Geometry and measures GM1.3



Constructions

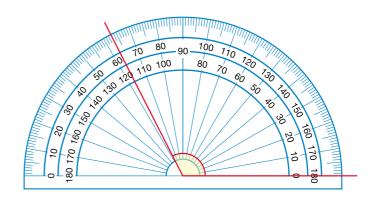
- Measuring and drawing reflex angles
- Constructing a triangle given two sides and the included angle
- Constructing a triangle given two angles and the included side
- Solving problems using constructions

Keywords

You should know

explanation 1

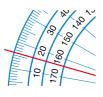
Stephen is measuring an angle between two lines. He uses a 180° protractor. The diagram shows the angle that he is trying to measure.

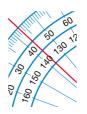


Stephen thinks that the reading could be 123°, 117°, 63° or 77°.

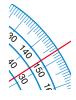
- How do you know the angle cannot be either 63° or 77°?
- Which is the correct reading, 123° or 117°?
- **2** Find the **acute** angles shown on these protractor scales.

a

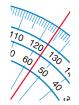


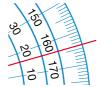






3 Find the **obtuse** angles shown on these protractor scales.









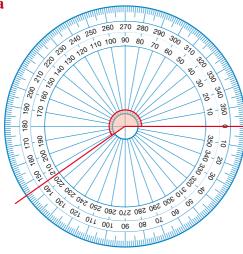
- **4** Use a protractor to draw these angles.
 - **a** 60°
- 75°
- c 130° d 155°
- e 42°

- 132°
- **g** 58°
- h 163° i 56°
- i 108°

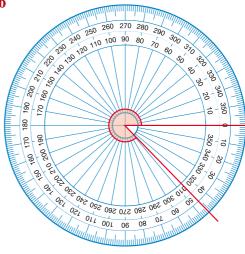
explanation 2

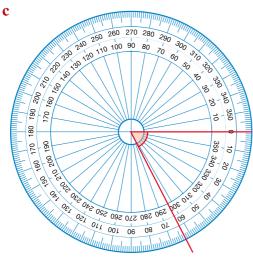
5 These are 360° protractors. Find the angles shown.



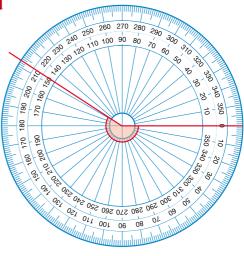


b



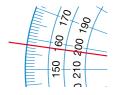


d

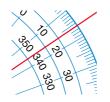


6 Use the information given on these diagrams to find the unknown *reflex* angles.

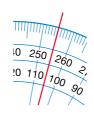
a



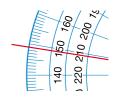
h



C



d



7 Use a protractor to draw these reflex angles.

a 300°

b 245°

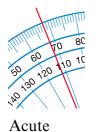
c 198°

d 273°

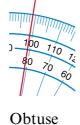
e 317°

8 Find the size of each angle. Use the type of angle and the measurement shown on the protractor scales to help you.

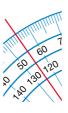
a



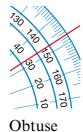
b



c



u



Acute





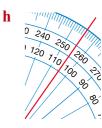
Reflex



Acute



Reflex



- flex Obtuse
- **9** Use a protractor to draw these angles.

a 45°

b 30°

c 120°

d 75°

e 145°

f 163°

g 28°

h 200°

i 260°

j 335°

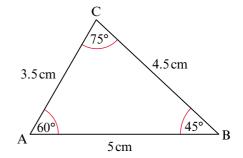
explanation 3

- **10** Look at triangle ABC. Write down the size of these sides and angles.
 - a AB

b AC

c CB

- **d** ∠ABC
- e ∠CAB
- f ∠BCA

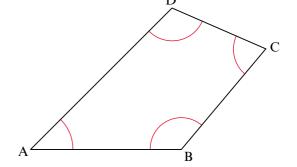


- 11 Look at quadrilateral ABCD. Measure the size of these sides and angles.
 - a AB

