Geometry and measures GM4.2

Measures

- Converting between measurements of area
- Converting between measurements of volume
- Finding the least and greatest length of a measurement
- Solving problems using compound units
- Converting between compound units

Keywords

You should know

explanation 1a

explanation 1b

explanation 1c

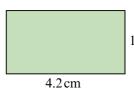
- 1 The length of a garden is given as 18 m correct to the nearest metre.
 - **a** What is the least possible length of the garden?
 - **b** What is the greatest possible length of the garden?
- **2** The length of a pencil is given as 7.6cm correct to the nearest millimetre.
 - a What is the greatest possible length of the pencil?
 - **b** What is the least possible length of the pencil?
- **3** The length of a road is given as 45 km correct to the nearest kilometre.
 - **a** What is the maximum possible length of the road?
 - **b** What is the minimum possible length of the road?
- **4** The weight of a baby is given as 4.3 kg correct to one decimal place.
 - **a** What is the least possible weight of the baby?
 - **b** What is the greatest possible weight of the baby?
- 5 Jack measures the length and width of a rectangle. He gives the length as 6.5 cm and the width as 4.3 cm. Both measurements are given correct to the nearest millimetre.
 - **a** What is the least possible length and width?
 - **b** What is the greatest possible length and width?

explanation 2a

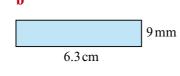
explanation 2b

- **6** Work out the area of each shape.
 - i Give your answer in square centimetres (cm²).
 - ii Give your answer in square millimetres (mm²).

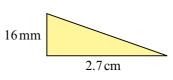
a



1.8 cm



c



- **7** Convert these areas to square millimetres.
 - $a 5 cm^2$
- **b** $2.3 \, \text{cm}^2$
 - c 68 cm²
- $d = 0.6 \,\mathrm{cm}^2$

- **8** Convert these areas to square centimetres.
 - $700 \, \text{mm}^2$
- $b 80 \text{ mm}^2$
- $c = 6320 \, \text{mm}^2$
- $d 8 \text{mm}^2$

- 9 Rajesh says: '3 m² is the same as 300 cm².' Rajesh is wrong. Explain why.
- **10** Convert these areas to square centimetres.
 - $a 5 m^2$
- **b** $2.8 \,\mathrm{m}^2$
- $c = 0.9 \,\mathrm{m}^2$
- $d = 0.056 \,\mathrm{m}^2$

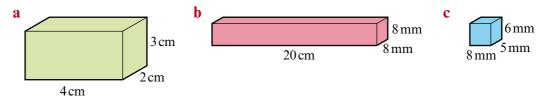
- **11** Convert these areas to square metres.
 - $a 40000 \,\mathrm{cm}^2$
- **b** $6700 \,\mathrm{cm}^2$ **c** $300 \,\mathrm{cm}^2$
- $d 345600 \text{ cm}^2$
- **12** Convert these areas to the units given in brackets.
 - a $5 \,\mathrm{cm}^2 \,\mathrm{(mm}^2\mathrm{)}$
- **b** $9 \,\mathrm{m}^2 \,\mathrm{(cm}^2)$
- $c 2 \text{km}^2 \text{ (m}^2\text{)}$

- $d 700 \, \text{mm}^2 \, (\text{cm}^2)$
- $e 8200 \, cm^2 \, (m^2)$
- $f 89000000 m^2 (km^2)$

- $g = 0.67 \, \text{cm}^2 \, (\text{mm}^2)$
- **h** $0.053 \,\mathrm{km^2 \, (m^2)}$ **i** $25 \,\mathrm{mm^2 \, (cm^2)}$
- $95 \, \text{cm}^2 \, (\text{m}^2)$
- $k 1 \text{ km}^2 \text{ (cm}^2)$
- $1 6 \text{ m}^2 \text{ (mm}^2\text{)}$

explanation 3

- **13** Work out the volume of each of these solids.
 - i Give your answers in cubic centimetres.
 - ii Give your answers in cubic millimetres.



