

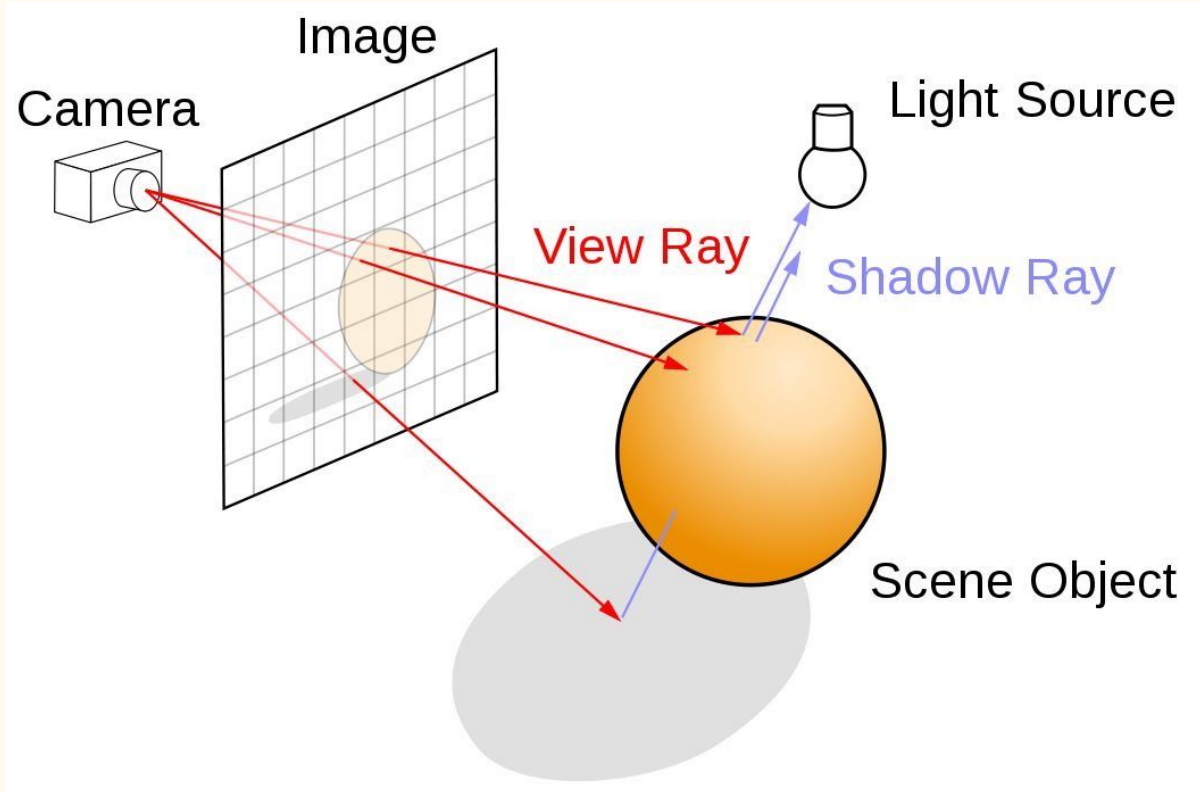
# IG3DA - Final presentation

## Comparison of BVH construction methods

---

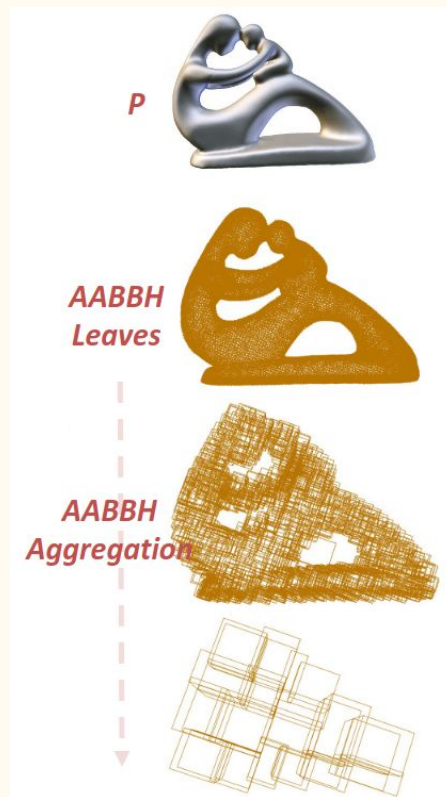
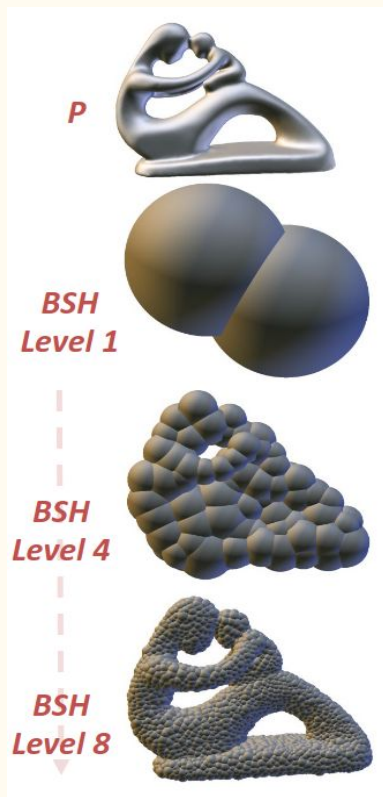
Kedadry Yannis