b DA

c BC

- d CD
- e ∠ABC
- **f** ∠BCD
- **g** ∠CDA
- h ∠DAB



12 Sketch triangle ABC. Add the measurements to your sketch.

$$AB = 6 \text{ cm}$$

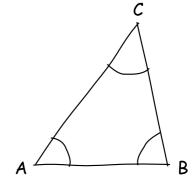
$$\angle ABC = 55^{\circ}$$

$$AC = 5 \text{ cm}$$

$$\angle ACB = 80^{\circ}$$

$$BC = 4.3 \,\mathrm{cm}$$

$$\angle BAC = 45^{\circ}$$

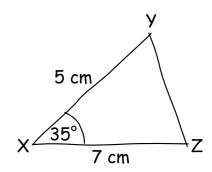


explanation 4a

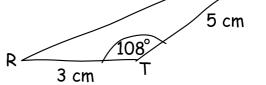
explanation 4b

explanation 4c

- **13** Look at the sketch of triangle XYZ.
 - **a** Use the information in this sketch to construct triangle XYZ.
 - **b** i Find the length of YZ.
 - ii Find ∠XZY.
 - iii Find ∠XYZ.



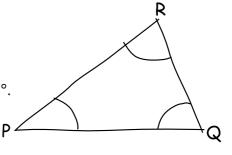
- **14** Look at the sketch of triangle RST.
 - **a** Use the information in this sketch to construct triangle RST.
 - **b** i Find the length of RS.
 - ii Find ∠TRS.
 - iii Find ∠TSR.



- **15** Look at the sketch of triangle PQR.
 - a Copy the sketch of triangle PQR. Add this information to your sketch.

$$PQ = 8.5 \text{ cm}, QR = 3.6 \text{ cm}, \angle PQR = 67^{\circ}.$$

- **b** Construct triangle PQR.
- c Measure PR and ∠PRQ.



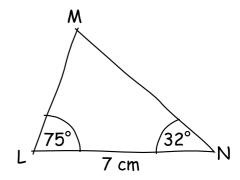
explanation 5a

explanation 5b

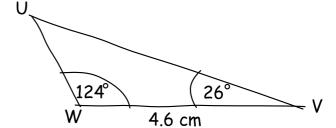
explanation 5c

explanation 5d

- **16** Look at the sketch of triangle LMN.
 - a Use the information in this sketch to construct triangle LMN.
 - **b** i Find the length of LM.
 - ii Find the length of MN.



- 17 Look at the sketch of triangle UVW.
 - **a** Use the information in this sketch to construct triangle UVW.

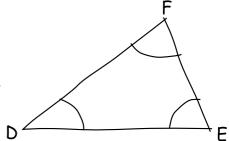


- **b** i Find the length of UW.
 - ii Find the length of UV.
- **18** Look at the sketch of triangle DEF.
 - a Copy the sketch of triangle DEF.

 Add this information to your sketch.

DE =
$$7.8 \,\mathrm{cm}$$
, $\angle DEF = 68^{\circ}$, $\angle FDE = 32^{\circ}$.

- **b** Construct triangle DEF.
- **c** Measure DF and EF.



19 The sketch shows part of a spider's web.

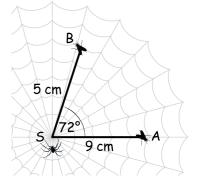
Two flies get caught in the web at A and B.

The spider at S can tell how far away each fly is and what direction it is in.

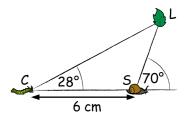
$$SA = 9 cm$$

 $SB = 5 cm$
 $\angle ASB = 72^{\circ}$

- a Construct the triangle ABS.
- **b** Measure the distance between the two flies.



20 A caterpillar at C and a snail at S are 6cm apart. They both see a tasty leaf at L. The direction of L from C and from S is shown in the sketch.



- a i Calculate ∠CSL. Explain your answer.
 - ii Explain why angle CLS is 42°.
- **b** Construct the triangle CSL.
- **c** Measure the lengths CL and SL to the nearest millimetre.
- *d The caterpillar moves twice as fast as the snail. Which one will reach the leaf first?