** Basic Assumptions:

- 1. Owner can sell all the soaps she has made in every month.
- 2. We ignore "10 soaps in stock" condition.
- 3. Ignore working hours constraints.
- 4. Ignore raw materials constraints, calculation based on the average statistics in the past.
- 5. Tax and packaging fees all included in the final OF(objective function).
- 1. Constraints:
- Number constraints:

$$\sum_{i=1}^{6} x_i \le 400$$
 (max bar/month)

• monthly output ≥ market demand:

$$\frac{9}{10} x_1 \ge 20\% \sum_{i=1}^{6} x_i$$

$$\frac{9}{10} x_2 \ge 20\% \sum_{i=1}^{6} x_i$$

$$\frac{9}{10}$$
 x₃ \geq 15% $\sum_{i=1}^{6}$ x_i

$$\frac{9}{10} x_4 \ge 10\% \sum_{i=1}^{6} x_i$$

$$\frac{9}{10} x_5 \ge 10\% \sum_{i=1}^{6} x_i$$

$$rac{9}{10} \, x_6 \geq 15\% \, \sum_{i=1}^6 \, x_i$$

• integer constraint:

 X_i is an integer (i \in [1, 6])

2. Set slack vars, artificial vars and excess vars:

Slack vars: s₁

Excess vars: $e_1 \rightarrow e_6$

Artificial vars: a₁ -> a₆

Symbol projection:

$$(x_1 \rightarrow x_6) \Longrightarrow (x_1 \rightarrow x_6)$$

$$x_7 \Longrightarrow s_1$$

$$(x_8 \rightarrow x_{13}) \Rightarrow (e_1 \rightarrow e_6)$$

$$(x_{14} -> x_{19}) \Longrightarrow (a_1 -> a_6)$$

3. Standard form:

$$x_{1}+ x_{2}+ x_{3}+ x_{4}+ x_{5}+ x_{6}+ s_{1}=400$$
 $7x_{1}-2x_{2}-2 x_{3}-2 x_{4}-2 x_{5}-2 x_{6}-e_{1}+a_{1}=0$
 $-2x_{1}+7x_{2}-2 x_{3}-2 x_{4}-2 x_{5}-2 x_{6}-e_{2}+a_{2}=0$
 $-x_{1}-x_{2}+5x_{3}-x_{4}-x_{5}-x_{6}-e_{3}+a_{3}=0$
 $-x_{1}-x_{2}-x_{3}+8x_{4}-x_{5}-x_{6}-e_{4}+a_{4}=0$
 $-x_{1}-x_{2}-x_{3}-x_{4}+8x_{5}-x_{6}-e_{5}+a_{5}=0$
 $-x_{1}-x_{2}-x_{3}-x_{4}+8x_{5}-x_{6}-e_{6}+a_{6}=0$

