Adding and subtracting fractions

- Converting between mixed numbers and improper fractions
- Adding and subtracting fractions using efficient methods
- **Converting between fractions and decimals**

Keywords

You should know

explanation 1a

explanation 1b

- 1 Convert these mixed numbers into improper fractions.
 - **a** $2\frac{5}{8}$

- **b** $1\frac{7}{9}$ **c** $3\frac{3}{8}$ **d** $4\frac{7}{11}$ **e** $3\frac{3}{4}$

- **f** $5\frac{4}{5}$ **g** $8\frac{7}{9}$ **h** $4\frac{11}{12}$ **i** $9\frac{5}{6}$ **j** $7\frac{5}{8}$
- **2** Convert these improper fractions into mixed numbers, simplifying where possible.

- **b** $\frac{18}{5}$ **c** $\frac{9}{6}$ **d** $\frac{13}{3}$ **e** $\frac{16}{7}$

- **f** $\frac{53}{8}$ **g** $\frac{81}{12}$ **h** $\frac{75}{20}$ **i** $\frac{81}{7}$ **j** $\frac{54}{5}$
- $\frac{1}{9}$ m $\frac{98}{7}$ n $\frac{69}{15}$ o $\frac{78}{16}$

explanation 2a

explanation 2b

3 Match each fraction in the left-hand column of the table to its equivalent fraction in the right-hand column.

$\frac{3}{8}$	$\frac{2}{3}$
<u>28</u> 49	$\frac{4}{7}$
<u>2</u> 11	$\frac{72}{120}$
<u>64</u> 96	<u>22</u> 121
$\frac{3}{5}$	45 120

- 4 Find the lowest common denominator for each pair of fractions.
 - a $\frac{2}{3}$ and $\frac{5}{6}$

- **b** $\frac{5}{8}$ and $\frac{2}{5}$ **c** $\frac{5}{7}$ and $\frac{4}{9}$ **d** $\frac{7}{12}$ and $\frac{5}{8}$

- e $\frac{1}{12}$ and $\frac{7}{30}$ f $\frac{3}{14}$ and $\frac{2}{35}$ g $\frac{13}{72}$ and $\frac{5}{6}$ h $\frac{11}{12}$ and $\frac{5}{42}$
- **5** Add each pair of fractions. Simplify your answers where possible.
 - $\frac{3}{8} + \frac{1}{4}$
- **b** $\frac{5}{7} + \frac{3}{14}$
- **c** $\frac{7}{12} + \frac{5}{8}$ **d** $\frac{9}{15} + \frac{7}{10}$

- e $\frac{2}{7} + \frac{1}{6}$ f $\frac{3}{11} + \frac{4}{9}$ g $\frac{1}{13} + \frac{3}{5}$ h $\frac{7}{9} + \frac{5}{6}$

6 Work these out.

$$\frac{5}{12} + \frac{1}{36}$$

- **a** $\frac{5}{12} + \frac{1}{36}$ **b** $\frac{11}{12} + \frac{1}{5}$ **c** $\frac{4}{9} + \frac{5}{7}$ **d** $\frac{3}{14} + \frac{10}{21}$

- e $\frac{7}{9} + \frac{5}{6}$ f $\frac{5}{24} + \frac{3}{8}$ g $\frac{9}{16} + \frac{13}{24}$ h $\frac{16}{21} + \frac{9}{14}$
- Tom and his brother cooked two pizzas. Tom ate $\frac{11}{12}$ of the first one, and his brother ate $\frac{7}{8}$ of the second one. What fraction of a pizza was left?



- Each month Saba's employer deducts $\frac{3}{8}$ of her salary for tax, $\frac{1}{16}$ for insurance and $\frac{1}{6}$ for her pension. What fraction of her pay is deducted each month?
- **9** A gas supplier gives customers a discount of $\frac{1}{16}$ of their bill if they pay on time, and a further discount of $\frac{1}{12}$ of the bill if they pay by direct debit. What fraction of the bill is deducted altogether if a customer pays on time by direct debit?
- **10** Work these out.

a
$$\frac{3}{4} - \frac{3}{8}$$

a
$$\frac{3}{4} - \frac{3}{8}$$
 b $\frac{11}{12} - \frac{5}{6}$ **c** $\frac{7}{9} - \frac{4}{7}$ **d** $\frac{5}{6} - \frac{3}{5}$

$$\frac{7}{9} - \frac{4}{7}$$

d
$$\frac{5}{6} - \frac{3}{5}$$

$$e \frac{8}{21} - \frac{3}{14}$$

$$f = \frac{4}{5} - \frac{3}{8}$$

$$\frac{2}{3} - \frac{5}{8}$$

e
$$\frac{8}{21} - \frac{3}{14}$$
 f $\frac{4}{5} - \frac{3}{8}$ **g** $\frac{2}{3} - \frac{5}{8}$ **h** $\frac{11}{15} - \frac{12}{45}$