# Quick recap on RayTracing



# BVH Construction

Top-Down

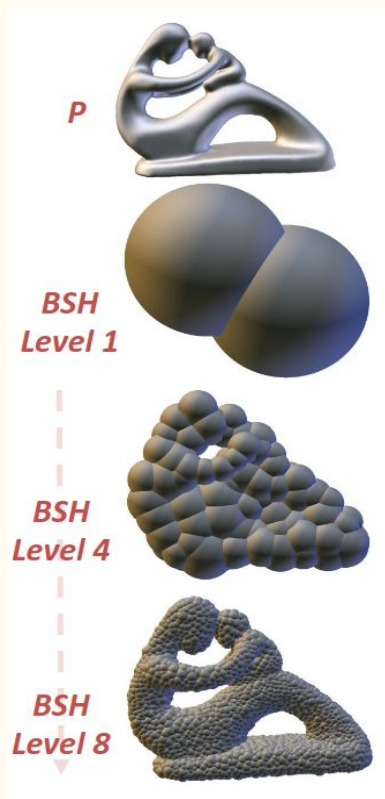


Bottom-Up



# Top Down approach:

Top-Down



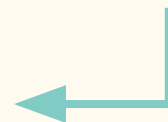
AABBH  
Leaves



AABBH  
Aggregation



Bottom-Up



# Surface Area Heuristic:

$$\text{Total SAH of a BVH} = C_i \sum_{n \in I} \frac{A(n)}{A(\text{root})} + C_l \sum_{n \in L} \frac{A(n)}{A(\text{root})} + C_t \sum_{n \in L} \frac{A(n)}{A(\text{root})} N(n)$$

$A$  - Surface Area of a node's bounding box

$I$  - Internal nodes

$L$  - Leaf node

$N$  - Number of triangles in a node

$C_i$  - Cost of traversing an internal node

$C_l$  - Cost of traversing a leaf node

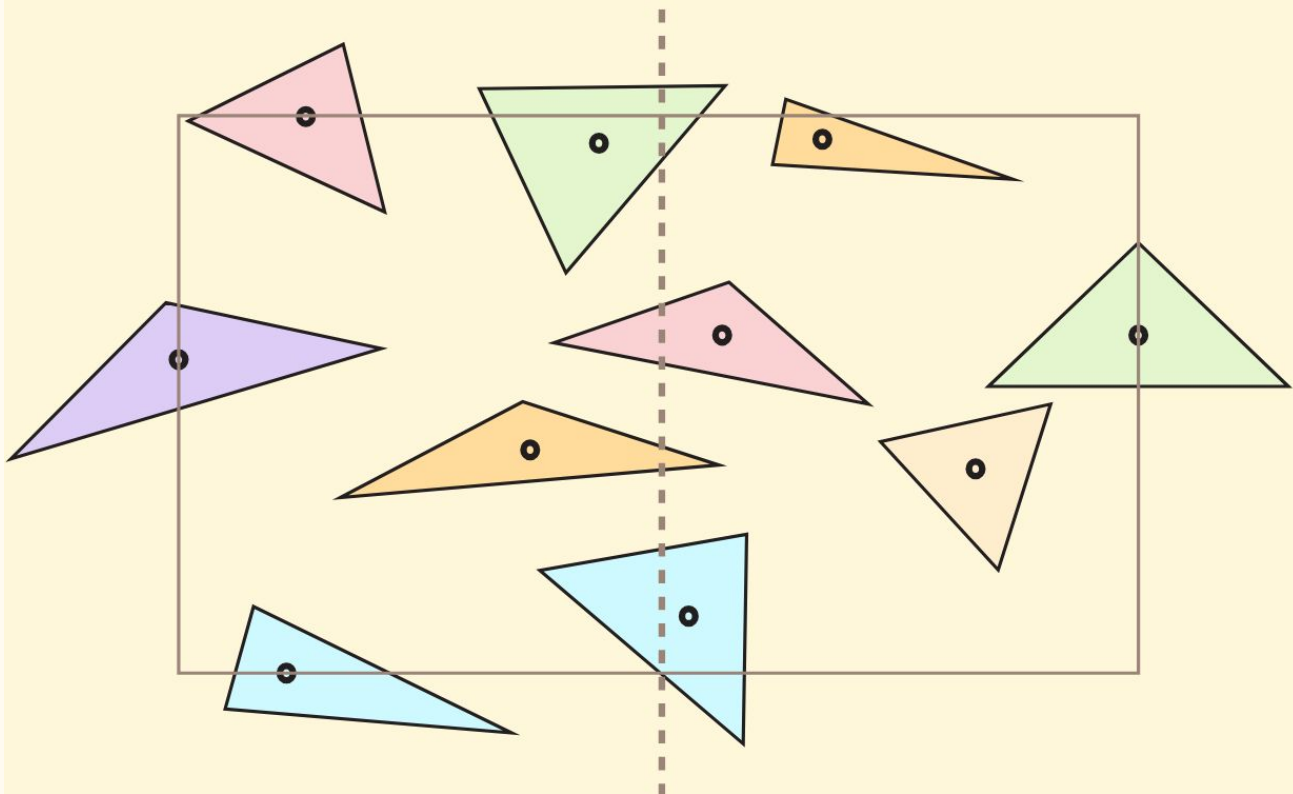
$C_t$  - Cost of intersecting a triangle

