

Lexical Analysis

CMPT 379: Compilers

Instructor: Anoop Sarkar

anoopsarkar.github.io/compilers-class

Lexical Analyzer using NFAs

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Lexical Analyzer using NFAs

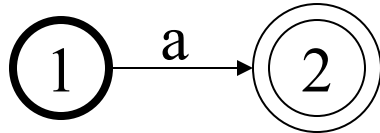
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- If no final state is reached then raise an error
- Pick the final state (token) that has the longest match in the input,
 - e.g. prefer DFA #8 over all others because it read the input until i_{30} and none of the other DFAs reached i_{30}
 - If two DFAs reach the same input character then pick the one that is listed first in the ordered list

Lexical Analysis using NFAs

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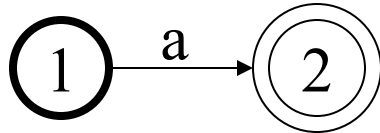
TOKEN_A = a

Lexical Analysis using NFAs



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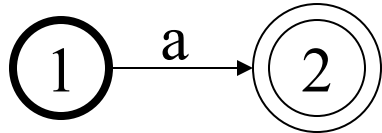
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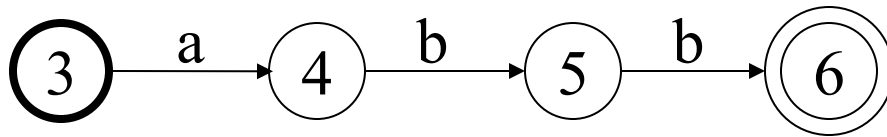
TOKEN_A = a

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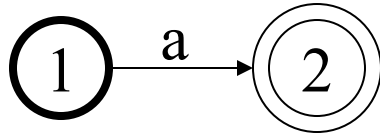


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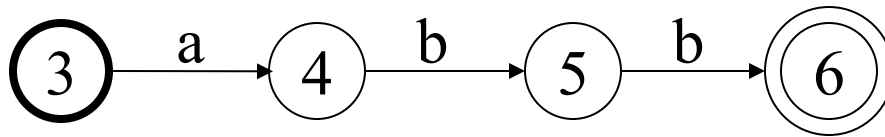


TOKEN_B = abb

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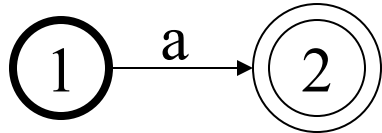
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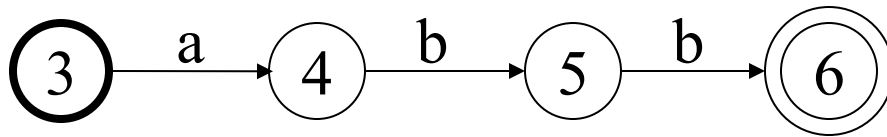
TOKEN_B = abb

