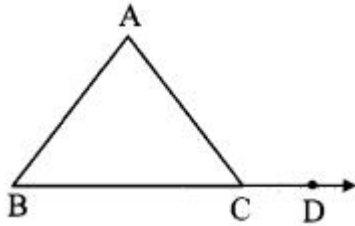


## Practice Set 3.1 Geometry 9th Std Maths Part 2 Answers Chapter 3 Triangles

Practice Set 3.1 Geometry 9th Standard Question 1.

In the adjoining figure,  $\angle ACD$  is an exterior angle of  $\triangle ABC$ .  $\angle B = 40^\circ$ ,  $\angle A = 70^\circ$ . Find the measure of  $\angle ACD$ .



Solution:

$$\angle A = 70^\circ, \angle B = 40^\circ \text{ [Given]}$$

$\angle ACD$  is an exterior angle of  $\triangle ABC$ . [Given]

$$\therefore \angle ACD = \angle A + \angle B$$

$$= 70^\circ + 40^\circ$$

$$\therefore \angle ACD = 110^\circ$$

Question 2.

In  $\triangle PQR$ ,  $\angle P = 70^\circ$ ,  $\angle Q = 65^\circ$ , then find  $\angle R$ .

Solution:

$$\angle P = 70^\circ, \angle Q = 65^\circ \text{ [Given]}$$

In  $\triangle PQR$ ,

$$\angle P + \angle Q + \angle R = 180^\circ \text{ [Sum of the measures of the angles of a triangle is } 180^\circ]$$

$$\therefore 70^\circ + 65^\circ + \angle R = 180^\circ$$

$$\therefore \angle R = 180^\circ - 70^\circ - 65^\circ$$

$$\therefore \angle R = 45^\circ$$

Practice Set 3.1 Geometry 9th Question 3.

The measures of angles of a triangle are  $x^\circ$ ,  $(x - 20)^\circ$ ,  $(x - 40)^\circ$ . Find the measure of each angle.

Solution:

The measures of the angles of a triangle are  $x^\circ$ ,  $(x - 20)^\circ$ ,  $(x - 40)^\circ$ . [Given]

$$\therefore x^\circ + (x - 20)^\circ + (x - 40)^\circ = 180^\circ \text{ [Sum of the measures of the angles of a triangle is } 180^\circ]$$

$$\therefore 3x - 60 = 180$$

$$\therefore 3x = 180 + 60$$

$$\therefore 3x = 240$$

$$\therefore x = 240$$

$$\therefore x = 2403$$

$$\therefore x = 80^\circ$$

$\therefore$  The measures of the remaining angles are

$$x - 20^\circ = 80^\circ - 20^\circ = 60^\circ,$$

$$x - 40^\circ = 80^\circ - 40^\circ = 40^\circ$$

$\therefore$  The measures of the angles of the triangle are  $80^\circ$ ,  $60^\circ$  and  $40^\circ$ .

9th Class Geometry Practice Set 3.1 Question 4.

The measure of one of the angles of a triangle is twice the measure of its smallest angle and the measure of the other is thrice the measure of the smallest angle. Find the measures of the three angles.

Solution:

Let the measure of the smallest angle be  $x^\circ$ .

One of the angles is twice the measure of the smallest angle.

$\therefore$  Measure of that angle =  $2x^\circ$

Another angle is thrice the measure of the smallest angle.

$\therefore$  Measure of that angle =  $3x^\circ$

$\therefore$  The measures of the remaining two angles are  $2x^\circ$  and  $3x^\circ$ .

Now,  $x^\circ + 2x^\circ + 3x^\circ = 180^\circ$  [Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$$\therefore 6x = 180$$

$$\therefore x = 180$$

$$\therefore x = 1806$$

$$\therefore x^\circ = 30^\circ$$

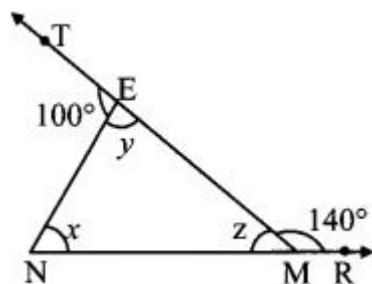
The measures of the remaining angles are  $2x^\circ = 2 \times 30^\circ = 60^\circ$

$$3x^\circ = 3 \times 30^\circ = 90^\circ$$

The measures of the three angles of the triangle are  $30^\circ$ ,  $60^\circ$  and  $90^\circ$ .

Question 5.

In the adjoining figure, measures of some angles are given. Using the measures, find the values of  $x$ ,  $y$ ,  $z$ .



Solution:

i.  $\angle NET = 100^\circ$  and  $\angle EMR = 140^\circ$

$$\angle EMN + \angle EMR = 180^\circ$$

$$\therefore z + 140^\circ = 180^\circ$$

$$\therefore z = 180^\circ - 140^\circ$$

$$\therefore z = 40^\circ$$

ii. Also,  $\angle NET + \angle NEM = 180^\circ$  [Angles in a linear pair]

$$\therefore 100^\circ + y = 180^\circ$$

$$\therefore y = 180^\circ - 100^\circ$$

$$\therefore y = 80^\circ$$

iii. In  $\triangle ENM$ ,

$\therefore \angle ENM + \angle NEM + \angle EMN = 180^\circ$  [Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$$\therefore x + 80^\circ + 40^\circ = 180^\circ$$

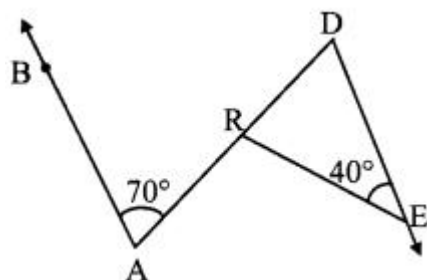
$$\therefore x = 180^\circ - 80^\circ - 40^\circ$$

$$\therefore x = 60^\circ$$

$$\therefore x = 60^\circ, = 80^\circ, z = 40^\circ$$

Question 6.

In the adjoining figure, line  $AB \parallel$  line  $DE$ . Find the measures of  $\angle DRE$  and  $\angle ARE$  using given measures of some angles.



