

Introduction to Data Science Course

# Evaluation

Le Ngoc Thanh  
lntanh@fit.hcmus.edu.vn  
Department of Computer Science

# Assessment

- ◎ Accuracy: The predictive capability of the classifier
- ◎ Effectiveness:
  - Cost to create the model *chi phí train*
  - Cost to use the model *chi phí chạy*
- ◎ Robustness: ability to solve noise or missing value
- ◎ Scale: Efficiency with Big Data
- ◎ Understandable *khó hiểu: khó customize, điều chỉnh, fix bug*
- ◎ Other properties: Tree size, ~~number of laws~~, quality of law...

# Accuracy

◎ The dataset is divided into two completely independent parts.

- Training set
- Test set

Training  
Validation

◎ Measures to evaluate accuracy: confusion matrix, fault rate,...

◎ The method of estimating the accuracy of the classifier:

- Holdout method, Random Subsampling

Cross-validation

Bootstrap

## Some concepts (1/2)

### ◎ Let's:

- Positive tuples are samples belonging to a major class that is concerned
- Negative tuples are the models that belong to the remaining classes

◎ P is the number of positive sample, N is number of negative samples in the test set.

◎ TP (True Positives): number of positive samples are classified correctly

◎ TN (True Negatives): number of negative samples are classified correctly

## Some concepts (2/2)

- ◎ FP (False Positives): number of negative samples are classified incorrectly to positive samples
- ◎ FN (False Negatives): number of positive samples are classified incorrectly to negative samples.

|              |   | Predicted class |      |         |
|--------------|---|-----------------|------|---------|
|              |   | +               | −    | Total   |
| Actual class | + | $TP$            | $FN$ | $P$     |
|              | − | $FP$            | $TN$ | $N$     |
| Total        |   | $P'$            | $N'$ | $P + N$ |

**Confusion Matrix**

# Confusion Matrix

| A\P | C  | ¬C |     |
|-----|----|----|-----|
| C   | TP | FN | P   |
| ¬C  | FP | TN | N   |
|     | P' | N' | All |

- ⊙ Data in computer store, positive samples P are samples with `buys_computer = yes`

| Actual class\Predicted class     | <code>buys_computer = yes</code> | <code>buys_computer = no</code> | Total |
|----------------------------------|----------------------------------|---------------------------------|-------|
| <code>buys_computer = yes</code> | <b>6954</b>                      | <b>46</b>                       | 7000  |
| <code>buys_computer = no</code>  | <b>412</b>                       | <b>2588</b>                     | 3000  |
| Total                            | 7366                             | 2634                            | 10000 |

- ⊙ Determine TP, TN, FP, FN?
- ⊙ Ideally, the sub diagonal should be 0 or approximately 0

# Accuracy

◎ Accuracy: sample rate in test set is classified correctly.

$$accuracy = \frac{TP + TN}{P + N}$$

◎ Example:

- accuracy = (6954 + 2588)/ 10000 = 0.95

| Actual class\Predicted class | buy_computer = yes | buy_computer = no | Total |
|------------------------------|--------------------|-------------------|-------|
| buy_computer = yes           | <b>6954</b>        | <b>46</b>         | 7000  |
| buy_computer = no            | <b>412</b>         | <b>2588</b>       | 3000  |
| Total                        | 7366               | 2634              | 10000 |

# Error Rate

- ◎ Error Rate: The sample rate was incorrectly classified in the test set (= 1 - accuracy)

$$\text{error rate} = \frac{FP + FN}{P + N}$$

- ◎ Example:

- error rate = (412 + 46)/ 10000 = 0.05

| Actual class\Predicted class | buy_computer = yes | buy_computer = no | Total |
|------------------------------|--------------------|-------------------|-------|
| buy_computer = yes           | <b>6954</b>        | <b>46</b>         | 7000  |
| buy_computer = no            | <b>412</b>         | <b>2588</b>       | 3000  |
| Total                        | 7366               | 2634              | 10000 |



# Class imbalance (1/2)

◎ Classes of interest can be rare compared to other classes

◎ Example:

- In the phishing detection application, the class of interest is "fraud" but occurs much less than those of the class "Nonfraudulant".
- In diagnosis, the class of interest is "cancer", the sample rate is labeled "yes" much lower than the label "no".



