



## Using equations

- How to solve equations involving brackets
- How to form and solve simple equations

Keywords

You should know

explanation 1a

explanation 1b

explanation 1c

explanation 1d

**1** Solve these equations.

**a**  $2n = 6$

**b**  $3p + 1 = 4$

**c**  $5y - 2 = 13$

**d**  $3x - 2 = 16$

**e**  $8 = 12a - 4$

**f**  $22 = 6b - 8$

**g**  $12 + 4p = 4$

**h**  $6a + 1 = -5$

**i**  $5d - 4 = -19$

**2** Each table gives instructions for solving an equation. Copy and complete.

**a** Solve  $5x - 2 = 3x + 9$

Action to both sides	Effect
$- 3x$	$2x - 2 = 9$
$+ 2$	$2x = 11$
$\div 2$	

**b** Solve  $x - 3 = 7x - 15$

Action to both sides	Effect
$- x$	
$+ 15$	
$\div 6$	

**c** Solve  $12k + 7 = 2k$

Action to both sides	Effect
$- 2k$	
$- 7$	
$\div 10$	

**d** Solve  $\frac{p}{2} + 9 = 3p$

Action to both sides	Effect
$\times 2$	
$- p$	
$\div 5$	

**3** Solve these equations using a method similar to question 2.

**a**  $8x - 19 = 5x + 2$

**b**  $6a - 7 = 2a + 13$

**c**  $3x - 4 = 10x - 25$

**d**  $7x - 2 = 10x - 5$

**e**  $2 + 8x = 5x + 8$

**f**  $7k - 3 = 5k - 6$

4

How do I solve  
 $24 = 9 - 3m$ ?

Add  $3m$  to both sides first  
to make the  $m$  positive. Then  
try to solve the equation.



**a** Follow Jane's advice and solve  $24 = 9 - 3m$ .

**b** Explain how to solve  $30 - 10p = 9$ .

**5** Solve these equations.

**a**  $x = 12 - 3x$

**b**  $5 - 2n = n + 17$

**c**  $12 - m = 17 - 11m$

explanation 2a

explanation 2b

explanation 2c

**6** Solve these equations.

**a**  $2(x + 1) = 6$

**b**  $5(m - 2) = 15$

**c**  $5 = 2(a - 1)$

**d**  $4(p - 6) = 0$

**e**  $3(y + 6) - 24 = 0$

**f**  $2(z + 1) + 3 = 5$

**g**  $\frac{x+1}{2} = 3$

**h**  $\frac{8}{b} = 4$

**i**  $5 + \frac{8}{c} = 21$

**j**  $4 - \frac{9}{k} = 7$

**k**  $\frac{3}{p} + 4 = 0$

**l**  $\frac{25}{g} = g$

**7** Copy and complete the table to solve the equation  $-3 = \frac{1+q}{1-q}$ .

Action to both sides	Effect
Multiply by $(1 - q)$	
Subtract $q$	
Add 3	
Divide by 2	

**8**

How do I solve  
 $6(2y - 1) - (8y - 3) = 21$ ?

Collect like terms.  
 But first check the  
 second line.



$6(2y - 1) - (8y - 3) = 21$   
 $\rightarrow 12y - 6 - 8y - 3 = 21$   
 one mistake

- a** What error has Ellie made in her second line? Complete the solution for her.  
**b** Solve  $3(4n - 1) - 2(2n - 7) = 51$ .

**9** Solve each equation. Use a method similar to questions **8**.

- |                                      |                                     |
|--------------------------------------|-------------------------------------|
| <b>a</b> $5(x - 4) + 3(x + 12) = 0$  | <b>b</b> $8 + 4(2x + 5) = x$        |
| <b>c</b> $3(x + 2) - (x - 1) = 8$    | <b>d</b> $7(x - 1) - 2(x - 3) = 14$ |
| <b>e</b> $3(2x - 3) + 2(1 - 2x) = 6$ | <b>f</b> $9x + 14 = 2(3x + 8)$      |
| <b>g</b> $5(1 - 3x) = 4(2 - 3x)$     | <b>h</b> $5(x - 1) = 3(x + 5)$      |

