Formulae

- Using a formula
- Simplifying expressions in algebra
- **Building and simplifying a formula**

Keywords

You should know

explanation 1a

explanation 1b

1 What is the value of each expression?

a
$$2 + 3 \times 4$$

b
$$21 - 2 \times 9$$

$$c 5(2+6)$$

d
$$5 \times 2 + 6$$

e
$$8 \times 6 - 3 \times 4$$

f
$$8(6-3) \times 4$$

$$\mathbf{g} \quad 3 \times 5 + 6 \times 4$$

h
$$7 + 6 \div 2$$

$$i (7+6) \div 2$$

i
$$10 \div 2 + 12 \div 3$$
 k $15 - 7 + 4$

$$k 15 - 7 + 4$$

$$115 - (7 + 4)$$

2 What is the value of each expression?

a
$$3 \times 4 \times 5$$

b
$$3 \times (4 \times 5)$$

c
$$54 \div 6 \div 3$$

d
$$54 \div (6 \div 3)$$

$$\mathbf{f} = 18 - 10 - 6$$

$$\mathbf{g} \quad 4 + 7 + 5$$

h
$$4 + (7 + 5)$$

$$\mathbf{i} \quad 9 + (7 - 3)$$

$$\mathbf{j} = 9 + 7 - 3$$

$$k 30 - 21 + 8$$

3 Find the value of each expression when x = 5.

a
$$x + 3$$

d
$$4x - 7$$

e
$$10 - x$$

f
$$27 - 2x$$

g
$$15 - x + 3$$

h
$$12 - x - 4$$
 i $4 - x$

$$\mathbf{i} \quad 4 - x$$

$$i$$
 $-2x$

k
$$10 - 2x$$

$$1 -2x + 10$$

4 Find the value of each expression when y = 3.

a
$$3(y+6)$$

b
$$50 - 4(v + 1)$$

c
$$12 + 2(y - 1)$$

d
$$3(y + 2y)$$

$$e 10 - 2(6 - v)$$

$$\mathbf{f} = 3y - y$$

g
$$(y-2)+(7-2y)$$
 h $y-(2-y)$

h
$$y - (2 - y)$$

$$(y + 1) \times (y + 2)$$

5 Find the value of each expression when x = 12.

a
$$\frac{x}{3}$$

b
$$\frac{x+8}{4}$$

$$\frac{x-3}{3}$$

d
$$\frac{3x}{4}$$

e
$$\frac{2x}{3}$$
 f $\frac{5x}{6}$

$$f = \frac{5x}{6}$$

$$\mathbf{g} = \frac{60}{x}$$

h
$$\frac{108}{x}$$

*i
$$\frac{18}{x-3}$$

6 Find the value of each expression when x = 7 and y = 4.

$$\mathbf{a} \quad x + y$$

b
$$x-y$$

$$\mathbf{c} \quad x + 2y$$

$$\mathbf{d} \quad 2x + y$$

$$\mathbf{e} \quad x + 3y$$

d
$$2x + y$$
 e $x + 3y$ **f** $20 - x - y$

$$\mathbf{g} = 3(x+y)$$

h
$$2x + 5y$$

g
$$3(x+y)$$
 h $2x+5y$ **i** $5-(x-y)$

$$\frac{x+1}{y}$$

$$k = \frac{15}{x-y}$$

explanation 2a

explanation 2b

7 Simplify these expressions.

a
$$x + 2 + 3$$

b
$$x + 9 - 2$$

a
$$x + 2 + 3$$
 b $x + 9 - 2$ **c** $x + 3 \times 4$

$$\mathbf{d} \quad x + x$$

e
$$x + x + x$$

e
$$x + x + x$$
 f $x + x - x$

$$\mathbf{g} \quad 2x + x$$

$$\mathbf{h} = 2x - x$$

h
$$2x - x$$
 i $2x + 3x$

$$3x-2x$$

$$\mathbf{k}$$
 $5x + 3x + x$

j
$$3x - 2x$$
 k $5x + 3x + x$ **l** $9x - 2x - 4x$

8 Copy and complete these expressions.

a
$$39 + 27 + 1 = 39 + 1 + \square = \square$$

b
$$28 + 75 + 25 + 11 = 28 + \square + 11 = \square$$

c
$$327 - 98 - 2 + 30 = 327 - \square + 30 = \square$$

d
$$579 + 86 - 79 = 579 - \square + \square = \square$$

e
$$49 + 78 + 51 + 65 + 22 = 49 + \square + 78 + \square + 65 = \square$$

9 Explain what question **8** shows about addition and subtraction.

- **10** Work out these expressions by rewriting in the simplest order.
 - a 75 + 49 + 25 + 51 + 88
- **b** 53 + 94 + 6 + 75 + 47
- c 78 + 67 18 + 40
- **d** 139 43 56 1
- e 11 18 + 58 21
- $\mathbf{f} = 32 54 16 + 68$
- 11 Simplify these expressions by rewriting to group together like terms.