## Class imbalance (2/2)

- ◎ Classifier is correct in negative samples but completely incorrect in positive samples
  - ◎ Example:
    - A classifier of accuracy 99% shows a very high probability of prediction. However, if the wrong 1% belongs to the positive sample, 99% becomes pointless
- Resolution by measure sensitivity and specificity

# Sensitivity và Specificity

- ◎ Sensitivity: correct positive sample recognition ratio

$$\text{sensitivity} = \frac{TP}{P}$$

- ◎ Specificity: correct negative sample recognition ratio

$$\text{specificity} = \frac{TN}{N}$$

## Sensitivity vs. Specificity

- ◎ The classifier has a high accuracy of 96.40%.
- ◎ However, the ability to identify positive samples is quite low because of low sensitivity.

| <i>Classes</i> | <i>yes</i> | <i>no</i>   | <i>Total</i>  | <i>Recognition (%)</i> |
|----------------|------------|-------------|---------------|------------------------|
| <i>yes</i>     | <b>90</b>  | <b>210</b>  | 300           | 30.00                  |
| <i>no</i>      | <b>140</b> | <b>9560</b> | 9700          | 98.56                  |
| <b>Total</b>   | <b>230</b> | <b>9770</b> | <b>10,000</b> | <b>96.40</b>           |

## Precision vs. Recall

Google → Trả 10 kg, 6 tấn cà, 50 kg  
↓  
có 5 tấn đậu.

- ◎ Precision: is the proportion of the class that assigns a label to positive is actually positive.

$$precision = \frac{TP}{TP + FP} = \frac{5}{5 + 5} = \frac{1}{2}$$

- ◎ Recall: is the positive sample rate assigned by the classifier.

$$recall = \frac{TP}{TP + FN} = \frac{TP}{P} = \frac{5}{50} = \frac{1}{10}$$

# Precision and Recall

◎ Precision(yes) =  $90/230 = 39.13\%$

◎ Recall(yes) =  $90/300 = 30.00\%$

| <i>Classes</i> | <i>yes</i> | <i>no</i>   | <i>Total</i> |
|----------------|------------|-------------|--------------|
| <i>yes</i>     | <b>90</b>  | <b>210</b>  | 300          |
| <i>no</i>      | <b>140</b> | <b>9560</b> | 9700         |
| Total          | 230        | 9770        | 10,000       |

# Precision and Recall

## ◎ Highest precision is 1.0:

- Showing each sample that the marking class belongs to the positive is actually positive.
- Unable to show the number of positive samples is classified incorrectly

## ◎ Highest recall is 1.0:

- Showing all positive samples is labeled properly.
- Unable to present how many other samples are mislabeled in the positive.

# F-Score

- ◎ F-score: A combination of precision and recall

$$F = \frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$$

$\beta = 1$   
Cân bằng 2  
hàng này

- ◎ F-score is harmonic mean between precision and recall
- ◎ Equally weighted between precision and recall ( $\beta=1$ )
- ◎ If you want to one over another, you can set  $\beta=2$ ,  $\beta=0.5$

$$F_{\beta} = \frac{(1 + \beta^2) \times \text{precision} \times \text{recall}}{\beta^2 \times \text{precision} + \text{recall}}$$



# Example

| classes            | buy_computer =<br>yes | buy_computer =<br>no | total | recognition(%) |
|--------------------|-----------------------|----------------------|-------|----------------|
| buy_computer = yes | 6954                  | 46                   | 7000  | 99.34          |
| buy_computer = no  | 412                   | 2588                 | 3000  | 86.27          |
| total              | 7366                  | 2634                 | 10000 | 95.42          |

