



Angles and polygons

- Finding the sum of the exterior angles of a polygon
- Finding the sum of the interior angles of a polygon
- Finding the angle between a radius and tangent
- Proving statements in geometry

Keywords

You should know

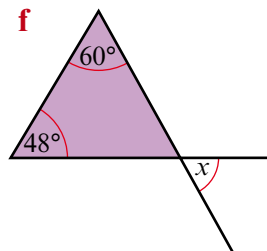
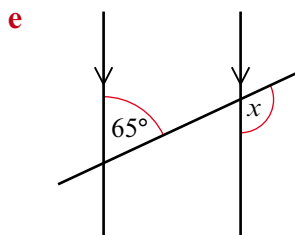
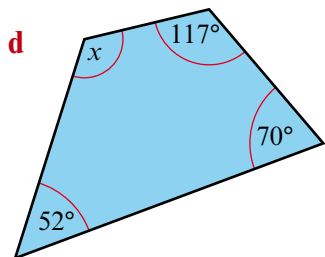
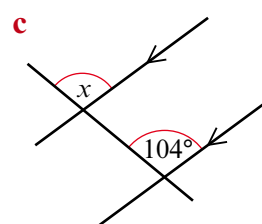
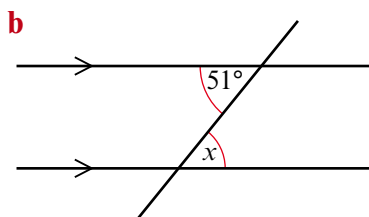
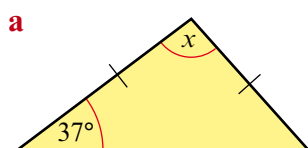
explanation 1a

explanation 1b

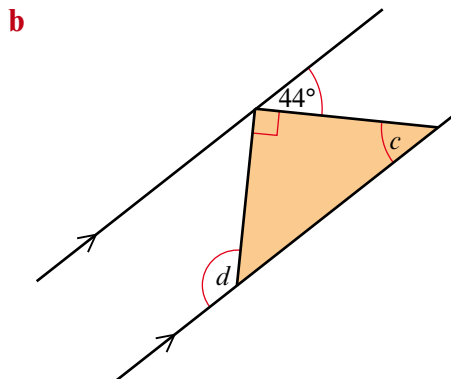
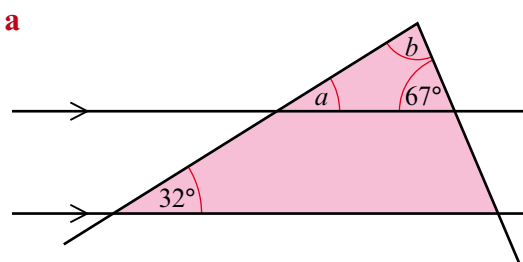
explanation 1c

