$Last\ Name = \underline{\hspace{1cm}}, First\ Name = \underline{\hspace{1cm}}$ $ONID\ login = = \underline{\hspace{1cm}} @oregonstate.edu$

- 1. (0.5pts) Under what condition does a DFA M recognize the empty language? Use the mathematical language $(\delta^*, \forall, \exists, \text{ etc.})$
- 2. (2.5pt) Prove $(u^R)^R = u$ for any string u. (0.5pts) First define reverse:

(2pts) Now prove by induction (on _____); please clearly mark base case, inductive hypothesis (IH), by definition, and by IH. (Hint: You can use the theorem from HW2 that $(xy)^R = y^R x^R$.)

- 3. (1pt) Draw the following two DFAs:
 - (a) "binary number divisible by 4" (3 states) | (b) "binary number divisible by 3"

4. (1pt) Use the table-filling algorithm to show that the two above machines are not equivalent.