## **Powers of 10**

- Working with positive powers of 10
- Multiplying and dividing by powers of 10
- Ordering numbers less than 1 using inequality signs

**Keywords** 

You should know

## explanation 1

1 Copy and complete each of these. The first one has been done for you.

**a** 
$$10^3 = 10 \times 10 \times 10 = 1000$$

**b** 
$$10^2 = \square \times \square = \square$$

**c** 
$$10^0 = \Box$$

**d** 
$$10^5 =$$
 =

**e** 
$$10^7 =$$
\_\_\_\_\_ =  $\Box$ 

**2** Write these numbers without using powers.

**a** 
$$3 \times 10^4$$

**b** 
$$7 \times 10^6$$

**c** 
$$4 \times 10^{1}$$

**d** 
$$5 \times 10^4$$

**e** 
$$3 \times 10^8$$

**f** 
$$2.7 \times 10^4$$

$$9.2 \times 10^8$$

**h** 
$$1.8 \times 10^9$$

**3** Write these numbers using powers of 10.

$$d \quad 1\,000\,000\,000$$

## explanation 2a

explanation 2b

**4** Work out these multiplications without using a calculator.

**a** 
$$8.23 \times 100$$

**d** 
$$5.8 \times 0.1$$

**e** 
$$3.724 \times 0.01$$

**g** 
$$0.641 \times 0.1$$

$$0.098 \times 0.01$$

$$k 459.87 \times 0.1$$

1 
$$45689.02 \times 0.001$$

**5** Work these out without using a calculator.

**a** 
$$28.7 \div 10$$

**f** 
$$2.147 \div 100$$

$$\mathbf{g} = 0.435 \div 10000$$

**h** 
$$1634.7 \div 1000000$$

**6** Work these out without using a calculator.

**a** 
$$0.09 \div 0.001$$

**b** 
$$78.45 \div 0.01$$

c 
$$78987.4 \div 0.001$$

**d** 
$$8.007 \div 0.001$$

e 
$$72.1 \div 0.1$$

$$982 \div 0.01$$

$$\mathbf{g}$$
 1042 ÷ 0.001

**h** 
$$0.473 \div 0.1$$

$$0.62 \div 0.01$$

$$0.85 \div 0.001$$

$$k 25.9 \div 0.01$$

1 
$$3.14 \div 0.001$$

**7** State whether each of these calculations is true or false. If false, write a correct calculation to give the answer shown.

**a** 
$$0.74 \times 0.001 = 0.0074$$

**b** 
$$430 \div 1000 = 0.430$$

$$0.265 \times 0.0001 = 0.0000265$$

**d** 
$$0.265 \div 10000 = 0.00000265$$

**8** Fill in the blanks without using a calculator.

**a** 
$$67.2 \times \square = 0.672$$

**b** 
$$\Box \div 0.01 = 67.2$$

c 
$$824 \div 1000 = \square$$

**d** 
$$0.824 \times 1000 = \Box$$

e 
$$101010 \div 0.001 = \square$$

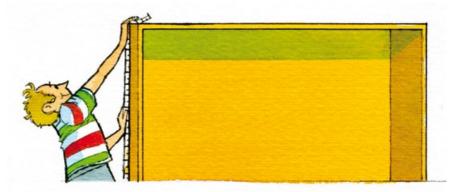
**f** 
$$0.215 \times \square = 21500$$

$$\mathbf{g} \quad 0.009 \times \square = 0.0009$$

**h** 
$$0.05 \div \square = 50$$

**9** Nathan measured the height of a cupboard as 2.1 m.

How many 0.1 m high boxes can he stack, one on top of the other, in the cupboard?



**10** William filled six test tubes with 0.01 litres of liquid in each.

How much liquid did he use altogether?

- 11 How many litres would be needed to fill these?
  - **a** 5 bottles with 0.1 litres in each
- **b** 6 cups with 0.01 litres in each
- c 8 test tubes with 0.001 litres each
- **d** 14 cups with 0.01 litres in each