TOKEN_C = a*b+

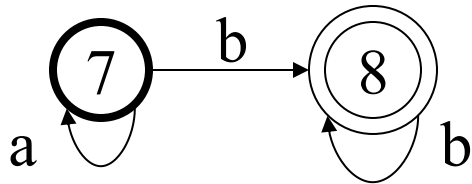
Lexical Analysis using NFAs



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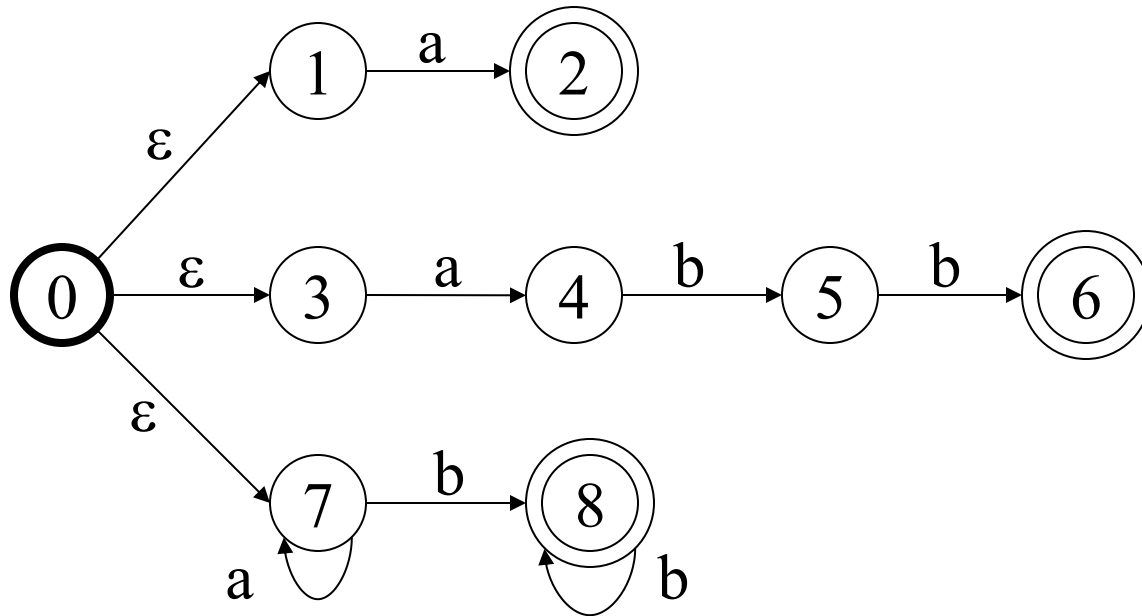


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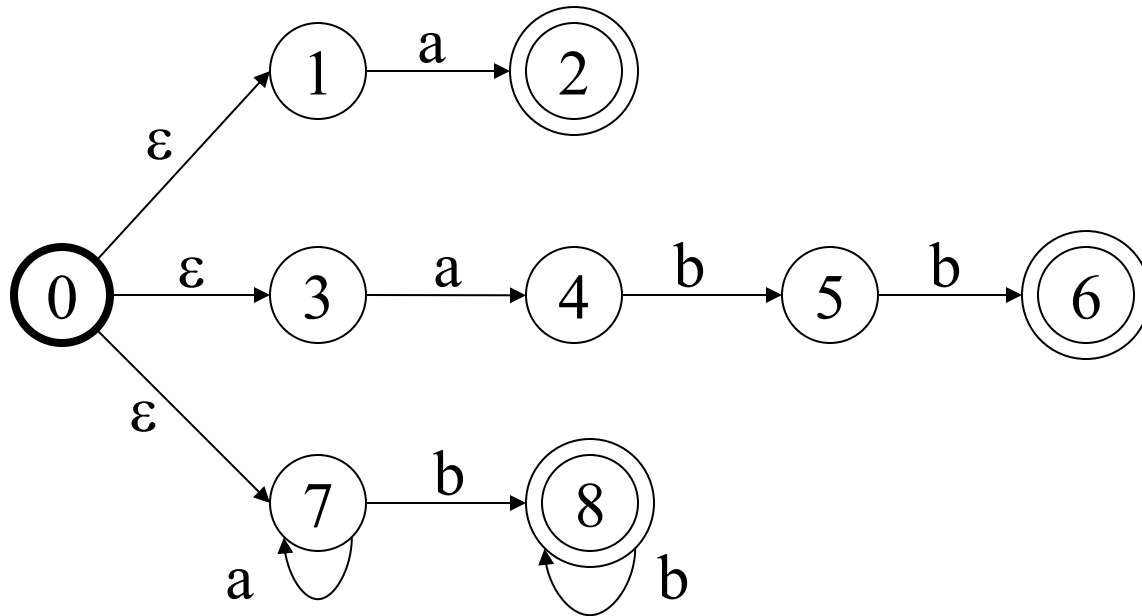


