Using letters

- Distinguishing between equations, formulae and functions
- Identifying and using an identity
- **Using negative indices**
- Using the index laws in algebra and with standard form

Keywords

You should know

explanation 1a

explanation 1b

explanation 1c

explanation 1d

1 Solve these equations.

a
$$3x - 7 = 17$$

b
$$\frac{x}{4} + 5 = 23$$

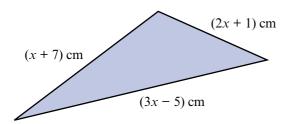
c
$$3(2x-5)=24$$

d
$$6x + 5 = 8x - 5$$

d
$$6x + 5 = 8x - 5$$
 e $4(2x - 7) = 8 - x$ **f** $\frac{2x - 3}{5} = 7$

$$f = \frac{2x-3}{5} = \frac{1}{5}$$

2



The triangle has a perimeter of 27 cm.

Form an equation and solve it to find the value of x and the length of each side of the triangle.

- 3 Jane is x years old and her brother Tom is two years older than her, while her sister Hannah is three times her age. The sum of their ages is 57.
 - Write expressions in terms of x for Tom's age and Hannah's age.
 - Write an equation for the sum of their ages.
 - Solve your equation to find Jane's age.

explanation 2a

explanation 2b

explanation 2c

explanation 2d

4 State whether each of the following is a formula, equation or function. Some parts may have more than one answer.

a 5x - 3 = 17

b $\frac{c}{6} - 5 = \frac{3}{5}$

c y = 5x - 7

- **d** $A = \pi r^2$ where A is the area and r is the radius of the circle.
- e p = 2l + 2w where p is the perimeter, l is the length and w is the width.

 $y = 3x^3 + 5$

5(x+2) = 3x - 7

h 3x + 2y = 18

5 Copy and complete the table of values for these functions without using a calculator.

a y = 6x - 1

b y = 7 - 2x

c 2y + 3x = 12

x	-1	-3		5		
у			0		11	-5

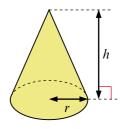
6 The volume of a cone is given by the formula $V = \frac{1}{3}\pi r^2 h$.

Find the volume of these cones.

a
$$r = 4 \text{ cm}, h = 6 \text{ cm}$$

b
$$r = 7 \,\mathrm{cm}, h = 12 \,\mathrm{cm}$$

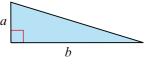
$$r = 1.2 \text{ cm}, h = 3.5 \text{ cm}$$



7 The perimeter P of a right-angled triangle is given by the formula

$$P = a + b + \sqrt{a^2 + b^2}$$
.

Find the perimeter of each of these triangles.



- **a** a = 3 cm, b = 4 cm
- **b** $a = 12.5 \,\mathrm{cm}, b = 30 \,\mathrm{cm}$
- $a = 6.1 \,\mathrm{cm}, b = 3.2 \,\mathrm{cm}$

- **8** Copy and complete these identities. Check by substituting some values of x.
 - **a** $4(x + 7) \equiv 4x + \square$

- **b** $7(2x+5) \equiv x +$
- **c** 2(-7) = 6x -
- **d** $9x 12 \equiv 3(\square 4)$
- **e** $5(2x-3) \equiv -$
- $f 15x + 25 \equiv 5(+)$
- **9** Which of these expressions are identically equal to $r \div \frac{S}{t}$?

 - A $\frac{r \div s}{t}$ B $r \times \frac{t}{s}$ C $\frac{r}{1} \div \frac{s}{t}$ D $\frac{t}{rs}$

- $\mathbf{E} \frac{rt}{s}$
- **10** Which of these expressions are identically equal to 7 + 3(x + 2)?
 - **A** 7 + 3x + 2
- **B** 10x + 20
- **C** 7 + 3x + 6

D 9 + 3x

E 3x + 13

explanation 3a

explanation 3b /

explanation 3c

- 11 Write these using indices.
 - **a** $d \times d \times d \times d \times e \times e$
- **b** $g \times h \times h \times g \times h \times g \times h \times g \times h \times g$
- **c** $4 \times p \times p \times p \times q \times q \times r$ **d** $4 \times y \times y \times 5 \times z \times z \times z \times z$
- e $6 \times a \times a \times 4 \times b \times b \times c \times c \times c$
- **f** $4 \times m \times 4 \times n \times n \times n \times 2 \times p \times p \times p \times p$
- **12** Find the value of each of these without using a calculator.

- **a** 2^3 **b** 4^3 **c** 3^4 **d** 2^5 **e** 10^8 **f** $(-2)^2$

- **g** $(-3)^3$ **h** $2^3 \times 5^2$ **i** $10^2 \div 5^2$ **j** $(-5)^2 + 3^4$ **k** $27 5^3$

- **13** Simplify these, leaving your answer as a power.