**F-measure(B-Yes)= 96.81%**

# Summary of the measurements

| A\P | C  | ¬C |     |
|-----|----|----|-----|
| C   | TP | FN | P   |
| ¬C  | FP | TN | N   |
|     | P' | N' | All |

| Measure                                                         | Formula                                                                                                              |
|-----------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------|
| accuracy, recognition rate                                      | $\frac{TP + TN}{P + N}$                                                                                              |
| error rate, misclassification rate                              | $\frac{FP + FN}{P + N}$                                                                                              |
| sensitivity, true positive rate, recall                         | $\frac{TP}{P}$                                                                                                       |
| specificity, true negative rate                                 | $\frac{TN}{N}$                                                                                                       |
| precision                                                       | $\frac{TP}{TP + FP}$                                                                                                 |
| $F$ , $F_1$ , $F$ -score, harmonic mean of precision and recall | $\frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$                            |
| $F_\beta$ , where $\beta$ is a non-negative real number         | $\frac{(1 + \beta^2) \times \text{precision} \times \text{recall}}{\beta^2 \times \text{precision} + \text{recall}}$ |

## Exercise 3

- ◎ Data relating to the customer classification is deceptive or non-deceptive by a bank before lending:

|               |                      | <i>Predict</i>   |                      |              |
|---------------|----------------------|------------------|----------------------|--------------|
| <i>Actual</i> | <b>Class</b>         | <b>Deceptive</b> | <b>Non-deceptive</b> | <b>Total</b> |
|               | <b>Deceptive</b>     | 44               | 15                   | 59           |
|               | <b>Non-deceptive</b> | 20               | 146                  | 166          |
|               | <b>Tổng</b>          | 64               | 161                  | 225          |

- ◎ Suppose the class of interest is deceptive, create confusion matrix
- ◎ Calculating the measurements accuracy, error rate, sensitivity, specificity, precision, F-Score

$$- \text{Accuracy: } \frac{44 + 116}{225} = \checkmark$$

$$- \text{Error rat} = \frac{20 + 15}{225} \checkmark$$

$$- \text{Sensitivity} = \frac{44}{59} \checkmark$$

$$- \text{specificity} = \frac{116}{166} \checkmark$$

$$\text{precision} = \frac{44}{64} \quad 68,75$$

$$\text{recall} = \frac{44}{59} \quad 0,75$$

$$F_{\text{score}} = 0,72$$

# Estimation methods



# Reliability when estimating

- ◎ Whether the figures are calculated from the measurements that are reliable?
    - Depends on the type of data
    - Depend on how the data is collected
    - Depends on how to divide data into training and test episodes.
    - ...
- Method is required to reliably estimate the accuracy

# Holdout Method

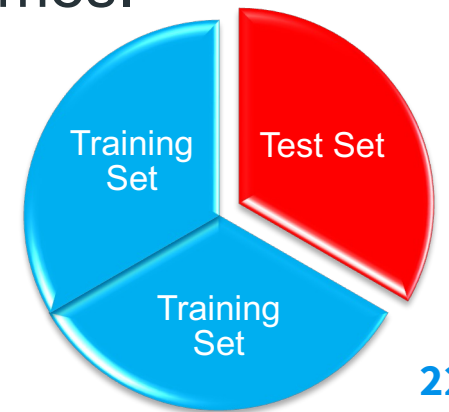
◎ Data is randomly divided into 2 independent sections

- Training set up 2/3 to draw the model
- Test set accounted for 1/3 to estimate accuracy

→ Samples may not represent all data, missing class in the experiment set

◎ Random sampling: is the variant of holdout

- Repeat holdout k times, the accuracy is the average of all times.



