## **Vocabulary**

Word	Meaning
Consistent	If it has at least one solution.
Row equivalent	If a sequence of row operations transforms one matrix into the other.
Unique solution	If and only if there are no free variables
Homogeneous	Linear systems of the form $A\mathbf{x}=0$
Inhomogeneous	Linear systems of the form $A\mathbf{x}=\mathbf{b}$ where $\mathbf{b}  eq 0$
Trivial solution	The solution is the zero vector
Linearly independent	If no vector can be made from other vectors
Row operations	Addition, Interchange, Scaling
Pivot position	A leading 1 in the RREF of A
Pivot column	Is a column of A that contains a pivot position
Domain	$T:\mathbb{R}^n o\mathbb{R}^m$ ; $\mathbb{R}^n$ is the domain of $T$
Codomain	$T:\mathbb{R}^n o\mathbb{R}^m$ ; $\mathbb{R}^m$ is the codomain of $T$
Image	The vector $T(\vec{x})$ is the image of $\vec{x}$ under $T$
Range	The set of all possible images $T(\vec{x})$ or simply the <b>span of A</b>
Standard vectors	The column of the identity matrix (think $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$ and $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ )
Onto	All the elements in the codomain are mapped to. (A spans the entire codomain), Every <b>row</b> is pivotal
One-To-One	Each mapping is unique (2 vectors can <b>NOT</b> map to the same vector), Every <b>column</b> is pivotal
Transpose	The matrix whose columns are the rows of $\boldsymbol{A}$
Invertible	$A \in \mathbb{R}^{n  imes n}$ is invertible if there is a $C \in \mathbb{R}^{n  imes n}$ such that: $AC = CA = I_n$
Elementary Matrix	Differs from $I_n$ by one row operation.
Singular	A matrix that is not invertible ( $A^{-1}$ DNE)
Subset	A subset of $\mathbb{R}^n$ any collection of vectors that are in $\mathbb{R}^n$
Subspace	If $H\in\mathbb{R}^n$ , for $c\in\mathbb{R}$ and $\vec{u},\vec{v}\in H$ , $c\vec{u}\in H$ and $\vec{u}+\vec{v}\in H$ must be true if $H$ is a subspace.
Column Space	This is a subspace spanned by the column of $A$ .

Word	Meaning
Null Space	This is a subspace spanned by all $ec{x}$ such that $Aec{x}=ec{0}$ .