 - **a** $6^5 \times 6^2$ **b** $5^{12} \div 5^4$ **c** $(3^4)^6$
- **d** $\frac{7^5 \times 7^2}{7^3}$

- **e** $a^2 \times a^7$ **f** $(b^5)^3 \div b^6$ **g** $\frac{x \times x^3}{x^{-2}}$
 - **h** $(g^{10})^{-2} \times g^{20}$

explanation 4

14 Copy and complete these statements.

a
$$4^{-1} = \frac{1}{4^1} = \frac{1}{\Box}$$

b
$$5^{-2} = \frac{1}{\Box} = \frac{1}{\Box}$$

$$c 10^{-1} = \frac{1}{\Box} = \frac{1}{\Box}$$

c
$$10^{-1} = \frac{1}{\Box} = \frac{1}{\Box}$$
 d $10^{-2} = \Box = \Box$

15 Match each index statement in the top row to its value from the bottom row.

$$4^{-2}$$

$$10^{-3}$$

$$(-4)^2$$

$$5^{-3}$$

$$4^{-2}$$
 10^{-3} $(-4)^2$ 5^{-3} $(-10)^3$ $-(4)^2$ 5^3 $(-5)^3$

$$-(4)^{2}$$

$$(-5)^3$$

$$-125$$

$$\frac{1}{16}$$

125
$$-16$$
 -125 $\frac{1}{16}$ -1000 16 $\frac{1}{125}$

$$\frac{1}{125}$$

$$\frac{1}{1000}$$

16 Find the value of each expression without using a calculator.

a
$$2^{-3}$$

$$b 4^{-2}$$

$$c 3^{-2}$$

d
$$2^{-4}$$

a
$$2^{-3}$$
 b 4^{-2} **c** 3^{-2} **d** 2^{-4} **e** 10^{-5}

$$\mathbf{f} \quad (-2)^{-2}$$

$$\mathbf{g} \ (-3)^{-3}$$

$$h 2^{-6}$$

f
$$(-2)^{-2}$$
 g $(-3)^{-3}$ **h** 2^{-6} **i** $(-6)^{-3}$ **j** 10^{-4}

17 How many values can you find for x and y to make this statement true? $x^{y} = 64$

18 Simplify these, leaving your answer as a power. Write each answer in two different ways.

a
$$5^2 \div 5^3$$

b
$$6^2 \div 6^5$$

$$\mathbf{c} \quad a^2 \div a^7$$

d
$$\frac{3^5 \times 3^2}{3^{10}}$$

d
$$\frac{3^5 \times 3^2}{3^{10}}$$
 e $\frac{y^{-1} \times y^3}{y^5}$ **f** $(p^{10})^2 \div p^{30}$

$$(p^{10})^2 \div p^{30}$$

explanation 5a

explanation 5b

explanation 5c

19 Use the index laws to simplify these expressions.

a
$$3a \times 5a^2$$

b
$$2c^3 \times 2c^2$$

a
$$3a \times 5a^2$$
 b $2c^3 \times 2c^2$ **c** $4n^2 \times n^{-2}$ **d** $m^2 \times 3m$

$$m^2 \times 3m$$

e
$$4b^3 \times 3b^2$$

f
$$4p^2 \div 2p^3$$

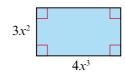
g
$$8x^2 \div 2x^-$$

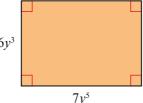
e
$$4b^3 \times 3b^2$$
 f $4p^2 \div 2p^3$ **g** $8x^2 \div 2x^{-1}$ **h** $4xy^2 \times 3x^3y^2$

- **20** Use the index laws to simplify these expressions.
- **a** $4n^4p \div 2n^2p$ **b** $4t^8r^3 \times 3t^4$ **c** $3g^2 \times 2g^3 \times 2g$ **d** $10b^8 \div 5b^8$

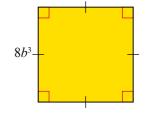
- e $\frac{9a^2}{3a}$ f $\frac{10n^6p^8}{2n^5p^3}$ g $c^4 \times 3c^2 \times 2c^5 \times c^3$ h $\frac{(3b^2 \times 4b^4)}{6b^3}$ i $(2x^7)^3$ j $(10y^3)^4$ k $(6a^2)^2$ l $(2m^3)^{-3}$

- **21** Write an expression for the area of each shape. Use the index laws to simplify them.

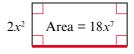


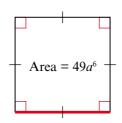


c



- **22** Write and simplify an expression for the red length of each shape.
 - a





- **23** Work these out. Give your answers in standard form.
 - **a** $(3 \times 10^2) \times (2 \times 10^5)$
 - $(4 \times 10^6) \times (6 \times 10^4)$
 - e $(7 \times 10^{-2}) \times (3 \times 10^{4})$
 - $g (6 \times 10^6) \div (2 \times 10^2)$
 - i $(9.6 \times 10^3) \div (2 \times 10^{-5})$
 - $k (2 \times 10^6) \div (8 \times 10^5)$
 - $\mathbf{m} \ (6 \times 10^6)^2$
 - $(2 \times 10^{-2})^4$

- **b** $(3.2 \times 10^{-3}) \times (3 \times 10^{2})$
- **d** $(3.2 \times 10^6) \times (3 \times 10^5)$
- f $(6 \times 10^{-4}) \times (2.5 \times 10^{-3})$
 - **h** $(8.4 \times 10^{-3}) \div (4 \times 10^{5})$
 - $(3 \times 10^7) \div (6 \times 10^5)$
- $(4.8 \times 10^{-5}) \div (2 \times 10^{-2})$
 - $n (5 \times 10^3)^3$
 - $(2 \times 10^4)^{-2}$