

# 2018 Applications of Mathematics National 5 - Paper 1 Finalised Marking Instructions

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#### General marking principles for National Applications of Mathematics

Always apply these general principles. Use them in conjunction with the detailed marking instructions, which identify the key features required in candidates' responses.

For each question, the marking instructions are generally in two sections:

- generic scheme this indicates why each mark is awarded
- illustrative scheme this covers methods which are commonly seen throughout the marking

In general, you should use the illustrative scheme. Only use the generic scheme where a candidate has used a method not covered in the illustrative scheme.

- (a) Always use positive marking. This means candidates accumulate marks for the demonstration of relevant skills, knowledge and understanding; marks are not deducted for errors or omissions.
- (b) If you are uncertain how to assess a specific candidate response because it is not covered by the general marking principles or the detailed marking instructions, you must seek guidance from your team leader.
- (c) One mark is available for each •. There are no half marks.
- (d) If a candidate's response contains an error, all working subsequent to this error must still be marked. Only award marks if the level of difficulty in their working is similar to the level of difficulty in the illustrative scheme.
- (e) Only award full marks where the solution contains appropriate working. A correct answer with no working receives no mark, unless specifically mentioned in the marking instructions.
- (f) Candidates may use any mathematically correct method to answer questions, except in cases where a particular method is specified or excluded.
- (g) If an error is trivial, casual or insignificant, for example  $6 \times 6 = 12$ , candidates lose the opportunity to gain a mark, except for instances such as the second example in point (h) below.

(h) If a candidate makes a transcription error (question paper to script or within script), they lose the opportunity to gain the next process mark, for example

This is a transcription error and so the mark is not awarded.  $x^2 + 5x + 7 = 9x + 4$ This is no longer a solution of a quadratic equation, so the mark is not awarded. x = 1

The following example is an exception to the above

This error is not treated as a transcription error, as the candidate deals with the intended quadratic equation. The candidate has been given the benefit of the doubt and all marks awarded.  $x^2 + 5x + 7 = 9x + 4$ x - 4x + 3 = 0(x - 3)(x - 1) = 0x = 1 or 3

#### (i) Horizontal/vertical marking

If a question results in two pairs of solutions, apply the following technique, but only if indicated in the detailed marking instructions for the question.

Example:

•5 •6  
•5 
$$x = 2$$
  $x = -4$   
•6  $y = 5$   $y = -7$ 

Horizontal: • $^5$  x = 2 and x = -4 Vertical: • $^5$  x = 2 and y = 5 • $^6$  y = 5 and y = -7

You must choose whichever method benefits the candidate, **not** a combination of both.

(j) In final answers, candidates should simplify numerical values as far as possible unless specifically mentioned in the detailed marking instruction. For example

 $\frac{15}{12}$  must be simplified to  $\frac{5}{4}$  or  $1\frac{1}{4}$   $\frac{43}{1}$  must be simplified to 43

 $\frac{15}{0.3}$  must be simplified to 50  $\frac{\frac{4}{5}}{3}$  must be simplified to  $\frac{4}{15}$ 

 $\sqrt{64}$  must be simplified to 8\*

\*The square root of perfect squares up to and including 100 must be known.

- (k) Commonly Observed Responses (COR) are shown in the marking instructions to help mark common and/or non-routine solutions. CORs may also be used as a guide when marking similar non-routine candidate responses.
- (I) Do not penalise candidates for any of the following, unless specifically mentioned in the detailed marking instructions:
  - working subsequent to a correct answer
  - correct working in the wrong part of a question
  - legitimate variations in numerical answers/algebraic expressions, for example angles in degrees rounded to nearest degree
  - omission of units
  - bad form (bad form only becomes bad form if subsequent working is correct), for example

$$(x^3 + 2x^2 + 3x + 2)(2x + 1)$$
 written as  
 $(x^3 + 2x^2 + 3x + 2) \times 2x + 1$   
 $= 2x^4 + 5x^3 + 8x^2 + 7x + 2$   
gains full credit

- repeated error within a question, but not between questions or papers
- (m) In any 'Show that...' question, where candidates have to arrive at a required result, the last mark is not awarded as a follow-through from a previous error, unless specified in the detailed marking instructions.
- (n) You must check all working carefully, even where a fundamental misunderstanding is apparent early in a candidate's response. You may still be able to award marks later in the question so you must refer continually to the marking instructions. The appearance of the correct answer does not necessarily indicate that you can award all the available marks to a candidate.
- (o) You should mark legible scored-out working that has not been replaced. However, if the scored-out working has been replaced, you must only mark the replacement working.
- (p) If candidates make multiple attempts using the same strategy and do not identify their final answer, mark all attempts and award the lowest mark. If candidates try different valid strategies, apply the above rule to attempts within each strategy and then award the highest mark.

