

T.C.A.S.: TCAS Can Always Solve

A Numerical Analysis Method for Limit Evaluation

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Abstract

Contents

| | | |
|----------|--|----------|
| 1 | Introduction | 2 |
| 1.1 | The Limit of a Function | 2 |
| 1.2 | Polish Notation | 2 |
| 1.3 | The Shortcomings of the Naive Approach | 2 |
| 2 | The Gruntz Algorithm | 2 |
| 2.1 | The Most Rapidly Varying Subexpression | 2 |
| 2.2 | Power Series Representation | 2 |
| 2.3 | Caveats and Limitations | 2 |
| 3 | TCAS | 2 |
| 3.1 | Parsing | 2 |
| 3.2 | Finding the MRV | 2 |
| 3.3 | Evaluating the Result | 2 |
| 3.4 | Performance Considerations | 2 |

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3 TCAS

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3.2 Finding the MRV

3.3 Evaluating the Result

3.4 Performance Considerations

References

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