Fractions and decimals

- Expressing one quantity as a fraction of another
- Using equivalent fractions
- Changing between improper fractions and mixed numbers
- Writing fractions as decimals

Keywords

You should know

explanation 1

- **1** Each of these shapes is divided into smaller parts of equal size.
 - a Write the fraction of each shape that is coloured blue.

i



ii



iii



iv



V



vi



- **b** Write the fraction of each shape that is not coloured blue.
- 2 Two shapes are shown below. Each one has one part out of three coloured red. Does either shape have $\frac{1}{3}$ coloured red? Explain your answer.

Shape A

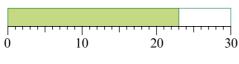


Shape B

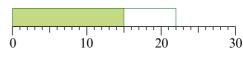


3 Use the numbered scales to find the fraction of each of these rectangles that is green.

a



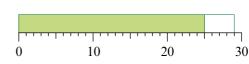
b



c



d



- 4 Write the first number as a fraction of the second for each of these pairs.
 - **a** 16, 25
- 9, 11

42, 53

- **d** 73, 90
- 17, 30 e

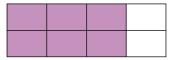
3, 100

explanation 2a

explanation 2b

5 For each diagram, find a pair of equivalent fractions that show how much of the diagram is coloured purple.

a



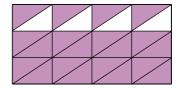
b



c



d



6 Copy and complete.

$$\frac{2}{3} = \frac{10}{10}$$

b
$$\frac{4}{7} = \frac{\square}{21}$$
 c $\frac{3}{8} = \frac{12}{\square}$

$$c \frac{3}{8} = \frac{12}{12}$$

d
$$\frac{4}{5} = \frac{8}{10} = \frac{25}{25}$$

d
$$\frac{4}{5} = \frac{8}{\Box} = \frac{\Box}{25}$$
 e $\frac{3}{10} = \frac{\Box}{30} = \frac{27}{\Box}$ **f** $\frac{5}{6} = \frac{35}{\Box} = \frac{\Box}{54}$

$$\frac{5}{6} = \frac{35}{10} = \frac{1}{54}$$

7 Copy and complete.

a
$$\frac{21}{28} = \frac{3}{1}$$

b
$$\frac{35}{45} = \frac{\Box}{9}$$

$$c \frac{50}{75} = \frac{2}{1}$$

d
$$\frac{44}{88} = \frac{22}{1} = \frac{20}{2}$$
 e $\frac{36}{48} = \frac{9}{1} = \frac{20}{4}$ **f** $\frac{60}{1} = \frac{20}{30} = \frac{2}{1}$

$$e^{\frac{36}{48}} = \frac{9}{10} = \frac{1}{4}$$

$$f = \frac{60}{10} = \frac{20}{30} = \frac{2}{10}$$

- **8** Write each of these fractions in their lowest terms.
 - $\frac{45}{90}$

b $\frac{55}{77}$

 $\frac{54}{72}$

d $\frac{72}{240}$

 $\frac{225}{250}$

9 Write $\frac{108}{144}$ in its simplest form.

explanation 3a

explanation 3b

10 You can use a fraction wall to compare fractions.

> Use the fraction wall to help you. Copy and complete each statement, using < or >.

- **a** $\frac{2}{7} \square \frac{1}{3}$ **b** $\frac{3}{5} \square \frac{4}{7}$
- c $\frac{2}{3} \square \frac{7}{8}$ d $\frac{3}{8} \square \frac{2}{5}$
- e $\frac{4}{5}\Box\frac{6}{7}$ f $\frac{5}{6}\Box\frac{2}{3}$

$\frac{1}{8}$	$\frac{1}{8}$		1/8		1/8	$\frac{1}{8}$		1/8		$\frac{1}{8}$		<u>1</u> 8	
$\frac{1}{7}$	$\frac{1}{7}$	<u>7</u>	$\frac{1}{7}$		1	<u>1</u>		1 7		$\frac{1}{7}$		<u>1</u> 7	
$\frac{1}{6}$		$\frac{1}{6}$		$\frac{1}{6}$		$\frac{1}{6}$			<u>1</u> 6		$\frac{1}{6}$		
$\frac{1}{5}$			<u>1</u> 5		$\frac{1}{5}$			1/4		$\frac{1}{5}$			
$\frac{1}{4}$			$\frac{1}{4}$			$\frac{1}{4}$				$\frac{1}{4}$			
$\frac{1}{3}$				$\frac{1}{3}$					$\frac{1}{3}$				
$\frac{1}{2}$						$\frac{1}{2}$							