Solution:

i.  $\angle BAD = 70^\circ$ ,  $\angle DER = 40^\circ$  [Given]

line  $AB \parallel$  line  $DE$  and seg  $AD$  is their transversal.

$\therefore \angle EDA = \angle BAD$  [Alternate Angles]

$$\therefore \angle EDA = 70^\circ \dots (i)$$

In  $\triangle DRE$ ,

$\angle EDR + \angle DER + \angle DRE = 180^\circ$  [Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$$\therefore 70^\circ + 40^\circ + \angle DRE = 180^\circ \text{ [From (i) and D - R - A]}$$

$$\therefore \angle DRE = 180^\circ - 70^\circ - 40^\circ$$

$$\therefore \angle DRE = 70^\circ$$

ii.  $\angle DRE + \angle ARE = 180^\circ$  [Angles in a linear pair]

$$\therefore 70^\circ + \angle ARE = 180^\circ$$

$$\therefore \angle ARE = 180^\circ - 70^\circ$$

$$\therefore \angle ARE = 110^\circ$$

$$\therefore \angle DRE = 70^\circ, \angle ARE = 110^\circ$$

Triangles Class 9 Practice Set 3.1 Question 7.

In  $\triangle ABC$ , bisectors of  $\angle A$  and  $\angle B$  intersect at point  $O$ . If  $\angle C = 70^\circ$ , find the measure of  $\angle AOB$ .

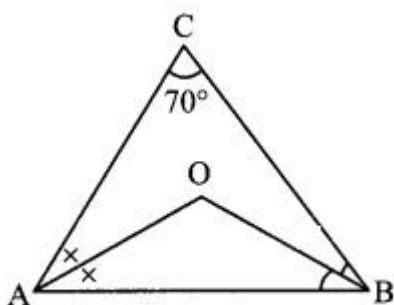
Solution:

$$\angle OAB = \angle OAC = \frac{1}{2} \angle BAC \dots (i) \text{ [Seg AO bisects } \angle BAC]$$

$$\angle OBA = \angle OBC = \frac{1}{2} \angle ABC \dots (ii) \text{ [Seg BO bisects } \angle ABC]$$

In  $\triangle ABC$ ,

$$\angle BAC + \angle ABC + \angle ACB = 180^\circ \text{ [Sum of the measures of the angles of a triangle is } 180^\circ]$$



$$\therefore \angle BAC + \angle ABC + 70^\circ = 180^\circ$$

$$\therefore \angle BAC + \angle ABC = 180^\circ - 70^\circ$$

$$\therefore \angle BAC + \angle ABC = 110^\circ$$

$$\therefore 12(\angle BAC) + 12(\angle ABC) = 12 \times 110^\circ \text{ [Multiplying both sides by 12]}$$

$$\therefore \angle OAB + \angle OBA = 55^\circ \dots(iii) \text{ [From (i) and (ii)]}$$

In  $\triangle OAB$ ,

$$\angle OAB + \angle OBA + \angle AOB = 180^\circ \text{ [Sum of the measures of the angles of a triangle is } 180^\circ]$$

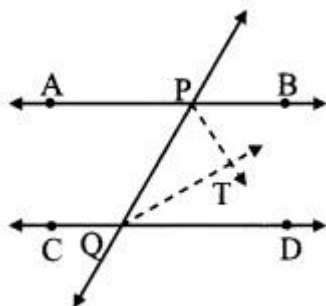
$$\therefore 55^\circ + \angle AOB = 180^\circ \text{ [From (iii)]}$$

$$\therefore \angle AOB = 180^\circ - 55^\circ$$

$$\therefore \angle AOB = 125^\circ$$

Question 8.

In the adjoining figure, line  $AB \parallel$  line  $CD$  and line  $PQ$  is the transversal. Ray  $PT$  and ray  $QT$  are bisectors of  $\angle BPQ$  and  $\angle PQD$  respectively. Prove that  $m \angle PTQ = 90^\circ$ .



Given: line  $AB \parallel$  line  $CD$  and line  $PQ$  is the transversal.

ray  $PT$  and ray  $QT$  are the bisectors of  $\angle BPQ$  and  $\angle PQD$  respectively.

To prove:  $m \angle PTQ = 90^\circ$

Solution:

Proof:

$$\angle TPB = \angle TPQ = \frac{1}{2} \angle BPQ \dots(i) \text{ [Ray } PT \text{ bisects } \angle BPQ]$$

$$\angle TQD = \angle TQP = \frac{1}{2} \angle PQD \dots(ii) \text{ [Ray } QT \text{ bisects } \angle PQD]$$

line  $AB \parallel$  line  $CD$  and line  $PQ$  is their transversal. [Given]

$$\therefore \angle BPQ + \angle PQD = 180^\circ \text{ [Interior angles]}$$

$$\therefore \frac{1}{2} (\angle BPQ) + \frac{1}{2} (\angle PQD) = \frac{1}{2} \times 180^\circ \text{ [Multiplying both sides by } \frac{1}{2}]$$

$$\angle TPQ + \angle TQP = 90^\circ$$

In  $\triangle PTQ$ ,

$$\angle TPQ + \angle TQP + \angle PTQ = 180^\circ \text{ [Sum of the measures of the angles of a triangle is } 180^\circ]$$

$$\therefore 90^\circ + \angle PTQ = 180^\circ \text{ [From (iii)]}$$

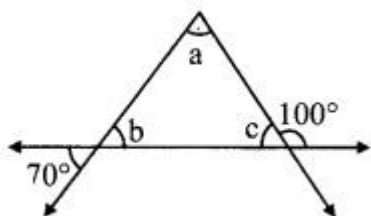
$$\therefore \angle PTQ = 180^\circ - 90^\circ$$

$$= 90^\circ$$

$$\therefore m\angle PTQ = 90^\circ$$

Triangle Practice Set 3.1 Question 9.

Using the information in the adjoining figure, find the measures of  $\angle a$ ,  $\angle b$  and  $\angle c$ .



