

Maharashtra State Board 12th Physics Solutions Chapter 9 Current Electricity

1. Choose the correct option.

i) Kirchhoff's first law, i.e., $\Sigma I = 0$ at a junction, deals with the conservation of

- (A) charge
- (B) energy
- (C) momentum
- (D) mass

Answer:

- (A) charge

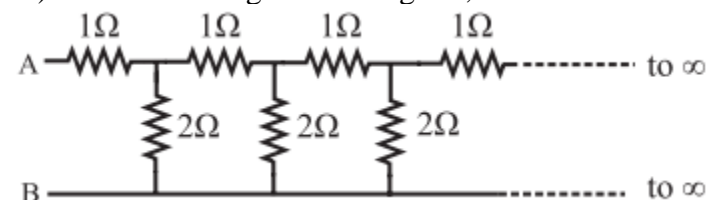
ii) When the balance point is obtained in the potentiometer, a current is drawn from

- (A) both the cells and auxiliary battery
- (B) cell only
- (C) auxiliary battery only
- (D) neither cell nor auxiliary battery

Answer:

- (D) neither cell nor auxiliary battery

iii) In the following circuit diagram, an infinite series of resistances is shown. Equivalent resistance between points A and B is



- (A) infinite
- (B) zero
- (C) 2Ω
- (D) 1.5Ω

Answer:

- (C) 2Ω

iv) Four resistances 10Ω , 10Ω , 10Ω and 15Ω form a Wheatstone's network. What shunt is required across 15Ω resistor to balance the bridge

- (A) 10Ω
- (B) 15Ω
- (C) 20Ω
- (D) 30Ω

Answer:

- (D) 30Ω

v) A circular loop has a resistance of 40Ω . Two points P and Q of the loop, which are one quarter of the circumference apart are connected to a 24 V battery, having an internal resistance of 0.5Ω . What is the current flowing through the battery.

- (A) 0.5 A
- (B) 1 A
- (C) 2 A
- (D) 3 A

Answer:

- (D) 3 A

vi) To find the resistance of a gold bangle, two diametrically opposite points of the bangle are connected to the two terminals of the left gap of a metre bridge. A resistance of 4Ω is introduced in the right gap. What is the resistance of the bangle if the null point is at 20 cm from the left end?

- (A) 2Ω
- (B) 4Ω
- (C) 8Ω
- (D) 16Ω

Answer:

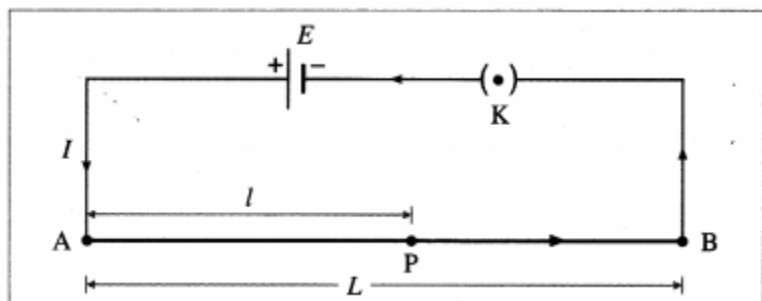
- (A) 2Ω

2. Answer in brief.

i) Define or describe a Potentiometer.

Answer:

The potentiometer is a device used for accurate measurement of potential difference as well as the emf of a cell. It does not draw any current from the circuit at the null point. Thus, it acts as an ideal voltmeter and it can be used to determine the internal resistance of a cell. It consists of a long uniform wire AB of length L , stretched on a wooden board. A cell of stable emf (E), with a plug key K in series, is connected across AB as shown in the following figure.



ii) Define Potential Gradient.

Answer:

Potential gradient is defined as the potential difference (the fall of potential from the high potential end) per unit length of the wire.

iii) Why should not the jockey be slid along the potentiometer wire?

Answer:

Sliding the jockey on the potentiometer wire decreases the cross sectional area of the wire and thereby affects the fall of potential along the wire. This affects the potentiometer readings. Hence, the jockey should not be slid along the potentiometer wire.

iv) Are Kirchhoff's laws applicable for both AC and DC currents?

Answer:

Kirchhoff's laws are applicable to both AC and DC circuits (networks). For AC circuits with different loads, (e.g. a combination of a resistor and a capacitor, the instantaneous values for current and voltage are considered for addition.

[Note : Gustav Robert Kirchhoff (1824-87), German physicist, devised laws of electrical network and, with Robert Wilhelm Bunsen, (1811-99), German chemist, did pioneering work in chemical spectroscopy. He also contributed to radiation.]

v) In a Wheatstone's meter-bridge experiment, the null point is obtained in middle one third portion of wire. Why is it recommended?

Answer:

1. The value of unknown resistance X , may not be accurate due to non-uniformity of the bridge wire and development of contact resistance at the ends of the wire.
2. To minimise these errors, the value of R is so adjusted that the null point is obtained in the middle one-third of the wire (between 34 cm and 66 cm) so that the percentage errors in the measurement of I_X and I_R are minimum and nearly the same.

vi) State any two sources of errors in meterbridge experiment. Explain how they can be minimized.

Answer:

The chief sources of error in the metre bridge experiment are as follows :

1. The bridge wire may not be uniform in cross section. Then the wire will not have a uniform resistance per unit length and hence its resistance will not be proportional to its length.
2. End resistances at the two ends of the wire may be introduced due to
 1. the resistance of the metal strips
 2. the contact resistance of the bridge wire with the metal strips
 3. unmeasured lengths of the wire at the ends because the contact points of the wire with the metal strips do not coincide with the two ends of the metre scale attached.