- 11 Write these groups of fractions in order of size, smallest first. Use the fraction wall.
- **a** $\frac{1}{2}, \frac{1}{3}, \frac{2}{5}$ **b** $\frac{3}{5}, \frac{4}{7}, \frac{5}{8}$ **c** $\frac{3}{4}, \frac{5}{6}, \frac{5}{7}$

- **d** $\frac{7}{8}, \frac{6}{7}, \frac{3}{4}, \frac{5}{6}$ **e** $\frac{1}{2}, \frac{4}{7}, \frac{3}{8}, \frac{2}{5}$ **f** $\frac{2}{3}, \frac{4}{7}, \frac{3}{5}, \frac{5}{8}$
- **12** Write each pair of fractions with a common denominator. State which is the smaller.
 - $\frac{5}{12}, \frac{9}{20}$
- **b** $\frac{7}{10}, \frac{11}{15}$
- $c \frac{3}{8}, \frac{5}{12}$
- **d** $\frac{9}{16}, \frac{13}{24}$ **e** $\frac{4}{25}, \frac{16}{75}$ **f** $\frac{25}{27}, \frac{17}{18}$

explanation 4

- **13** Write these improper fractions as mixed numbers.
- **a** $\frac{7}{3}$ **b** $\frac{11}{4}$ **c** $\frac{24}{5}$ **d** $\frac{31}{8}$ **e** $\frac{45}{11}$ **f** $\frac{99}{10}$

- **14** Write these mixed numbers as improper fractions.
 - **a** $4\frac{2}{3}$ **b** $2\frac{1}{5}$ **c** $6\frac{3}{4}$ **d** $9\frac{1}{2}$ **e** $7\frac{4}{5}$ **f** $5\frac{8}{9}$

- **15** Give your answers to these divisions as proper fractions in their lowest terms.
- **a** $4 \div 6$ **b** $9 \div 12$ **c** $14 \div 20$ **d** $15 \div 18$

- **e** $24 \div 30$ **f** $25 \div 75$ **g** $50 \div 75$ **h** $48 \div 60$
- **16** Give your answers to these divisions as mixed numbers in their simplest form.

- **a** $18 \div 5$ **b** $30 \div 4$ **c** $24 \div 10$ **d** $21 \div 14$

- **e** $50 \div 8$ **f** $11 \div 6$ **g** $40 \div 32$ **h** $250 \div 150$

explanation 5

- 17 Write these decimals as fractions in their lowest terms.
 - **a** 0.3
- **b** 0.1
- **c** 0.7
- **d** 0.9

- **e** 0.5 **f** 0.25 **g** 0.75 **h** 0.8

- i 0.24
- j 0.35 **k** 0.6
- 1 0.55

18 a Copy and complete.

$$\frac{1}{5} = \frac{1}{10}$$

- i $\frac{1}{5} = \frac{\Box}{10}$ ii $\frac{2}{5} = \frac{\Box}{10}$ iii $\frac{7}{20} = \frac{\Box}{100}$ iv $\frac{11}{25} = \frac{\Box}{100}$

- $\mathbf{v} = \frac{9}{20} = \frac{\square}{100}$ $\mathbf{vi} = \frac{3}{50} = \frac{\square}{100}$ $\mathbf{vii} = \frac{49}{50} = \frac{\square}{100}$ $\mathbf{viii} = \frac{18}{75} = \frac{\square}{25} = \frac{\square}{100}$
- **b** Write each fraction in part **a** as a decimal.
- **19** Write each fraction as a decimal.

- **a** $\frac{19}{20}$ **b** $\frac{7}{25}$ **c** $\frac{27}{60}$ **d** $\frac{126}{200}$
- **20** Write each set of numbers in order of size, smallest first.
 - **a** $\frac{3}{4}$ 0.7 0.59 $\frac{1}{2}$ **b** $\frac{27}{50}$ 0.62 0.575 $\frac{3}{4}$ **c** 0.8 $\frac{7}{10}$ $\frac{15}{20}$

- 21 Copy the number line. Show the output for this function machine on your number line.