Solution:

i.  $\angle c + 100^\circ = 180^\circ$  [Angles in a linear pair]

$$\therefore \angle c = 180^\circ - 100^\circ$$

$$\therefore \angle c = 80^\circ$$

ii.  $\angle b = 70^\circ$  [Vertically opposite angles]

iii.  $\angle a + \angle b + \angle c = 180^\circ$  [Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$$\angle a + 70^\circ + 80^\circ = 180^\circ$$

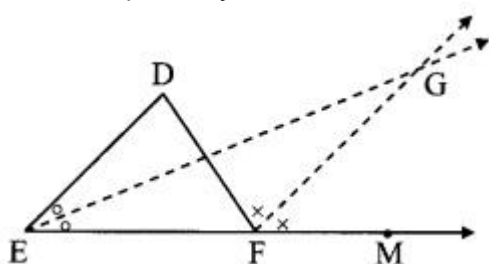
$$\therefore \angle a = 180^\circ - 70^\circ - 80^\circ$$

$$\therefore \angle a = 30^\circ$$

$$\therefore \angle a = 30^\circ, \angle b = 70^\circ, \angle c = 80^\circ$$

Practice Set 3.1 Geometry Question 10.

In the adjoining figure, line  $DE \parallel$  line  $GF$ , ray  $EG$  and ray  $FG$  are bisectors of  $\angle DEF$  and  $\angle DFM$  respectively. Prove that,



i.  $\angle DEG = \frac{1}{2} \angle EDF$

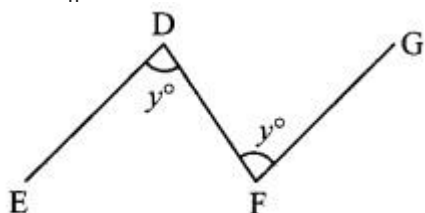
ii.  $EF = FG$

Solution:

i.  $\angle DEG = \angle FEG = x^\circ$  .....(i) [Ray  $EG$  bisects  $\angle DEF$ ]

$\angle GFD = \angle GFM = y^\circ$  .....(ii) [Ray  $FG$  bisects  $\angle DFM$ ]

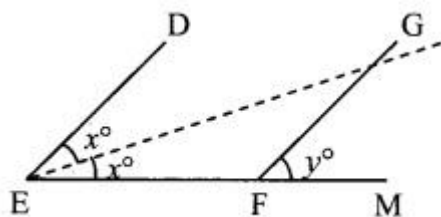
line  $DE \parallel$  line  $GF$  and  $DF$  is their transversal. [Given]



$\therefore \angle EDF = \angle GFD$  [Alternate angles]

$\therefore \angle EDF = y^\circ \dots(iii)$  [From (ii)]

line  $DE \parallel$  line  $GF$  and  $EM$  is their transversal. [Given]



$\therefore \angle DEF = \angle GFM$  [Corresponding angles]

$\therefore \angle DEG + \angle FEG = \angle GFM$  [Angle addition property]

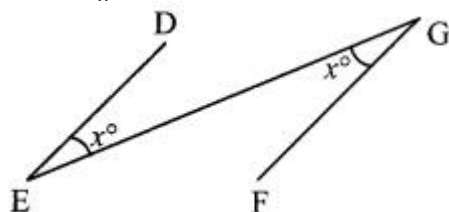
$\therefore x^\circ + x^\circ = y^\circ$  [From (i) and (ii)]

$\therefore 2x^\circ = y^\circ$

$\therefore x^\circ = \frac{1}{2}y^\circ$

$\therefore \angle DEG = \frac{1}{2}\angle EDF$  [From (i) and (iii)]

ii. line  $DE \parallel$  line  $GF$  and  $GE$  is their transversal. [Given]



$\therefore \angle DEG = \angle FGE \dots(iv)$  [Alternate angles]

$\therefore \angle FEG = \angle FGE \dots(v)$  [From (i) and (iv)]

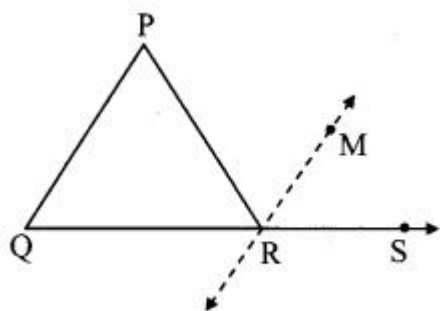
$\therefore$  In  $\triangle FEG$ ,

$\angle FEG = \angle FGE$  [From (v)]

$\therefore EF = FG$  [Converse of isosceles triangle theorem]

### Maharashtra Board Class 9 Maths Chapter 3 Triangles Practice Set 3.1 Intext Questions and Activities

Class 9 Geometry Practice Set 3.1 Question 1. Can you give an alternative proof of the above theorem by drawing a line through point R and parallel to seg PQ in the above figure? (Textbook pg. no. 25)



Solution:

Yes.

Construction: Draw line RM parallel to seg PQ through a point R.

Proof:

seg PQ  $\parallel$  line RM and seg PR is their transversal. [Construction]

$\therefore \angle PRM = \angle QPR$  .....(i) [Alternate angles]

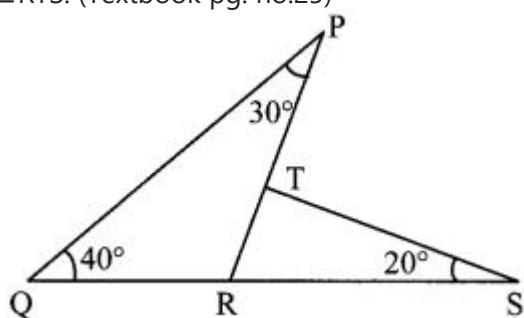
seg PQ  $\parallel$  line RM and seg QR is their transversal. [Construction]

$\therefore \angle SRM = \angle PQR$  .....(ii) [Corresponding angles]

$\therefore \angle PRM + \angle SRM = \angle QPR + \angle PQR$  [Adding (i) and (ii)]

$\therefore \angle PRS = \angle PQR + \angle QPR$  [Angle addition property]

3 Triangles Question 2. Observe the given figure and find the measures of  $\angle PRS$  and  $\angle RTS$ . (Textbook pg. no.25)



Solution:

$\angle PRS$  is an exterior angle of  $\triangle PQR$ .

