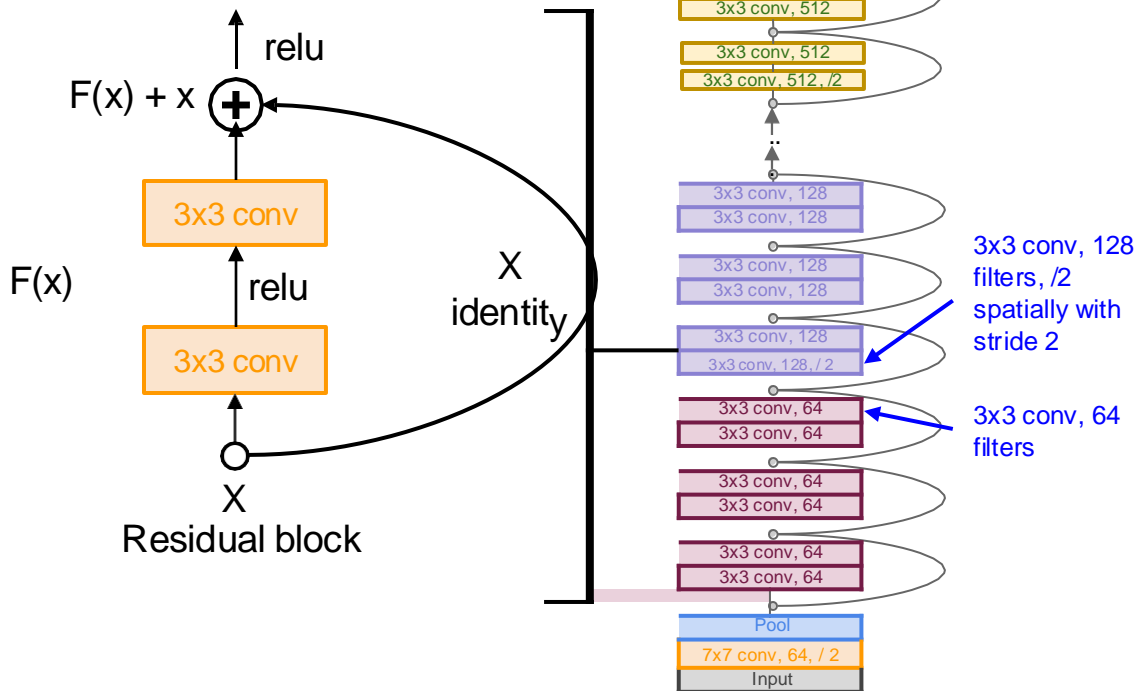


# Case Study: ResNet

[He et al., 2015]

Full ResNet architecture:

- Stack residual blocks
  - Every residual block has two 3x3 conv layers
  - Periodically, double # of filters and downsample spatially using stride 2 (/2 in each dimension)
- Reduce the activation volume by half.