explanation 1d

1 In each diagram, find the size of x . Give reasons for your answers.

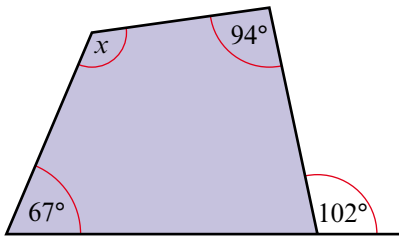


2 Find the size of each angle marked by a letter. Give reasons for your answers.

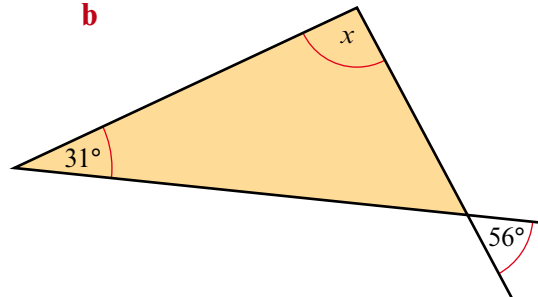


3 In each diagram, find the size of x .

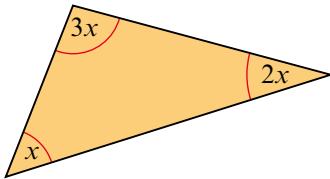
a



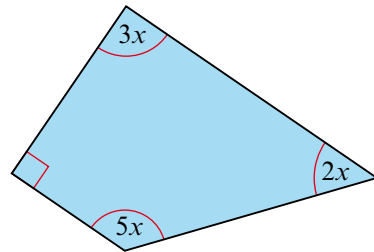
b



c

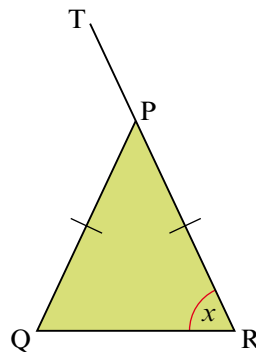


d

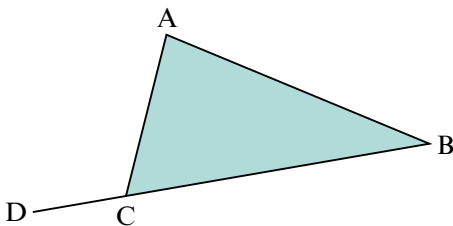


explanation 2

4 Prove that angle $TPQ = 2x$.



5 Prove that angle $DCA = \text{angle } CAB + \text{angle } ABC$.

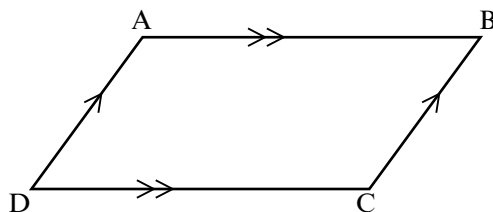


Note

Your answer proves that, in general:
The exterior angle of a triangle
equals the sum of the two interior
opposite angles.

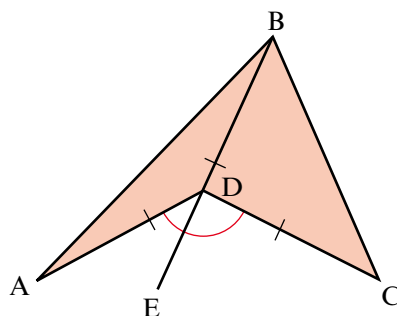
- 6** Prove that $\angle ADC = \angle ABC$.

Hint: Copy the diagram and draw in the diagonal BD.



- 7** Prove that $\angle ADC = 2 \times \angle ABC$.

Hint: Copy the diagram and label $\angle ABD$ as x and $\angle DBC$ as y .



explanation 3a

explanation 3b

- 8** This question is about regular hexagons.

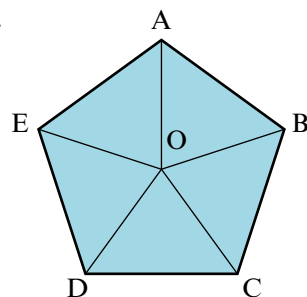
- a** Work out the angles at the centre of a regular hexagon.
- b** Use your answer to part **a** to draw a regular hexagon.

- 9** This question is about regular nonagons.

- a** Work out the angles at the centre of a regular nonagon.
- b** Use your answer to part **a** to draw a regular nonagon.

- 10** The diagram shows a regular pentagon, with centre O.

- a** Work out the size of $\angle AOB$.
- b** Work out the size of $\angle OAB$.
- c** Work out the size of $\angle EAB$.
- d** $\angle EAB$ is an interior angle of the polygon.
Work out the sum of all the interior angles in the pentagon.



