Mental methods (2)

- **Knowing mental strategies for working out calculations**
- Knowing mental strategies for solving problems involving fractions, decimals and percentages
- **Estimating the square roots of non-square numbers**
- Estimating the answer to calculations by rounding

Keywords

You should know

explanation 1a

explanation 1b

1 Work out these sums mentally.

$$e 81 + 16$$

$$f 475 + 38$$

2 Work out these subtractions mentally.

- **3** Work out in your head the change given for each item of shopping.
 - Seven pens costing 48p each and paid for using a £5.00 note.
 - **b** A rubber costing 37p and a ruler costing 54p paid for using a £1.00 coin.
 - c A magazine costing £1.70 and a newspaper costing 63p paid for using a £5.00 note.
 - d Some fruit costing £2.68 and some flowers costing £3.75 paid for using a £10.00 note.
 - e Food costing £38.72 and paid for using a £50.00 note.
 - A service for a car costing £129.25 and paid for using three £50.00 notes.



explanation 2

4 Work out these multiplications mentally.

- **a** 27×0.2
- **b** 55×0.3
- c 72×0.4
- **d** 125×0.02

- e 320×0.04
- $f 410 \times 0.05$
- **g** 228×0.02
- **h** 820×0.04

5 a A child's moneybox contains thirty-six 20p coins. How much money, in pounds, is this?

- **b** A biro cost 40p. Calculate the cost, in pounds, of buying sixty biros.
- c A sausage machine produces one hundred and twenty sausages each hour. Each sausage is 8 cm long.

Calculate the total length, in metres, of sausages produced in these times.

- i 1 hour ii 8 hours
- d A child's footprint is 15 cm long. Calculate the total distance, in metres, walked after two hundred and eighty footsteps when she walks so that her footsteps lie end to end.

explanation 3

6 Work out these multiplications mentally.

- **a** 23 × 11
- **b** 16 × 11
- c 32 × 12
- **d** 45 × 19

- **e** 65 × 19
- **f** 125 × 29
- **g** 140×51
- **h** 23 × 99

7 Work these out.

- **a** The total number of pupils in 22 classes of 31 pupils each.
- **b** The area of a rectangle 32 cm long and 19 cm wide.
- c The area of a square garden of edge length 29 m.
- d The number of chairs in a hall, when there are 29 rows and 15 chairs in each row.

8 Work these out mentally.

- **a** $220 + 6 \times 19$
- **b** $39 \times 8 71 \times 3$
- $c 49^2$

9 59 people pay £19.99 each to go on a coach trip.

> Work out mentally how much they pay altogether.



explanation 4

10 Work these out mentally.

a 930 ÷ 15

b $612 \div 12$ **c** $504 \div 18$

d 288 ÷ 9

e 720 ÷ 120

 $f 1155 \div 21$

g $784 \div 28$

h 2688 ÷ 24

i 207 ÷ 1.8

 $155 \div 2.5$

 $k 119 \div 0.35$

 $1 22.56 \div 0.16$

11 Work these out.

a 810 people are split equally into 15 groups. How many people are there in each group?

- **b** A lottery win of £115680 is shared equally by a syndicate of 12 people. How much does each person receive?
- **12** Rob can walk 2.6 miles in an hour. He is planning an 11.7 mile walk. Without using a calculator, work out how long it will take him to complete the walk.



explanation 5a

explanation 5b

explanation 5c

13 Copy and complete these tables without using a calculator.

Decimal	Fraction	Percentage
	$\frac{1}{2}$	
0.25		
0.333		
	<u>1</u>	
		20%
0.666		
	$\frac{3}{4}$	

Decimal	Fraction	Percentage
	1/8	
	$\frac{\frac{1}{8}}{\frac{5}{8}}$	
		80%
		150%
1.2		
	$\frac{29}{20}$ $\frac{5}{2}$	
	$\frac{5}{2}$	

14 Work these out mentally.

- 50% of 40
- **b** 25% of 80
- **c** $\frac{1}{10}$ of 120 **d** $\frac{3}{10}$ of 120

- 0.1 of 70
- **f** 0.4 of 70
- **g** 60% of 70
- **h** $\frac{2}{3}$ of 93

- $\frac{1}{8}$ of 248
- $\frac{5}{8}$ of 248
- k 120% of 50
- 160% of 90

- **m** 240% of 60
- 175% of 100
- 2% of 110
- 105% of 6

15 Work these out without using a calculator.

- a In a school of 320 pupils 45% are girls. How many girls are there?
- **b** In a typical family, $\frac{3}{8}$ of income is spent on food. Calculate how much is spent on food by a family with a monthly income of £1200.
- c In a survey of 450 earthworms, it was found that 36% were over 6 cm in length. How many earthworms in the survey were over 6cm long?
- **d** Due to high demand, a shop decides to increase the price of one of its games consoles by 11%. If the original price was £180, calculate the new selling price.
- Better Books decides to reduce the price of its books by $\frac{1}{3}$. What is the new price of a book that was originally selling for £24.90?

explanation 6

16 Use estimation to match the value of each square root to a number in the box.

a
$$\sqrt{5}$$

b
$$\sqrt{24}$$

$$d \sqrt{108}$$

$$\mathbf{f} = \sqrt{2}$$

$$\mathbf{g} = \sqrt{150}$$

$$h \sqrt{410}$$

17 Use your answers to question 16 to help find the approximate length of the side of a square with each area.

a Area =
$$34 \,\mathrm{cm}^2$$

b Area =
$$108 \,\text{m}^2$$

c Area =
$$5 \text{ m}^2$$

explanation 7a

explanation 7b

18 Estimate the answer to each calculation, showing your method clearly.

$$\mathbf{f} \quad \frac{12 \times 31}{5}$$

$$\frac{189 \times 211}{8}$$

h
$$8 \times \sqrt{17}$$

i
$$\sqrt{52} \times \sqrt{14}$$

$$\mathbf{j} \quad \frac{\sqrt{15} \times 89}{4}$$

$$\mathbf{k} \quad \frac{\sqrt{125} \times \sqrt{67}}{\sqrt{15}}$$

1
$$23^2 \times \sqrt{6}$$

$$\mathbf{m} \ \frac{31^2}{9 \times \sqrt{105}}$$

$$n \quad 19^2 \times 41^2 \times \sqrt{10}$$

$$\left(\frac{1}{3}\right)^2 \times 385$$

19 Sean estimates the value of $\frac{36 \times 29}{0.7}$ using $\frac{40 \times 30}{0.5}$.

- **a** Find the value of Sean's estimate. Is this larger or smaller than the true value?
- **b** Find a way to improve on Sean's estimate and work it out.
- **c** Use a calculator to find the true value to the nearest whole number.