#### For example:

Strategy 1 attempt 1 is worth 3 marks.	Strategy 2 attempt 1 is worth 1 mark.
Strategy 1 attempt 2 is worth 4 marks.	Strategy 2 attempt 2 is worth 5 marks.
From the attempts using strategy 1, the resultant mark would be 3.	From the attempts using strategy 2, the resultant mark would be 1.

In this case, award 3 marks.

## Detailed marking instructions for each question

Question		on	Generic scheme	Illustrative scheme	Max mark
1.			•¹ Process: calculate 3% of 400	•¹ 12	3
			• Process: calculate max and min	• <sup>2</sup> 412 and 388	
			• Process: calculate fraction that will be rejected	$\bullet^3$ $\frac{4}{13}$ cakes will be rejected	

# Notes:

1. Correct answer with no working

award 3/3

2. Incorrect answer with no working

award 0/3

- 3. •¹ can be implied by subsequent working
- 4. Where answer is incorrect, •³ can be awarded if there is evidence of where the fraction has come from

## **Commonly Observed Responses:**

1. 403 and 397 leading to an answer of  $\frac{11}{13}$ 

award 2/3 **x** ✓ ✓

2.	•¹ Process: calculate cost of city break $•¹$ 270 + 90 × 4 + 450 + 30 = 1110	3
	•² Strategy/process: know how to find number of weeks  •² Evidence of dividing cost by 50 or other appropriate strategy	
	•³ Process/communication: find number of weeks	

#### Notes:

- 1.  $\bullet^2$  is only available for a relevant calculation involving 50
- 2. 3 not available for error in calculation eg 1110  $\div$  50 = 22·1 leading to 23

#### **Commonly Observed Responses:**

1. 
$$270 + 90 + 450 + 30 = 840 \rightarrow 16.8$$
 leading to 17

award 2/3 × ✓ ✓

Question		Generic scheme Illustrative scheme		Max mark
<b>3.</b> (a)		•¹ Communication: 4 points correct	•¹ Evidence	2
		•² Communication: all 8 points correct	•² Evidence	
Notes:		H 99 104 104 107 W 17 18 19 19	120   124   127   130   24   22   25   24	
Commonly	Obse	rved Responses:		
(b)		•³ Communication: consistent line of best fit	•³ Evidence	1
Notes:	<u>'</u>			
Commonly	/ Obse	rved Responses:		
(c)		• <sup>4</sup> Communication: answer	• <sup>4</sup> Evidence	1
Notes:		consistent with line of best fit		
1. Wh	ween	height falls between 2 whole number	s accept either number or any value in	
1. Wh	ween		s accept either number or any value in	
1. Wh	ween	height falls between 2 whole number	es accept either number or any value in	2
1. Wh bet	ween	height falls between 2 whole number  rved Responses:  •¹ Process: calculate new	T	2
1. Wh bet	ween	height falls between 2 whole number  rved Responses:  •¹ Process: calculate new temperature  •² Communication: mark	•1 -28	2
1. Wh bet  Commonly  4.  Notes:  1. Cor	v Obse	height falls between 2 whole number  rved Responses:  1 Process: calculate new temperature  2 Communication: mark temperature on Celsius scale  emperature marked with no working	•¹ −28  •² Evidence  award 2/	2
1. Wh bet  Commonly  4.  Notes:  1. Cor	v Obse	height falls between 2 whole number  rved Responses:  1 Process: calculate new temperature  2 Communication: mark temperature on Celsius scale	•¹ −28  •² Evidence  award 2/	2
1. Wh bet  Commonly  4.  Notes:  1. Cor 2. Wh	Obse	height falls between 2 whole number  rved Responses:  1 Process: calculate new temperature  2 Communication: mark temperature on Celsius scale  emperature marked with no working	•¹ −28  •² Evidence  award 2/	2
1. Wh bet  Commonly  4.  Notes:  1. Cor 2. Wh  Commonly  1. 6°C	Obsevered to	height falls between 2 whole number rved Responses:  •¹ Process: calculate new temperature  •² Communication: mark temperature on Celsius scale  emperature marked with no working candidate writes 28 then marks –28 or	•¹ −28  •² Evidence  award 2/	2 2