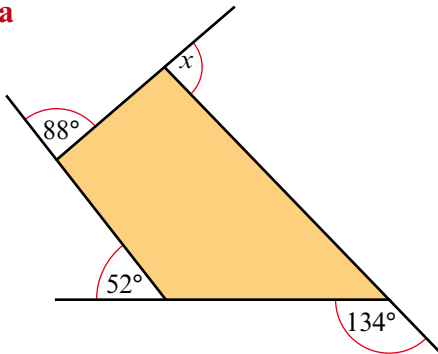
- 11** Work out the sum of all the interior angles in a regular octagon.
Use a similar method to that in question **10**.

explanation 4a

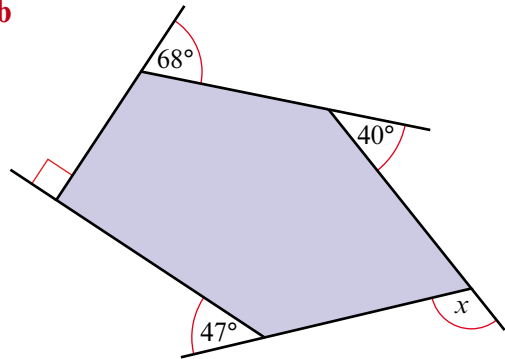
explanation 4b

12 In each diagram, find the size of x .

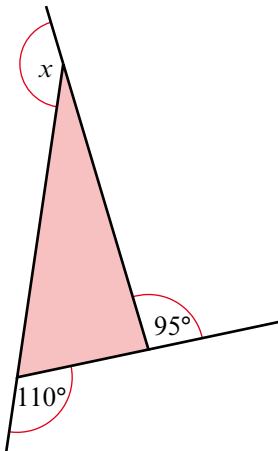
a



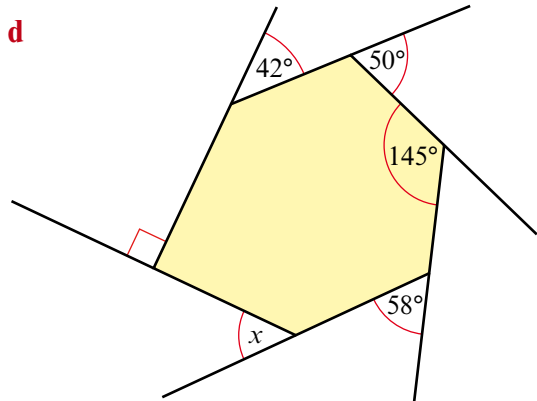
b



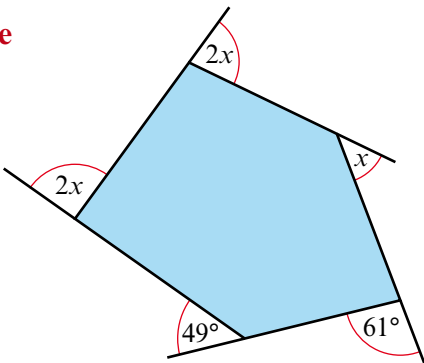
c



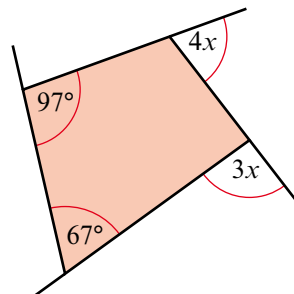
d



e



f



13 The exterior angles of a pentagon are $2x$, $2x$, $3x$, $4x$ and $4x$.

a Find the value of x .

b What is the size of each of the pentagon's exterior angles?

- 14** The exterior angles of a hexagon are x , $2x$, $3x$, $3x$, $4x$ and $5x$.
What is the size of each of the hexagon's exterior angles?

explanation 5a

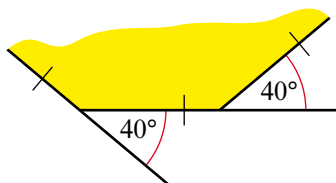
explanation 5b

- 15** Below are the numbers of sides of regular polygons.
What is the size of an exterior angle in each regular polygon?

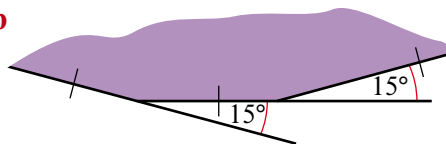
- a** 5 sides **b** 8 sides **c** 10 sides
d 15 sides **e** 16 sides **f** 30 sides

- 16** Each diagram shows part of a regular polygon.
How many sides does each regular polygon have?