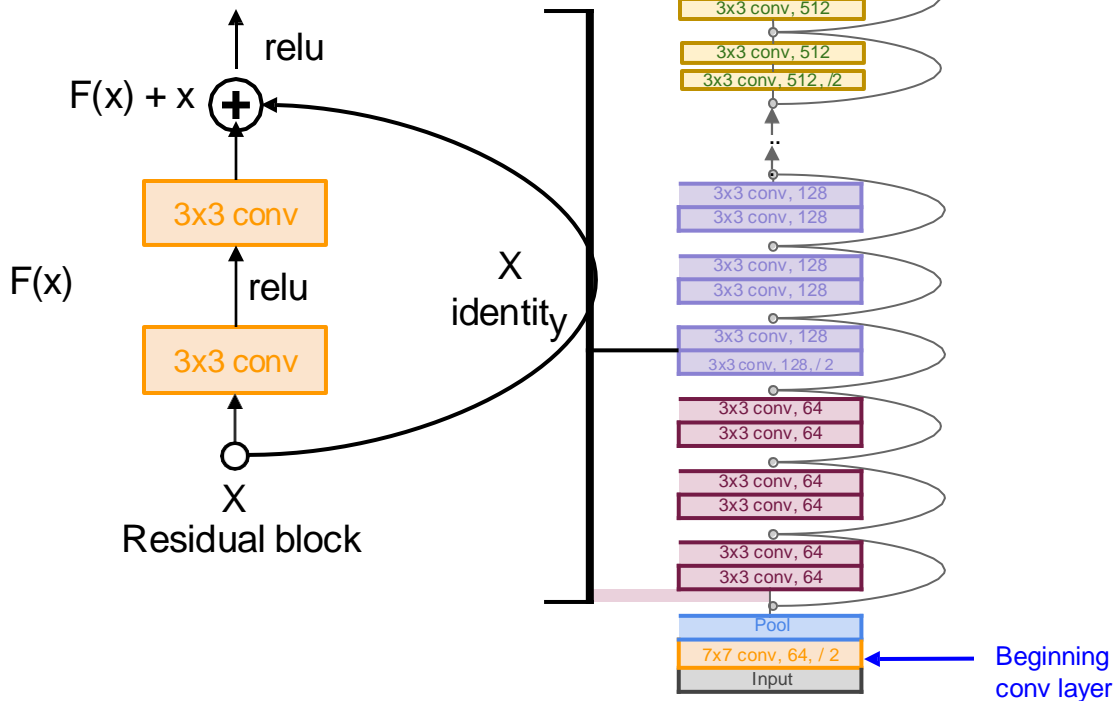


# Case Study: ResNet

[He et al., 2015]

Full ResNet architecture:

- Stack residual blocks
- Every residual block has two 3x3 conv layers
- Periodically, double # of filters and downsample spatially using stride 2 (/2 in each dimension)
- Additional conv layer at the beginning (stem)

