Equations

- Solving equations using inverse operations
- Solving equations involving brackets

Keywords

You should know

explanation 1a

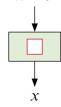
explanation 1b

1 Write the inverse of each operation.

$$\mathbf{f} \times 10$$

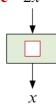
2 Write down the missing operation in each flowchart. Use inverse operations.

a
$$x + 8$$

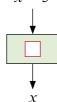


b
$$x - 9$$



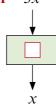


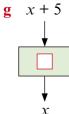
d x - 5



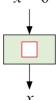


$$\mathbf{f}$$
 3x





h x - 6





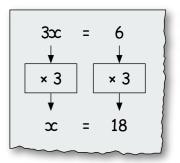
explanation 2a

explanation 2b

3 Tariq's homework was wrong.

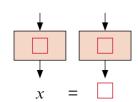
His mistake was to multiply both sides of the equation by 3.

- a What operation should he have used?
- **b** Write out the method and answer correctly.

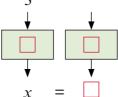


4 Copy and complete these flowcharts.

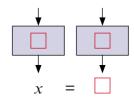
$$x - 2 = 6$$



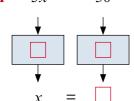
b
$$\frac{x}{3}$$
 = 12



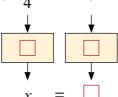
$$\mathbf{c} \quad x + 7 = 12$$



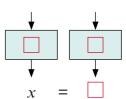
d
$$5x = 30$$



$$e^{\frac{X}{4}} = 8$$



$$f x - 6 = 11$$



5 Solve these equations.

a
$$\frac{x}{6} = 10$$

b
$$4j = 32$$

$$p - 12 = 38$$

d
$$k + 56 = 90$$

$$\frac{t}{2} = 50$$

f
$$2r = 30$$

$$x - 24 = 26$$

h
$$3y = 24$$

$$i \quad 5m = 75$$

$$\frac{s}{4} = 12$$

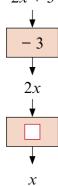
$$\mathbf{k} \quad w + 32 = 74$$

$$\frac{n}{25} = 8$$

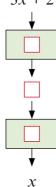
explanation 3

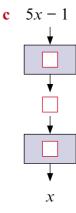
6 Copy and complete these flowcharts. Use inverse operations.

a 2x + 3



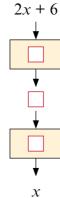
b 3x + 2





d

4x - 5
<u> </u>
—
χ



explanation 4

7 This equation has been solved correctly.

Why is 4x - 3 not the same as 1x?

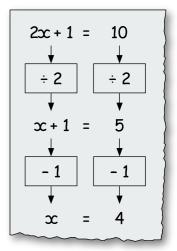
Why is 4x - 3 + 3 not equal to 4x - 6? b

Why is the first step to add 3? c

d Why is the next step to divide by 4?

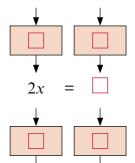
Substitute x = 6 into 4x - 3. How does this tell you that x = 6 is the correct solution to the equation? 4x - 3 =21 + 3 + 3 4x24 = ÷ 4 ÷ 4 ∞ 6

- **8** This equation has *not* been solved correctly.
 - a Substitute x = 4 into 2x + 1. How does this tell you that x = 4 is *not* the correct solution to the equation?
 - **b** What mistake has been made in the working?
 - **c** Write out the correct solution.
 - **d** Use substitution to show your answer is correct.

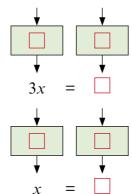


9 Copy and complete the flowcharts to solve these equations. Use inverse operations. Use substitution to check your answers.

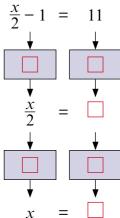
$$2x + 5 = 17$$



b
$$3x + 6 =$$



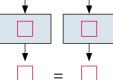
15



10 Copy and complete the flowcharts to solve these equations. Use inverse operations. Use substitution to check your answers.

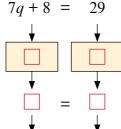
a
$$5p - 6 =$$

x



$$p = \square$$

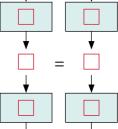
b
$$7q + 8 =$$





$$q = \square$$

$$\begin{array}{cccc} \mathbf{c} & \frac{r}{2} + 2 & = & 6 \\ \downarrow & & \downarrow \end{array}$$





11 Solve these equations. Use inverse operations.

a
$$3x - 10 = 26$$

b
$$2t + 12 = 30$$

$$c$$
 5 p - 6 = 34

d
$$2w + 18 = 18$$

e
$$6r - 10 = 20$$

e
$$6r - 10 = 20$$
 f $\frac{t}{2} + 2 = 12$

$$\mathbf{g} \quad 4d - 10 = 18$$

g
$$4d - 10 = 18$$
 h $\frac{y}{2} - 2 = 5$

i
$$4e + 5 = 7$$

$$\frac{b}{2} - 1 = 8$$

$$\mathbf{k} = 6f + 8 = 26$$

$$12g - 7 = 41$$

explanation 5

This equation involves brackets. 2(x-3) = 14

Substitute x = 10 into 2(x - 3) to show that x = 10 is the correct solution to the equation.

b Why is 2(x-3) the same as 2x-6?

c Copy and complete the flowchart.

$$2(x-3) = 14$$

$$\downarrow \qquad \qquad \downarrow$$

$$2x-6 = 14$$

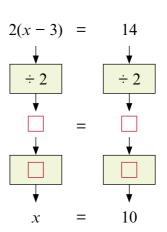
$$\downarrow \qquad \qquad \downarrow$$

$$\downarrow \qquad \qquad \downarrow$$

$$\downarrow \qquad \qquad \downarrow$$

$$x = 10$$

d Copy and complete this flowchart. Start by dividing by 2.



*13 Copy and complete these flowcharts. Start by expanding the brackets. The first one has been started for you.

20 a 2(x+3) =

$$2x + 6 = 20$$

$$2x + 6 = 20$$

$$-6$$

$$2x = 14$$

$$x = \square$$

d
$$2(x-5) = 8$$

$$\begin{array}{ccc} \downarrow & \downarrow \\ \gamma & = & \end{array}$$

a
$$3(x + 2) = 12$$

d $2(n - 4) = 16$

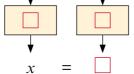
$$\mathbf{g} \quad 3(f-2) = 24$$

b
$$3(x+1) = 12$$

$$\Box$$
 = \Box

$$x = \Box$$

e
$$4(x+3) = 20$$

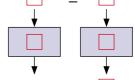


b
$$4(t-3) = 28$$

e
$$3(p+1) = 15$$

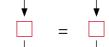
h
$$6(a-4)=30$$

$$c 2(x-6) = 24$$



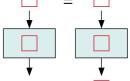
$$x = \square$$

12



f 6(x-5) =





$$x = \square$$

- c 5(m+3) = 25
- **f** 5(y-2) = 35
- 2(x-10)=60