To optimize a top-down BVH:

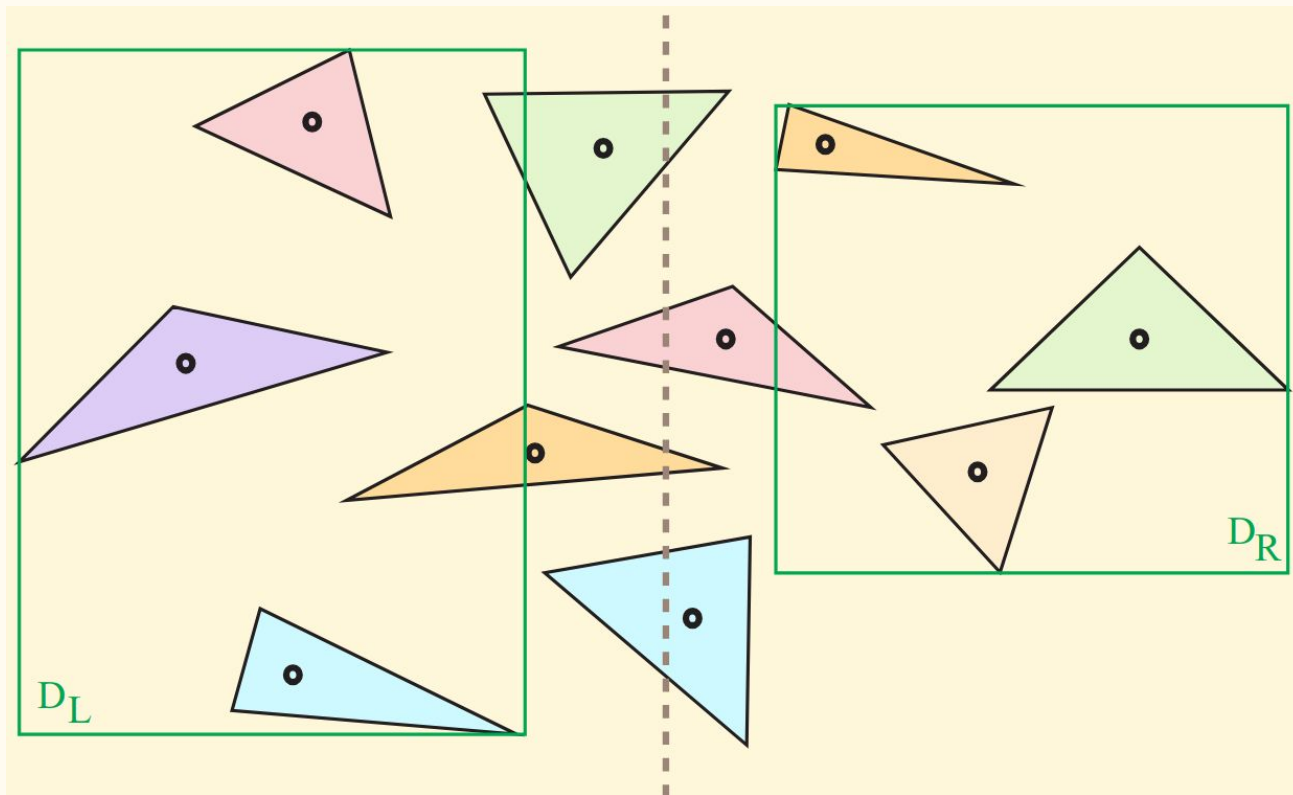
$$E_r = C_i A(n) + C_l (A(n_l) N(n_l)) + A(n_r) N(n_r),$$