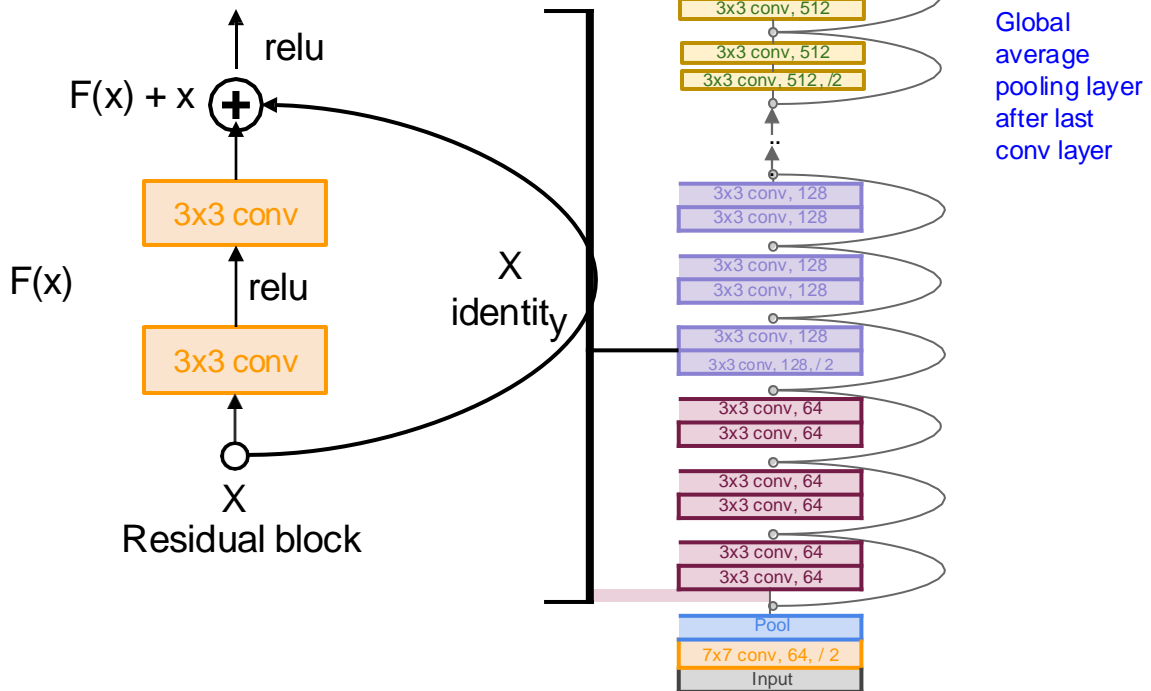


# Case Study: ResNet

[He et al., 2015]

## Full ResNet architecture:

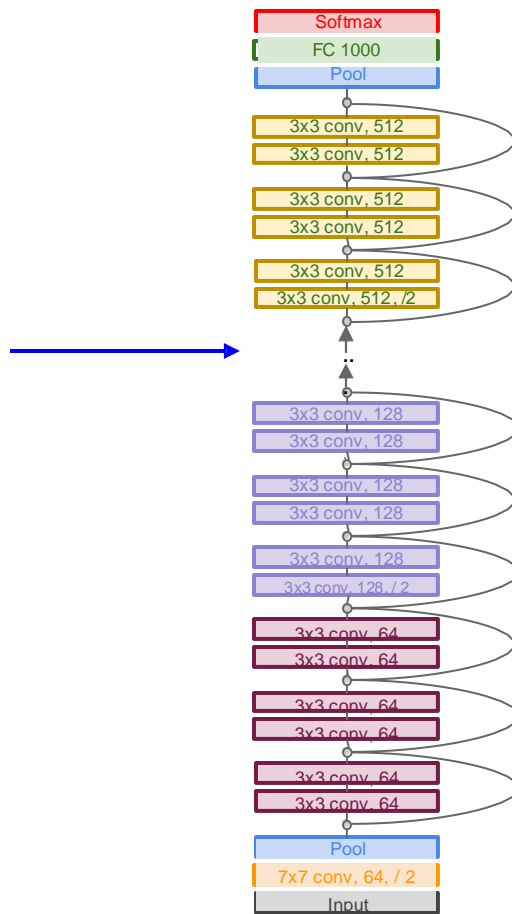
- Stack residual blocks
- Every residual block has two 3x3 conv layers
- Periodically, double # of filters and downsample spatially using stride 2 (/2 in each dimension)
- Additional conv layer at the beginning (stem)
- No FC layers at the end (only FC 1000 to output classes)
- (In theory, you can train a ResNet with input image of variable sizes)



# Case Study: ResNet

[He et al., 2015]

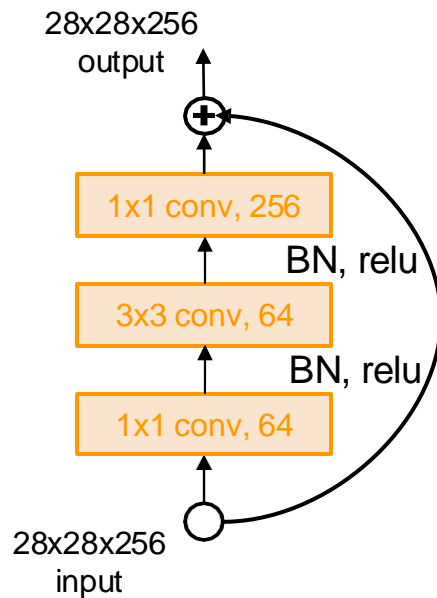
Total depths of 18, 34, 50,  
101, or 152 layers for  
ImageNet



# Case Study: ResNet

*[He et al., 2015]*

For deeper networks (ResNet-50+), use “bottleneck” layer to improve efficiency (similar to GoogLeNet)