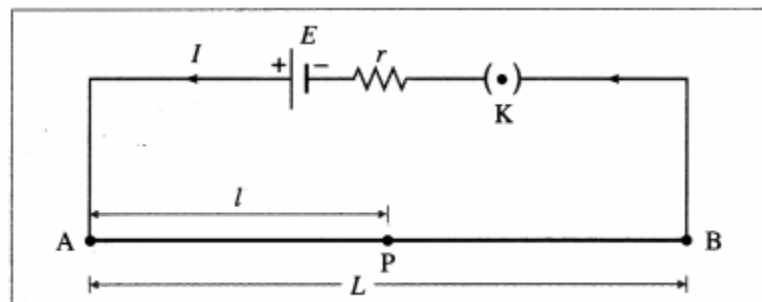
Such errors are almost unavoidable but can be minimized considerably as follows :

1. Readings must be taken by adjusting the standard known resistance such that the null point is obtained close to the centre of the wire. When several readings are to be taken, the null points should lie in the middle one-third of the wire.
2. The measurements must be repeated with the standard resistance (resistance box) and the unknown resistance interchanged in the gaps of the bridge, obtaining the averages of the two results.

vii) What is potential gradient? How is it measured? Explain.

Answer:

Consider a potentiometer consisting of a long uniform wire AB of length L and resistance R , stretched on a wooden board and connected in series with a cell of stable emf E and internal resistance r and a plug key K as shown in below figure.



Let I be the current flowing through the wire when the circuit is closed.

Current through AB, $I = \frac{E}{R+r}$

Potential difference across AB. $V_{AB} = IR$

$$\therefore V_{AB} = ER(R+r)$$

The potential difference (the fall of potential from the high potential end) per unit length of the wire,

$$V_{ABL} = ER(R+r)L$$

As long as E and r remain constant, V_{ABL} will remain constant, V_{ABL} is known as potential gradient along AB and is denoted by K. Thus the potential gradient is calculated by measuring the potential difference between ends of the potentiometer wire and dividing it by the length of the wire.

Let P be any point on the wire between A and B and $AP = l$ = length of the wire between A and P.

$$\text{Then } V_{AP} = Kl$$

$\therefore V_{AP} \propto l$ as K is constant in a particular case. Thus, the potential difference across any length of the potentiometer wire is directly proportional to that length. This is the principle of the potentiometer.

viii) On what factors does the potential gradient of the wire depend?

Answer:

The potential gradient depends upon the potential difference between the ends of the wire and the length of the wire.

ix) Why is potentiometer preferred over a voltmeter for measuring emf?

Answer:

A voltmeter should ideally have an infinite resistance so that it does not draw any current from the circuit. However a voltmeter cannot be designed to have infinite resistance. A potentiometer does not draw any current from the circuit at the null point. Therefore, it gives more accurate measurement. Thus, it acts as an ideal voltmeter.

x) State the uses of a potentiometer.

Answer:

The applications (uses) of the potentiometer :

1. Voltage divider :
The potentiometer can be used as a voltage divider to change the output voltage of a voltage supply.
2. Audio control:
Sliding potentiometers are commonly used in modern low-power audio systems as audio control devices. Both sliding (faders) and rotary potentiometers (knobs) are regularly used for frequency attenuation, loudness control and for controlling different characteristics of audio signals.
3. Potentiometer as a sensor:
If the slider of the potentiometer is connected to the moving part of a machine, it can work as a motion sensor. A small displacement of the moving part causes a change in potential which is further amplified using an amplifier circuit. The potential difference is calibrated in terms of displacement of the moving part.
4. To measure the emf (for this, the emf of the standard cell and potential gradient must be known).
5. To compare the emf's of two cells.
6. To determine the internal resistance of a cell.

xi) What are the disadvantages of a potentiometer?

Answer:

Disadvantages of a potentiometer over a voltmeter :

1. The use of a potentiometer is an indirect measurement method while a voltmeter is a direct reading instrument.
2. A potentiometer is unwieldy while a voltmeter is portable.
3. Unlike a voltmeter, the use of a potentiometer in measuring an unknown emf requires a standard . source of emf and calibration.

xii) Distinguish between a potentiometer and a voltmeter.

Answer:

Potentiometer	Voltmeter
1. A potentiometer is used to determine the emf of a cell, potential difference and internal resistance.	1. A voltmeter can be used to measure the potential difference and terminal voltage of a cell. But it cannot be used to measure the emf of a cell.
2. Its accuracy and sensitivity are very high.	2. Its accuracy and sensitivity are less as compared to a potentiometer.
3. It is not a portable instrument.	3. It is a portable instrument.
4. It does not give a direct reading.	4. It gives a direct reading.

xiii) What will be the effect on the position of zero deflection if only the current flowing through the potentiometer wire is

(i) increased (ii) decreased.

Answer:

(1) On increasing the current through the potentiometer wire, the potential gradient along the wire will increase. Hence, the position of zero deflection will occur at a shorter length.

(2) On decreasing the current through the potentiometer wire, the potential gradient along the wire will decrease. Hence, the position of zero deflection will occur at a longer length.

[Note : In the usual notation,

$$E_1 = (IRL) \quad I_1 = \text{constant}$$

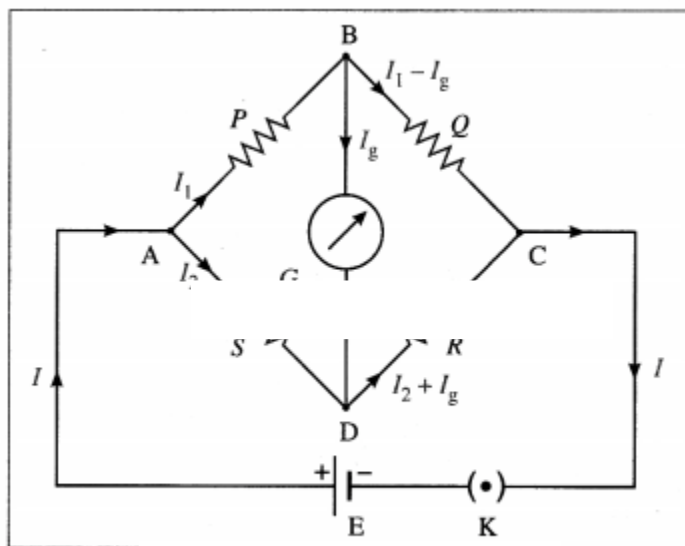
Hence, (i) E , decreases when I is increased (ii) I_1 increases when I is decreased.]

Question 3.

Obtain the balancing condition in case of a Wheatstone's network.