$$E_t = C_t A(n) N(n),$$

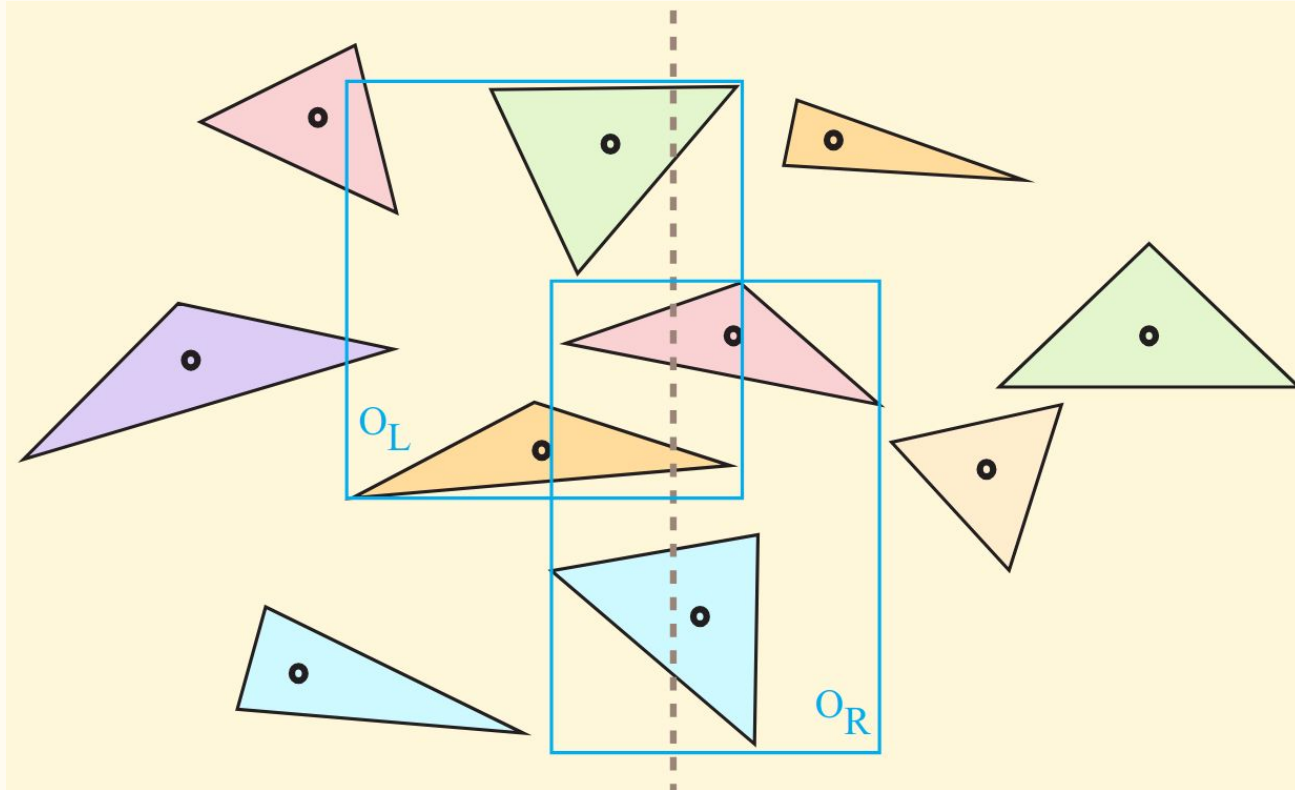
# SAH Guided Mid-Point Split Partitioning :



