Mental methods (1)

Using facts you know to answer unfamiliar questions

Keywords

You should know

You should answer the questions in this topic without using a calculator.

explanation 1

1 Write these fractions as decimals.

$$\frac{1}{5}$$

b
$$\frac{3}{4}$$

a
$$\frac{1}{5}$$
 b $\frac{3}{4}$ **c** $\frac{7}{20}$ **d** $\frac{6}{25}$

d
$$\frac{6}{2}$$

$$e \frac{3}{8}$$

$$\mathbf{f} = \frac{2}{3}$$

$$\mathbf{g} = \frac{1}{2}$$

$$h = \frac{9}{1}$$

i
$$\frac{2}{3}$$

i
$$\frac{2}{3}$$
 j $\frac{1}{6}$ k $\frac{2}{5}$ l $\frac{7}{8}$

$$\mathbf{k} = \frac{2}{5}$$

2 Use your answers to question 1 to write each fraction as a percentage.

3 Change these percentages to decimals.

4 Write each percentage in question 3 as a fraction. Give each answer in its simplest form.

explanation 2a

explanation 2b

explanation 2c

5 Calculate these percentages.

- **6** Work out the following percentages.
 - 15% of £38
- 35% of 72 kg c 21% of £62
- **d** 43% of 56 litres

- 64% of 39 km
- 72% of 3 m
- 5% of 20 hours
- **h** 3% of 15 g

7 The prices shown do not include VAT.





£550



- Work out the VAT, at a rate of 17.5%, for each item.
- Find the total cost of each item, including VAT.
- **8** In a sale all items are reduced by 15%. For each item calculate these values.
 - i The amount of the reduction
- ii The sale price
- trainers costing £45 before the sale
- tennis racquet costing £38 before the sale
- football costing £16 before the sale
- d hockey stick costing £55 before the sale



explanation 3

9 Copy and complete this table.

| 3 | × | 4 | = | |
|-----|---|---|---|--|
| 2 | × | 4 | = | |
| 1 | × | 4 | = | |
| 0.1 | × | 4 | = | |
| 0.2 | × | 4 | = | |
| 0.3 | × | 4 | = | |

10 Use the fact that $8 \times 4 = 32$ to answer the following questions.

- a 8×0.4
- **b** 0.8×4
- $c = 0.8 \times 0.4$

- d 80×4
- e 80×0.4
- **f** 0.8×400

- **g** 80×40 **h** 8×0.04 **i** 80×0.04

11 Use the fact that $9 \times 7 = 63$ to answer these questions.

- **a** 0.9×7
- **b** 0.9×0.7
- $\mathbf{c} \quad 9 \times 0.7$
- **d** 9×0.07 **e** 90×7
- $\mathbf{f} \quad 9 \times 700$

- **g** 0.09×7
- $h 90 \times 0.7$
- i 0.09×700

12 Use the answer to the first division in each row to work out the other divisions in the row.

- **a** $20 \div 4$
- **b** 2 ÷ 4
- $c 0.2 \div 4$
- **d** $0.02 \div 4$

- **e** $60 \div 5$ **f** $6 \div 5$
- **g** $0.6 \div 5$ **h** $0.06 \div 5$

- i 18 ÷ 2
- $1.8 \div 2$
- $k = 0.18 \div 2$
- $1 \quad 0.018 \div 2$

- $m 10 \div 4$
- $\mathbf{n} = 1 \div 4$
- **o** $0.1 \div 4$
- **p** $0.01 \div 4$

13 Copy and complete.

a $0.2 \times \square = 6$

b $4 \times \Box = 0.8$

 $0.1 \times \square = 0.4$

d $3 \div \square = 3$

e $\Box \div 5 = 0.2$

 $\mathbf{f} = 10 \div \Box = 0.5$

14 Make 36 using the digits 1, 3, 3 and 5 once, together with any combination of the symbols $+, -, \times, \div$ and brackets.

15 Andy was born in 1982. Using the digits of that year, in any order, together with any combination of the symbols $+, -, \times, \div$ and brackets, how many numbers between 1 and 30 can you make?