4. OF(objective function):

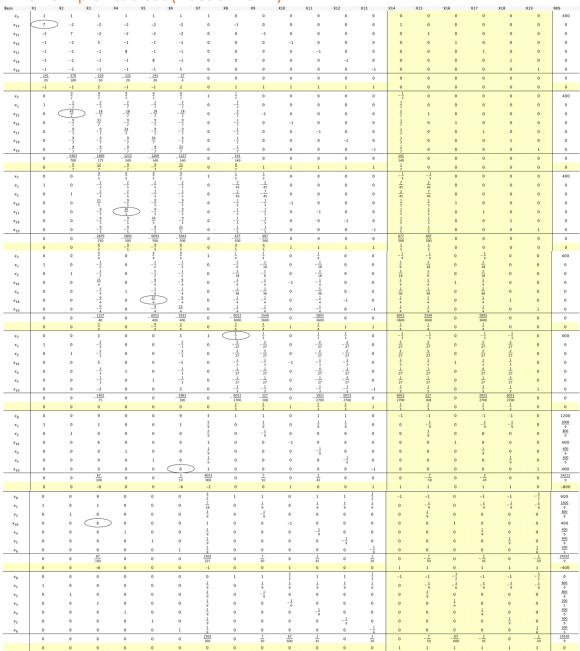
Unit: dollars

Max z =
$$7.05x_1+5.79x_2+6.38x_3+6.65x_4+7.05x_5+6.75x_6$$

Min w = $-7.05x_1-5.79x_2-6.38x_3-6.65x_4-7.05x_5-6.75x_6$

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	X1	X2	Х3	X4	X5	X6 >	17	X8	X9	X10	X11	X12	X13	X14	X15	X16	X17	X18	X19	RHS
×7	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	400.0
14	7.00 -2.00	7.00	-2.00 -2.00	-2.00 -2.00	-2.00 -2.00	-2.00 -2.00	0.00	-1.00 0.00	0.00 -1.00	0.00	0.00	0.00	0.00	1.00 0.00	0.00 1.00	0.00	0.00	0.00	0.00	0.00
16	-1.00	-1.00	5.00	-1.00	-1.00	-1.00	0.00	0.00	0.00	-1.00	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.00
17	-1.00	-1.00	-1.00	8.00	-1.00	-1.00	0.00	0.00	0.00	0.00	-1.00	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00
18	-1.00 -1.00	-1.00 -1.00	-1.00 -1.00	-1.00 -1.00	8.00 -1.00	-1.00 5.00	0.00	0.00	0.00	0.00	0.00	-1.00 0.00	0.00 -1.00	0.00	0.00	0.00	0.00	1.00 0.00	0.00 1.00	0.00
14	-7.05	-5.79	-6.38	-6.65	-7.05	-6.75	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	-1.00	-1.00	2.00	-1.00	-1.00	2.00	0.00	1.00	1.00	1.00	1.00	1.00	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
x ₇ x ₁	1.00	1.29 -0.29	1.29 -0.29	1.29 -0.29	1.29 -0.29	1.29 -0.29	0.00	0.14	0.00	0.00	0.00	0.00	0.00	-0.14 0.14	0.00	0.00	0.00	0.00	0.00	400.0
15	0.00	6.43	-2.57	-2.57	-2.57	-2.57	0.00	-0.29	-1.00	0.00	0.00	0.00	0.00	0.29	1.00	0.00	0.00	0.00	0.00	0.00
16	0.00	-1.29	4.71	-1.29	-1.29	-1.29	0.00	-0.14	0.00	-1.00	0.00	0.00	0.00	0.14	0.00	1.00	0.00	0.00	0.00	0.0
17	0.00	-1.29 -1.29	-1.29 -1.29	7.71 -1.29	-1.29 7.71	-1.29 -1.29	0.00	-0.14 -0.14	0.00	0.00	-1.00 0.00	0.00 -1.00	0.00	0.14	0.00	0.00	1.00 0.00	0.00 1.00	0.00	0.0
18	0.00	-1.29	-1.29	-1.29	-1.29	4.71	0.00	-0.14	0.00	0.00	0.00	0.00	-1.00	0.14	0.00	0.00	0.00	0.00	1.00	0.0
	0.00	-7.80	-8.39	-8.66	-9.06	-8.76	0.00	-1.01	0.00	0.00	0.00	0.00	0.00	1.01	0.00	0.00	0.00	0.00	0.00	0.0
	0.00	-1.29 0.00	1.71	-1.29 1.80	-1.29 1.80	1.71	1.00	0.86	0.20	0.00	0.00	0.00	0.00	-0.20	-0.20	0.00	0.00	0.00	0.00	400.
х ₇ х ₁	1.00	0.00	-0.40	-0.40	-0.40	-0.40	0.00	-0.16	-0.04	0.00	0.00	0.00	0.00	0.16	0.04	0.00	0.00	0.00	0.00	0.0
х2	0.00	1.00	-0.40	-0.40	-0.40	-0.40	0.00	-0.04	-0.16	0.00	0.00	0.00	0.00	0.04	0.16	0.00	0.00	0.00	0.00	0.0
16	0.00	0.00	4.20	-1.80	-1.80	-1.80	0.00	-0.20	-0.20	-1.00	0.00	0.00	0.00	0.20	0.20	1.00	0.00	0.00	0.00	0.0