# SAH Guided Mid-Point Split Partitioning :

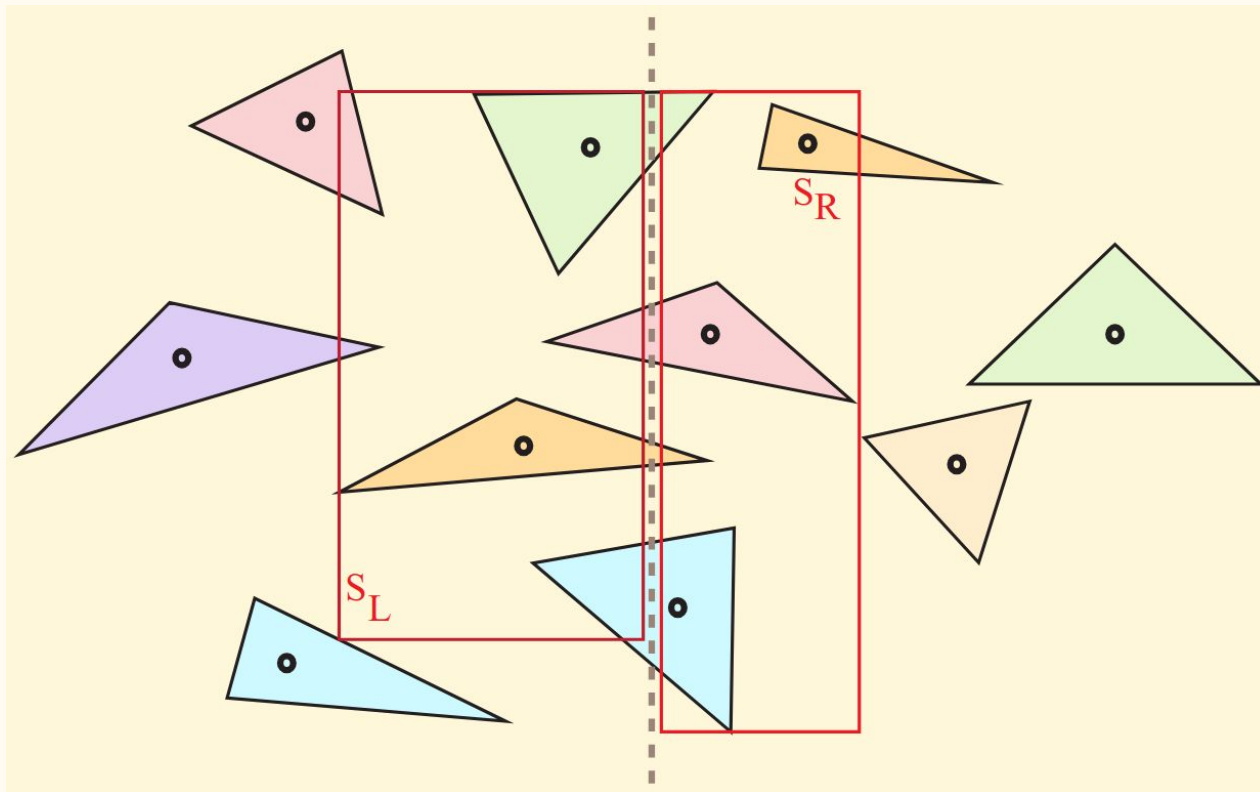


# SAH Guided Mid-Point Split Partitioning :





# SAH Guided Mid-Point Split Partitioning :



# SAH Guided Mid-Point Split Partitioning :

SAH cost of keeping  
the overlap sets

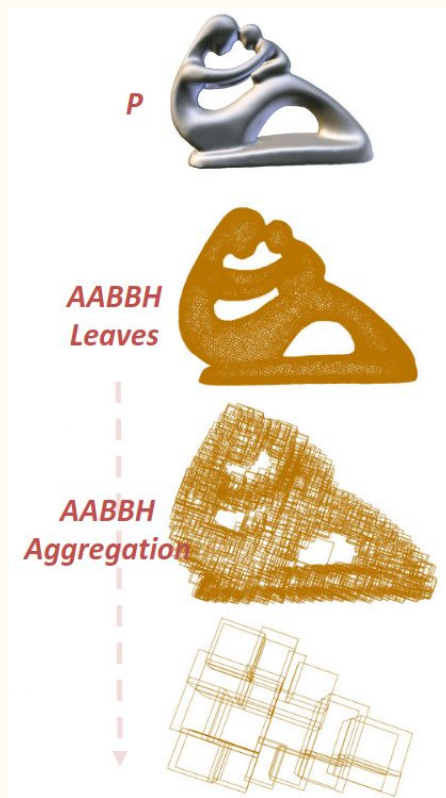
$$C_O = A(D_L \cup O_L)|D_L \cup O_L| + A(D_R \cup O_R)|D_R \cup O_R|$$