Answer:

Wheatstone's network or bridge is a circuit for indirect measurement of resistance by null comparison method by comparing it with a standard known resistance. It consists of four resistors with resistances P , Q , R and S arranged in the form of a quadrilateral $ABCD$. A cell (E) with a plug key (K) in series is connected across one diagonal AC and a galvanometer (G) across the other diagonal BD as shown in the following figure.



With the key K closed, currents pass through the resistors and the galvanometer. One or more of the resistances is adjusted until no deflection in the galvanometer can be detected. The bridge is then said to be balanced.

Let I be the current drawn from the cell. At junction A , it divides into a current I_1 through P and a current I_2 through S .

$I = I_1 + I_2$ (by Kirchhoff's first law).

At junction B , current I_g flows through the galvanometer and current $I_1 - I_g$ flows through Q . At junction D , I_2 and I_g combine. Hence, current $I_2 + I_g$ flows through R from D to C . At junction C , $I_1 - I_g$ and $I_2 + I_g$ combine. Hence, current $I_1 + I_2 (= I)$ leaves junction C .

Applying Kirchhoff's voltage law to loop $ABDA$ in a clockwise sense, we get,

$$-I_1P - I_gG + I_2S = 0 \quad \dots\dots\dots (1)$$

where G is the resistance of the galvanometer.

Applying Kirchhoff's voltage law to loop $BCDB$ in a clockwise sense, we get,

$$-(I_1 - I_g)Q + (I_2 + I_g)R + I_gG = 0 \quad \dots\dots\dots (2)$$

When $I_g = 0$, the bridge (network) is said to be balanced. In that case, from Eqs. (1) and (2), we get,

$$I_1P = I_2S \quad \dots\dots\dots (3)$$

$$\text{and } I_1Q = I_2R \quad \dots\dots\dots (4)$$

From Eqs. (3) and (4), we get,

$$PQ = SR$$

This is the condition of balance.

Alternative Method: When no current flows through the galvanometer, points B and D must be at the same potential.

$$\therefore V_B = V_D$$

$$\therefore V_A - V_B = V_A - V_D \quad \dots\dots\dots (1)$$

$$\text{and } V_B - V_C = V_D - V_C \quad \dots\dots\dots (2)$$

$$\text{Now, } V_A - V_B = I_1P \text{ and } V_A - V_D = I_2S \quad \dots\dots\dots (3)$$

$$\text{Also, } V_B - V_C = I_1Q \text{ and } V_D - V_C = I_2R \quad \dots\dots\dots (4)$$

Substituting Eqs. (3) and (4) in Eqs. (1) and (2), we get,

$$I_1P = I_2S \quad \dots\dots\dots (5)$$

$$\text{and } I_1Q = I_2R \quad \dots\dots\dots (6)$$

Dividing Eq. (5) by Eq. (6), we get,

$$PQ = SR$$

This is the condition of balance.

[Note : In the determination of an unknown resistance using Wheatstone's network, the unknown resistance is connected in one arm of the network (say, AB), and a standard known variable resistance is connected in an adjacent arm. Then, the other two arms are called the ratio arms. Also, because the positions of the cell and galvanometer can be interchanged, without a change in the condition of balance, the branches AC and BD in figure are called the conjugate arms.]

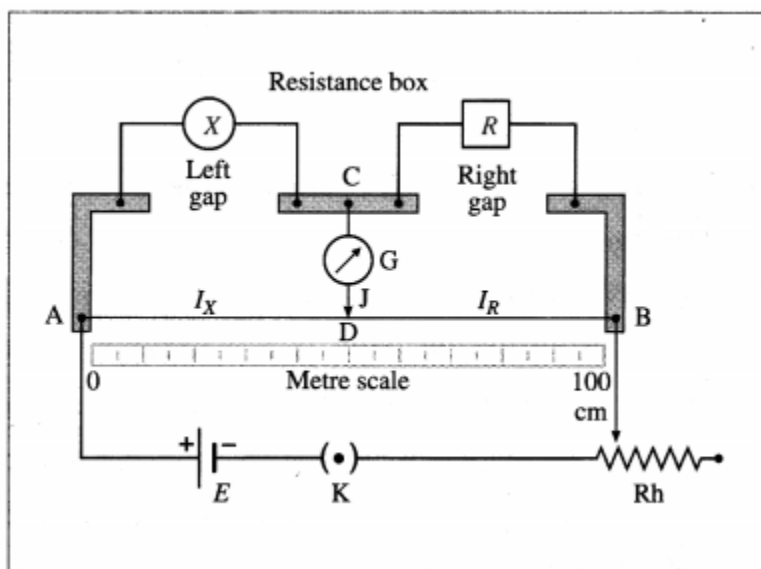
Question 4.

Explain with neat circuit diagram, how you will determine the unknown resistance by using a meter-bridge.

Answer:

A metre bridge consists of a rectangular wooden board with two L-shaped thick metallic strips fixed along its three edges. A single

thick metallic strip separates two L-shaped strips. A wire of length one metre and uniform cross section is stretched on a metre scale fixed on the wooden board. The ends of the wire are fixed to the L-shaped metallic strips.



An unknown resistance X is connected in the left gap and a resistance box R is connected in the right gap as shown in above figure. One end of a centre-zero galvanometer (G) is connected to terminal C and the other end is connected to a pencil jockey (J). A cell (E) of emf E , plug key (K) and rheostat (Rh) are connected in series between points A and B .

Working : Keeping a suitable resistance (R) in the resistance box, key K is closed to pass a current through the circuit. The jockey is tapped along the wire to locate the equipotential point D when the galvanometer shows zero deflection. The bridge is then balanced and point D is called the null point and the method is called as null deflection method. The distances l_X and l_R of the null point from the two ends of the wire are measured.

$$\frac{X}{R} = \frac{\text{resistance of the wire of length } l_X (R_{AD})}{\text{resistance of the wire of length } l_R (R_{DB})}$$

$$\therefore \frac{X}{R} = \frac{R_{AD}}{R_{DB}} \quad \dots (1)$$

Now, $R = \rho \frac{l}{A}$ where l is the length of the wire,

ρ is the resistivity of the material of the wire and
 A is the area of cross section of the wire.

$$\therefore R_{AD} = \rho \frac{l_X}{A} \text{ and } R_{DB} = \rho \frac{l_R}{A} \quad \dots (2)$$

$$\therefore \frac{X}{R} = \frac{R_{AD}}{R_{DB}} = \frac{\rho l_X / A}{\rho l_R / A}$$

$$\therefore \frac{X}{R} = \frac{l_X}{l_R}$$

$$\therefore X = \frac{l_X}{l_R} \times R$$

As R , l_X and l_R are known, the unknown resistance X can be calculated.

