🔆 Algebra A3.1

Expressions and equations

- Simplifying algebraic expressions
- Solving equations using inverse operations
- Expanding brackets

Keywords

You should know

explanation 1a

explanation 1b

- **1** Write an expression for each set of instructions. Start with *x*.
 - a Multiply by 4.
 - **b** Subtract 6.
 - c Add 14.
 - **d** Divide by 3.
 - e Subtract from 5.
- **2** Write an expression for each set of instructions. Start with *x*.
 - a Subtract 11 then divide the answer by 5.
 - **b** Add 7 then multiply the answer by 2.
 - c Multiply by 3 then add 5 and divide the answer by 4.
 - **d** Subtract from 10 and multiply the answer by 3.
 - e Divide by 3 then add 5.
- **3** Write an expression for each set of instructions. Start with *y*.
 - a Divide by 10.
 - **b** Multiply by 3 and divide by 5.
 - c Divide by 4 then subtract 3.
 - **d** Multiply by 5 then subtract the answer from 17.
 - e Subtract 9 and divide 20 by the answer.
 - f Multiply by 3 then divide by 4 and subtract the answer from 10.

4 Write the instructions contained in these expressions. Start with x.

a
$$2(x-5)$$

b
$$21 - 5x$$

c
$$\frac{x}{3} + 4$$

d
$$\frac{x+8}{4}$$

e
$$35 - 4(x+1)$$

$$f = \frac{18}{x-3}$$

5 Find the value of each of these expressions when x = 5.

a
$$3(x+2)$$

b
$$11 + 2x$$

$$\frac{4x-2}{3}$$

d
$$\frac{35}{x}$$

e
$$10 + 3(x + 1)$$

$$\mathbf{f}$$
 $x(x-2)$

$$\mathbf{g} \quad x(x+1)$$

h
$$\frac{x+10}{x}$$

i
$$2x - \frac{3x}{5}$$

6 Give the value of these expressions as mixed numbers when x = 9.

a
$$\frac{x}{4}$$

b
$$\frac{2x}{5}$$

c
$$\frac{x+1}{3}$$

d
$$\frac{10}{x}$$

e
$$3 + \frac{x}{4}$$

b
$$\frac{2x}{5}$$
 c $\frac{x+1}{3}$ **d** $\frac{10}{x}$ **e** $3+\frac{x}{4}$ **f** $x-\frac{x}{5}$

explanation 2

7 Simplify each of these expressions.

a
$$2x - 3 + 3$$

b
$$\frac{x}{4} + 7 - 7$$

c
$$\frac{5x}{5}$$

$$\mathbf{d} \quad \frac{3x}{3}$$

e
$$\frac{x}{4} \times 4$$

$$\mathbf{f} = \frac{x+3}{7} \times 7$$

8 Copy and complete the following expressions so that they simplify to x.

a
$$x + 8 - \square$$

b
$$x - 9 + \Box$$

c
$$x - \Box + 6$$

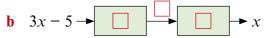
d
$$\frac{4x}{\Box}$$

e
$$\frac{4x}{1} + 5 - 1$$

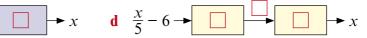
$$\mathbf{f} \quad \frac{x-9}{7} \times \square + \square$$

9 Copy and complete these function machines.





$$\frac{x+7}{4}$$



e
$$3(x+2)$$
 \longrightarrow x f $\frac{4x}{5}$ \longrightarrow x

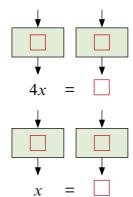
explanation 3

10 Copy and complete.

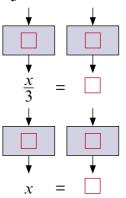
a
$$5x = 45$$

$$\begin{array}{ccc}
 & \downarrow & \downarrow \\
 & \vdots & 5 \\
 & \downarrow & \downarrow \\
 & x & = & \square
\end{array}$$

b
$$4x + 11 = 39$$



$$\frac{x}{3} - 7 = 118$$



11 Solve these equations.

$$\frac{x}{10} = 17$$

d
$$x - 134 = 270$$

b
$$4x = 64$$

$$\frac{x}{11} = 20$$

$$x + 99 = 147$$

f
$$12x = 60$$

12 Solve these equations.

a
$$x - 47 = 86$$

b
$$10x = 140$$

c
$$5x = 75$$

$$\frac{x}{8} = 31$$

e
$$x + 58 = 94$$

f
$$\frac{x}{25} = 4$$

13 Copy and complete the steps to solve the following equations.

a
$$3x - 17 = 16$$

$$3x = \square$$

$$x = \square$$

b
$$2(x+12)=68$$

$$x + 12 = \Box$$

$$x = \square$$

$$\frac{x}{5} + 112 = 126$$

$$\frac{x}{5} = \square$$

$$x = \square$$

d
$$\frac{5x}{3} = 15$$

$$5x = \square$$

$$x = \square$$

e
$$11 = \frac{x-19}{6}$$

$$\square = x - 19$$

$$x = \square$$

$$\mathbf{f}$$
 75 = 5(x - 32)