explanation 3a

explanation 3b

**12** Work these out without using a calculator.

$$\mathbf{a} \quad 6 \times 0.9$$

**b** 
$$30 \times 0.07$$

c 
$$700 \times 0.4$$

**d** 
$$0.7 \times 5000$$

**e** 
$$0.85 \times 200$$

**f** 
$$20 \times 0.034$$

**g** 
$$0.06 \times 60$$

**h** 
$$0.004 \times 80$$

i 
$$4000 \times 0.12$$

$$j = 0.32 \times 300$$

$$k = 5000 \times 0.011$$

$$1.0.25 \times 40000$$

**13** Work these out without using a calculator.

**a** 
$$0.06 \times 0.05$$

**b** 
$$0.007 \times 0.08$$

c 
$$0.32 \times 0.04$$

**d** 
$$0.0005 \times 0.7$$

$$e 0.7 \times 0.006$$

**f** 
$$0.008 \times 0.09$$

$$\mathbf{g} = 0.0001 \times 0.02$$

**h** 
$$0.0003 \times 0.0009$$

i 
$$0.008 \times 0.0008$$

$$0.0007 \times 0.00003$$

$$k = 0.009^2$$

$$1 \quad 0.0007^2$$

**14** Copy and complete these.

a 
$$63 \div 0.09 = \frac{63}{0.09} = \frac{1}{9} = \frac{1}{3} = 1$$

$$\times 100 \div 3$$

**b** 
$$0.9 \div 0.015 = \frac{0.9}{0.015} = \frac{1}{15} = \frac{1}{5} = \frac{1}{5}$$

- **15** Work these out without using a calculator.
  - **a**  $8 \div 0.2$

**b**  $70 \div 0.5$ 

 $c 300 \div 0.6$ 

**d**  $40 \div 0.08$ 

- e  $540 \div 0.09$
- $f 8100 \div 0.81$

**g**  $930 \div 0.003$ 

- **h**  $4900 \div 0.7$
- i 81 ÷ 0.009

 $j 2100 \div 0.03$ 

- $k \quad 360 \div 0.06$
- 1 40 000 ÷ 0.008

- **16** Work these out without using a calculator.
  - **a**  $3.5 \div 0.5$

- **b**  $2.1 \div 0.07$
- **c**  $6.4 \div 0.008$

**d**  $0.72 \div 0.8$ 

- **e**  $0.054 \div 0.6$
- **f**  $0.0093 \div 0.03$

- **g**  $0.081 \div 0.09$
- **h**  $0.0077 \div 0.011$
- i  $0.305 \div 0.05$
- 17 Write two possible questions using multiplication and division by decimals (as in questions 4 to 16) which would give you each answer.
  - **a** 9.6
- **b** 150
- **c** 0.56
- **d** 3200
- **e** 0.00063

## explanation 4

The next few questions use the following conversions:

1 kg = 1000 g, 1 g = 1000 mg, 1 litre = 1000 ml, 1 km = 1000 m, 1 m = 1000 mm.

- **18** Convert these measurements.
  - a 0.32 m into km
- **b** 93 mm into m
- **c** 42.57 km into m

- d 305 m into mm
- e 4820 mm into m
- f 397 cm into m

- **g** 5680 m into km
- **h** 89.76 km into m
- i 3 mm to m

- **19** Convert these.
  - a 64 g into mg
- **b** 7924 mg into g
- c 4.389 kg into g

- **d** 567.9 g into kg
- **e** 0.0754 kg into g
- f 54 g into kg

- **20** Convert these.
  - a 945 ml into litres
- **b** 0.734 litres into ml
- c 457 ml into litres

- d 0.009 litres into ml
- e 0.4 ml into litres
- f 3.7 ml into litres

**21** Five gigabytes could be written as  $5 \times 10^9$  bytes.

Write each of these measurements using powers of 10.

- **a** 2 gigabytes = \_\_\_\_\_\_ bytes
- **b** 2 megabytes = \_\_\_\_\_ bytes
- **c** 2 kilobytes = \_\_\_\_\_ bytes
- **d** 7.4 megabytes = \_\_\_\_\_ bytes

explanation 5a

explanation 5b

- **22** Place one of =, > and < between each of these pairs.
  - a 120 cm 1.2 m
- **b** 8.75 litres 8750 ml
- c 6km 600 000 mm
- d 920 m 0.92 km

- e  $0.57 \,\mathrm{g} \,\square \, 0.0057 \,\mathrm{kg}$  f  $25 \,\mathrm{kg} \,\square \, 25\,000 \,\mathrm{g}$
- **g** 0.333 m 333 mm
- $h = 0.75 \,\mathrm{m} \,\square \,75 \,\mathrm{mm}$
- 23 Draw number lines going from -5 to 4 and use one to illustrate each of these inequalities.

  - **a**  $x \le 3$  **b**  $x \le -2$  **c**  $x \ge 1$  **d**  $x \ge -3$

- **e** x < 3 **f** x < -4 **g** x > -1 **h** x > 0
- **24** Write down the inequality show by each number line.