SAH cost of using  
the split sets

$$C_S = A(D_L \cup S_L)|D_L \cup S_L| + A(D_R \cup S_R)|D_R \cup S_R|,$$

# Bottom Up approach:

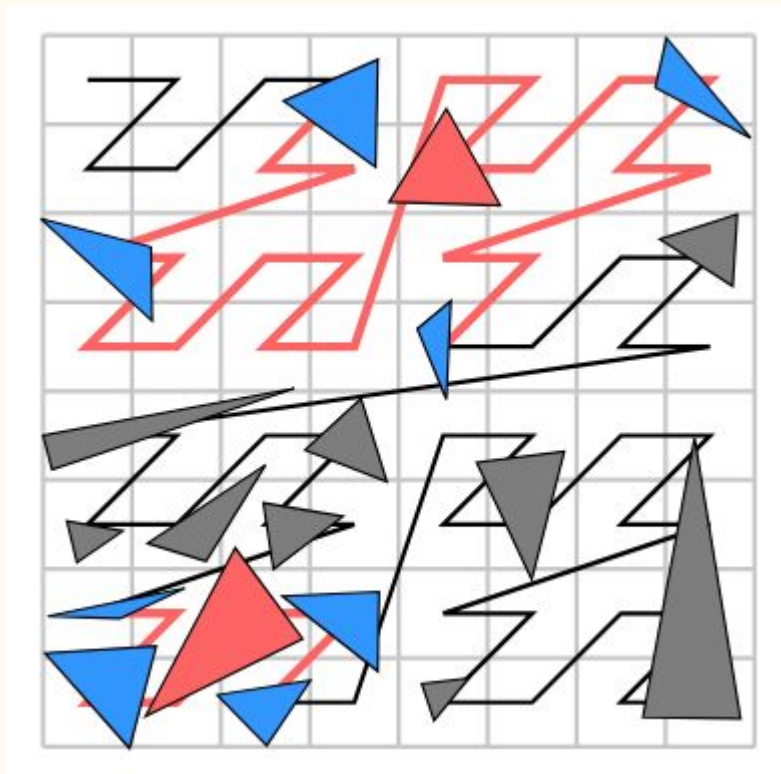
Top-Down



Bottom-Up



# Ploc algorithm:

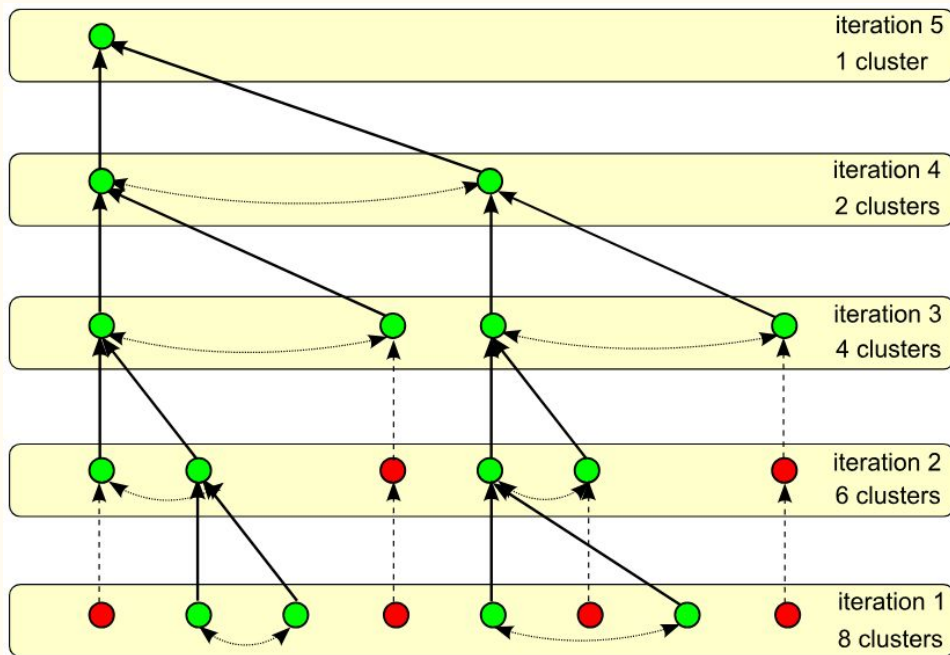


```

1:  $\mathcal{C}_{in} \leftarrow \mathcal{C}_{out} \leftarrow [C_0, C_1 \dots, C_{n-1}]$ 
2:  $\mathcal{N} \leftarrow \mathcal{P} \leftarrow [0, 1 \dots, n-1]$ 
3:  $c \leftarrow n$ 
4: while  $c > 1$  do
5:   for  $i \leftarrow 0$  to  $c-1$  in parallel do
6:     /* NEAREST NEIGHBOR SEARCH */
7:      $d_{min} \leftarrow \infty$ 
8:     for  $j \leftarrow \max(i-r, 0)$  to  $\min(i+r, c-1)$  do
9:       if  $i \neq j \wedge d_{min} > d(\mathcal{C}_{in}[i], \mathcal{C}_{in}[j])$  then
10:         $d_{min} \leftarrow d(\mathcal{C}_{in}[i], \mathcal{C}_{in}[j])$ 
11:         $\mathcal{N}[i] \leftarrow j$ 
12:      end if
13:    end for
14:    BARRIER()
15:    /* MERGING */
16:    if  $\mathcal{N}[\mathcal{N}[i]] = i \wedge i < \mathcal{N}[i]$  then
17:       $\mathcal{C}_{in}[i] \leftarrow \text{CLUSTER}(\mathcal{C}_{in}[i], \mathcal{C}_{in}[\mathcal{N}[i]])$ 
18:       $\mathcal{C}_{in}[\mathcal{N}[i]] \leftarrow \clubsuit$ 
19:    end if
20:    BARRIER()
21:    /* COMPACTION */
22:     $\mathcal{P}[i] \leftarrow \text{PREFIXSCAN}(\mathcal{C}_{in}[i] \neq \clubsuit)$ 
23:    if  $\mathcal{C}_{in}[i] \neq \clubsuit$  then
24:       $\mathcal{C}_{out}[\mathcal{P}[i]] \leftarrow \mathcal{C}_{in}[i]$ 
25:    end if
26:    BARRIER()
27:  end for
28:   $c \leftarrow \mathcal{P}[c-1]$ 
29:  if  $\mathcal{C}_{in}[c-1] \neq \clubsuit$  then
30:     $c \leftarrow c+1$ 
31:  end if
32:  SWAP( $\mathcal{C}_{in}, \mathcal{C}_{out}$ )
33: end while

