Fractions and percentages of amounts

Calculating a fraction of an amount

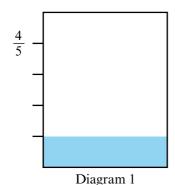
Calculating a percentage of an amount

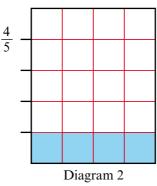
Keywords

You should know

explanation 1

1 Here are some diagrams divided into smaller parts.





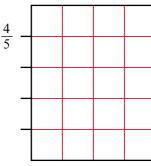
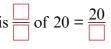


Diagram 3

- What fraction of Diagram 1 is blue?
- Copy Diagram 2 and write the missing fractions on the vertical scale.
- Copy and complete.

The number of blue squares in Diagram 2 is $\frac{1}{100}$ of $20 = \frac{20}{100}$



- Copy Diagram 3 and shade $\frac{4}{5}$ of the squares.
- Copy and complete.

The number of shaded squares in Diagram 3 is $\frac{4}{5}$ of $20 = \square \times \frac{1}{5}$ of 20

 $= \Box$

- 2 a $\frac{1}{5}$ of a number is 23. What is of $\frac{2}{5}$ the number?
 - **b** $\frac{1}{11}$ of a number is 32. What is $\frac{3}{11}$ of the number?

- 3 a i Copy and complete. $\frac{1}{3} = \frac{\square}{9}$
 - ii $\frac{1}{9}$ of a number is 42. What is $\frac{1}{3}$ of the number?
 - **b** i Copy and complete. $1 = \frac{\square}{5}$
 - ii $\frac{1}{5}$ of a number is 61. What is the number?
- 4 A man spent $\frac{1}{3}$ of each day sleeping. He lived for 78 years.

How much time did he spend asleep?



5 Work out these amounts.

a i
$$\frac{1}{5}$$
 of 40

ii
$$\frac{2}{5}$$
 of 40

iii
$$\frac{3}{5}$$
 of 40

b i
$$\frac{1}{10}$$
 of 60 ii $\frac{3}{10}$ of 60 iii $\frac{7}{10}$ of 60

ii
$$\frac{3}{10}$$
 of 60

iii
$$\frac{7}{10}$$
 of 60

c i
$$\frac{1}{12}$$
 of 36

ii
$$\frac{5}{12}$$
 of 36

ii
$$\frac{5}{12}$$
 of 36 iii $\frac{11}{12}$ of 36

d i
$$\frac{1}{7}$$
 of 28

ii
$$\frac{2}{7}$$
 of 28

iii
$$\frac{5}{7}$$
 of 28

6 Write down the missing numbers.

a
$$\frac{\Box}{5}$$
 of 20 = 12

b
$$\frac{3}{8}$$
 of $\square = 21$

b
$$\frac{3}{8}$$
 of $\square = 21$ **c** $\frac{11}{\square}$ of $24 = 22$

d
$$\frac{5}{10}$$
 of 27 = 15

e
$$\frac{7}{20}$$
 of $\Box = 35$

d
$$\frac{5}{10}$$
 of 27 = 15 **e** $\frac{7}{20}$ of $\square = 35$ **f** $\frac{\square}{50}$ of 200 = 52

- **7** Find the number of minutes in these fractions of an hour.
 - **a** $\frac{1}{2}$

b $\frac{1}{4}$

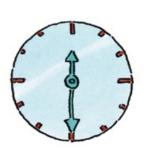
d $\frac{5}{12}$

- $e \frac{1}{6}$
- **f** $\frac{5}{6}$

 $\frac{2}{3}$

- **h** $\frac{7}{10}$
- $i \frac{2}{5}$

 $\frac{4}{15}$



8 Find the number of degrees in these fractions of a turn.

There are 360° in a complete turn.

e $\frac{2}{3}$ f $\frac{3}{10}$

explanation 2a

explanation 2b

9 Work out these values.

a $\frac{2}{5} \times 30$ **b** $\frac{3}{4} \times 64$ **c** $\frac{6}{25} \times 75$

d $20 \times \frac{7}{10}$ **e** $32 \times \frac{11}{16}$ **f** $21 \times \frac{3}{7}$