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Lexical Analysis using NFAs



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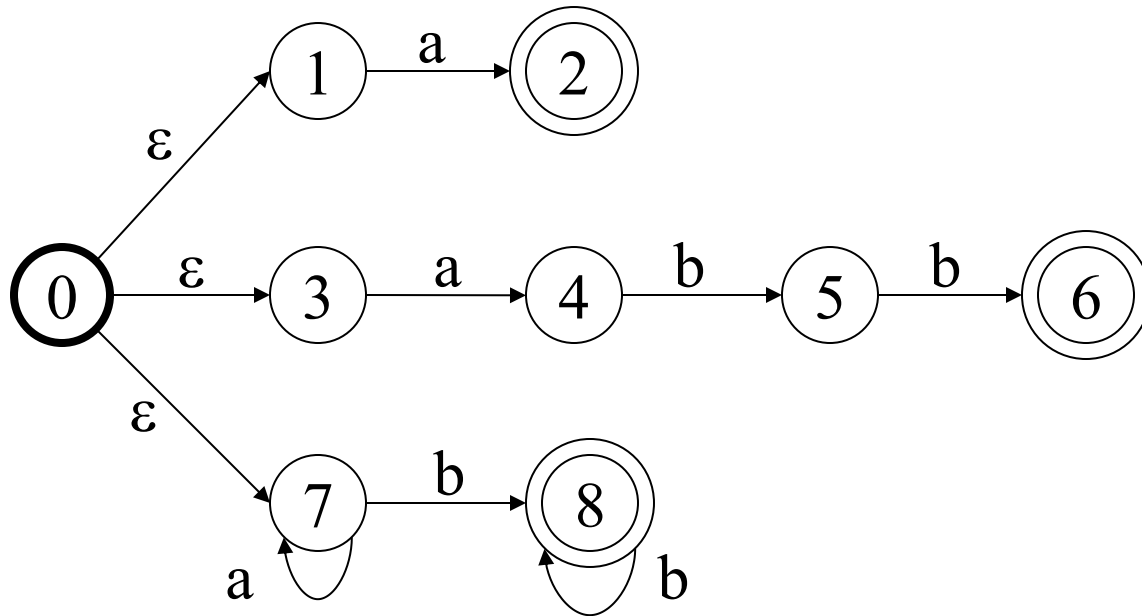
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Lexical Analysis using NFAs



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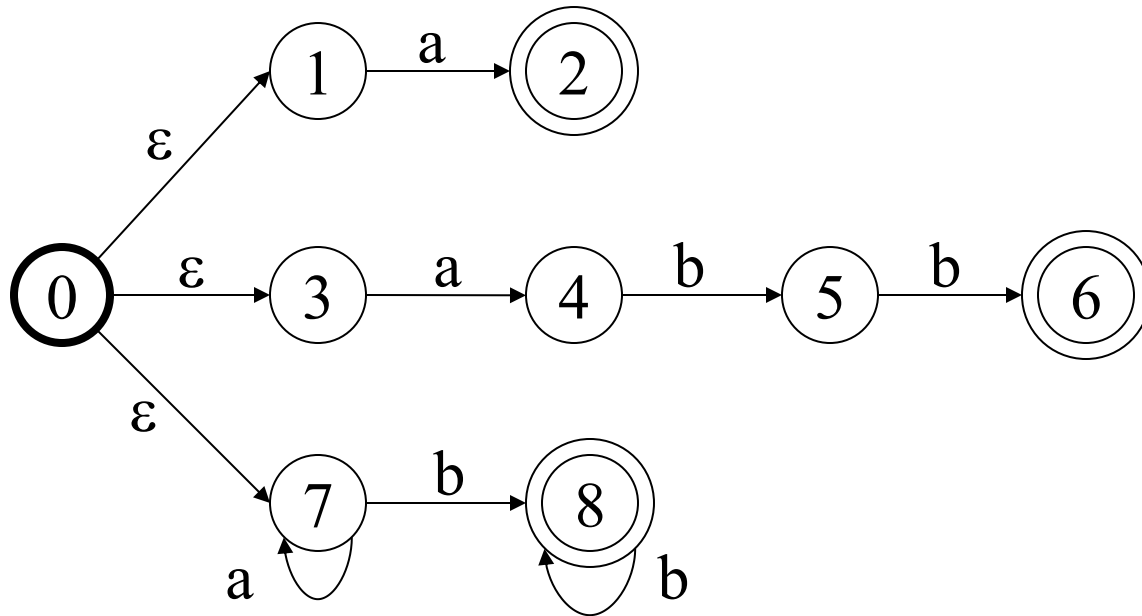
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1,
3,
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Lexical Analysis using NFAs



