Basis

Refer to <u>Vocabulary</u> for definitions.

Say we wish to find the basis for $H=\left\{\vec{x}\in\mathbb{R}^4|x_1-3x_2-5x_3+7x_4=0\right\}$ (Note: this is <u>set builder notation</u>)

We must:

- 1. Convert this into a $A\vec{x}=0$ form
- 2. Convert this into Parametric Vector Form
- 3. Profit???

$$Aec{x} = 0$$

$$[1 \quad -3 \quad -5 \quad 7] egin{bmatrix} x_1 \ x_2 \ x_3 \ x_4 \end{bmatrix} = 0$$

$$\begin{bmatrix} 3x_2 + 5x_3 - 7x_4 \ x_2 \ x_3 \ x_4 \end{bmatrix} = 0$$

$$x_2 \begin{bmatrix} 3 \ 1 \ 0 \ 0 \end{bmatrix} + x_3 \begin{bmatrix} 5 \ 0 \ 1 \ 0 \end{bmatrix} + x_4 \begin{bmatrix} -7 \ 0 \ 0 \ 1 \end{bmatrix} = 0$$
 The basis of $H = \begin{bmatrix} \begin{bmatrix} 3 \ 1 \ 0 \ 0 \end{bmatrix}, \begin{bmatrix} 5 \ 0 \ 1 \ 0 \end{bmatrix}, \begin{bmatrix} -7 \ 0 \ 0 \ 1 \end{bmatrix}$

The basis of H also happens to be the null space in this case due to the equation being $x_1 - 3x_2 - 5x_3 + 7x_4 = 0$.