Online, December 12-13th, 2023



increasingxor ● EN

# Increasing XOR (increasingxor)

An array B consisting of k positive integers is beautiful if and only if there exists an array  $C = [C_0, C_1, \ldots, C_{k-1}]$  such that C is a permutation of B and the sequence of its prefix-XORs is strictly increasing. That is,  $P_0 < P_1 < \cdots < P_{k-1}$  where  $P_i = C_0 \oplus C_1 \oplus \ldots C_i$  for each  $i = 0, \ldots, k-1$ .

The bitwise XOR  $a \oplus b$  of two integers a and b is defined in the following way: the i-th bit of  $a \oplus b$  is 1 if and only if exactly one among a and b has 1 in the i-th bit.

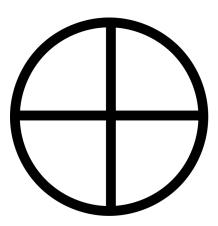


Figure 1: The XOR symbol.

Given an array A consisting of N positive integers, you have to determine for each non-empty prefix of A whether it is beautiful.

Among the attachments of this task you may find a template file increasingxor.\* with a sample incomplete implementation.

#### Input

The first line contains the only integer N. The second line contains N integers,  $A_0, A_1, \ldots, A_{N-1}$ .

### Output

You should print N lines. In the ith line, you must write YES if the ith prefix is beautiful and NO otherwise.

#### **Constraints**

- $1 \le N \le 200\,000$ .
- $1 \le A_i < 2^{30}$  for each  $i = 0 \dots N 1$ .

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## **Scoring**

Your program will be tested against several test cases grouped in subtasks. In order to obtain the score of a subtask, your program needs to correctly solve all of its test cases.

- Subtask 1 (0 points) Examples.

- Subtask 2 (10 points)  $N \le 10$ .

- Subtask 3 (11 points)  $A_i \le 7$  for each  $i = 0 \dots N - 1$ .

- Subtask 4 (35 points)  $N \le 500$ .

- Subtask 5 (44 points) No additional limitations.

### **Examples**

input	output
5 3 1 4 1 5	YES YES YES YES NO
5 3 3 5 8 19	YES NO NO NO YES

## **Explanation**

In the first sample case:

- 1. The 1st prefix is *beautiful* because a sequence consisting of a single element is, by definition, strictly increasing.
- 2. For the 2nd prefix, the permutation 1, 3 is suitable as the sequence  $1, 2 = 1 \oplus 3$  is strictly increasing.
- 3. For the 3rd prefix, the permutation 1, 3, 4 is suitable as the sequence  $1, 2 = 1 \oplus 3, 6 = 1 \oplus 3 \oplus 4$  is strictly increasing.
- 4. For the 4th prefix, the permutation 1, 3, 4, 1 is suitable as the sequence 1, 2, 6, 7 is strictly increasing.
- 5. It can be checked that the 5th prefix is not beautiful.

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