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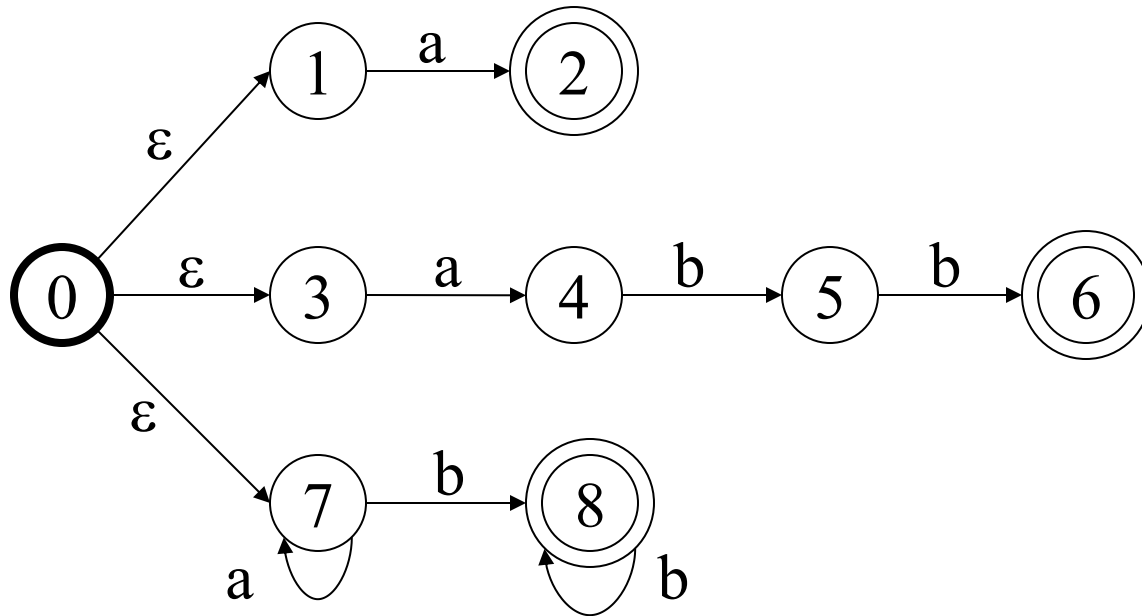
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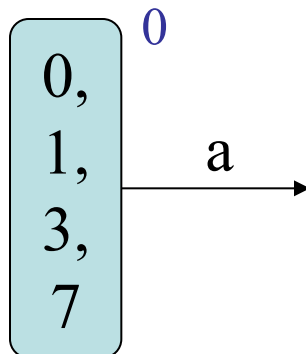
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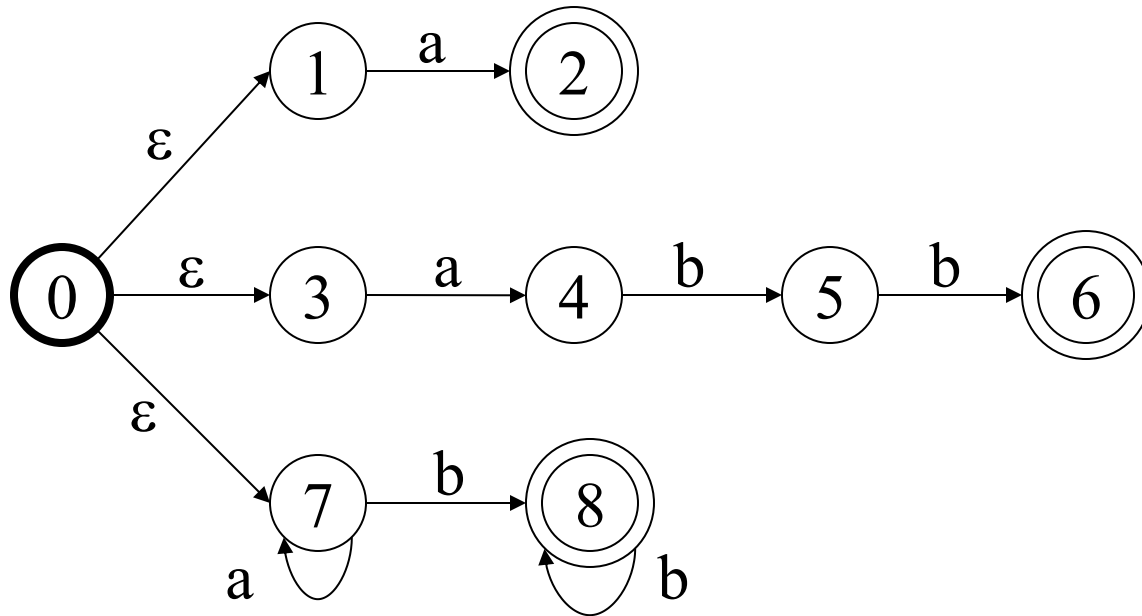