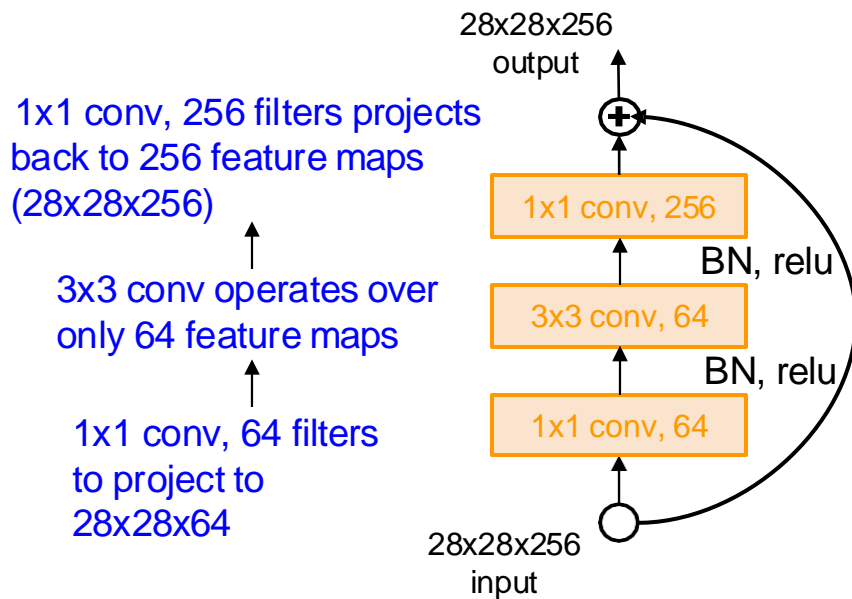




# Case Study: ResNet

[He et al., 2015]

For deeper networks (ResNet-50+), use “bottleneck” layer to improve efficiency (similar to GoogLeNet)



# Case Study: ResNet

*[He et al., 2015]*

Training ResNet in practice:

- Batch Normalization after every CONV layer
- Xavier initialization from He et al.
- SGD + Momentum (0.9)
- Learning rate: 0.1, divided by 10 when validation error plateaus
- Mini-batch size 256
- Weight decay of  $1e-5$
- No dropout used

# Case Study: ResNet

[He et al., 2015]

## Experimental Results

- Able to train very deep networks without degrading (152 layers on ImageNet, 1202 on Cifar)
- Deeper networks now achieve lower training error as expected
- Swept 1st place in all ILSVRC and COCO 2015 competitions

## MSRA @ ILSVRC & COCO 2015 Competitions

### • 1st places in all five main tracks

- ImageNet Classification: “Ultra-deep” (quote Yann) 152-layer nets
- ImageNet Detection: 16% better than 2nd
- ImageNet Localization: 27% better than 2nd
- COCO Detection: 11% better than 2nd
- COCO Segmentation: 12% better than 2nd

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ILSVRC 2015 classification winner (3.6% top 5 error) -- better than “human performance”! (Russakovsky 2014)

# Summary: CNN Architectures

## Case Studies

- AlexNet
- VGG
- ResNet

## Also.....

- ZFNet
- GoogLeNet
- SENet
- Wide ResNet
- ResNeXT
- DenseNet
- MobileNets
- NASNet

# Main takeaways

**AlexNet** showed that you can use CNNs to train Computer Vision models.

**VGG** shows that bigger networks work better

**ResNet** showed us how to train extremely deep networks

- Limited only by GPU & memory!
- Showed diminishing returns as networks got bigger

After ResNet: CNNs were better than the human metric and focus shifted to other topics:

- Efficient Networks: **MobileNet**, **ShuffleNet**
- **Neural Architecture Search** can now automate architecture design

# Summary: CNN Architectures

- Many popular architectures are available in model zoos.
- ResNets are good defaults to use.  
True for > 8 years!
- Networks have gotten increasingly deep over time.
- Many other aspects of network architectures are also continuously being investigated and improved.