11 Simplify where possible then work these out.

$$\frac{33}{55} - \frac{14}{77}$$

b
$$\frac{10}{12} - \frac{19}{30}$$

$$\frac{15}{20} - \frac{4}{8}$$

a
$$\frac{33}{55} - \frac{14}{77}$$
 b $\frac{10}{12} - \frac{19}{30}$ **c** $\frac{15}{20} - \frac{4}{8}$ **d** $\frac{20}{30} - \frac{10}{16}$

$$\frac{45}{60} - \frac{3}{18}$$

e
$$\frac{45}{60} - \frac{3}{18}$$
 f $\frac{13}{15} - \frac{6}{16}$ g $\frac{39}{52} - \frac{16}{64}$ h $\frac{16}{18} - \frac{3}{9}$

$$\frac{39}{52} - \frac{16}{64}$$

h
$$\frac{16}{18} - \frac{3}{9}$$

12 Work these out.

$$\frac{7}{8} + \frac{3}{4} - \frac{1}{2}$$

a
$$\frac{7}{8} + \frac{3}{4} - \frac{1}{2}$$
 b $\frac{7}{24} + \frac{7}{12} - \frac{5}{6}$ **c** $\frac{1}{2} + \frac{1}{5} - \frac{1}{3}$ **d** $\frac{3}{4} - \frac{1}{3} + \frac{5}{6}$

$$\frac{1}{2} + \frac{1}{5} - \frac{1}{3}$$

d
$$\frac{3}{4} - \frac{1}{3} + \frac{5}{6}$$

explanation 3a

explanation 3b

explanation 3c

13 Work these out.

a
$$1\frac{1}{2} + 2\frac{3}{4}$$
 b $2\frac{2}{3} + 1\frac{1}{4}$ **c** $2\frac{4}{5} + 1\frac{1}{2}$ **d** $5\frac{1}{2} + \frac{7}{10}$

b
$$2\frac{2}{3} + 1\frac{1}{4}$$

c
$$2\frac{4}{5} + 1\frac{1}{2}$$

d
$$5\frac{1}{2} + \frac{7}{10}$$

e
$$5\frac{1}{6} + 7\frac{4}{7}$$

$$\mathbf{f} = 2\frac{1}{2} + 4\frac{1}{3}$$

$$g = 8\frac{5}{8} + 3\frac{3}{11}$$

e
$$5\frac{1}{6} + 7\frac{4}{7}$$
 f $2\frac{1}{2} + 4\frac{1}{3}$ g $8\frac{5}{8} + 3\frac{3}{11}$ h $6\frac{8}{15} + 4\frac{9}{45}$

14 Work these out.

a
$$2\frac{4}{5} - 1\frac{1}{2}$$

b
$$2\frac{2}{3} - \frac{3}{5}$$

c
$$5\frac{5}{6} - 3\frac{2}{3}$$

a
$$2\frac{4}{5} - 1\frac{1}{2}$$
 b $2\frac{2}{3} - \frac{3}{5}$ **c** $5\frac{5}{6} - 3\frac{2}{3}$ **d** $4\frac{5}{8} - 1\frac{7}{24}$

15 Work these out.

a
$$5\frac{1}{6} + 3\frac{2}{3}$$

b
$$2\frac{1}{7} + 13\frac{1}{5}$$

a
$$5\frac{1}{6} + 3\frac{2}{3}$$
 b $2\frac{1}{7} + 13\frac{1}{5}$ **c** $7\frac{11}{12} - 2\frac{3}{16}$ **d** $8\frac{2}{9} - 4\frac{3}{7}$

d
$$8\frac{2}{9} - 4\frac{3}{7}$$

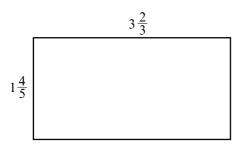
16 One photograph is $5\frac{1}{4}$ inches wide and another is $7\frac{5}{8}$ inches wide.

Narinder wants to paste them side by side in a book.

What is the minimum width the page in the book must be?



- 17 Liz made lemonade which filled two bottles. One bottle held $2\frac{4}{5}$ litres and the other $1\frac{1}{4}$ litres. How much more lemonade was in the larger bottle?
- **18** These are the dimensions of a storeroom in yards. Work out the perimeter of the room using an efficient strategy.



19 The table shows some of the ingredients for a cake.

Ingredient	Actual weight (ounces)
Flour	$3\frac{3}{4}$
Sugar	$4\frac{1}{8}$
Margarine	$4\frac{1}{4}$
Sultanas	$3\frac{3}{8}$

- a Find the total weight of the flour and sugar.
- **b** Find the difference between the weight of the sugar and sultanas.
- c Find the total weight of the margarine and sultanas.
- **d** Find the total weight of all four ingredients.

explanation 4a

explanation 4b

- **20** Convert these fractions to decimals.
 - **a** $\frac{3}{4}$
- **b** $\frac{5}{8}$
- $\frac{7}{20}$
- **d** $\frac{16}{25}$
- Which of these fractions could you express as a terminating decimal? Convert each fraction into a terminating decimal or a decimal to 2 d.p.
 - **a** $\frac{3}{4}$
- **b** $\frac{20}{25}$
- $\frac{64}{200}$
- d $\frac{22}{91}$
- $e \frac{18}{72}$