Linear Combinations

Given vectors $\mathbf{v_1}, \mathbf{v_2}, \dots, \mathbf{v_p} \in \mathbb{R}^n$, and scalars c_1, c_2, \dots, c_p , the vector \mathbf{y} where

$$\mathbf{y} = c_1 \mathbf{v_1} + c_2 \mathbf{v_2} + \ldots + c_p \mathbf{v_p}$$

is called a linear combination of $\mathbf{v_1}, \mathbf{v_2}, \dots, \mathbf{v_p}$ with the weights c_1, c_2, \dots, c_p . This is also called a vector equation.

$$c_1 - c_2 = 1$$

 $c_1 + c_2 = 3$
 $0c_1 + 0c_2 = 1$

We need c_1 and c_2 such that:

$$c_1 egin{bmatrix} 1 \ 1 \end{bmatrix} + c_2 egin{bmatrix} -1 \ 1 \end{bmatrix} = egin{bmatrix} 1 \ 3 \end{bmatrix}$$

So,

$$egin{bmatrix} c_1 \ c_1 \end{bmatrix} + egin{bmatrix} -c_2 \ c_2 \end{bmatrix} = egin{bmatrix} 1 \ 3 \end{bmatrix}$$

So finally,

$$c_1-c_2=1$$

$$c_1+c_2=3$$

Same question, can ${\bf y}$ be represented as a linear combination of ${\bf v}_1 \ {\rm and} \ {\bf v}_2$:

$$c_1 \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} + c_2 \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \\ 1 \end{pmatrix}$$

$$c_1 - c_2 = 1$$
$$c_1 + c_2 = 3$$
$$0c_1 + 0c_2 = 1$$

Thus, the system is **inconsistent** (no consistent).