Question		n	Generic scheme	Illustrative scheme	Max mark
5.			•¹ Strategy: know how to add fractions	•¹ evidence of attempt to change both fractions to a valid common denominator	3
			• Process: add fractions	$\bullet^2$ $\frac{3}{7} + \frac{1}{3} = \frac{9}{21} + \frac{7}{21} = \frac{16}{21}$	
			• Process: calculate fraction who had vegetarian option	$\bullet$ <sup>3</sup> $\frac{5}{21}$	
			Alternative Strategy		3
			•¹ Strategy: know how to convert a fraction to a decimal	•¹ evidence of numerator divided by denominator	
			• Process: add decimals	$\bullet^2$ 0.333 + 0.428 = 0.761	
			• Process: calculate decimal who had vegetarian option	•³ 0·239 or 0·238	

- 1. only available for answer of  $\frac{16}{21}$ , 0.7610... or equivalent
- 2. The final answer does not need to be in its simplest form
- 3. Candidates working in decimals must work to at least 3 decimal places for •2 to be awarded
- 4. Candidates working in percentages must work to at least 1 decimal place for ●² to be awarded

# **Commonly Observed Responses:**

1. 23.9% or 23.8%

award 3/3 ✓ ✓ ✓

2.  $\frac{3}{7} + \frac{1}{3} = \frac{4}{10}$  leading to an answer of  $\frac{6}{10}$ 

award 1/3 **x x √** 

6.	•	<ul> <li>Strategy: know correct order of operations</li> </ul>	•¹ evidence	2
	•	<ul> <li>Process/communication: complete calculation and state conclusion</li> </ul>	• 18·1 and consistent conclusion	

#### **Notes:**

#### Commonly Observed Responses:

1.  $(27 \cdot 2 - 4 \cdot 6) \times 3 + 4 \cdot 7 = 72 \cdot 5$  no he is incorrect

award 1/2 × ✓

2.  $27 \cdot 2 - (4 \cdot 6 \times 3 + 4 \cdot 7) = 8 \cdot 7$  yes he is correct

award 1/2 × ✓

3.  $(27 \cdot 2 - 4 \cdot 6 + 4 \cdot 7) \times 3 = 81 \cdot 9$  no he is incorrect

award 1/2 × ✓

4.  $(27 \cdot 2 - 4 \cdot 6) \times (3 + 4 \cdot 7) = 174 \cdot 02$  no he is incorrect

award 1/2 × ✓

Question		on	Generic scheme	Illustrative scheme	Max mark
7.	(a)		•¹ Process: calculate amount of Bolivian boliviano	$\bullet^1$ 750 × 9 = 6750	1

1. Accept £6750

# **Commonly Observed Responses:**

(b)	• Strategy/process: calculate amount of Bolivian boliviano left and convert back to pounds	= 450 2
	• Process: calculate Argentine peso $\bullet^3$ 450 × 20 = 9000	

#### Notes:

- 1. When the answer to ●² is not a whole number of pounds, it must be rounded or truncated to at least 2 decimal places
- 2. For •³ accept any correct rounding or truncation to an accuracy of at least the nearest 10 peso

# **Commonly Observed Responses:**

8.	•¹ Strategy: know to calculate the sale price in two stages	•¹ evidence	3
	• Process: calculate 75% of the price	• <sup>2</sup> 525	
	• Process: calculate final price	•³ 498·75	

#### Notes:

# **Commonly Observed Responses:**

1. 70% of 700 = 490

award 1/3 **× × √** 

Q	uestion	Generic scheme	Illustrative scheme	Max mark
9.		•¹ Strategy/process: know how to deal with flight time	•¹ 11:10pm or equivalent	3
		• Strategy: know how to deal with time difference	•² eg 11:10 + 8 = 7:10am or 8:50 - 8 = 00:50am or equivalent	
		• Process: calculate stop time	•³ 1 hour 40 minutes	
Com 1	monly Obse	erved Responses:  and 40 minutes with relevant working and 40 minutes with relevant working  • 1 Process: find 80% of 35	award 3/  award 2/3 $\checkmark$ $\checkmark$ award 2/3 $\checkmark$ $\checkmark$ • 1 28	1
Note	es:			
Com	monly Obse	erved Responses:		
	(b)	• Strategy/process: calculate overall percentage	• <sup>2</sup> 67	1
Note	es:	,		
Com	monly Obse	erved Responses:		

Q	Question		Generic scheme	Illustrative scheme	Max mark
11.			•¹ Strategy: know how to find perimeter	•¹ evidence of $3 \cdot 14 \times 20 + 34 + 34$	3
			• Process: calculate semi circles	$\bullet^2  3 \cdot 14 \times 20 = 62 \cdot 8$	
			• Strategy/process: calculate total length of ribbon needed	$\bullet^3$ 62·8 + 34 + 34 + 2·8 = 133·6	

