Geometry and measures GM3.2

Triangles

- Recognising and naming different types of triangle
- Defining a triangle
- Constructing a triangle using SAS or ASA

Keywords

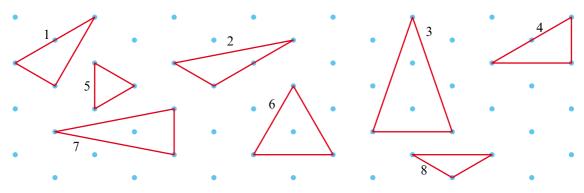
You should know

explanation 1a

explanation 1b

explanation 1c

1 The triangles in the diagram are drawn on isometric dotty paper.



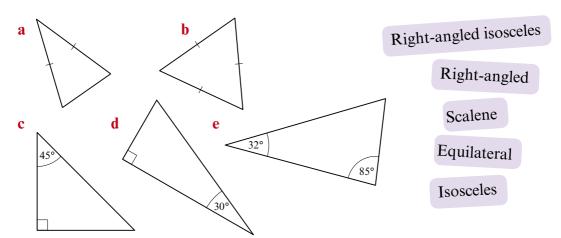
List the triangles that are

a equilateral

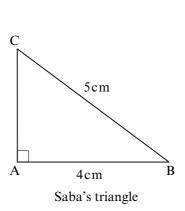
- **b** isosceles
- c right-angled

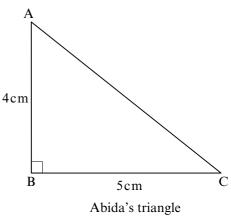
- d obtuse-angled
- e scalene
- f acute-angled

2 Pick the best label for each of these triangles.

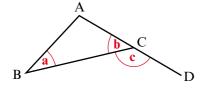


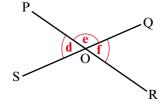
- 3 A class was asked to draw a right-angled triangle ABC with $AB = 4 \,\text{cm}$ and $BC = 5 \,\text{cm}$. The triangles that Saba and Abida drew are shown.
 - a Are the triangles the same?
 - **b** Who is right? Explain your answer.



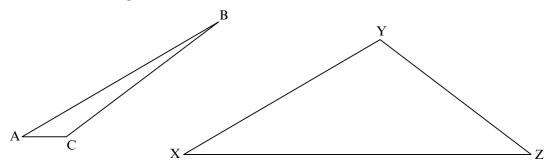


4 Use three letters to describe each of the angles shown in the diagram.





5 Here are two triangles ABC and XYZ.



- **a** Are the two triangles the same?
- **b** Measure these lengths and angles.
 - i AB
- ii XY

iii BC

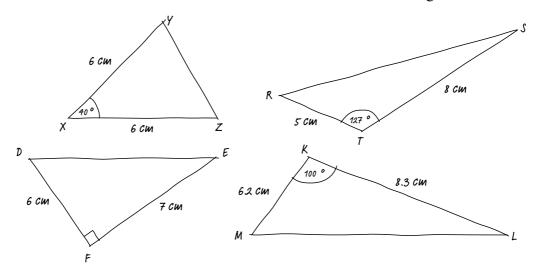
- iv YZ
- v Angle BAC
- vi Angle YXZ
- c If you know the lengths of two sides of a triangle and one of its angles, is this always enough information to be able to draw that triangle?

explanation 2a explanation 2b explanation 2c

- 6 You are given the lengths of two sides of a triangle. Which angle do you need to know to complete the information for SAS when the given sides are
 - a XY and YZ
- **b** AC and AB
- c PR and QR

It's a good idea to sketch the triangles first.

7 a Use the information in these sketches to construct the triangles.



- **b** Measure these lengths and angles on your diagrams.
 - i YZ
- ii Angle XYZ
- iii RS
- iv Angle RST

- v DE
- vi Angle EDF
- vii ML
- viii Angle KML
- 8 Construct triangle PQR where PQ = 7.3 cm, QR = 4.8 cm and angle PQR = 50°.

Measure PR and angle PRQ.

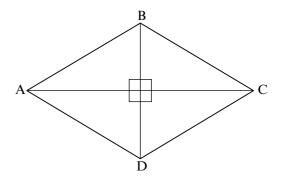
Sketch the triangles first.

- **9** Construct triangle ABC where AC = 8.6 cm, AB = 3.9 cm and angle BAC = 120°. Measure BC and angle ABC.
- 10 Construct triangle RST where RT = 5.7 cm, TS = 6.4 cm and angle RTS = 90°. Measure RS and angle RST.

11 ABCD is a rhombus. AC and BD cross at their midpoints.

$$AC = 8 \text{ cm} \text{ and } BD = 6 \text{ cm}.$$

Construct a triangle and use it to work out the perimeter of the rhombus. Explain how you did it.



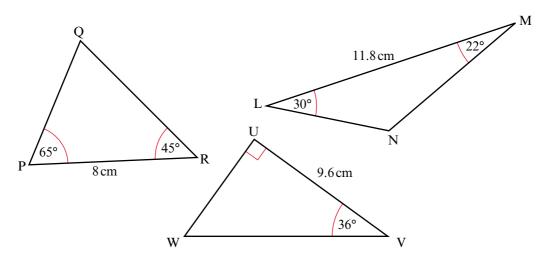
explanation 3a

explanation 3b

explanation 3c

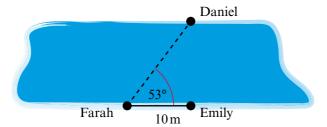
explanation 3d

- 12 You are given the size of two angles in a triangle. Which side do you need to know to complete the information for ASA when the given angles are
 - **a** $\angle ABC$ and $\angle ACB$
- **b** ∠FHG and ∠FGH
- c ∠JKL and ∠KLJ
- **13** a Use the information in these sketches to construct the triangles.



- **b** Find these lengths from your diagrams.
 - i PQ
- ii QR
- iii UW
- $\quad \text{iv} \quad WV$
- v LN
- vi MN
- **14** Construct triangle DEF where DE = $9.2 \, \text{cm}$, $\angle DEF = 45^{\circ}$ and $\angle FDE = 57^{\circ}$. Measure DF.

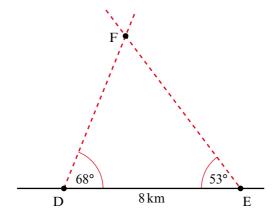
- **15** Construct triangle KLM where LM = 11.3 cm, ∠KLM = 38° and ∠KML = 64°. Measure KL.
- **16** Construct triangle OPQ where OP = $7.4 \,\text{cm}$, \angle QOP = 52° and \angle QPO = 41° . Measure PQ.
- Daniel, Emily and Farah are trying to find the width of a river.Emily stands to face Daniel on the opposite side of the river.Farah measures 10 m along the river bank from Emily.She measures the angle between the directions of Daniel and Emily as 53°.



Construct a triangle to show this information. How wide is the river?

You don't need to draw a line 10 m long! Use centimetres to represent metres.

18 The diagram shows two coastguard stations D and E, 8km apart. A distress flare F is sighted at the position shown.



Construct a triangle using this information. Find the distance of the flare from each of the coastguard stations.