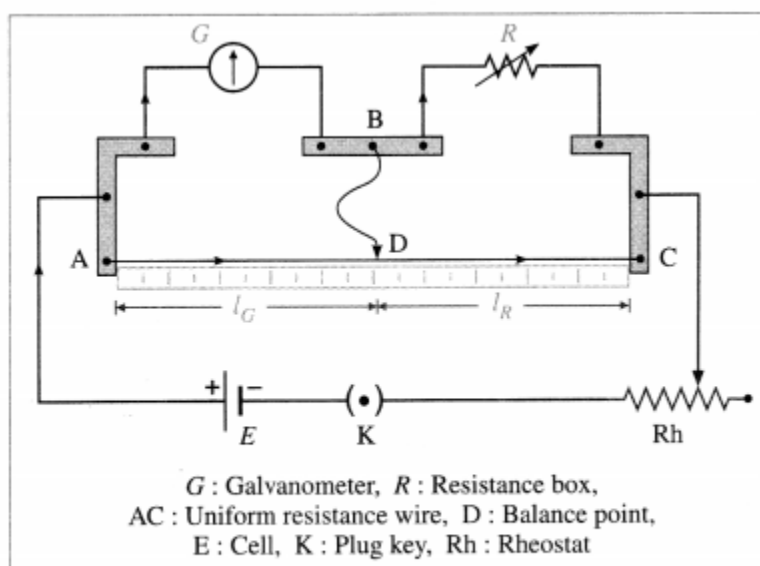
Question 5.

Describe Kelvin's method to determine the resistance of a galvanometer by using a meter bridge.

Answer:

Kelvin's method :

Circuit: The metre bridge circuit for Kelvin's method of determination of the resistance of a galvanometer is shown in below figure. The galvanometer whose resistance G is to be determined, is connected in one gap of the metre bridge. A resistance box providing a variable known resistance R is connected in the other gap. The junction B of the galvanometer and the resistance box is connected directly to a pencil jockey. A cell of emf E , a key (K) and a rheostat (Rh) are connected across AC .



Kelvin's metre bridge circuit for the measurement of galvanometer resistance

Working : Keeping a suitable resistance R in the resistance box and maximum resistance in the rheostat, key K is closed to pass the current. The rheostat resistance is slowly reduced such that the galvanometer shows about $2/3$ rd of the full-scale deflection.

On tapping the jockey at end-points A and C , the galvanometer deflection should change to opposite sides of the initial deflection. Only then will there be a point D on the wire which is equipotential with point B . The jockey is tapped along the wire to locate the equipotential point D when the galvanometer shows no change in deflection. Point D is now called the balance point and Kelvin's method is thus an equal deflection method. At this balanced condition,

$GR = \text{resistance of the wire of length } l_G = \text{resistance of the wire of length } l_R$

where l_G = the length of the wire opposite to the galvanometer, l_R = the length of the wire opposite to the resistance box.

If λ = the resistance per unit length of the wire,

$$GR = \lambda l_G \lambda l_R = l_G l_R$$

$$\therefore G = R l_G l_R$$

The quantities on the right hand side are known, so that G can be calculated.

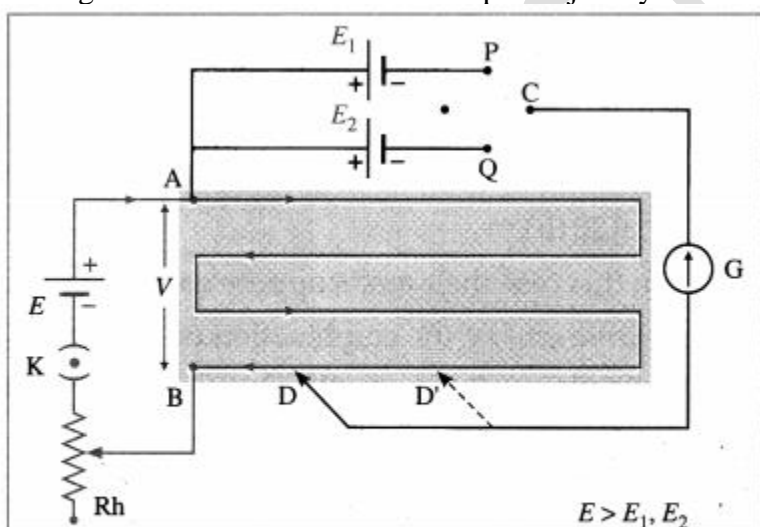
[Note : The method was devised by William Thom-son (Lord Kelvin, 1824-1907), British physicist.]

Question 6.

Describe how a potentiometer is used to compare the emfs of two cells by connecting the cells individually.

Answer:

A battery of stable emf E is used to set up a potential gradient V/L along a potentiometer wire, where V = potential difference across the length L of the wire. The positive terminals of the cells, whose emf's (E_1 and E_2) are to be compared, are connected to the high potential terminal A . The negative terminals of the cells are connected to a galvanometer G through a two-way key. The other terminal of the galvanometer is connected to a pencil jockey. The emf E should be greater than both the emf's E_1 and E_2 .



Comparison of two emf's using a potentiometer by the direct method

Connecting point P to C , the cell with emf E_1 is brought into the circuit. The jockey is tapped along the wire to locate the null point D at a distance l_1 from A . Then,

$$E_1 = Z_1(V/L)$$

Now, without changing the potential gradient (i.e., without changing the rheostat setting) point Q (instead of P) is connected to C , bringing the cell with emf E_2 into the circuit. Let its null point D' be at a distance l_2 from A , so that

$$E_2 = l_2(V/L)$$

$$\therefore E_1 E_2 = l_1 l_2$$

Hence, by measuring the corresponding null lengths l_1 and l_2 , E_1/E_2 can be calculated. The experiment is repeated for different potential gradients using the rheostat.

