

Nets and solid shapes

- Constructing a net for a solid shape
- Finding the surface area of a solid shape
- Relating the number of vertices, faces and edges of a solid shape

Keywords

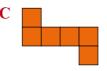
You should know

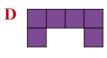
explanation 1

1 a Which of these diagrams could be used as a net for a cube?



В

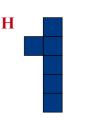




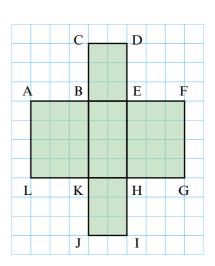




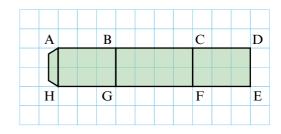




- **b** How many vertices does a cube have?
- **c** How many faces?
- d How many edges?
- **2** The diagram shows a partly completed net for a cuboid drawn on a grid of 1 cm squares.
 - **a** What shape is needed to complete the net? Give its size.
 - b There are a number of options for where to place the missing part. List the edges where it could be attached.
 - **c** When the cuboid is made, which points will
 - i meet A
- ii be furthest from E
- **d** Give the dimensions of the completed cuboid.
- e Find the area of each of these rectangles.
 - i ABKL
- ii CDEB
- iii BEHK
- **f** Work out the total surface area of the cuboid.



- **3** The diagram shows a partly completed net for a cuboid on a grid of 1 cm squares.
 - a Copy the diagram and complete it by drawing rectangles on the edges BC, DE and FE.

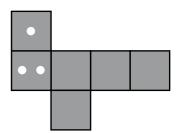


- b The net has a flap on the edge AH.

 How many flaps are needed altogether? Add the necessary flaps to your net.
- **c** Work out the surface area of the cuboid.
- **4** Copy this net for a cube onto paper or card and add any necessary flaps.

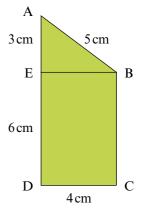
The cube is to be made into a dice.

- **a** Complete the labels so that opposite faces add up to 7. In how many ways can this be done?
- **b** Make the dice.



explanation 2

- **5** Here is a partly completed net for a triangular prism.
 - a Copy and complete the sketch by adding a triangle to the edge DC and rectangles to ED and BC. Include the measurements on your sketch.
 - **b** Work out the surface area of the triangular prism.
 - **c** Which of the labelled points will be furthest from A when the prism is complete?
 - **d** Find the numbers of vertices, faces and edges of a triangular prism.

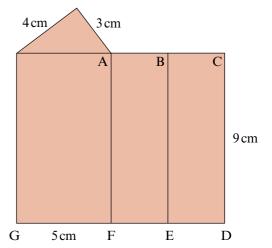


6 Kay found the surface area of the prism in question **5** with this calculation.

$$3 \times 4 + 6(3 + 4 + 5)$$

- a Explain why Kay's method works.
- **b** Write an expression to find the surface area of a prism twice as long, but otherwise the same as the one in question 5.
- **c** Use your expression to calculate the surface area of this prism.

- 7 Here is a partly completed net of a triangular prism.
 - a Write down the length of
 - i AB
- ii BC
- b Copy the net and complete it by adding a triangle to the edge GF. Label the lengths of its sides.
- c Repeat part b but, this time, attach the triangle to the edge FE.
- **d** Work out the surface area of the triangular prism.



2cm

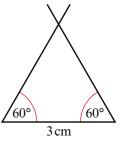
 \mathbf{C}

3cm

D

В

- 8 Read the whole question before you do part a.
 - **a** Use a ruler and protractor to construct the triangle shown. Check that each side is 3 cm long.
 - **b** Use your triangle as part of a net for a triangular prism of length 5 cm.
 - c Add flaps to your net and make the prism.



F

E

G

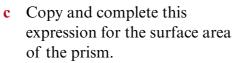
- **9** The diagram shows the net of a prism.
 - **a** Which labelled point will be joined to A when it is complete?
 - **b** Write down these lengths
 - i AB

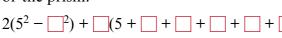
ii BC

- iii CD
- iv DE

8cm

- v EF
- vi FG

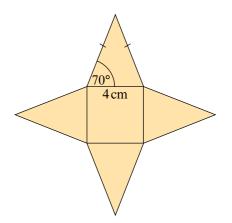




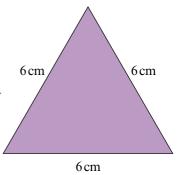
- **d** What is the surface area?
- e Find the number of vertices, faces and edges of the prism.
- f What is the smallest shape that can be added to the prism to make a cuboid?

explanation 3

- **10 a** Construct the net shown for a square-based pyramid and add any flaps as necessary.
 - **b** Cut out the net and make the pyramid.
 - c The angle at the base of the triangle is 70°. What would happen if this angle was 45°?
 - **d** Find the number of vertices, faces and edges of the pyramid.



- **11** a Construct the triangle shown below.
 - **b** Join the midpoints of the sides to make the net of a tetrahedron and add the flaps.
 - **c** Cut out the net and fold to make the tetrahedron.
 - **d** Find the number of vertices, faces and edges of the tetrahedron.



12 a Use your results from questions 1, 5, 9, 10 and 11 to complete the table.

Shape	Vertices (V)	Faces (F)	Edges (E)
Cube			
Triangular prism			
Prism			
Square-based pyramid			
Tetrahedron			

- **b** Try to find a formula connecting the values of V, F and E.
- **13** Find the length of each edge of a cube if its surface area is
 - $a 96 \text{ cm}^2$
- **b** 216 cm²
- $c 486 \, cm^2$