```

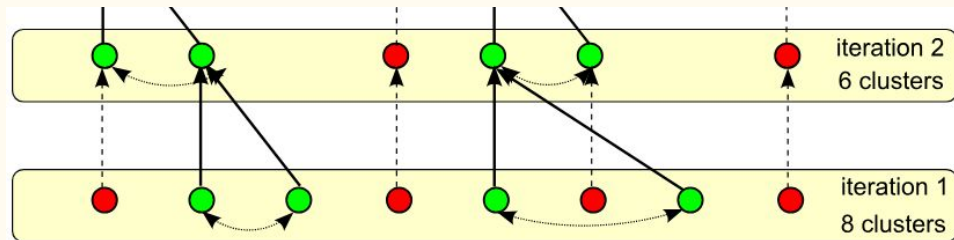
# Ploc algorithm:



```

1:  $\mathcal{C}_{in} \leftarrow \mathcal{C}_{out} \leftarrow [C_0, C_1, \dots, C_{n-1}]$ 
2:  $\mathcal{N} \leftarrow \mathcal{P} \leftarrow [0, 1, \dots, n-1]$ 
3:  $c \leftarrow n$ 
4: while  $c > 1$  do
5:   for  $i \leftarrow 0$  to  $c-1$  in parallel do
6:     /* NEAREST NEIGHBOR SEARCH */
7:      $d_{min} \leftarrow \infty$ 
8:     for  $j \leftarrow \max(i-r, 0)$  to  $\min(i+r, c-1)$  do
9:       if  $i \neq j \wedge d_{min} > d(\mathcal{C}_{in}[i], \mathcal{C}_{in}[j])$  then
10:         $d_{min} \leftarrow d(\mathcal{C}_{in}[i], \mathcal{C}_{in}[j])$ 
11:         $\mathcal{N}[i] \leftarrow j$ 
12:      end if
13:    end for
14:    BARRIER()
15:    /* MERGING */
16:    if  $\mathcal{N}[\mathcal{N}[i]] = i \wedge i < \mathcal{N}[i]$  then
17:       $\mathcal{C}_{in}[i] \leftarrow \text{CLUSTER}(\mathcal{C}_{in}[i], \mathcal{C}_{in}[\mathcal{N}[i]])$ 
18:       $\mathcal{C}_{in}[\mathcal{N}[i]] \leftarrow \clubsuit$ 
19:    end if
20:    BARRIER()
21:    /* COMPACTION */
22:     $\mathcal{P}[i] \leftarrow \text{PREFIXSCAN}(\mathcal{C}_{in}[i] \neq \clubsuit)$ 
23:    if  $\mathcal{C}_{in}[i] \neq \clubsuit$  then
24:       $\mathcal{C}_{out}[\mathcal{P}[i]] \leftarrow \mathcal{C}_{in}[i]$ 
25:    end if
26:    BARRIER()
27:  end for
28:   $c \leftarrow \mathcal{P}[c-1]$ 
29:  if  $\mathcal{C}_{in}[c-1] \neq \clubsuit$  then
30:     $c \leftarrow c+1$ 
31:  end if
32:  SWAP( $\mathcal{C}_{in}, \mathcal{C}_{out}$ )
33: end while
  