17	0.00	0.00	-1.80 -1.80	7.20	7.20	-1.80 -1.80	0.00	-0.20 -0.20	-0.20 -0.20	0.00	-1.00 0.00	0.00 -1.00	0.00	0.20	0.20	0.00	1.00 0.00	0.00 1.00	0.00	0.0
19	0.00	0.00	-1.80	-1.80	-1.80	4.20	0.00	-0.20	-0.20	0.00	0.00	0.00	-1.00	0.20	0.20	0.00	0.00	0.00	1.00	0.0
	0.00	0.00	-11.52	-11.79	-12.19	-11.89	0.00	-1.35	-1.21	0.00	0.00	0.00	0.00	1.35	1.21	0.00	0.00	0.00	0.00	0.0
х ₇	0.00	0.00	2.25	-1.80 0.00	-1.80 2.25	2.25	1.00	0.80	0.80	0.00	0.25	0.00	0.00	-0.25	0.20 -0.25	0.00	0.00 -0.25	0.00	0.00	400
×1	1.00	0.00	-0.50	0.00	-0.50	-0.50	0.00	-0.17	-0.06	0.00	-0.06	0.00	0.00	0.17	0.06	0.00	0.06	0.00	0.00	0.0
12	0.00	1.00	-0.50	0.00	-0.50	-0.50	0.00	-0.06	-0.17	0.00	-0.06	0.00	0.00	0.06	0.17	0.00	0.06	0.00	0.00	0.
16	0.00	0.00	3.75 -0.25	0.00 1.00	-2.25	-2.25 -0.25	0.00	-0.25 -0.03	-0.25 -0.03	-1.00 0.00	-0.25 -0.14	0.00	0.00	0.25	0.25	1.00 0.00	0.25	0.00	0.00	0.0
×4	0.00	0.00	-0.25	0.00	6.75	-0.25	0.00	-0.03	-0.03	0.00	-0.14	-1.00	0.00	0.03	0.03	0.00	0.14	1.00	0.00	0.0
19	0.00	0.00	-2.25	0.00	-2.25	3.75	0.00	-0.25	-0.25	0.00	-0.25	0.00	-1.00	0.25	0.25	0.00	0.25	0.00	1.00	0.0
	0.00	0.00	-14.46	0.00	-15.13	-14.83	0.00	-1.68	-1.54	0.00	-1.64	0.00	0.00	1.68	1.54	0.00	1.64	0.00	0.00	0.0
κ,	0.00	0.00	3.00	0.00	-2.25 0.00	0.75 3.00	1.00	0.75	0.75	0.00	0.75	0.33	0.00	-0.33	0.25 -0.33	0.00	0.25 -0.33	-0.33	0.00	400
x ₁	1.00	0.00	-0.67	0.00	0.00	-0.67	0.00	-0.19	-0.07	0.00	-0.07	-0.07	0.00	0.19	0.07	0.00	0.07	0.07	0.00	0.0
x,	0.00	1.00	-0.67	0.00	0.00	-0.67	0.00	-0.07	-0.19	0.00	-0.07	-0.07	0.00	0.07	0.19	0.00	0.07	0.07	0.00	0.0
16 K4	0.00	0.00	3.00	0.00	0.00	-3.00 -0.33	0.00	-0.33 -0.04	-0.33 -0.04	-1.00 0.00	-0.33 -0.15	-0.33 -0.04	0.00	0.33	0.33	1.00	0.33	0.33	0.00	0.0
^4 Xe	0.00	0.00	-0.33	0.00	1.00	-0.33	0.00	-0.04	-0.04	0.00	-0.04	-0.15	0.00	0.04	0.04	0.00	0.04	0.15	0.00	0.0
19	0.00	0.00	-3.00	0.00	0.00	3.00	0.00	-0.33	-0.33	0.00	-0.33	-0.33	-1.00	0.33	0.33	0.00	0.33	0.33	1.00	0.0
	0.00	0.00	-19.51 0.00	0.00	0.00	-19.88 0.00	0.00	-2.24 0.67	-2.10 0.67	1.00	-2.20 0.67	-2.24 0.67	1.00	0.33	0.33	0.00	2.20	2.24 0.33	0.00	0.0
X _R	0.00	0.00	9.00	0.00	0.00	9.00	3.00	1.00	1.00	0.00	1.00	1.00	0.00	-1.00	-1.00	0.00	-1.00	-1.00	0.00	1200
x ₁	1.00	0.00	1.00	0.00	0.00	1.00	0.56	0.00	0.11	0.00	0.11	0.11	0.00	0.00	-0.11	0.00	-0.11	-0.11	0.00	222.
×2	0.00	0.00	6.00	0.00	0.00	0.00	1.00	0.00	-0.11 0.00	0.00 -1.00	0.00	0.00	0.00	0.00	0.11	1.00	0.00	0.00	0.00	88. 400.
16 C4	0.00	0.00	0.00	1.00	0.00	0.00	0.11	0.00	0.00	0.00	-0.11	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	400.