[Note : This method is used when the two emf's have comparable magnitudes. Then, the errors of measurement of their balancing lengths will also be of comparable magnitudes.]

Question 7.

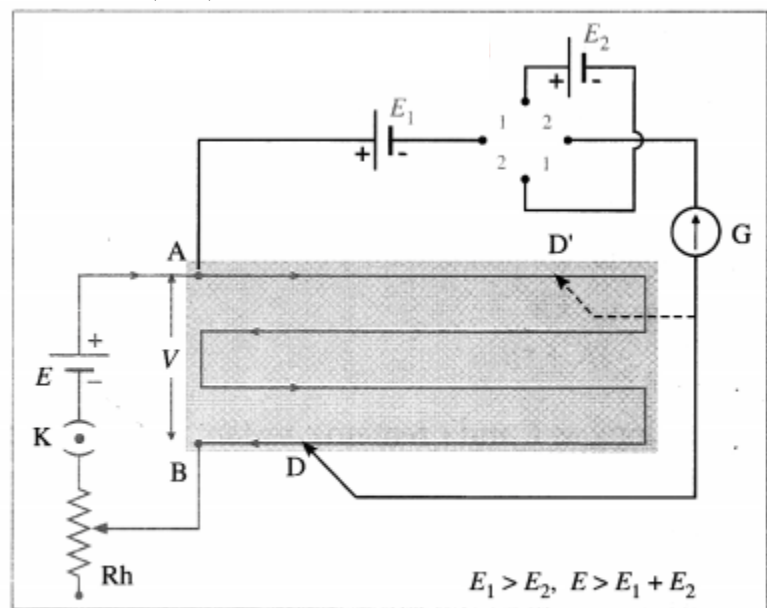
Describe how a potentiometer is used to compare the emfs of two cells by combination method.

Answer:

A battery of stable emf E is used to set up a potential gradient V/L , along the potentiometer wire, where V = potential difference across length L of the wire. The positive terminal of the cell 1 is connected to the higher potential terminal A of the potentiometer; the

negative terminal is connected to the galvanometer G through the reversing key. The other terminal of the galvanometer is connected to a pencil jockey. The cell 2 is connected across the remaining two opposite terminals of the reversing key. The other terminal of the galvanometer is connected to a pencil jockey. The emf E_1 should be greater than the emf E_2 ; this can be adjusted by trial and error.

Two plugs are inserted in the reversing key in positions 1 – 1. Here, the two cells assist each other so that the net emf is $E_1 + E_2$. The jockey is tapped along the wire to locate the null point D. If the null point is a distance l_1 from A, $E_1 + E_2 = l_1 (V/L)$



**Comparison of two emf's using a potentiometer
by the combination method (the sum and difference method)**

For the same potential gradient (without changing the rheostat setting), the plugs are now inserted into position 2 – 2. (instead of 1 – 1). The emf E_2 then opposes E_1 and the net emf is $E_1 - E_2$. The new null point D' is, say, a distance l_2 from A and $E_1 - E_2 = l_2 (V/L)$

$$\therefore E_1 + E_2 \over E_1 - E_2 = l_1 \over l_2 \therefore E_1 E_2 = l_1 - l_2 \over l_1 - l_2$$

Here, the emf E should be greater than $E_1 + E_2$. The experiment is repeated for different potential gradients using the rheostat. [Note : This method is used when $E_1 \gg E_2$, so that $E_1 + E_2$ and $E_1 - E_2$ have comparable magnitudes. Then, the errors of measurement of l_1 and l_2 will also be of comparable magnitudes.]

Question 8.

Describe with the help of a neat circuit diagram how you will determine the internal resistance of a cell by using a potentiometer. Derive the necessary formula.

Answer:

Principle : A cell of emf \mathcal{E} and internal resistance r , which is connected to an external resistance R , has its terminal potential difference V less than its emf E . If I is the corresponding current,

$$E V = I (R + r) I R = R + r R = 1 + r R \text{ (when } R \rightarrow \infty, V \rightarrow E \text{)}$$

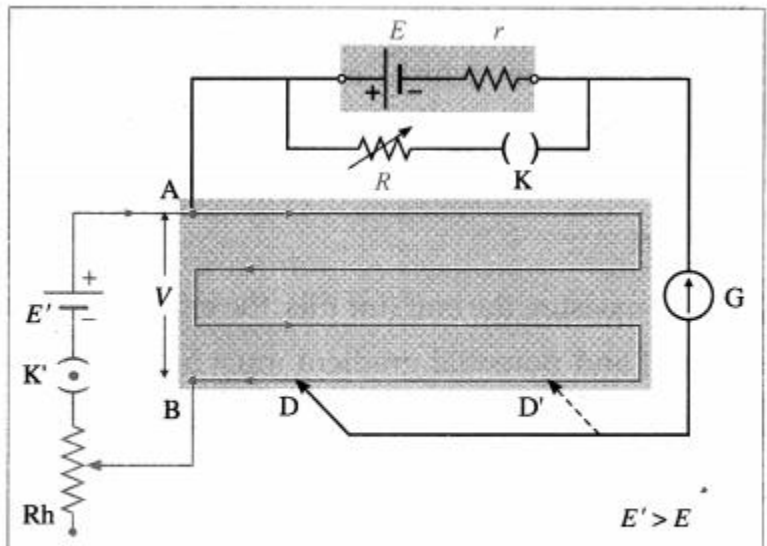
$$\therefore r = E - V \over V R$$

Working : A battery of stable emf E' is used to set up a potential gradient V/L , along the potentiometer wire, where V = potential difference across the length L of the wire. The negative terminal is connected through a centre-zero galvanometer G to a pencil jockey. A resistance box R with a plug key K in series is connected across the cell.

