Geometry and measures GM1.2

Circles

- Identifying different parts of a circle
- Finding the circumference of a circle
- Finding the area of a circle

Keywords

You should know

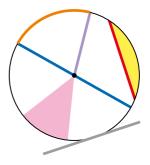
explanation 1a

explanation 1b

explanation 1c

explanation 1d

1 Each of the seven colours shows a different part of the circle.



- a Describe what each colour shows. The yellow part has been done for you.
 - Yellow: A segment is the shape formed by cutting off part of a circle with a straight line.
- **b** What would the orange part become if it stretched all round the edge of the circle?
- **c** What is half the blue line?
- **d** Write down one fact about the grey line.
- **2** The diagrams show different circles. Describe each circle as 'circumscribed' or 'inscribed'.

a



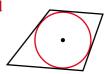
b



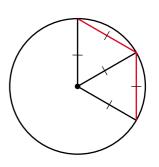
c



d



- **3** The diagram shows a circle with two chords, the same length as the radius, joined to the centre by radii.
 - **a** What type of triangles are created?
 - **b** What are the angles in each of the triangles?
 - c How many of these triangles will fit inside the circle?
 - **d** What polygon is formed?



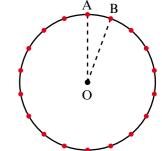
- **4** Explain how to draw a hexagon where all the sides are 4cm. Draw this polygon.
- 5 Jade wants to draw some regular polygons. She starts by drawing a circle of radius 5 cm and marking a radius with a dashed line.
 - a Describe how Jade can draw these shapes.
 - i regular pentagon
- ii regular heptagon
- **b** Draw the pentagon and measure the length of each side.
- **c** Draw the heptagon and measure the length of each side.
- **d** Ask your teacher for the actual lengths. How accurate are your drawings?

explanation 2a

explanation 2b

explanation 2c

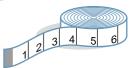
6 Jack wants to check that the formula $C = \pi d$ works out the circumference of a circle. He draws a circle with radius 6 cm and divides it into 18 equal parts. Jack measures the straight-line distance AB with a ruler. It is 2.1 cm.



- **a** Using Jack's measurement of AB, explain how to approximate the circumference of the circle.
- **b** Work out an approximate value for the circumference.
- c How could you improve the estimation of the circumference?
- **d** Work out the circumference using $C = \pi d$, when d = 12 cm. Compare this with your approximate value.

- 7 A tin of tuna has a diameter of 8.5 cm. Riaz measures the circumference using a tape measure. The measured length is 27 cm.
 - a Use a formula to calculate the circumference to 1 decimal place.
 - **b** Which gives the most accurate answer, measuring or calculating?





8 The table shows the measurements of five circles. Complete the table. Use the formula $C = \pi d$ to calculate each circumference C to 1 decimal place.

Diameter (cm)	6	9			
Radius (cm)			5	20	26
C (cm)	8 •	□ □ • 3	3 🗆 • 🔲	1	6

9 Find the circumference of each coin correct to 1 decimal place.



diameter 20.3 mm



radius 9 mm



radius 12.5 mm



diameter 22.5 mm



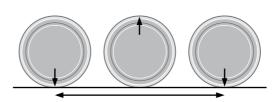
radius 14.2 mm



diameter 2.33 cm

- Bella says that she uses C = πd to find the circumference of a circle.
 Bhavin says he uses C = 2πr.
 Explain why these two formulae give the same answer for the circumference.
- 11 a Sahib rolls a baked bean tin on its side for one complete revolution.





The radius of the tin is 3.7 cm. How far has it moved along the table?

b Gina has a tin of golden syrup, with a diameter of 8.1 cm. How much further does Gina's tin roll along the table after one revolution than Sahib's?

- 12 Sherman has a counter device on his bike. It counts the number of revolutions his wheel has made. His wheels are 40 cm in diameter.
 - a Sherman rides to his grandmother's house.The counter reads 1989.How far away does his grandmother live?
 - b How many revolutions does his wheel have to make to travel 1 km?



- **13** Keefe's dad has a measuring wheel with a 5-digit counter. The radius of the wheel is 12 cm.
 - **a** Find the circumference of the measuring wheel in metres.
 - Keefe and his dad use this to measure the length of the school football pitch.The counter shows a reading of 106 revolutions. How long is the pitch?



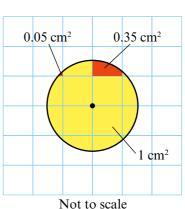
c One of the shortest pitches in the Football Premier League has a length of 100.6 m.

To make the school pitch the same length, what number would the counter have to read?

explanation 3a

explanation 3b

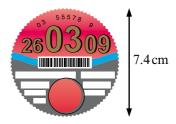
- **14** Chika is counting squares to estimate the area of the circle. Each square is 1 cm².
 - **a** Estimate the area of the circle by counting full and part squares.
 - **b** What is the radius of this circle?
 - c Use the formula $A = \pi r^2$ to find the area of the circle.
 - **d** Which is the more accurate way of finding how many square centimetres fit inside a circle?
 - e Give two reasons why π is an important number.



- **15** Here are two letters and three expressions that people often get mixed up.
 - r, d, πd , $2\pi r$, πr^2

Describe the meaning of each expression.

16 What is the area of a car tax disc?

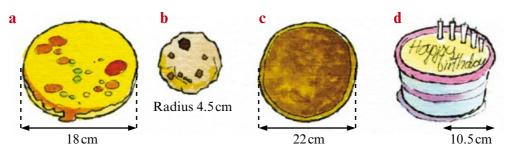


- 17 Find the area of circles with each of the following measurements. Give your answers correct to 2 decimal places.
 - \mathbf{a} radius = 8 cm

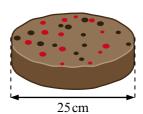
b diameter = $11 \, \text{cm}$

c radius = 6.8 cm

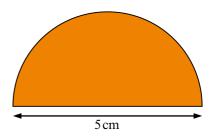
- d diameter = 3.6 cm
- **18** Find the area of the top of the cheesecake, cookie, pizza and birthday cake. Give your answers correct to 2 decimal places.



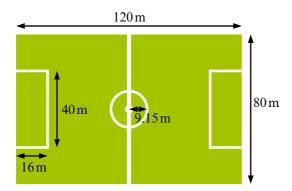
- 19 How much ribbon would be needed to fit round the edge of the birthday cake in question 18?
- **20** The diagram shows a fruit cake.
 - **a** How many square centimetres of marzipan are needed for the top of the fruit cake?
 - **b** A ribbon is fastened round the edge of the cake. How many centimetres of ribbon are needed if there is to be a 1 cm overlap of ribbon?



- **21** The diagram shows a semicircle.
 - **a** Explain to your partner how to find the area of the semicircle correct to 2 decimal places.
 - **b** Ask your partner to explain how to find the perimeter of the semicircle correct to 2 decimal places.



- **22** The centre circle of a football pitch has a radius of 9.15 m.
 - a Find the area of the centre circle to nearest square metre.
 - **b** Find the circumference of the centre circle to 1 decimal place.

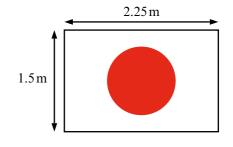


23 The Japanese flag has a white background with a red circle to represent the sun.

The radius of the red circle is $\frac{3}{10}$ of the height of the flag.



- **b** Find the area of the red circle.
- c What is the area of the white part of the flag?



- **24** The diagram shows a pattern on a circle.
 - a Find the area of the whole circle.
 - **b** Find the area of the red region of the circle.

