CS 331: Artificial Intelligence Naïve Bayes

Thanks to Andrew Moore for some course material

Naïve Bayes

- · A special type of Bayesian network
- Makes a conditional independence assumption
- · Typically used for classification

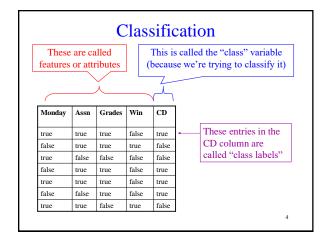
2

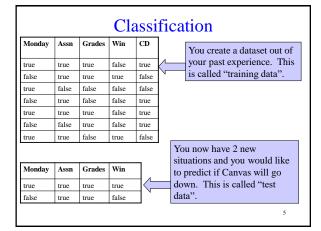
Classification

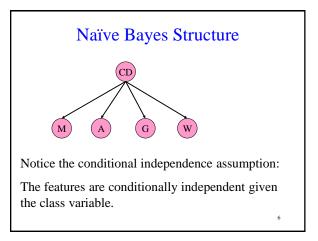
Suppose you are trying to classify situations that determine whether or not Canvas will be down. You've come up with the following list of variables (which are all Boolean):

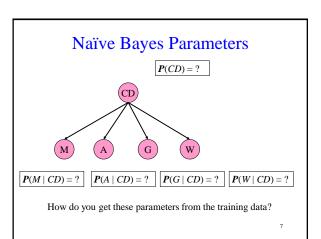
Monday	Is a Monday					
Assn	CS331 assignment					
	due					
Grades	CS331 instructor					
	needs to enter grades					
Win	The Beavers won the					
	football game					

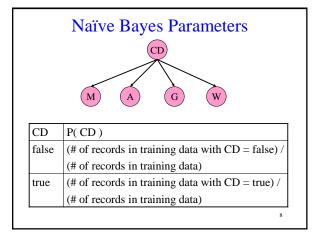
We also have a Boolean variable called CD which stands for "Canvas down"

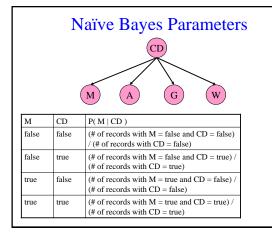


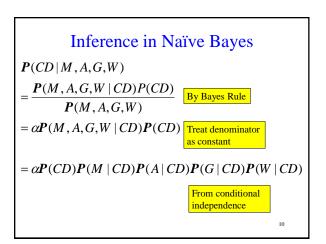












Prediction

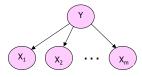
- Suppose you are now in a day when M=true, A=true, G=true, W=true.
- You need to predict if CD=true or CD=false.
- We will use the notation that CD=true is equivalent to cd and CD=false is equivalent to ¬cd.

11

Prediction

- You need to compare:
 - $P(cd | m, a, g, w) = \alpha P(cd) P(m | cd) P(a | cd) P(g | cd) P(w | cd)$
 - $\begin{array}{l} \ P(\neg cd \mid m, \, a, \, g, \, w) = \alpha \ P(\neg cd \,) \ P(\ m \mid \neg cd \,) \ P(\\ a \mid \neg cd \,) \ P(\ g \mid \neg cd \,) \ P(\ w \mid \neg cd \,) \end{array}$
- Whichever probability is the bigger of the two above, that is your prediction for CD
- Because you take the max of the two probabilities above, you can ignore α (since it is the same in both)

The General Case



- 1. Estimate P(Y=v) as fraction of records with Y=v
- Estimate P(X_i=u | Y=v) as fraction of "Y=v" records that also have X=u.
- To predict the Y value given observations of all the X_i values, compute

$$Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} \ P(Y = v \mid X_1 = u_1 \cdots X_m = u_m)$$

13

Naïve Bayes Classifier

$$Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} \ P(Y = v \mid X_1 = u_1 \cdots X_m = u_m)$$

$$Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} \frac{P(Y = v, X_1 = u_1 \cdots X_m = u_m)}{P(X_1 = u_1 \cdots X_m = u_m)}$$

$$Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} \frac{P(X_1 = u_1 \cdots X_m = u_m \mid Y = v)P(Y = v)}{P(X_1 = u_1 \cdots X_m = u_m)}$$

$$Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} P(X_1 = u_1 \cdots X_m = u_m \mid Y = v) P(Y = v)$$

 $Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} \ P(Y = v) \prod_{j=1}^{m} P(X_j = u_j \mid Y = v)$

1.4

Technical Point #1

- The probabilities $P(X_j = u_j \mid Y = v)$ can sometimes be really small
- This can result in numerical instability since floating point numbers are not represented exactly on any computer architecture
- To get around this, use the log of the last line in the previous slide i.e.

$$Y^{\text{predict}} = \underset{v}{\operatorname{argmax}} \left[\log(P(Y=v)) + \sum_{j=1}^{m} \log(P(X_{j}=u_{j} | Y=v)) \right]$$

15

Technical Point #2

- When estimating parameters, what happens if you don't have any records that match a certain combination of features?
- For example, in our training data, we didn't have M=false, A=false, G=false, W=false
- This means that $P(X_j = u_j | Y = v)$ in the formula below will be 0 and the entire expression will be 0.

$$P(Y = v) \prod_{j=1}^{m} P(X_j = u_j | Y = v)$$

Even more horrible things happen if you had this expression in log space

16

Uniform Dirichlet Priors

Let N_i be the number of values that X_i can take on.

$$P(X_j = u_j | V = v) = \frac{(\text{\#records with } X_j = u_j \text{ and } V = v) + 1}{(\text{\#records with } V = v) + N_j}$$

What happens when you have no records with V = v?

$$P(X_j = u_j | V = v) = \frac{1}{N_i}$$

This means that each value of X_j is equally likely in the absence of data. If you have a lot of data, it dominates the $1/N_j$ value. We call this trick a "uniform Dirichlet prior".