So from the theorem of remote interior angles,

$\angle PRS = \angle PQR + \angle QPR$

$= 40^\circ + 30^\circ$

$\therefore \angle PRS = 70^\circ$

$\therefore \angle TRS = 70^\circ$  ...[P - T - R]

In  $\triangle RTS$ ,

$\angle TRS + \angle RTS + \angle TSR = 180^\circ$  ...[Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$\therefore 70^\circ + \angle RTS + 20^\circ = 180^\circ$

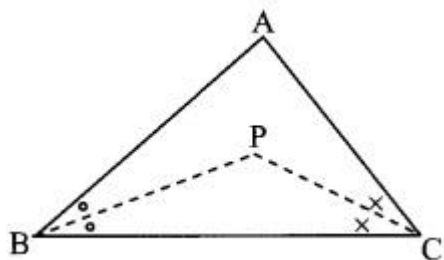
$\therefore \angle RTS + 90^\circ = 180^\circ$

$\therefore \angle RTS = 180^\circ$

$\therefore \angle RTS = 90^\circ$

9th Class Geometry Triangles Question 3. In the given figure, bisectors of  $\angle B$  and  $\angle C$  of  $\triangle ABC$  intersect at point P. Prove that  $\angle BPC = 90^\circ + \frac{1}{2}\angle BAC$ .

Complete the proof by filling in the blanks. (Textbook pg. no.27)



Solution:

Proof:

In  $\triangle ABC$ ,

$\angle BAC + \angle ABC + \angle ACB = 180^\circ$  ...[Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$\therefore \angle BAC + \angle ABC + \angle ACB = 180$  ... [Multiplying each term by 12]

$\therefore \angle BAC + \angle PBC + \angle PCB = 90^\circ$

$\therefore \angle PBC + \angle PCB = 90^\circ - \angle BAC$  .....(i)

In  $\triangle BPC$ ,

$\angle BPC + \angle PBC + \angle PCB = 180^\circ$  .....[Sum of measures of angles of a triangle]

$\therefore \angle BPC + 90^\circ - \angle BAC = 180^\circ$  .....[From (i)]

$\therefore \angle BPC = 180^\circ - 90^\circ + \angle BAC$

$= 180^\circ - 90^\circ + \angle BAC$

$= 90^\circ + \angle BAC$

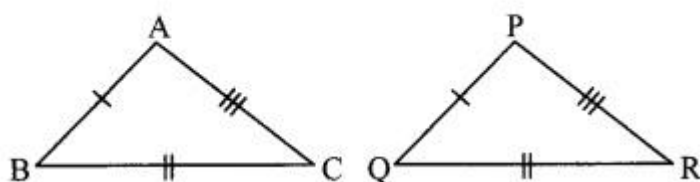
## Practice Set 3.2 Geometry 9th Std Maths Part 2

### Answers Chapter 3 Triangles

Question 1.

In each of the examples given below, a pair of triangles is shown. Equal parts of triangles in each pair are marked with the same signs. Observe the figures and state the test by which the triangles in each pair are congruent.

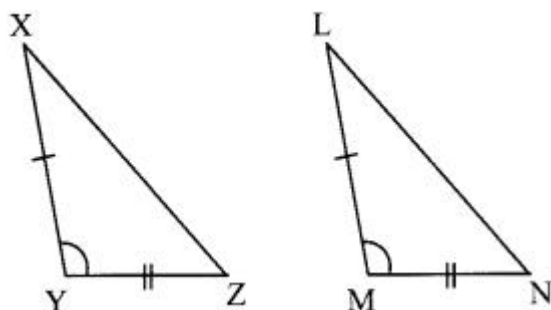
i.



By SSS test

$\triangle ABC \cong \triangle PQR$

ii.

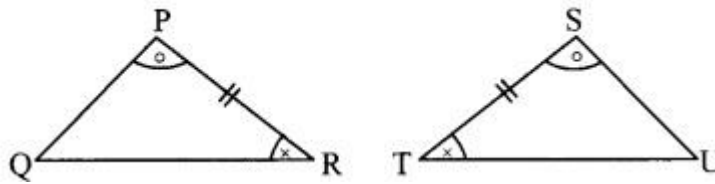


By SAS test

$\triangle XYZ \cong \triangle LMN$

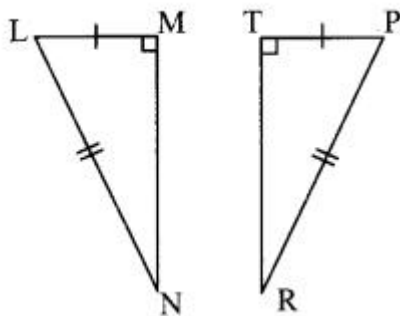


iii.



By ASA test  
 $\Delta PQR \cong \Delta STU$

iv.



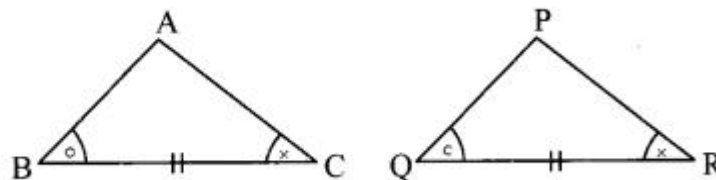
By hypotenuse side test  
 $\Delta LMN \cong \Delta PTR$

Question 2.

Observe the information shown in pairs of triangles given below. State the test by which the two triangles are congruent. Write the remaining congruent parts of the triangles.

Solution:

i.



From the information shown in the figure,

In  $\Delta ABC$  and  $\Delta PQR$ ,

$\angle ABC \cong \angle PQR$

seg  $BC \cong$  seg  $QR$

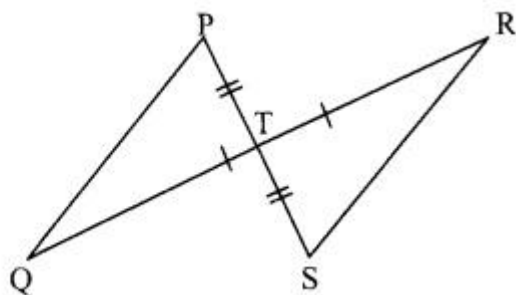
$\angle ACB \cong \angle PRQ$

$\therefore \Delta ABC \cong \Delta PQR$  [ASA test]

$\therefore \angle BAC \cong \angle QPR$  [Corresponding angles of congruent triangles]

seg  $AB \cong$  seg  $PQ$  and seg  $AC \cong$  seg  $PR$  [Corresponding sides of congruent triangles]

ii.



