Span

Given vectors $\vec{v_1}, \vec{v_2}, \dots, \vec{v_p} \in \mathbb{R}^n$. The set of all linear combinations of $\vec{v_1}, \vec{v_2}, \dots, \vec{v_p}$ is called the **span** of $\vec{v_1}, \vec{v_2}, \dots, \vec{v_p}$.

Thus, $span\{\vec{v_1}, \vec{v_2}, \dots, \vec{v_p}\}$ can be represented like this:

$$c_1\vec{v_1}, c_2\vec{v_2}, \ldots, c_p\vec{v_p}$$

Where c_1, c_2, \ldots, c_p are scalars.

Is \vec{y} in the span of vectors \vec{v}_1 and \vec{v}_2 ?

$$ec{v}_1=egin{pmatrix}1\-2\-3\end{pmatrix}$$
 , $ec{v}_2=egin{pmatrix}2\5\6\end{pmatrix}$, and $ec{y}=egin{pmatrix}7\4\15\end{pmatrix}$.

$$c_1egin{bmatrix}1\-2\-3\end{bmatrix}+c_2egin{bmatrix}2\5\6\end{bmatrix}=egin{bmatrix}7\4\15\end{bmatrix}$$

$$egin{bmatrix} c_1 \ -2c_1 \ -3c_1 \end{bmatrix} + egin{bmatrix} 2c_2 \ 5c_2 \ 6c_2 \end{bmatrix} = egin{bmatrix} 7 \ 4 \ 15 \end{bmatrix}$$

$$\begin{pmatrix} 1 & 2 & 7 \\ -2 & 5 & 4 \\ -3 & 6 & 15 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 2 & 7 \\ -2 & 5 & 4 \\ -1 & 2 & 5 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 2 & 7 \\ 0 & 1 & -6 \\ -1 & 2 & 5 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 2 & 7 \\ 0 & 1 & -6 \\ 0 & 1 & 3 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 19 \\ 0 & 1 & -6 \\ 0 & 1 & 3 \end{pmatrix}$$

$$\begin{pmatrix}
1 & 0 & 19 \\
0 & 1 & -6 \\
0 & 0 & 9
\end{pmatrix}$$

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$$\begin{pmatrix} 1 & 0 & 19 \\ 0 & 1 & -6 \\ 0 & 0 & 1 \end{pmatrix}$$

So y is not in span $\{\vec{v_1}, \vec{v_2}\}$ Look at Row Operations