## **Consistent Systems**

## **Augmented Matrices**

This:

$$\left\{egin{array}{l} x_1-2x_2+x_3=0 \ 2x_2-8x_3=7 \end{array}
ight.$$

Becomes:

$$\begin{pmatrix} 1 & -2 & 1 & 0 \\ 0 & 2 & -8 & 7 \end{pmatrix}$$

A linear system is consistent if it has at least one solution.

Two matrices are **row equivalent** if a sequence of row operations transforms one matrix into the other.

Suppose

$$A = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}, \quad B = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \quad C = \begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix}, \quad \vec{b} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

A and B are row equivalent

A and C are not row equivalent

Are the augmented matrices  $(A \,|\: \vec{b})$  and  $(C \,|\: \vec{b})$  consistent?

$$\begin{pmatrix} A \mid \vec{b} \end{pmatrix} = \begin{pmatrix} 1 & 1 \mid 1 \\ 0 & 1 \mid 1 \end{pmatrix}$$

$$\left(A \mid \vec{b}\right) = \begin{pmatrix} 1 & 0 \mid 0 \\ 0 & 1 \mid 1 \end{pmatrix}$$

So A and  $\vec{b}$  are consistent.

A and C are not consistent.