17

What You Should Know

- How to learn the parameters for a Naïve Bayes model
- How to make predictions with a Naïve Bayes model
- · How to implement a Naïve Bayes Model

Programming Assignment #3

You will classify text into two classes.

There are two files:

1. Training data: trainingSet.txt

2. Testing data: testSet.txt

19

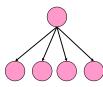
Programming Assignment #3

Two parts to this assignment:

- 1. Pre-processing step
- 2. Classification step

20

1. Preprocessing Step



- Recall that naïve Bayes has the structure shown to the right
- The nodes correspond to random variables, which are the features or attributes in the data
- What are the features in the documents?
- Note: a "document" in our assignment is a Yelp review

21

The Vocabulary

- The features of the documents will be the presence/absence of words in the vocabulary
- The vocabulary is the list of words that are known to the classifier
- Ideally, the vocabulary would be all the words in the English language
- For this assignment, you will form the vocabulary using all the words in the training data

22

Bag of Words

Suppose you have the following documents:

 Training Data
 Class Label

 This is an excellent laptop
 Class 0

 No, this is not sarcasm!
 Class 1

 Test Data

 Excellent Laptop =P
 Class 1

You will ignore punctuation for this assignment

The vocabulary will be:

this, is, an, excellent, laptop, no, not, sarcasm

23

Bag of Words

Vocab: this, is, an, excellent, laptop, no, not, sarcasm

Keep this in alphabetical order to help with debugging

Vocab: an, excellent, is, laptop, no, not, sarcasm, this

Training data

Next, convert your training and test data into features

Training Data

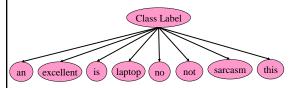
an	excellent	is	laptop	no	not	sarcasm	this	Class Label
1	1	1	1	0	0	0	1	0
0	0	1	0	1	1	1	1	1

Test Data

an	excellent	is	laptop	no	not	sarcasm	this	Class Label
0	1	0	1	0	0	0	0	1

You will output the training data in feature form, with the features alphabetized (we will grade you on this output).

2. Classification Step (Training Phase)



- Your naïve Bayes classifier now looks something like the above
- You still need to fill in the conditional probability tables in each node
- This is done in the training phase (as described on slides 9 and 10)
- Remember to use the uniform Dirichlet prior trick (see slide 17)

26

2. Classification Step (Testing Phase)

Testing phase

- · Load the featurized test data
- For each document in the test data, predict its class label
- This requires computing: P(Class label | Words in document)

27

2. Classification Step (Testing Phase)

Suppose you have the following test instance:

Ì	an	excellent	is	laptop	no	not	sarcasm	this	Class Label
	0	1	0	1	0	0	0	0	(to be predicted)

 $P(Class = 1 \mid an = 0, excellent = 1, is = 0, laptop = 1, no = 0, not$ = 0, sarcasm = 0, this = 0)

 $= \alpha P(Class = 1) * P(an = 0|Class = 1) * P(excellent = 1|Class = 1) *$ P(is = 0|Class = 1) * P(laptop = 1|Class = 1) * P(no=0|Class = 1) *P(not = 0|Class = 1) * P(sarcasm = 0|Class = 1) *P(this = 0|Class = 1)

Note: Use P(Word = 1 | Class) if you have a 1 for the word. Otherwise use

2. Classification Step (Testing Phase)

an	excellent	is	laptop	no	not	sarcasm	this	Class Label
0	1	0	1	0	0	0	0	(to be predicted)

Then compute the following:

 $P(Class = 0 \mid an = 0, excellent = 1, is = 0, laptop = 1, no = 0, not$ = 0, sarcasm = 0, this = 0) $= \alpha P(Class = 0) * P(an = 0|Class = 0) * P(excellent = 1|Class = 0) *$

P(is = 0|Class = 0) * P(laptop = 1|Class = 0) * P(no=0|Class = 0) *P(not = 0|Class = 0) * P(sarcasm = 0|Class = 0) *P(this = 0|Class = 0)

2. Classification Step (Testing Phase)

an	excellent	is	laptop	no	not	sarcasm	this	Class Label
0	1	0	1	0	0	0	0	(to be predicted)

 $P(Class = 1 \mid an = 0, excellent = 1, is = 0, laptop$ = 1, no = 0, not = 0, sarcasm = 0, this = 0)

 $P(Class = 0 \mid an = 0, excellent = 1, is = 0, laptop$ = 1, no = 0, not = 0, sarcasm = 0, this = 0)

Predict Class = 1 otherwise predict Class = 0

2. Classification Step (Testing Phase)

- For each document in the testing data set, predict its class label
- Compare the predicted class label to the actual class label
- Output the accuracy for each class:

#correctly predicted class labels total # of prediction s

31

Results

There are two sets of results we require:

- 1. Results #1:
 - Use trainingSet.txt for the training phase
 - Use trainingSet.txt for the testing phase
 - Report accuracy
- 2. Results #2:
 - Use trainingSet.txt for the training phase
 - Use testSet.txt for the testing phase
 - Report accuracy