From the information shown in the figure,

In  $\triangle PQT$  and  $\triangle STR$ ,

seg  $PT \cong$  seg  $ST$

$\angle PTQ \cong \angle STR$  [Vertically opposite angles]

seg  $TQ \cong$  seg  $TR$

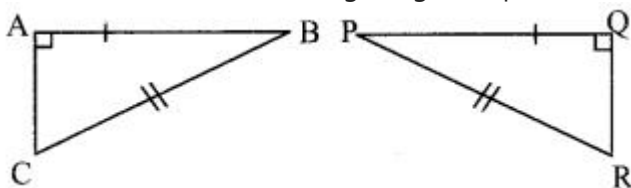
$\therefore \triangle PQT \cong \triangle STR$  [SAS test]

$\therefore \angle TPQ \cong \angle TSR$  and  $\angle TQP \cong \angle TRS$  [Corresponding angles of congruent triangles]

seg  $PQ \cong$  seg  $SR$  [Corresponding sides of congruent triangles]

Question 3.

From the information shown in the figure, state the test assuring the congruence of  $\triangle ABC$  and  $\triangle PQR$ . Write the remaining congruent parts of the triangles.



Solution:

In  $\triangle BAC$  and  $\triangle PQR$ ,

seg  $BA \cong$  seg  $PQ$

seg  $BC \cong$  seg  $PR$

$\angle BAC \cong \angle PQR = 90^\circ$  [Given]

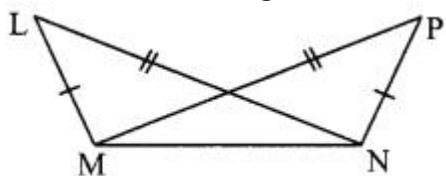
$\therefore \triangle BAC \cong \triangle PQR$  [Hypotenuse side test]

$\therefore$  seg  $AC \cong$  seg  $QR$  [c.s.c.t.]

$\angle ABC \cong \angle QPR$  and  $\angle ACB \cong \angle QRP$  [c.a.c.t.]

Question 4.

As shown in the adjoining figure, in  $\triangle LMN$  and  $\triangle PNM$ ,  $LM = PN$ ,  $LN = PM$ . Write the test which assures the congruence of the two triangles. Write their remaining congruent parts.



Solution:

In  $\triangle LMN$  and  $\triangle PNM$ ,

seg  $LM \cong$  seg  $PN$

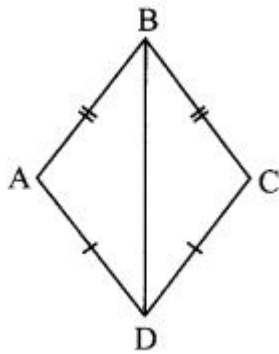
seg  $LN \cong$  seg  $PM$  [Given]

seg  $MN \cong$  seg  $NM$  [Common side]

$\therefore \triangle LMN \cong \triangle PNM$  [SSS test]  
 $\therefore \angle LMN \cong \angle PNM$ ,  
 $\therefore \angle MLN \cong \angle NPM$ , and  $\angle LNM \cong \angle PMN$  [c.a.c.t.]

Question 5.

In the adjoining figure,  $\text{seg } AB \cong \text{seg } CB$  and  $\text{seg } AD \cong \text{seg } CD$ . Prove that  $\triangle ABD \cong \triangle CBD$ .



Solution:

proof:

In  $\triangle ABD$  and  $\triangle CBD$ ,

$\text{seg } AB \cong \text{seg } CB$

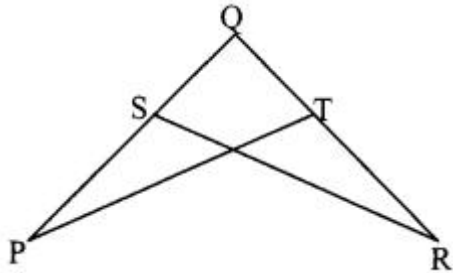
$\text{seg } AD \cong \text{seg } CD$  [Given]

$\text{seg } BD \cong \text{seg } BD$  [Common side]

$\therefore \triangle ABD \cong \triangle CBD$  [SSS test]

Question 6.

In the adjoining figure,  $\angle P \cong \angle R$ ,  $\text{seg } PQ \cong \text{seg } RQ$ . Prove that  $\triangle PQT \cong \triangle RQS$ .



Proof:

In  $\triangle PQT$  and  $\triangle RQS$ ,

$\angle P \cong \angle R$

$\text{seg } PQ \cong \text{seg } RQ$  [Given]

$\angle Q \cong \angle Q$  [Common angle]

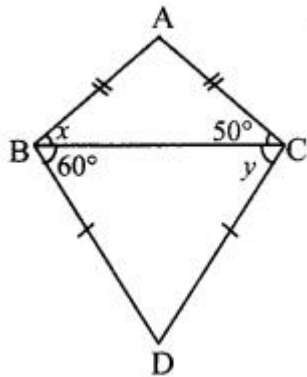
$\therefore \triangle PQT \cong \triangle RQS$  [ASA test]

## Practice Set 3.3 Geometry 9th Std Maths Part 2

### Answers Chapter 3 Triangles

Question 1.

Find the values of  $x$  and  $y$  using the information shown in the given figure. Find the measures of  $\angle ABD$  and  $\angle ACD$ .



Solution:

i.  $\angle ACB = 50^\circ$  [Given]

In  $\triangle ABC$ ,  $\text{seg } AC \cong \text{seg } AB$  [Given]

$\therefore \angle ABC \cong \angle ACB$  [Isosceles triangle theorem]

$\therefore x = 50^\circ$

ii.  $\angle DBC = 60^\circ$  [Given]

In  $\triangle BDC$ ,  $\text{seg } BD \cong \text{seg } DC$  [Given]

$\therefore \angle DCB \cong \angle DBC$  [Isosceles triangle theorem]

$\therefore y = 60^\circ$

iii.  $\angle ABD = \angle ABC + \angle DBC$  [Angle addition property]

$= 50^\circ + 60^\circ$

$\therefore \angle ABD = 110^\circ$

iv.  $\angle ACD = \angle ACB + \angle DCB$  [Angle addition property]

$= 50^\circ + 60^\circ$

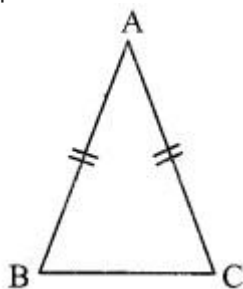
$\therefore \angle ACD = 110^\circ$

$\therefore x = 50^\circ, y = 60^\circ,$

$\angle ABD = 110^\circ, \angle ACD = 110^\circ$

Question 2.