explanation 3a

explanation 3b

**10** Brian, Keith and Nadeem each write an expression on a piece of card.

$2(3x + 5)$   
 Brian

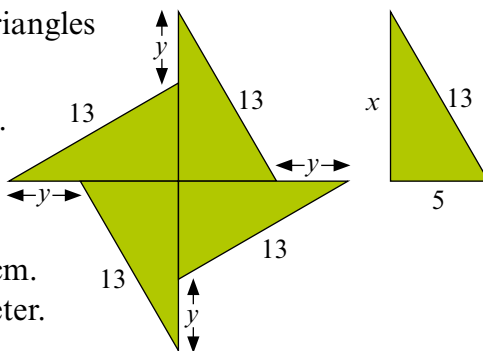
$10(x + 2)$   
 Keith

$2x - 39$   
 Nadeem

- a** What value of  $x$  makes the value of Brian's card equal to Keith's card?  
**b** Find the value of  $x$  that makes the sum of all these cards equal to zero.

- 11** A logo is made by placing four identical triangles together.

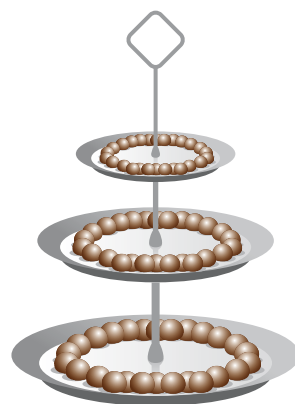
- a** Write an expression for  $y$  in terms of  $x$ .
- b** Write an expression for the perimeter of the logo. Simplify it.
- c** The actual perimeter of the logo is 80 cm. Write down an equation for the perimeter. Solve it to find  $x$ .



- 12** Handmade chocolates are arranged on a three-tier tray. The top tray contains 10 fewer chocolates than the middle tray. The bottom tray contains 3 times as many as the top tray.

Let  $x$  be the number of chocolates on the middle tray.

- a** Write the number of chocolates on the top tray in terms of  $x$ .
- b** How many chocolates are on the bottom tray? Give your answer in terms of  $x$ .
- c** There are 70 chocolates altogether. Write an equation and solve it to find  $x$ .
- d** How many chocolates are there on each tray?



- 13** At the start of a game, Peter and Sheila had 70 marbles altogether. They played a game and Peter lost 10 marbles to Sheila.

Let  $m$  be the number of marbles Peter had at the start.

- a** Copy and complete the table.

	Peter	Sheila
Number of marbles at the start of the game	$m$	
Number of marbles at the end of the game		

- b** At the end of the game, Sheila had four times as many marbles as Peter. Write an equation, in terms of  $m$ , to show this. Solve it to find the value of  $m$ .
- c** How many marbles did Peter have at the end of the game?



**14** Mrs Logan wrote a negative number on the board. She called the number  $n$ .

- a** Sarah added 3 to the number, and then multiplied her answer by 8.  
Write an expression for her result.
- b** David multiplied the original number by 6, and then added 2.  
Write an expression for his result.
- c** Sarah and David got the same final answer. Use your answers to parts **a** and **b** to write an equation. Solve it to find the value of  $n$ .

**15** David and Julie had 60 minutes of call time altogether.  
They each phoned a friend. David used 1 minute and Julie used 4 minutes.  
David then had four times as much call time as Julie had.

Let  $t$  be the number of minutes David had before he phoned his friend.

- a** Copy and complete the table.

	David	Julie
Number of minutes before call	$t$	
Number of minutes remaining after call		



- b** Write an equation and solve it to find  $t$ .

**16** A barrel contained 11 litres of water. Another barrel contained 3 litres of water. Linda added  $x$  litres of water to both barrels. The first barrel then had three times as much water as the second barrel had.

- a** Draw and complete a table, like that in question **15**.
- b** Write an equation in terms of  $x$ .
- c** Solve your equation to find the value of  $x$ .  
How much water was in each barrel after Linda added the extra water?

- 17** At the start of their holiday, Christine and Gavin had \$120 altogether.  
At the airport, their aunt gave them another \$21 each.  
Gavin then had twice as much as Christine.

Let  $x$  represent the amount Christine had before her aunt gave her \$21.

- a** Copy and complete the table.

	Christine	Gavin
At the start of the holiday	$x$	
At the airport		



- b** Write an equation and solve it to find  $x$ .  
**c** How much money did Gavin have at the airport?

- 18** Write an equation for each shape and solve it.