- **14** Convert these volumes into cubic millimetres.
 - $\mathbf{a} \quad 8 \, \mathrm{cm}^3$
- **b** $23.5 \,\mathrm{cm}^3$
- $c = 0.04 \, \text{cm}^3$
- $d 4.35 \, cm^3$

- **15** Convert these volumes into cubic centimetres.
 - $a 60000 \, \text{mm}^3$
- **b** $250\,000\,\mathrm{mm}^3$
- $c 8000 \, \text{mm}^3$
- $\frac{d}{d}$ 780 mm³
- 16 A large fish tank is in the shape of a cuboid. It has a length of 1.2 m, width of 40 cm and height of 55 cm. Work out the volume of the fish tank.
 - a Give your answer in cubic metres.
 - **b** Give your answer in cubic centimetres.
- **17** Convert these volumes into cubic centimetres.
 - a 4 m³
- **b** $0.024\,\mathrm{m}^3$
- $c 12 \,\mathrm{m}^3$
- $d = 603.2 \,\mathrm{m}^3$

- **18** Convert these volumes into cubic metres.
 - $a 7000000 \text{ cm}^3$

b $56000 \,\mathrm{cm}^3$

 $c 680 \, cm^3$

- $d 723000000 \text{ cm}^3$
- **19** Convert these volumes to the units given in brackets.
 - **a** $5 \,\mathrm{m}^3 \,\mathrm{(cm}^3)$

- **b** $450 \,\mathrm{mm}^3 \,\mathrm{(cm}^3)$
- c 67 000 cm³ (m³)

- $\frac{d}{d}$ 0.4 cm³ (mm³)
- $e 0.009 \,\mathrm{m}^3 \,\mathrm{(cm}^3)$
- $f 2 km^3 (m^3)$

- $\mathbf{g} = 34\,000\,000\,\mathrm{m}^3\,\mathrm{(km}^3)$
- $1 \text{ m}^3 \text{ (mm}^3)$

explanation 4a

explanation 4b

- **20** An aeroplane travels 2500 km in 5 hours. Work out its average speed.
- 21 Jackie walks 9 km in 1 hour and 20 minutes. Work out her average speed. Give your answer in kilometres per hour.
- 22 A cyclist takes $1\frac{3}{4}$ hours to travel a distance of 63 km. What is her average speed?
- 23 A cyclist travels at a steady speed of 16km/h. How far will she travel in 1 hour and 15 minutes?
- 24 A man walks at 5 km/h. He walks 12.5 km. How long does the walk take him?
- 25 Alan goes out for the day. He catches the train to a village that is 30 miles away and then cycles back. The average speed of the train is 50 miles per hour. It takes Alan 2 hours and 30 minutes to cycle home.
 - a Work out the time taken by the train. Give your answer in minutes.
 - **b** Work out Alan's speed while cycling.
 - **c** Work out Alan's average speed for the entire journey, assuming that he stops at the village for half an hour. Give your answer correct to one decimal place.

explanation 5

- **26** 400 cm³ of beeswax has a mass of 384 g. Work out the density of beeswax.
- **27** A block of wood measures 15 cm by 10 cm by 10 cm. The block has a mass of 810 g.
 - a Work out the volume of the block of wood.
 - **b** Work out the density of the wood.

- 28 Cubes of sugar have sides of length 1.5 cm. Fifty of these cubes have a mass of 143 g. Work out the density of sugar. Give your answer correct to three significant figures.
- 29 A stone has a mass of 320 kg. The density of the stone is 2500 kg/m³. Work out the volume of the stone.
- **30** A piece of copper has a volume of 0.07 m³. Copper has a density of 8930 kg/m³. Work out the mass of the copper.
- 31 The density of lead is 11 340 kg/m³. A cube made from lead has lengths of side 15 cm. Work out the mass of the cube.

explanation 6

- A metal bar is in the shape of a cuboid measuring 20 cm by 12 cm by 10 cm. The metal bar has a mass of 21.432 kg. Work out the density of the metal.
 - a Give your answer in grams per cubic centimetre.
 - **b** Give your answer in kilograms per cubic metre.
- 33 A kitchen worktop is in the shape of a cuboid. It is 2.4m long, 59cm wide and 3cm deep. The worktop is made of granite and has a mass of 114.3kg.

 Work out the density of granite. Give your answer in kilograms per cubic metre, correct to three significant figures.
- **34** An athlete runs 100 m in 9.6 seconds. Work out his average speed.
 - a Give your answer correct to two significant figures in metres per second.
 - **b** Give your answer correct to two significant figures in kilometres per hour.
- **35** A cyclist covers 6500 m in 20 minutes. Work out his average speed.
 - a Give your answer in metres per minute.
 - **b** Give your answer in kilometres per hour.
- **36** Jane runs 3.5 miles in 25 minutes. Work out her average speed in miles per hour.