The length of hypotenuse of a right angled triangle is 15. Find the length of median on its hypotenuse.



Solution:

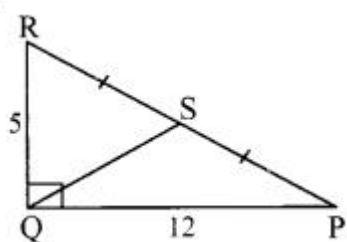
Length of hypotenuse = 15 [Given]

Length of median on the hypotenuse =  $\frac{1}{2}$  x length of hypotenuse [In a right angled triangle, the length of the median on the hypotenuse is half the length of the hypotenuse]  
 $= \frac{1}{2} \times 15 = 7.5$

$\therefore$  The length of the median on the hypotenuse is 7.5 units.

Question 3.

In  $\Delta PQR$ ,  $\angle Q = 90^\circ$ ,  $PQ = 12$ ,  $QR = 5$  and  $QS$  is a median. Find  $l(QS)$ .



Solution:

i.  $PQ = 12$ ,  $QR = 5$  [Given]

In  $\Delta PQR$ ,  $\angle Q = 90^\circ$  [Given]

$\therefore PR^2 = QR^2 + PQ^2$  [Pythagoras theorem]

$$= 25 + 144$$

$$\therefore PR^2 = 169$$

$\therefore PR = 13$  units [Taking square root of both sides]

ii. In right angled  $\Delta PQR$ , seg  $QS$  is the median on hypotenuse  $PR$ .

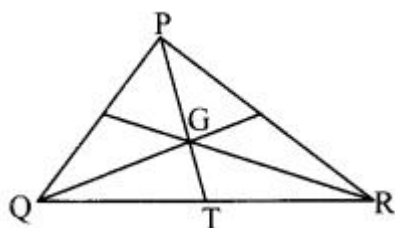
$\therefore QS = \frac{1}{2}PR$  [In a right angled triangle, the length of the median on the hypotenuse is half the length of the hypotenuse]

$$= \frac{1}{2} \times 13$$

$\therefore l(QS) = 6.5$  units

Question 4.

In the given figure, point  $G$  is the point of concurrence of the medians of  $\Delta PQR$ . If  $GT = 2.5$ , find the lengths of  $PG$  and  $PT$ .



Solution:

i. In  $\Delta PQR$ ,  $G$  is the point of concurrence of the medians. [Given]

The centroid divides each median in the ratio 2 : 1.

$$PG : GT = 2 : 1$$

$$\therefore \frac{PG}{GT} = \frac{2}{1}$$

$$\therefore \frac{PG}{2.5} = \frac{2}{1}$$

$$\therefore PG = 2 \times 2.5$$

$$\therefore PG = 5 \text{ units}$$

ii. Now,  $PT = PG + GT$  [P – G – T]

$$= 5 + 2.5$$

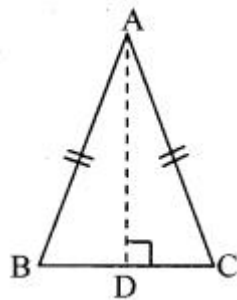
$$\therefore l(PG) = 5 \text{ units, } l(PT) = 7.5 \text{ units}$$

### Maharashtra Board Class 9 Maths Chapter 3 Triangles Practice Set 3.3 Intext Questions and Activities

Question 1.

Can the theorem of isosceles triangle be proved by doing a different construction?

(Textbook pg. no.34)



Solution:

Yes

Construction: Draw seg  $AD \perp$  seg BC.

Proof:

In  $\triangle ABD$  and  $\triangle ACD$ ,

seg  $AB \cong$  seg  $AC$  [Given]

$\angle ADB \cong \angle ADC$  [Each angle is of measure  $90^\circ$ ]

seg  $AD \cong$  seg  $AD$  [Common side]

$\therefore \triangle ABD \cong \triangle ACD$  [Hypotenuse side test]

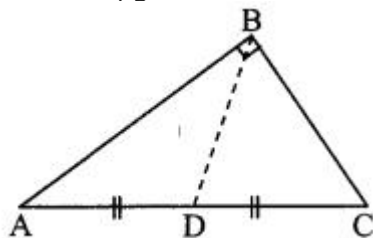
$\therefore \angle ABD \cong \angle ACD$  [c.a.c.t.]

$\therefore \angle ABC \cong \angle ACB$  [B-D-C]

Question 2.

Can the theorem of isosceles triangle be proved without doing any construction?

(Textbook pg, no.34)



Solution:

Yes

Proof:

In  $\triangle ABC$  and  $\triangle ACB$ ,

seg AB  $\cong$  seg AC [Given]  
 $\angle BAC \cong \angle CAB$  [Common angle]  
seg AC  $\cong$  seg AB [Given]  
 $\therefore \triangle ABC \cong \triangle ACB$  [SAS test]  
 $\therefore \angle ABC \cong \angle ACB$  [c. a. c. t.]

Question 3.

In the given figure,  $\triangle ABC$  is a right angled triangle, seg BD is the median on hypotenuse. Measure the lengths of the following segments.

- i. AD
- ii. DC
- iii. BD

From the measurements verify that  $BD = \frac{1}{2}AC$ . (Textbook pg. no. 37)

Solution:

AD = DC = BD = 1.9 cm  
AC = AD + DC [A – D – C]  
= 1.9 + 1.9  
= 2  $\times$  1.9 cm  
 $\therefore AC = 2 \times BD$   
 $\therefore BD = \frac{1}{2} AC$

## Practice Set 3.4 Geometry 9th Std Maths Part 2

### Answers Chapter 3 Triangles

Question 1.

In the adjoining figure, point A is on the bisector of  $\angle XYZ$ . If AX = 2 cm, then find AZ.