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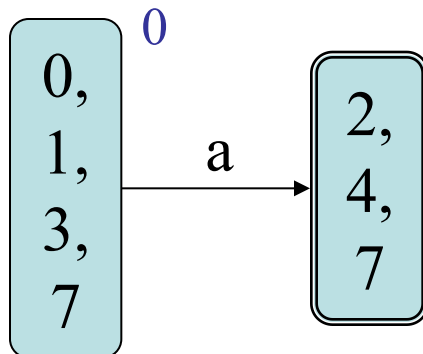
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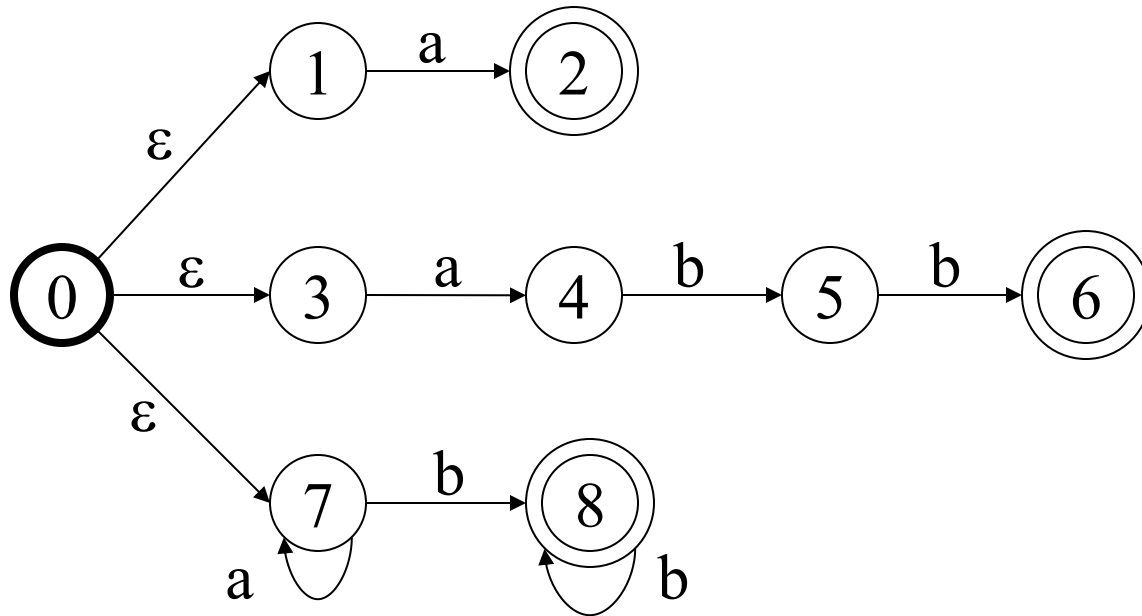
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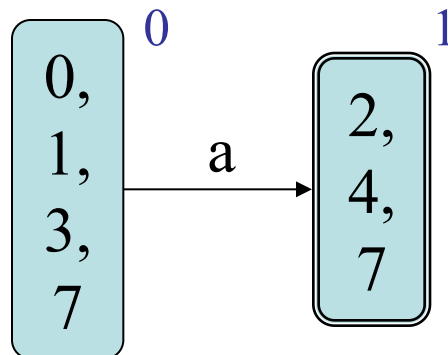