$$\square = x - 32$$

$$x = \square$$

$$\mathbf{g} = 2 = \frac{x + 10}{4}$$

$$\square = x + 10$$

$$x = \square$$

h
$$9 = 3(4 - x)$$

$$\square = 4 - x$$

$$x = \square$$

h
$$9 = 3(4 - x)$$
 i $x = \frac{x+4}{2}$

$$\square = x + 4$$

$$x = \square$$

14 Solve these equations.

a
$$\frac{x-24}{8} = 7$$
 b $9x + 73 = 109$ **c** $11(x+1)$ **d** $17 = \frac{x}{4} - 53$ **e** $25 = \frac{x+81}{4}$ **f** $40 = \frac{8x}{3}$

b
$$9x + 73 = 109$$

$$c$$
 11(x + 14) = 220

d
$$17 = \frac{x}{4} - 53$$

e
$$25 = \frac{x + 81}{4}$$

f
$$40 = \frac{8x}{3}$$

*15 Solve these equations and give your answers as fractions in their simplest form.

a
$$10x = 5$$

b
$$12x = 8$$

c
$$25x = 15$$

d
$$12x + 10 = 19$$

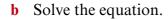
e
$$25x - 9 = 11$$

f
$$24 = 18x + 12$$

explanation 4

16 The perimeter of the rectangle shown is 76 cm.

a Write this information as an equation and simplify it.



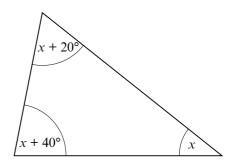
c Find the length of the longest side of the rectangle.



3x cm

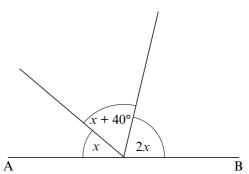
17 a Write an equation involving the sum of the angles of this triangle and simplify it.

- **b** Solve the equation.
- c Find the angles of the triangle.



18 In the diagram, AB is a straight line.

- a Write an equation involving the sum of the angles shown and simplify it.
- **b** Solve the equation.
- c Write down the size of each of the labelled angles.



explanation 5

- **19** Do you think that the statement x + y = y + x is always true, sometimes true or never true for numbers x and y? Give two examples to support your answer.
- **20** Repeat question 19 for each of the following statements.
 - $\mathbf{a} \quad x y = y x$

b x - y = -(y - x)

 \mathbf{c} xy = yx

- $\mathbf{d} \quad \frac{x}{v} = \frac{y}{x}$
- e x + y + 1 = -(1 y x) f (1 x) (1 + y) = -(x + y)

explanation 6

- **21** Simplify each of these expressions.
 - \mathbf{a} xy + 2yx
- **b** 5zx + xz
- c 2xy + 3yx xy

- d 5pq 3qp
- e rp + 6pr 2
 - \mathbf{f} pq + qp + pr
- $\mathbf{g} \quad a \times b \times c$ $\mathbf{h} \quad 2 \times w \times 3$

i $2pq + q \times 6 \times p$

- **22** a Work out these multiplications.

 - i $(5 \times 4) \times 3$ ii $5 \times (4 \times 3)$ iii $(3 \times 8) \times 2$ iv $3 \times (8 \times 2)$

- v $(7 \times 3) \times 5$ vi $7 \times (3 \times 5)$ vii $(4 \times 11) \times 2$ viii $4 \times (11 \times 2)$

- **b** Copy and complete. $(xy)z = \Box$
- **23** Write down which of the following expressions always have the same value as xyz.
 - ZXY
- x(yz)
- yxz
- y(zx)
- **24** Find the value of xyz when

 - **a** x = 3, y = 5, z = 20 **b** x = 4, y = 25, z = 9

 - **c** x = 2, y = 2.5, z = 7 **d** x = 10, y = 2, z = 1.9

 - e $x = \frac{1}{2}$, y = 12, z = 11 f $x = \frac{1}{2}$, y = 7.9, z = 20

Choose the simplest order to work out each calculation.