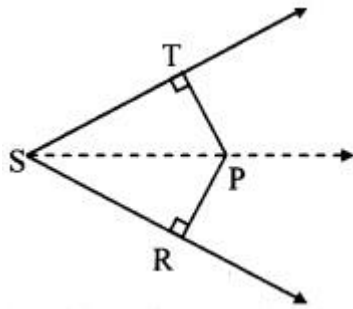
Solution:

AX = 2 cm [Given]  
Point A lies on the bisector of  $\angle XYZ$ . [Given]  
Point A is equidistant from the sides of  $\angle XYZ$ . [Every point on the bisector of an angle is equidistant from the sides of the angle]  
 $\therefore AZ = AX$   
 $\therefore AZ = 2 \text{ cm}$

Question 2.

In the adjoining figure,  $\angle RST = 56^\circ$ , seg PT  $\perp$  ray ST, seg PR  $\perp$  ray SR and seg PR  $\cong$  seg PT. Find the measure of  $\angle RSP$ .

State the reason for your answer.



Solution:

seg  $PT \perp$  ray  $ST$ , seg  $PR \perp$  ray  $SR$  [Given]

seg  $PR \cong$  seg  $PT$

$\therefore$  Point  $P$  lies on the bisector of  $\angle TSR$  [Any point equidistant from the sides of an angle is on the bisector of the angle]

$\therefore$  Ray  $SP$  is the bisector of  $\angle RST$ .

$\angle RSP = 56^\circ$  [Given]

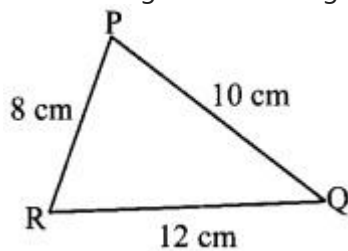
$\therefore \angle RSP = \frac{1}{2} \angle RST$

$= \frac{1}{2} \times 56^\circ$

$\therefore \angle RSP = 28^\circ$

Question 3.

In  $\triangle PQR$ ,  $PQ = 10$  cm,  $QR = 12$  cm,  $PR = 8$  cm. Find out the greatest and the smallest angle of the triangle.



Solution:

In  $\triangle PQR$ ,

$PQ = 10$  cm,  $QR = 12$  cm,  $PR = 8$  cm [Given]

Since,  $12 > 10 > 8$

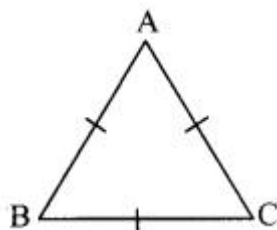
$\therefore QR > PQ > PR$

$\therefore \angle QPR > \angle PRQ > \angle PQR$  [Angle opposite to greater side is greater]

$\therefore$  In  $\triangle PQR$ ,  $\angle QPR$  is the greatest angle and  $\angle PQR$  is the smallest angle.

Question 4.

In  $\triangle FAN$ ,  $\angle F = 80^\circ$ ,  $\angle A = 40^\circ$ . Find out the greatest and the smallest side of the triangle. State the reason.





Solution:

In  $\triangle FAN$ ,

$\angle F + \angle A + \angle N = 180^\circ$  [Sum of the measures of the angles of a triangle is  $180^\circ$ ]

$$\therefore 80^\circ + 40^\circ + \angle N = 180^\circ$$

$$\therefore \angle N = 180^\circ - 80^\circ - 40^\circ$$

$$\therefore \angle N = 60^\circ$$

Since,  $80^\circ > 60^\circ > 40^\circ$

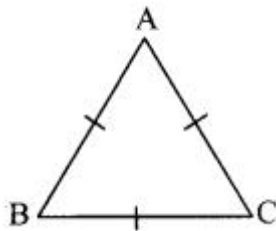
$$\therefore \angle F > \angle N > \angle A$$

$\therefore AN > FA > FN$  [Side opposite to greater angle is greater]

$\therefore$  In  $\triangle FAN$ ,  $AN$  is the greatest side and  $FN$  is the smallest side.

Question 5.

Prove that an equilateral triangle is equiangular.



Given:  $\triangle ABC$  is an equilateral triangle.

To prove:  $\triangle ABC$  is equiangular

i.e.  $\angle A \cong \angle B \cong \angle C$  ... (i) [Sides of an equilateral triangle]

In  $\triangle ABC$ ,

$\text{seg } AB \cong \text{seg } BC$  [From (i)]

$\therefore \angle C = \angle A$  (ii) [Isosceles triangle theorem]

In  $\triangle ABC$ ,

$\text{seg } BC \cong \text{seg } AC$  [From (i)]

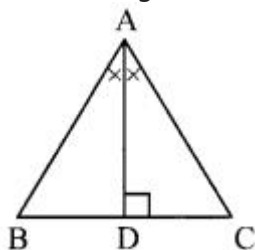
$\therefore \angle A \cong \angle B$  (iii) [Isosceles triangle theorem]

$\therefore \angle A \cong \angle B \cong \angle C$  [From (ii) and (iii)]

$\therefore \triangle ABC$  is equiangular.

Question 6.

Prove that, if the bisector of  $\angle BAC$  of  $\triangle ABC$  is perpendicular to side  $BC$ , then  $\triangle ABC$  is an isosceles triangle.



Given: Seg  $AD$  is the bisector of  $\angle BAC$ .

$\text{seg } AD \perp \text{seg } BC$

To prove:  $\triangle ABC$  is an isosceles triangle.

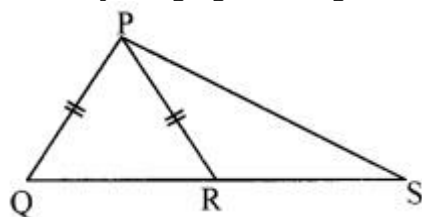
Proof.

In  $\triangle ABD$  and  $\triangle ACD$ ,

$\angle BAD \cong \angle CAD$  [seg AD is the bisector of  $\angle BAC$ ]  
seg AD  $\cong$  seg AD [Common side]  
 $\angle ADB \cong \angle ADC$  [Each angle is of measure  $90^\circ$ ]  
 $\therefore \triangle ABD \cong \triangle ACD$  [ASA test]  
 $\therefore$  seg AB  $\cong$  seg AC [c. s. c. t.]  
 $\therefore \triangle ABC$  is an isosceles triangle.

