

## 7.2.7

$$x_i = 3, 7, 10, 12, 5, 8, 4$$

1.  $x_i$  följer den diskreta försökstidens utgångar (geir ut)

$$2. p_X(k) = p(1-p)^{k-1}$$

$$3. L(\theta) = L(p) = \prod_{i=1}^{n=7} p(1-p)^{x_i-1} = p^7(1-p)^{\sum_{i=1}^7 x_i - 7}$$

$$4. l(\theta) = \ln(L(p)) = 7\ln(p) + \left(\sum_{i=1}^7 x_i - 7\right)\ln(1-p)$$

$$5. l(\theta) = 0 \Rightarrow \frac{d}{dp}(7\ln(p) + 42\ln(1-p))$$

$$= \frac{7}{p} - \frac{42}{1-p}$$

$$= \frac{7(1-p) - 42p}{p(1-p)} \Rightarrow$$

$$7(1-p) - 42p = 0 \quad \text{så} \quad 7 - 7p - 42p = 0 \Rightarrow 7 = 49p \Rightarrow p^* = \frac{1}{7}$$