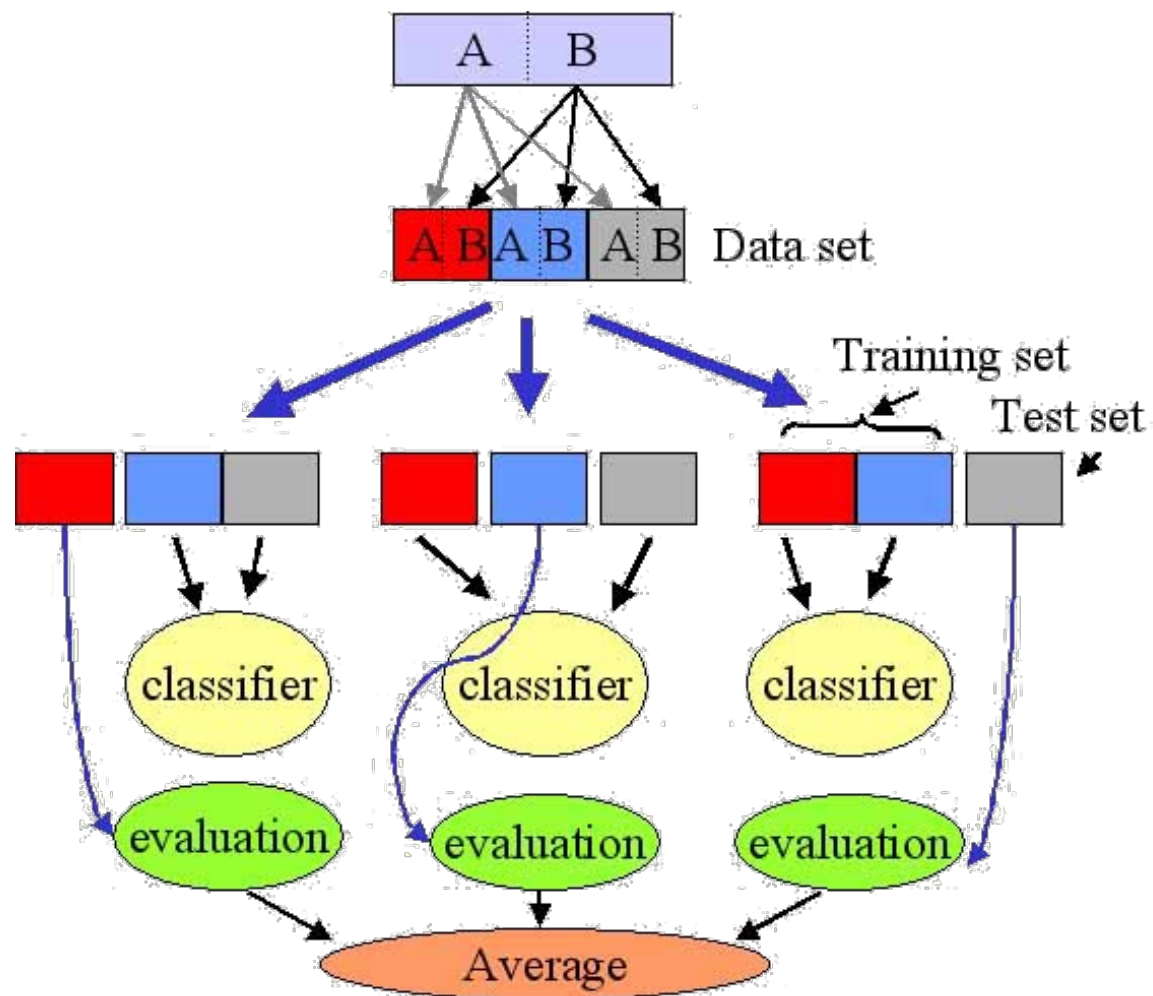
# K-fold Cross-Validation

- ◎ Randomly divide the data into K-independent and roughly equal size.  $D=\{D1, D2, \dots, Dk\}$ 
  - Perform k evaluation.
  - For the time i, the  $D_i$  episode was used as a test, the rest of the training
  - $K = 10$  commonly used
- ◎ Leave-one-out: is k fold with K is the number of samples (only applies when the data size is small)
- ◎ Stratified cross-validation: Distributing the classes of samples in each fold is roughly the same as the original data



# K-fold Cross-Validation


Học được hết dữ liệu



# Bootstrap cho dữ liệu quá nhỏ

- ◎ Usually apply to small datasets
- ◎ Each time a sample is selected, it is likely to be picked again and added to the training set
- ◎ There are a few bootstrap methods, which are common **.632 Bootstrap**
  - The d-size dataset will be sampled Bootstrap d times. So training set has d samples. Samples that do not include the training will be used to test. About 63.2% of data fall into training assignments and 36.8% for test episodes (because according to probability  $(1-1/d)^d \approx e^{-1} = 0.368$ )
  - Repeats the sampling k times and the accuracy:

$$Acc(M) = \frac{1}{k} \sum_{i=1}^k (0.632 \times Acc(M_i)_{test\_set} + 0.368 \times Acc(M_i)_{train\_set})$$



*The End*

90p, sd t̄a līn gīa' - BT :

- th̄a' k̄e'
- Tīn x̄i ly'
- Visualiz̄e
- Linear, quy tr̄inh
- M̄a n̄ r̄a n