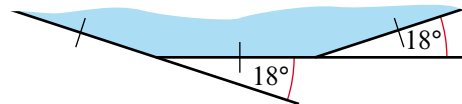
a



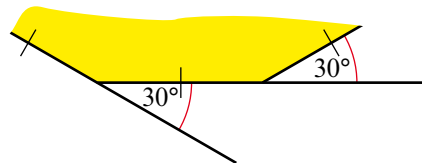
b



c



d



- 17** Each exterior angle of a regular polygon is 20° .
How many sides does the regular polygon have?

explanation 6a

explanation 6b

- 18** Below are the numbers of sides of regular polygons.
What is the sum of the interior angles in each regular polygon?

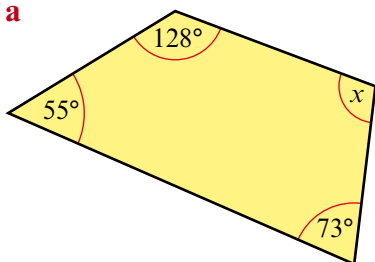
- a** 5 sides **b** 8 sides **c** 12 sides

- 19** Below are the numbers of sides of regular polygons.
What is the size of an interior angle in each regular polygon?

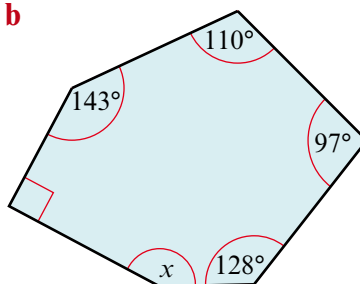
- a** 6 sides **b** 9 sides **c** 20 sides

20 In each of the following questions, find the size of the angle marked x .

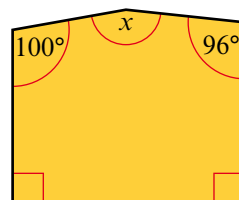
a



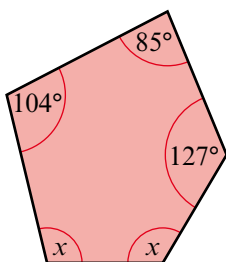
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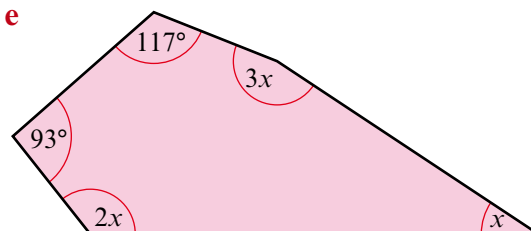
c



d



e

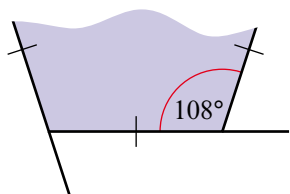


21 Eloise says: ‘The sum of the interior angles of a decagon is double the sum of the interior angles in a pentagon.’

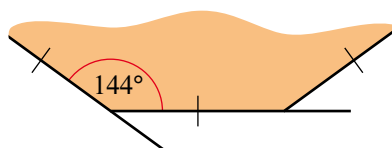
Is Eloise correct? Give an explanation for your answer.

22 Each diagram shows part of a regular polygon. In each case, work out the number of sides of the regular polygon.

a



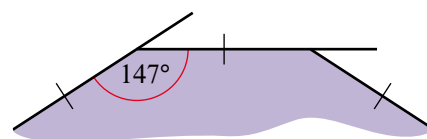
b



c



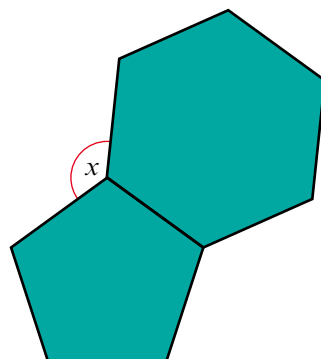
d



23 Sahil says: ‘I have drawn an accurate regular polygon. All the interior angles add up to 1000° .’

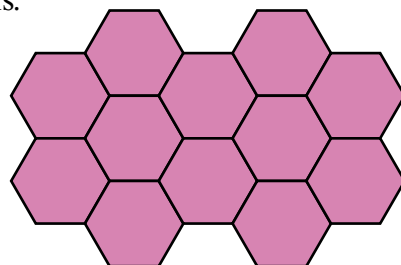
Could Sahil have drawn this regular polygon? Explain your answer.