- **a** x + 3 + x **b** x + 4 + x + 6 **c** 2x + 5 + x 3
- **d** x + x x + x x **e** 5x 3 x + 7 **f** 4 2x 4 + 7x
- 12 Simplify these expressions. Rewrite to group together like terms where necessary.
- **a** x + y + y **b** 2x y + y **c** 3x + y x + y

- **d** x + 3 + y + 5 **e** x y + y + x + 3 **f** 2x + y 3 x + 4y

- $\mathbf{g} \quad xy + xy$ $\mathbf{h} \quad 2xy + 3xy$ $\mathbf{i} \quad xyz + xyz$

- j 3xy 4y 2yx k 2zyx yx + 1 + xyz l 2 + p + pqr 2 3pqr
- 13 Write expressions for the following situations as simply as possible:
 - a Simon has x + 3 sweets. Jo has 4 more sweets than Simon. How many sweets does Jo have?
 - **b** Helen lives x miles away from school. Jane lives a further y miles from school. How many miles from school does Jane live?
 - **c** Rob has *n* marbles but loses 5 of them. How many does he have left?
 - **d** Liz has p marbles but loses q of them. How many does she have left?



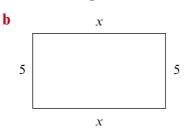
- **14** Jack has k computer games and Jill has t computer games. Jack swaps 3 of his games for 1 of Jill's.
 - **a** How many games does Jack then have?
 - **b** How many games does Jill have?

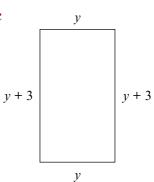
explanation 3

15 Find and simplify a formula for the perimeter, P, of each shape.

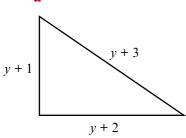
 χ \boldsymbol{x} χ

х

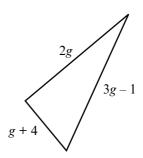


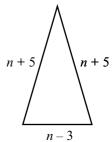


16 Find and simplify a formula for the perimeter, P, of each shape.

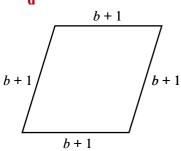


b

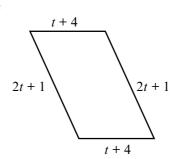




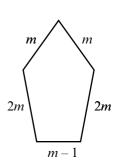
d



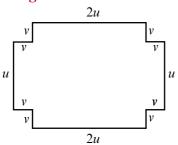
e



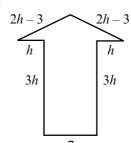
f



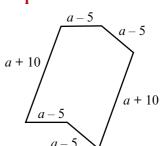
g



h



i



17 A

2x

В

x + 3

 \mathbf{C}

x-5

D

7-x

E

4-2x

F

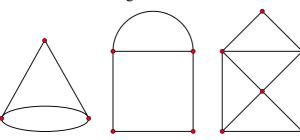
3x + 1

- a Which two cards total 4x + 4?
- **b** Which two cards total x + 5?
- **c** Which two cards total 4?
- **d** Which two cards total 10?
- e Which three cards total 12?
- f Which three cards total 3x + 11?
- **g** What is the total of all of the expressions on the cards?

explanation 4

- **18** Use the formula B = H + M.
 - a Find B when H = 5 and M = 7.
 - **b** Find B when H = 5 and M = 2.
 - c Find B when H = 3.5 and M = 2.
- **19** Use the formula $s = \frac{d}{t}$.
 - a Find s when d = 12 and t = 3.
 - **b** Find s when d = 56 and t = 8.
 - c Find s when d = 150 and t = 25.
 - d Find d when s = 20 and t = 11.
- **20** Use the formula F = ma.
 - a Find F when m = 3 and a = 10.
 - **b** Find *F* when m = 4.8 and a = 10.
 - c Find F when m = 5 and a = 1.3.
 - d Find m when F = 24 and a = 4.

21 Look at these diagrams.



N	A	R
3	4	3

N represents the number of red dots.

A represents the number of arcs or lines.

R represents the number of regions or spaces.

The table shows the values of N, A and R for the first diagram. Notice that the outside of the diagram counts as a region, so R = 3.

- a Copy and complete the table for the other two diagrams.
- **b** Draw some diagrams of your own and fill in the table.
- c Work out the value of N + A R for each row in the table. What do you notice? Copy and complete this formula:

$$N+A-R=\square$$
.

22 Copy and complete the table using the formula v = u + at.

и	а	t	v
16	2.7	8	
11	5.6	7	
	3.5	12	50
30	6.7		164
45		4.6	79.5

23 Use the formula $d = \frac{m}{v}$ to find d to 2 d.p. for these values of m and v.

a
$$m = 50$$
 and $v = 41$

b
$$m = 220$$
 and $v = 176$

$$m = 350 \text{ and } v = 423$$