10 Write the following as mixed numbers.

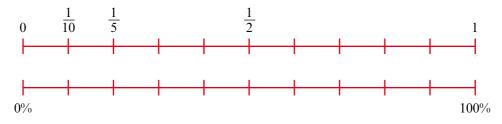
 $\frac{1}{3}$ of 8

b $15 \times \frac{1}{4}$ **c** $\frac{2}{3}$ of 11

d $\frac{3}{5} \times 9$ **e** $\frac{3}{4}$ of 21 **f** $44 \times \frac{5}{8}$

explanation 3

a Copy the diagram and fill in the missing values.



b Use your diagram to write these fractions as percentages.

 $\frac{1}{10}$

ii $\frac{3}{5}$

iii $\frac{9}{10}$

iv $\frac{2}{5}$

c Use your diagram to write these percentages as fractions.

i 20%

ii 50%

iii 70% iv 60%

- **12** Copy and complete.
 - **a** 30% of $40 = \frac{3}{100}$ of 40
- **b** 80% of 30 = \Box of 30
- 13 Work these out by writing the percentages as fractions.
 - **a** 20% of 60
- **b** 50% of 86
- c 25% of 36

- **d** 10% of 3000
- e 75% of 140
- **f** 90% of 1200

- **g** 40% of 65
- **h** 25% of 24
- i 60% of 25

explanation 4

- **14** Work these out and give your answers as decimals.
 - **a** 10% of 34
- **b** 50% of 8.6
- c 25% of 18

- **d** 30% of 25
- e 70% of 24
- **f** 10% of 6.9

- **15** Find 10% of each of these amounts.
 - **a** £80
- **b** £300
- c £1700
- d £25 000

- e £92
- **f** £7
- **g** £234
- **h** £67.50

- **i** £9.40
- £27.80
- **k** £0.70
- £1.50

- **16** Work out these values.
 - **a** 10% of £64
- **b** 5% of £64 **c** 15% of £64
- **d** 15% of £128

- **17** Work out these amounts.
 - a 10% of 46 kg
- **b** 20% of 46kg **c** 30% of 46kg

- **d** 15% of 46 kg
- e 10% of £24
- f 5% of £24

- **g** 2.5% of £24

- **h** 17.5% of £24 **i** 50% of 60 m

- 5% of 60 m
- **k** 45% of 60 m **l** 55% of 60 m

- **m** 50% of 84 g
- **n** 25% of 84 g **o** 12.5% of 84 g

Look for ways to use one answer to work out another.

- **18** Use the methods of question 17 to work these out.
 - **a** 20% of £70
- **b** 5% of 80 cm
- c 25% of 140 mm

- **d** 30% of £16
- e 12.5% of 48 g
- **f** 45% of 40 litres

- g 15% of 32 km
- h 7.5% of 120 people i 55% of 800 tonnes

19 a Copy and complete.

$$3 \times 33\frac{1}{3} = 3(33 + \square)$$

= 99 + \square
= \square

- **b** Write $33\frac{1}{3}\%$ as a fraction in its lowest terms.
- **20** a Find $33\frac{1}{3}\%$ of 21 m b Find $66\frac{2}{3}\%$ of 45 oz
- 21 A top sprinter can run at a speed of about 10 m/s.

A little-known fact is that some crocodiles can reach up to 40% of this speed.

How fast can these crocodiles run?



- **22** Find the sale price for each of these marked prices.
 - a Coat £93
- b Jacket £45
- c Jeans £27
- d Shirt £36
- e Boots £57
- f Jumper £25.80

- Sale Everything must go. 33_1% off
- **23** A salesperson earns 15% commission on sales.

Find the commission earned on each of these amounts.

£340

b £624

£2700

- **d** £84.60
- e £112.40
- £99
- **24** A car costing £81 000 lost $66\frac{2}{3}\%$ of its value after 4 years.

What was it then worth?