- 24** The diagram shows a regular hexagon and a regular pentagon.
Work out the size of the angle marked x .



- 25** The diagram shows a tessellation using hexagons.

- a** Explain why regular hexagons tessellate but regular octagons do not.
b Which other regular polygons will tessellate? Give an explanation for your answers.



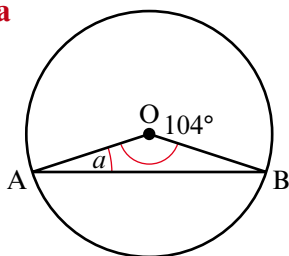
explanation 7a

explanation 7b

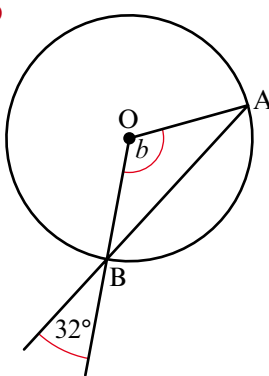
explanation 7c

- 26** Find the sizes of the angles a to f . Give reasons for your answers.

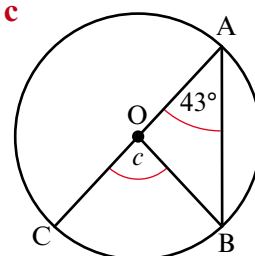
a



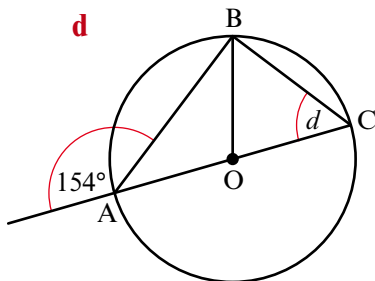
b



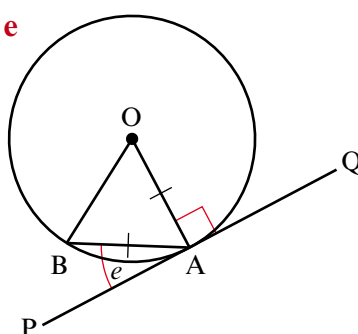
c



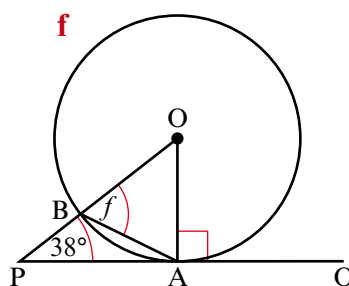
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e



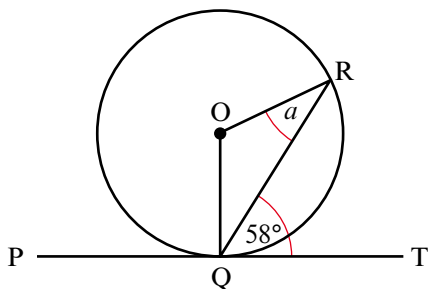
f



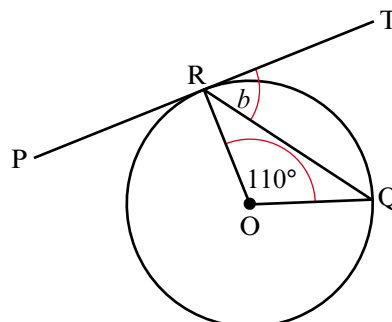
27 In each diagram, PT is a tangent to the circle.

Find the sizes of the angles a , b , c , d and e . Give reasons for your answers.