Firstly, key K is kept open; then, effectively, $R = \infty$. The jockey is tapped on the potentiometer wire to locate the null point D . Let the null length

$$AD = l_1, \text{ so that}$$

$$E = (V_{AB} / L) l_1$$



**Determination of the internal resistance
of a cell using a potentiometer**

With the same potential gradient, and a small resistance R in the resistance box, key K is closed. The new null length $AD' = l_2$ for the terminal potential difference V is found :

$$V = (V_{AB} / L) l_2$$

$$\therefore \frac{E}{V} = \frac{l_1}{l_2} \quad \therefore \frac{E - V}{V} = \frac{l_1 - l_2}{l_2} = \frac{l_1}{l_2} - 1$$

$$\text{Now, } r = \frac{E - V}{V} R$$

$$\therefore r = R \left(\frac{l_1}{l_2} - 1 \right)$$

R, l_1 , and l_2 being known, r can be calculated. The experiment is repeated with different potential gradients using the rheostat or with different values of R.

Question 9.

On what factors does the internal resistance of a cell depend?

Answer:

The internal resistance of a cell depends on :

1. Nature of the electrolyte :
The greater the conductivity of the electrolyte, the lower is the internal resistance of the cell.
2. Separation between the electrodes :
The larger the separation between the electrodes of the cell, the higher is the internal resistance of the cell. This is because the ions have to cover a greater distance before reaching an electrode.
3. Nature of the electrodes.
4. The internal resistance is inversely proportional to the common area of the electrodes dipping in the electrolyte.

Question 10.

A battery of emf 4 volt and internal resistance 1Ω is connected in parallel with another battery of emf 1 V and internal resistance 1Ω (with their like poles connected together). The combination is used to send current through an external resistance of 2Ω . Calculate the current through the external resistance.

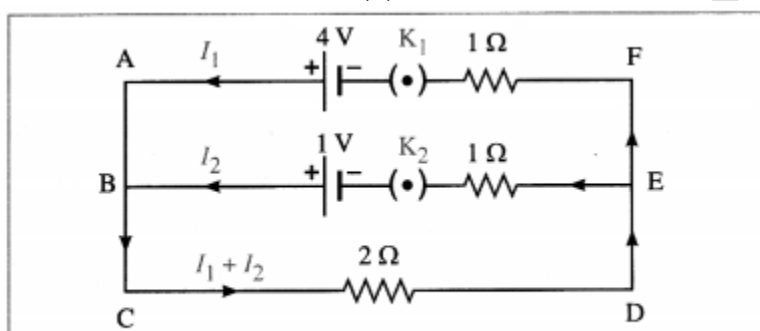
Answer:

Let I_1 and I_2 be the currents through the two branches as shown in below figure. The current through the 2Ω resistance will be $(I_1 + I_2)$ [Kirchhoff's current law].

Applying Kirchhoff's voltage law to loop ABCDEFA, we get,

$$-2(I_1 + I_2) - 1(I_1) + 4 = 0$$

$$\therefore 3I_1 + 2I_2 = 4 \dots\dots\dots (1)$$



Applying Kirchhoff's voltage law to loop ABCEFA, we get,

$$-2(I_1 + I_2) - 1(I_2) + 1 = 0$$

$$2I_1 + 3I_2 = 1 \dots\dots\dots (2)$$

Multiplying Eq. (1) by 2 and Eq. (2) by 3, we get,

$$6I_1 + 4I_2 = 8 \dots\dots\dots (3)$$

$$\text{and } 6I_1 + 9I_2 = 3 \dots\dots\dots (4)$$

Subtracting Eq. (4) from Eq. (3), we get,

$$-5I_2 = 5$$

$$\therefore I_2 = -1\text{A}$$

The minus sign shows that the direction of current I_2 is opposite to that assumed. Substituting this value of I_2 in Eq. (1), we get,

$$3I_1 + 2(-1) = 4$$

$$\therefore 3I_1 = 4 + 2 = 6$$

$$\therefore I_1 = 2\text{A}$$

Current through the 2Ω resistance = $I_1 + I_2 = 2 - 1$

= 1 A. It is in the direction as shown in the figure.

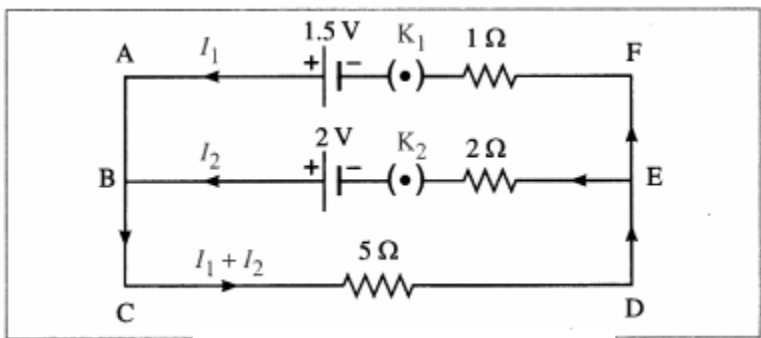
[Note : We may as well consider loop ABEFA and write the corresponding equation. But it does not provide any additional information.]

Question 11.

Two cells of emf 1.5 Volt and 2 Volt having respective internal resistances of 1Ω and 2Ω are connected in parallel so as to send current in same direction through an external resistance of 5Ω . Find the current through the external resistance.

Answer:

Let I_1 and I_2 be the currents through the two branches as shown in below figure. The current through the 5Ω resistor will be $I_1 + I_2$ [Kirchhoff's current law].



Applying Kirchhoff's voltage law to loop w ABCDEFA, we get,

$$-5(I_1 + I_2) - I_1 + 1.5 = 0$$

$$\therefore 6I_1 + 5I_2 = 1.5 \quad (1)$$

Applying Kirchhoff's voltage law to loop BCDEB, we get,

$$-5(I_1 + I_2) - 2I_2 + 2 = 0$$

$$\therefore 5I_1 + 7I_2 = 2 \quad (2)$$

Multiplying Eq. (1) by 5 and Eq. (2) by 6, we get,

$$30I_1 + 25I_2 = 7.5 \quad (3)$$

$$\text{and } 30I_1 + 42I_2 = 12 \quad (4)$$

Subtracting Eq. (3) from Eq. (4), we get,

$$17I_2 = 4.5$$

$$\therefore I_2 = 4.517 \text{ A}$$

Substituting this value of I_2 in Eq. (1), we get,

$$6I_1 + 5(4.517) = 1.5$$

$$\therefore 6I_1 + 22.517 = 1.5$$

$$\therefore 6I_1 = 1.5 - 22.517 = -21.017$$

$$I_1 = -3.503 \text{ A}$$

$$\therefore I_1 = 3.503 \text{ A}$$

Current through the 5 Ω resistance (external resistance)

$$= I_1 + I_2 = 3.503 + 4.517 = 8.02 \text{ A}$$

Question 12.