```

# Ploc algorithm:



$C_{in}$	0	1	2	3	4	5	6	7
NewC	0	1	0	0	1	0	0	0
P	0	0	1	1	1	2	2	2
$C_{in}$	0	8+0	♣	3	8+1	5	♣	7
$C_{in}$	1	1	0	1	1	1	0	1
$\neq \clubsuit$ P	0	1	2	2	3	4	5	5
$C_{out}$	0	8	3	9	5	7	X	X

```

1:  $C_{in} \leftarrow C_{out} \leftarrow [C_0, C_1, \dots, C_{n-1}]$ 
2:  $\mathcal{N} \leftarrow \mathcal{P} \leftarrow [0, 1, \dots, n-1]$ 
3:  $c \leftarrow n$ 
4: while  $c > 1$  do
5:   for  $i \leftarrow 0$  to  $c-1$  in parallel do
6:     /* NEAREST NEIGHBOR SEARCH */
7:      $d_{min} \leftarrow \infty$ 
8:     for  $j \leftarrow \max(i-r, 0)$  to  $\min(i+r, c-1)$  do
9:       if  $i \neq j \wedge d_{min} > d(C_{in}[i], C_{in}[j])$  then
10:         $d_{min} \leftarrow d(C_{in}[i], C_{in}[j])$ 
11:         $\mathcal{N}[i] \leftarrow j$ 
12:      end if
13:    end for
14:    BARRIER()
15:    /* MERGING */
16:    if  $\mathcal{N}[\mathcal{N}[i]] = i \wedge i < \mathcal{N}[i]$  then
17:       $C_{in}[i] \leftarrow \text{CLUSTER}(C_{in}[i], C_{in}[\mathcal{N}[i]])$ 
18:       $C_{in}[\mathcal{N}[i]] \leftarrow \clubsuit$ 
19:    end if
20:    BARRIER()
21:    /* COMPACTION */
22:     $\mathcal{P}[i] \leftarrow \text{PREFIXSCAN}(C_{in}[i] \neq \clubsuit)$ 
23:    if  $C_{in}[i] \neq \clubsuit$  then
24:       $C_{out}[\mathcal{P}[i]] \leftarrow C_{in}[i]$ 
25:    end if
26:    BARRIER()
27:  end for
28:   $c \leftarrow \mathcal{P}[c-1]$ 
29:  if  $C_{in}[c-1] \neq \clubsuit$  then
30:     $c \leftarrow c+1$ 
31:  end if
32:  SWAP( $C_{in}, C_{out}$ )
33: end while

```

# Implementation details:



A royalty-free  
open standard from: **KHRONOS**  
GROUP Visit us at:  
[www.khronos.org](http://www.khronos.org)





# Results:

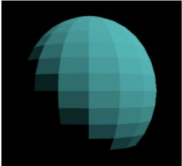



Scene	Triangles	BVH Construction Method	Time to Build (s)	Average FPS	Average Time Per Frame (ms)
	$\approx 500$	None	0	10	99.81
		Baseline Top-Down	<b>0.00285</b>	<b>60</b>	16.67
		Baseline Bottom-Up	0.00300	<b>60</b>	<b>16.65</b>
		SAH Guided Top-Down	0.00888	<b>60</b>	16.66
		PLOC	0.00486	<b>60</b>	16.66
		CPU Parallelized PLOC	0.02336	<b>60</b>	16.66
	$\approx 100,000$	None	0	X	X
		Baseline Top-Down	0.82288	54	18.41
		Baseline Bottom-Up	0.78625	58	17.25
		SAH Guided Top-Down	2.00633	56	17.70
		PLOC	1.27355	<b>60</b>	<b>16.67</b>
		CPU Parallelized PLOC	<b>0.61331</b>	<b>60</b>	<b>16.67</b>
	$\approx 1,000,000$	None	0	X	X
		Baseline Top-Down	10.74779	14	68.43
		Baseline Bottom-Up	10.70392	14	67.97
		SAH Guided Top-Down	26.89474	14	66.25
		PLOC	14.05147	<b>18</b>	<b>54.36</b>
		CPU Parallelized PLOC	<b>5.999515</b>	<b>18</b>	<b>54.36</b>
	$\approx 3,000,000$	None	0	X	X
		Baseline Top-Down	40.03281	11	85.4
		Baseline Bottom-Up	39.61821	20	51.0
		SAH Guided Top-Down	170.55518	20	50.68
		PLOC	45.59624	<b>24</b>	<b>40.39</b>
		CPU Parallelized PLOC	<b>19.17041</b>	<b>24</b>	<b>40.39</b>

TABLE I: Comparison of BVH Construction Methods (An *X* means *too slow to be measured*)