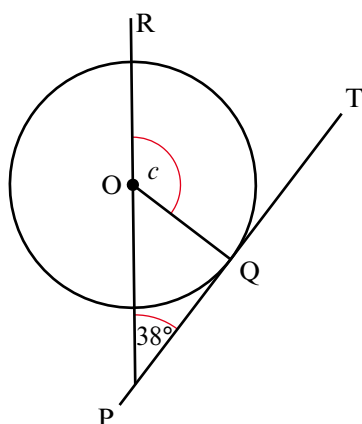
a



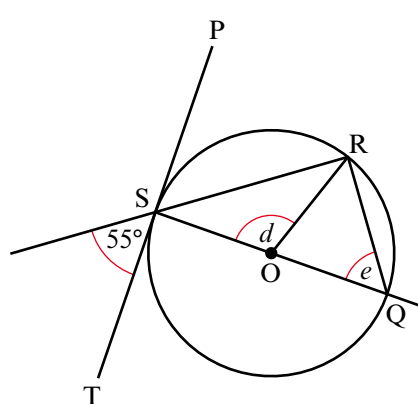
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c



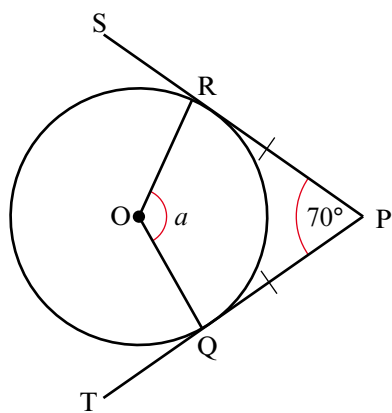
d



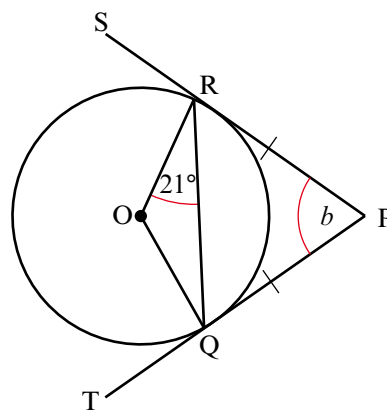
28 In these diagrams, PS and PT are both tangents to the circle.

Find the sizes of the angles marked a and b . Give reasons for your answers.

a



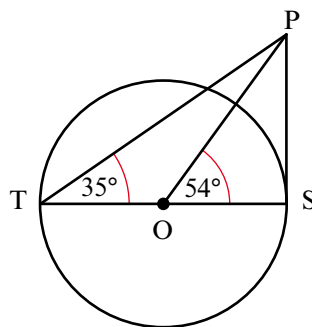
b



29 PS is a tangent to the circle.

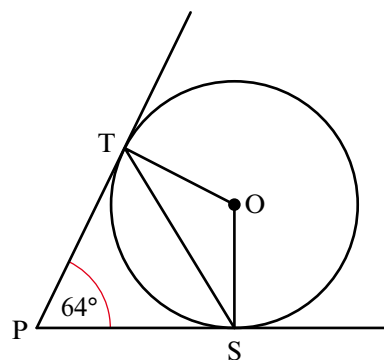
a Work out angle OPS.

b Work out angle OPT.



30 PS and PT are tangents to the circle centre O.

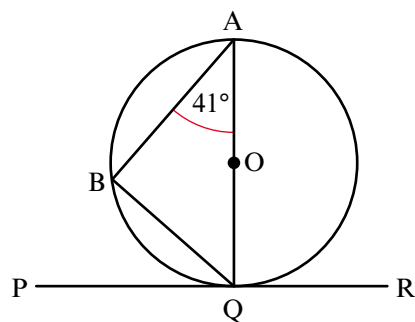
Work out the size of angle STO.



31 AQ is the diameter of a circle, centre O.

PQR is a tangent to the circle at Q.

Work out the size of angle PQB.



32 PQR is a tangent at Q to the circle, centre O.

Work out the size of angle OTQ.