A voltmeter has a resistance 30 Ω. What will be its reading, when it is connected across a cell of emf 2 V having internal resistance 10 Ω?

Answer:

Data: $E = 2\text{ V}$, $r = 10 \text{ } \Omega$, $R = 30 \text{ } \Omega$

The voltmeter reading, $V = IR$

$$= \frac{ER}{R+r}$$

$$= \frac{(2 \times 30)}{(30+10)}$$

$$= \frac{60}{40}$$

$$= 1.5 \text{ V}$$

Question 13.

A set of three coils having resistances 10 Ω, 12 Ω and 15 Ω are connected in parallel. This combination is connected in series with series combination of three coils of the same resistances. Calculate the total resistance and current through the circuit, if a battery of emf 4.1 Volt is used for drawing current.

Answer:

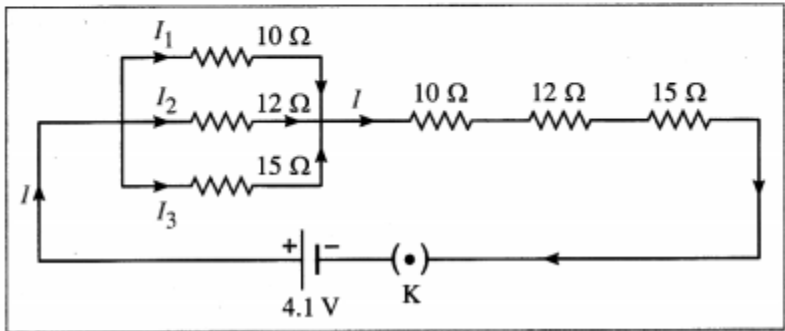
Below figure shows the electrical network. For resistances 10 Ω, 12 Ω and 15 Ω connected in parallel the equivalent resistance (R_p) is given by,

$$\frac{1}{R_p} = \frac{1}{10} + \frac{1}{12} + \frac{1}{15}$$

$$= \frac{6+5+4}{60}$$

$$= \frac{15}{60} = \frac{1}{4}$$

$$\therefore R_p = 4 \text{ } \Omega$$



For resistance R_p , 10 Ω, 12 Ω and 15 Ω connected in series, the equivalent resistance,

$$R_s = 4 + 10 + 12 + 15 = 41 \text{ } \Omega$$

Thus, the total resistance = $R_s = 41 \text{ } \Omega$

Now, $V = IR_s$

$$\therefore 4.1 = I \times 41$$

$$\therefore I = 0.1 \text{ A}$$

The total resistance and current through the circuit are 41Ω and 0.1 A respectively.

Question 14.

A potentiometer wire has a length of 1.5 m and resistance of 10Ω . It is connected in series with the cell of emf 4 V and internal resistance 5Ω . Calculate the potential drop per centimeter of the wire.

Answer:

Data : $L = 1.5 \text{ m}$, $R = 10 \Omega$, $E = 4 \text{ V}$, $r = 5 \Omega$

$$K = \frac{ER}{(R + r) L}$$

$$\therefore K = \frac{4 \times 10}{(10 + 5) 1.5}$$

$$= \frac{40}{15 \times \frac{15}{10}}$$

$$= \frac{400 \text{ V}}{225 \text{ m}} = \frac{400}{22500} \frac{\text{V}}{\text{cm}} = 0.0178 \frac{\text{V}}{\text{cm}}$$

The potential drop per centimeter of the wire is 0.0178 Vcm

Question 15.

When two cells of emfs. E_1 and E_2 are connected in series so as to assist each other, their balancing length on a potentiometer is found to be 2.7 m . When the cells are connected in series so as to oppose each other, the balancing length is found to be 0.3 m . Compare the emfs of the two cells.

Answer:

Data : $l_1 = 2.7 \text{ m}$ (cells assisting),

$l_2 = 0.3 \text{ m}$ (cells opposing)

$$E_1 + E_2 = Kl_1 \text{ and } E_1 - E_2 = Kl_2$$

$$\therefore E_1 + E_2 \quad E_1 - E_2 = Kl_1 \quad Kl_2$$

$$\therefore E_1 E_2 = l_1 + l_2 \quad l_1 - l_2 = 2.7 + 0.3 \quad 2.7 - 0.3 = 3.2 \quad 2.4 = 1.25$$

The ratio of the emf's of the two cells is 1.25 .

Question 16.

The emf of a cell is balanced by a length of 120 cm of potentiometer wire. When the cell is shunted by a resistance of 10Ω , the balancing length is reduced by 20 cm . Find the internal resistance of the cell.

Answer:

Data : $R = 10 \Omega$, $l_1 = 120 \text{ cm}$, $l_2 = 120 - 20 = 100 \text{ cm}$

$$r = R(l_1 - l_2)l_2$$

$$= 10 (120 - 100)100$$

$$= 2 \Omega$$

The internal resistance of the cell is 2Ω .

Question 17.

A potential drop per unit length along a wire is $5 \times 10^{-3} \text{ V/m}$. If the emf of a cell balances against length 216 cm of this potentiometer wire, find the emf of the cell.

Answer:

Data: $K = 5 \times 10^{-3} \text{ Vm}$, $L = 216 \text{ cm} = 216 \times 10^{-2} \text{ m}$

$$E = KL$$

$$\therefore E = 5 \times 10^{-3} \times 216 \times 10^{-2}$$

$$= 1080 \times 10^{-5}$$

$$= 0.01080 \text{ V}$$

The emf of the cell is 0.01080 volt .

(Note: For $K = 0.5 \text{ V/m}$, we get, $E = 1.08 \text{ V}$ (reasonable value)]

Question 18.

The resistance of a potentiometer wire is 8Ω and its length is 8 m . A resistance box and a 2 V battery are connected in series with it.