- 1.  $ullet^2$  is only available for a calculation involving  $3 \cdot 14$
- 2.  $\bullet$ <sup>3</sup> is only available for adding 2·8 to a previously calculated perimeter
- 3. Where a candidate considers area of part of the shape instead of perimeter, only  $ullet^2$  is available

# **Commonly Observed Responses:**

1. For $3.14 \times 10 + 34 + 34 + 2.8$ leading to a final answer of $102.2$	award 2/3 <b>× √</b> ✓
2. For $3.14 \times 40 + 34 + 34 + 2.8$ leading to a final answer of 196.4	award 2/3 × ✓ ✓
3. For $3 \cdot 14 \times 20 + 34 + 34$ leading to a final answer of $130 \cdot 8$	award 2/3 ✓ ✓ ×
4. For $3 \cdot 14 \times 10^2 + 34 + 34 + 2 \cdot 8$ leading to a final answer of $384 \cdot 8$	award 1/3 × ✓ ×
5. For $3 \cdot 14 \times 10^2 + 20 \times 27 \cdot 5 + 2 \cdot 8$ leading to a final answer of $866 \cdot 8$	award 1/3 <b>× √ ×</b>
6. For $3 \cdot 14 \times 10^2 + 20 \times 27 \cdot 5$ leading to a final answer of 864	award 1/3 <b>× √ ×</b>

Q	Question		Generic scheme	Illustrative scheme	Max mark
12.	(a)		•¹ Process: calculate scale distances	•¹ 82 ÷ 10 rep by 8·2 cm 46 ÷ 10 rep by 4·6 cm	3
			• Process/communication: correct bearing measured and correct length drawn	• Bearing of 042° (±1°) measured correctly and 8·2 cm (±0·1 cm) correctly drawn	
			• Process/communication: correct bearing measured and correct length drawn	• Bearing of 194° (±1°) measured correctly and 4.6 cm (±0.1 cm) correctly drawn	

- 1.
- alternatively available for 2 correct lengths drawn
   alternatively available for 2 correct angles measured
- •1 can be implied by drawing 2 lines of the correct length

# **Commonly Observed Responses:**

(b)	• Process: bearing consistent with diagram	• <sup>4</sup> evidence	2
	• Process: distance consistent with diagram	• <sup>5</sup> evidence	

#### Notes:

1. The third leg of the journey need not actually be drawn

# **Commonly Observed Responses:**

13.		•¹ Strategy: substitute correctly into Pythagoras' Theorem	$\bullet^1$ h <sup>2</sup> = 10 <sup>2</sup> - 6 <sup>2</sup>	3
		• Process: calculate height	•² 8	
		• 3 Process: calculate area	$\bullet^3 8 \times 12 \div 2 = 48$	

1. Correct answer with no working

- 2. 8 with no working  $\bullet^1$  and  $\bullet^2$  can be awarded
- 3.  $\bullet$ <sup>3</sup> is only available for using a height

#### **Commonly Observed Responses:**

1.  $\frac{1}{2} \times 12 \times 10$  leading to an answer of 60

award 0/3 \* \* \*

award 3/3

Question			Generic scheme	Illustrative scheme	Max mark
14.			•¹ Strategy/process: know to find total number of combinations	•¹ evidence of the 35 combinations	3
			• Process: find the number of combinations less than 5	•² 13	
			•³ Communication: state probability	$\bullet^3 \frac{13}{35}$	

#### Notes:

1. Correct answer with no working

award 3/3

- 2. The combinations need not be listed for award of  $\bullet^1$  and  $\bullet^2$
- 3. Where answer is incorrect, ●³ can only be awarded if numerator **and** denominator are consistent with working
- 4. The final answer does not need to be in its simplest form
- 5. Do not award  $\bullet^3$  for an answer written as a ratio

## **Commonly Observed Responses:**

1. 13:35

award 2/3 ✓ ✓ ×

2.  $\frac{35}{12}$ 

award 2/3 ✓ ✓ ×

15.		•1	Process: consistent units between two values	•1	25  cm = 0.25  m or 4  m = 400  cm	3
		•2	Communication: state gradient	•2	<del>25</del> <del>400</del>	
		•3	Process/communication: calculate equivalent fraction(s) and state conclusion	•3	Simplify $\frac{25}{400}$ to $\frac{1}{16}$ Yes, $\frac{1}{16} < \frac{1}{14}$	

1. Award  $\bullet^3$  for  $\frac{14}{224} < \frac{16}{224}$  or equivalent with correct conclusion

**Commonly Observed Responses:** 

1.  $\frac{25}{4}$  (with or without a conclusion)

award 1/3 **x** ✓ **x** 

[END OF MARKING INSTRUCTIONS]