Question 7.

In the adjoining figure, if seg PR  $\cong$  seg PQ, show that seg PS > seg PQ.



Solution:

Proof.

In  $\triangle PQR$ ,

seg PR  $\cong$  seg PQ [Given]

$\therefore \angle PQR \cong \angle PRQ$  ....(i) [Isosceles triangle theorem]

$\angle PRQ$  is the exterior angle of  $\triangle PRS$ .

$\therefore \angle PRQ > \angle PSR$  ....(ii) [Property of exterior angle]

$\therefore \angle PQR > \angle PSR$  [From (i) and (ii)]

i.e.  $\angle Q > \angle S$  ....(iii)

In  $\triangle PQS$ ,

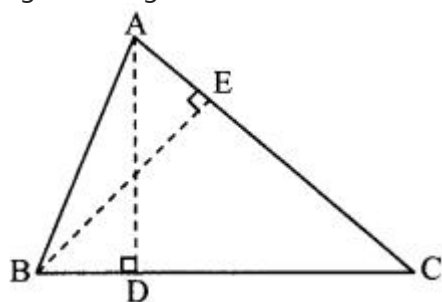
$\angle Q > \angle S$  [From (iii)]

$\therefore$  PS > PQ [Side opposite to greater angle is greater]

$\therefore$  seg PS > seg PQ

Question 8.

In the adjoining figure, in  $\triangle ABC$ , seg AD and seg BE are altitudes and AE = BD. Prove that seg AD = seg BE.



Solution:

Proof:

In  $\triangle ADB$  and  $\triangle BEA$ ,

seg BD  $\cong$  seg AE [Given]

$\angle ADB \cong \angle BEA = 90^\circ$  [Given]

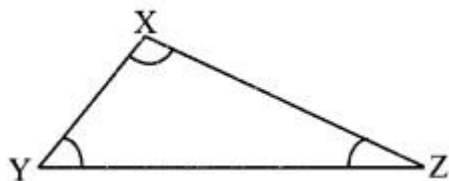
seg AB  $\cong$  seg BA [Common side]

$\therefore \triangle ADB \cong \triangle BEA$  [Hypotenuse-side test]  
 $\therefore \text{seg AD} \cong \text{seg BE}$  [c. s. c. t.]

### Maharashtra Board Class 9 Maths Chapter 3 Triangles Practice Set 3.4 Intext Questions and Activities

Question 1.

As shown in the given figure, draw  $\triangle XYZ$  such that side  $XZ >$  side  $XY$ . Find which of  $\angle Z$  and  $\angle Y$  is greater. (Textbook pg. no. 41)



Answer:

From the given figure,  $\angle Z = 25^\circ$  and  $\angle Y = 51^\circ$

$\therefore \angle Y$  is greater.

## Practice Set 3.5 Geometry 9th Std Maths Part 2 Answers Chapter 3 Triangles

Question 1.

If  $\triangle XYZ \sim \triangle LMN$ , write the corresponding angles of the two triangles and also write the ratios of corresponding sides.

Solution:

$\triangle XYZ \sim \triangle LMN$  [Given]

$\therefore \angle X \cong \angle L$

$\angle Y \cong \angle M$

$\angle Z \cong \angle N$  [Corresponding angles of similar triangles]

$XY/LM = YZ/MN = XZ/LN$  [Corresponding sides of similar triangles]

Question 2.

In  $\triangle XYZ$ ,  $XY = 4$  cm,  $YZ = 6$  cm,  $XZ = 5$  cm. If  $\triangle XYZ \sim \triangle PQR$  and  $PQ = 8$  cm, then find the lengths of remaining sides of  $\triangle PQR$ .

Solution:

$\triangle XYZ \sim \triangle PQR$  [Given]

$\therefore XY/PQ = YZ/QR = XZ/PR$  [Corresponding sides of similar triangles]

$\therefore PR = 10 \text{ cm}$   
 $\therefore QR = 12 \text{ cm}, PR = 10 \text{ cm}$

Question 3.

Draw a sketch of a pair of similar triangles. Label them. Show their corresponding angles by the same signs. Show the lengths of corresponding sides by numbers in proportion.

Solution:

$$\triangle GHI \sim \triangle STU$$

### **Maharashtra Board Class 9 Maths Chapter 3 Triangles Practice Set 3.5 Intext Questions and Activities**

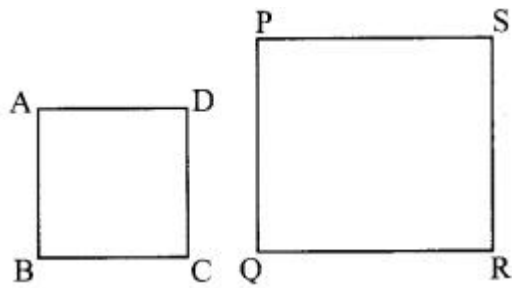
Question 1.

We have learnt that if two triangles are equiangular then their sides are in proportion. What do you think if two quadrilaterals are equiangular? Are their sides in proportion? Draw different figures and verify. Verify the same for other polygons. (Textbook pg no 50)

Answer:

If two quadrilaterals are equiangular then their sides will not necessarily be in proportion.

Case 1: The two quadrilaterals are of the same type.

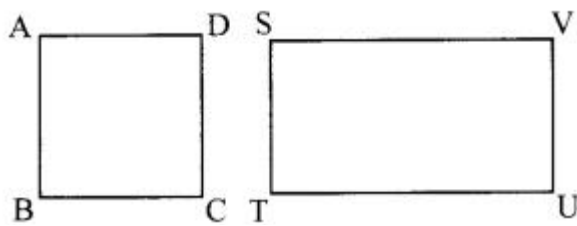


Consider squares ABCD and PQRS.

$$\angle A = \angle P, \angle B = \angle Q, \angle C = \angle R, \angle D = \angle S$$

$$ABPQ = BCQR = CDRS = ADPS$$

Case 2: The two quadrilaterals are of different types.



Consider square ABCD and rectangle STUV.

$$\angle A = \angle S, \angle B = \angle T, \angle C = \angle U, \angle D = \angle V$$