What should be the resistance in the box, if it is desired to have a potential drop of $1 \mu\text{V/mm}$?

Answer:

Data: $R = 8 \Omega$, $L = 8 \text{ m}$, $E = 2 \text{ V}$, $K = 1 \mu\text{V/mm}$

$$= 1 \times 10^{-6} \text{ V} / 10^{-3} \text{ m} = 10^{-3} \text{ Vm}$$

$$K = \frac{VL}{E(R + R_B)} \text{ where } R_B \text{ is the resistance in the box.}$$

$$\therefore 10^{-3} = \frac{2 \times 8}{(8 + R_B)8}$$

$$\therefore 8 + R_B = 210^{-3}$$

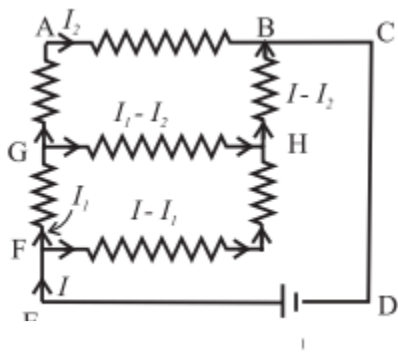
$$= 2 \times 10^3$$

$$\therefore R_B = 2000 - 8$$

$$= 1992 \Omega$$

Question 19.

Find the equivalent resistance between the terminals F and B in the network shown in the figure below given that the resistance of each resistor is 10 ohm .



Answer:

Applying Kirchhoff's voltage law to loop FGHF, we get,

$$-10I_1 - 10(I_1 - I_2) + 10(I - I_1) + 10(I - I_1) = 0$$

$$\therefore -10I_1 - 10I_1 + 10I_2 + 10I - 10I_1 + 10I - 10I_1 = 0$$

$$\therefore 20I - 40I_1 + 10I_2 = 0$$

$$\therefore 2I - 4I_1 + I_2 = 0 \dots\dots\dots (1)$$

Applying Kirchhoff's voltage law to loop GABHG, we get,

$$-10I_2 - 10I_2 + 10(I - I_2) + 10(I_1 - I_2) = 0$$

$$\therefore -20I_2 + 10I - 10I_2 + 10I_1 - 10I_2 = 0$$

$$\therefore 10I + 10I_1 - 40I_2 = 0 \dots\dots\dots (2)$$

$$\therefore I + I_1 - 4I_2 = 0 \dots\dots\dots (2)$$

Applying Kirchhoff's voltage law to loop EFHBCDE, we get,

$$-10(I - I_1) - 10(I - I_1) - 10(I - I_2) + E = 0$$

$$\therefore -10I + 10I_1 - 10I + 10I_1 - 10I + 10I_2 + E = 0$$

$$\therefore E = 30I - 20I_1 - 10I_2 \dots\dots\dots (3)$$

From Eq. (1), we get, $I_2 = 4I_1 - 2I \dots\dots\dots (4)$

From Eqs. (2) and (4), we get,

$$I + I_1 - 4(4I_1 - 2I) = 0$$

$$\therefore I + I_1 - 16I_1 + 8I = 0 \dots\dots\dots (5)$$

$$\therefore 9I = 15I_1 \therefore I_1 = \frac{3}{5}I = 0.6I \dots\dots\dots (5)$$

From Eqs. (4) and (5), we get,

$$I_2 = 4(0.6I) - 2I = 2.4I - 2I = 0.4I$$

$$= 12I - 10I = 2I$$

From Eqs. (3), (5) and (6), we get

$$E = 30I - 20(0.6I) - 10(0.4I)$$

$$= 30I - 12I - 4I = 14I$$

$$\therefore E = 14I$$

If R is the equivalent resistance between E and C,

$$E = RI$$

$$\therefore R = 14 \Omega$$

Question 20.

A voltmeter has a resistance of 100Ω . What will be its reading when it is connected across a cell of emf 2 V and internal resistance 20Ω ?

Answer:

Data: $E = 2 \text{ V}$, $r = 20 \Omega$, $R = 100 \Omega$

The voltmeter reading, $V = IR$

$$V = \frac{(2100+20)100}{200+100} = \frac{20000}{300} = 66.67 \text{ V}.$$

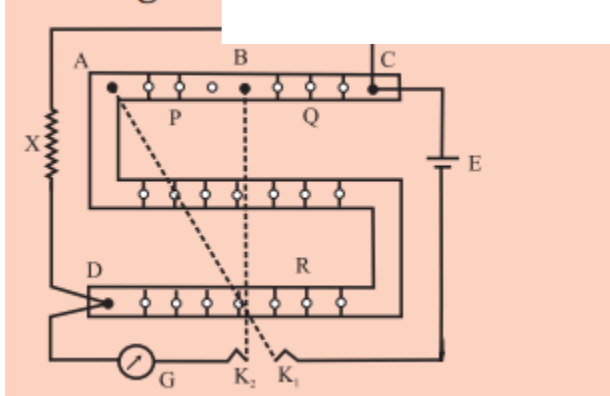
12th Physics Digest Chapter 9 Current Electricity Intext Questions and Answers

[Observe and Discuss \(Textbook Page No. 220\)](#)

Question 1.

Post Office Box

A post office box (PO Box) is a practical form of Wheatstone bridge as shown in the figure.



It consists of three arms P, Q and R. The resistances in these three arms are adjustable. The two ratio arms P and Q contain resistances of 10 ohm , 100 ohm and 1000 ohm each. The third arm R contains resistances from 1 ohm to 5000 ohm . The unknown resistance X (usually, in the form of a wire) forms the fourth arm of the Wheatstone's bridge. There are two tap keys K_1 and K_2 .

Answer:

The resistances in the arms P and Q are fixed to a desired ratio. The resistance in the arm R is adjusted so that the galvanometer shows no deflection. Now the bridge is balanced. The unknown resistance $X = RQ/P$, where P and Q are the fixed resistances in the ratio arms and R is the adjustable known resistance.

If L is the length of the wire used to prepare the resistor with resistance X and r is its radius, then the specific resistance (resistivity) of the material of the wire is given by
$$\rho = \frac{X\pi r^2 L}{L}$$

AllGuideSite