ζς	0.00	0.00	0.00	0.00	1.00	0.00	0.11	0.00	0.00	0.00	0.00	-0.11	0.00	0.00	0.00	0.00	0.00	0.11	0.00	44.
(19	0.00	0.00	0.00	0.00	0.00	€.00	1.00	0.00	0.00	0.00	0.00	0.00	-1.00	0.00	0.00	0.00	0.00	0.00	1.00	400.
	0.00	0.00	0.67 -6.00	0.00	0.00	0.30 -6.00	6.73 -2.00	0.00	0.14	0.00 1.00	0.04	0.00	0.00 1.00	0.00 1.00	-0.14 1.00	0.00	-0.04 1.00	0.00 1.00	0.00	2690 -800
ís.	0.00	0.00	9.00	0.00	0.00	0.00	1.50	1.00	1.00	0.00	1.00	1.00	1.50	-1.00	-1.00	0.00	-1.00	-1.00	-1.50	600.
K 1	1.00	0.00	1.00	0.00	0.00	0.00	0.39	0.00	0.11	0.00	0.11	0.11	0.17	0.00	-0.11	0.00	-0.11	-0.11	-0.17	155.
X ₂	0.00	1.00 0.00	6.00	0.00	0.00	0.00	1.00	0.00	-0.11 0.00	0.00 -1.00	0.00	0.00	0.00	0.00	0.11	0.00 1.00	0.00	0.00	0.00	88.4 400.
16 Ka	0.00	0.00	0.00	1.00	0.00	0.00	0.11	0.00	0.00	0.00	-0.11	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	444.
×ς	0.00	0.00	0.00	0.00	1.00	0.00	0.11	0.00	0.00	0.00	0.00	-0.11	0.00	0.00	0.00	0.00	0.00	0.11	0.00	44.4
x ₆	0.00	0.00	0.00	0.00	0.00	1.00	0.17	0.00	0.00	0.00	0.00	0.00	-0.17	0.00	0.00	0.00	0.00	0.00	0.17	66.6
	0.00	0.00	0.67 -6.00	0.00	0.00	0.00	6.68 -1.00	0.00	0.14	0.00 1.00	0.04	0.00	0.05	1.00	-0.14 1.00	0.00	-0.04 1.00	0.00 1.00	-0.05 1.00	2670 -400
× _R	0.00	0.00	0.00	0.00	0.00	0.00	0.00	1.00	1.00	1.50	1.00	1.00	1.50	-1.00	-1.00	-1.50	-1.00	-1.00	-1.50	0.0
x ₁	1.00	0.00	0.00	0.00	0.00	0.00	0.22	0.00	0.11	0.17	0.11	0.11	0.17	0.00	-0.11	-0.17	-0.11	-0.11	-0.17	88.
к,	0.00	1.00	0.00	0.00	0.00	0.00	0.22	0.00	-0.11	0.00	0.00	0.00	0.00	0.00	0.11	0.00	0.00	0.00	0.00	88.
х ₂ х ₄	0.00	0.00	0.00	0.00 1.00	0.00	0.00	0.17	0.00	0.00	-0.17 0.00	0.00 -0.11	0.00	0.00	0.00	0.00	0.17	0.00	0.00	0.00	66.
×4 ×c	0.00	0.00	0.00	0.00	1.00	0.00	0.11	0.00	0.00	0.00	0.00	-0.11	0.00	0.00	0.00	0.00	0.00	0.11	0.00	44.4
	0.00	0.00	0.00	0.00	0.00	1.00	0.17	0.00	0.00	0.00	0.00	0.00	-0.17	0.00	0.00	0.00	0.00	0.00	0.17	66.6
x ₆	0.00	0.00	0.00	0.00	0.00	0.00	6.56	0.00	0.14	0.11	0.04	0.00	0.05	0.00	-0.14	-0.11	-0.04	0.00	-0.05	2625

6. simplex tableau(fraction form):



7. Conclusion:

The optimal solution is (according to the decimal tableau above):

 $X_1 = 88.89$

 $X_2 = 88.89$

 $X_3 = 66.67$

 $X_4 = 44.44$

 $X_5 = 44.44$

 $X_6 = 66.67$

Optimal Profit = \$ 2625.56



integer constraint

In order to follow the Number Constrain:

 $X_1 = 88$

 $X_2 = 88$

 $X_3 = 66$

 $X_4 = 44$

 $X_5 = 44$

 $X_6 = 66$

Optimal Profit = \$ 2599.3