- **25** Simplify the following expressions.
 - \mathbf{a} 3pqr + 2rpq
- **b** p(qr) + 6rpq
- c 10r(qp) pqr
- d 4pqr + 11r(qp) prq

- **26** Simplify these expressions. The first one is done for you.
 - **a** $2 \times 4p = (2 \times 4)p = 8p$
- **b** $3 \times 5q$ **c** $4 \times 7t$

d $8r \times 3$

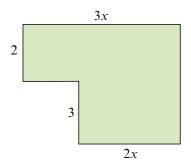
- e $9n \times 4$
- f $10k \times 3$
- **27** Simplify these expressions. The first one is done for you.
 - **a** $4 \times 3g + 5 \times 2g = 12g + 10g$ = 22g
- **b** $3 \times 4w + 2 \times 7w$

c $5 \times 4v - 3 \times 3v$

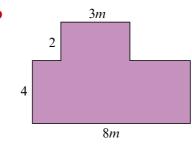
d $7 \times 3x - 5x \times 4$

e $6 \times 4y + y - 3 \times 2y$

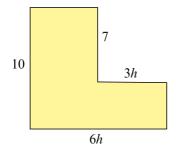
- \mathbf{f} $a + 3a \times 5 2 \times 4a$
- *28 Find and simplify an expression for the area of each of these figures.



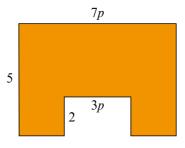
b



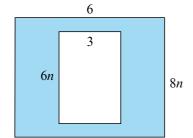
 \mathbf{c}



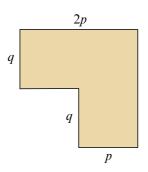
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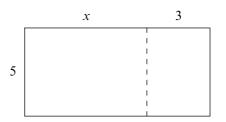


f



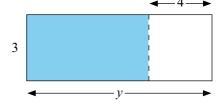
*29 Copy and complete the statement to show the total area in two different ways.

$$5(x + \square) = 5x + \square$$



*30 Copy and complete the statement to show the coloured area in two different ways.

$$3(y - \square) = \square - 12$$



explanation 7

31 Copy and complete the following steps to work out 24×19 .

$$24 \times 19 = 24 (20 - \square)$$

$$= 24 \times \square - 24 \times \square$$

$$= \square - \square$$

$$= \square$$

32 Use the method shown in question 31 to work out these calculations.

a
$$32 \times 29$$

33 Expand the brackets in these expressions.

a
$$4(x+5)$$

b
$$6(n-4)$$

c
$$3(5+t)$$

d
$$10(12-h)$$
 e $8(7+p)$ **f** $9(11-b)$

e
$$8(7+p)$$

$$\mathbf{f} = 9(11 - b)$$

g
$$x(3+y)$$
 h $r(5-t)$

h
$$r(5-t)$$

$$i k(n+2)$$

34 Expand the brackets in these expressions.

a
$$3(2x+1)$$

b
$$4(3n-2)$$

c
$$5(4-2k)$$

d
$$6(10+3j)$$
 e $2(9-5e)$

e
$$2(9-5e)$$

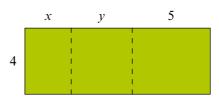
f
$$7(3d+4)$$

g
$$a(2b + 5)$$

h
$$g(9-3t)$$

g
$$a(2b+5)$$
 h $g(9-3t)$ **i** $2z(5+3y)$

- *35 Use the diagram to help you complete the statement below.
 - 4(x + +) =



- **36** Expand the brackets in these expressions.
 - **a** 5(p+q+3)

b 3(2a+b-6)

 $e^{4(12-m+2n)}$

d 10(2h+5-k)

e 6(5-3c-4d+2e)

- f 3n(2p + 3q 3)
- **37** Expand the brackets and simplify these expressions.
 - a 3(x+5)+2x

b 4(2n-3)-n

c 2(4-5t)+6

d 7(2a+3)-6a-11

e 8(w+2q)+w-9q

- f + 4h + 3(h + 5)
- **38** Expand the brackets and simplify these expressions.
 - **a** 5(3t+1)+4t+3

- **b** 4(m+2n+3)+m+4n+6
- c 14 + 3(7k + 2h + 5) 9k 10 d 11 + 5x + 3(x + 2y) 3y
- *39 Solve these equations by expanding the brackets first.
 - **a** 3(x + 2.5) = 19.5

b 4(x+3)+7=51

c 36 = 4(x + 3.5) + 6

d 15 = x + 4(2x - 3)

3x + 2(x + 7) = 59

- f = 5(x+1) 2x 26 = 0
- *40 Three friends count how many marbles they have. Paula has p marbles. Quentin has six fewer marbles than Paula. Rachel has twice as many marbles as the other two have in total.
 - **a** How many marbles does Quentin have, in terms of p?
 - **b** Write an expression for the number of marbles that Rachel has.
 - c Write an expression for the total number of marbles. Simplify it.
 - **d** Paula, Quentin and Rachel have 48 marbles altogether. Write an equation involving p.
 - Solve your equation. How many marbles does Rachel have?