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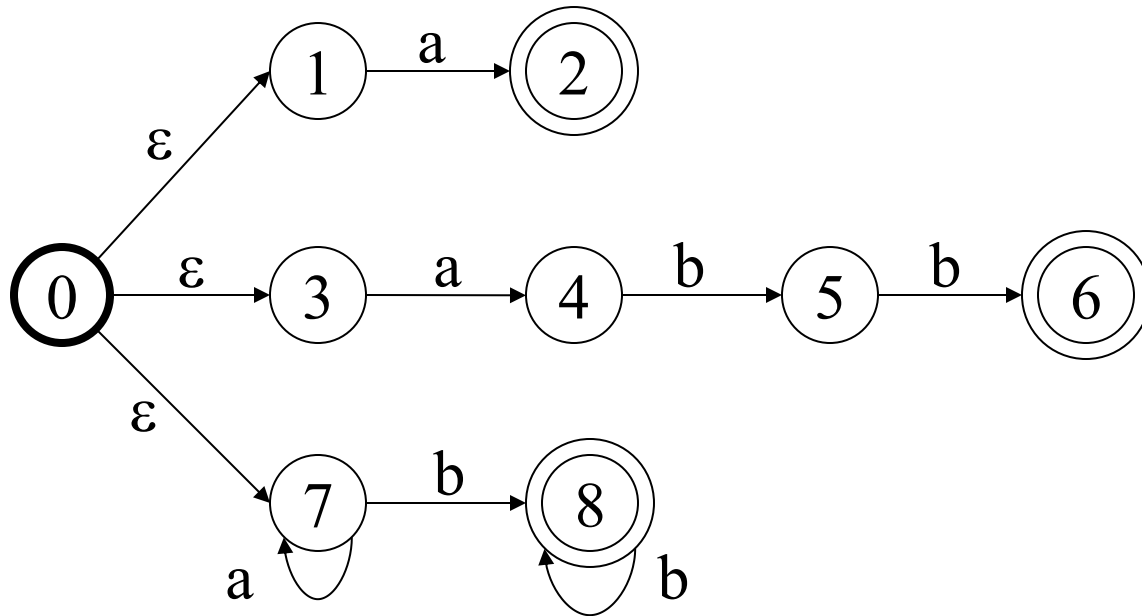
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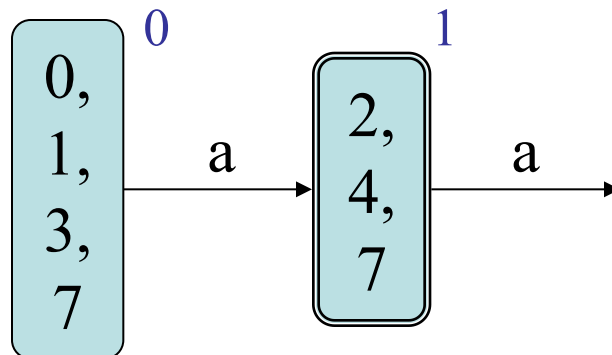
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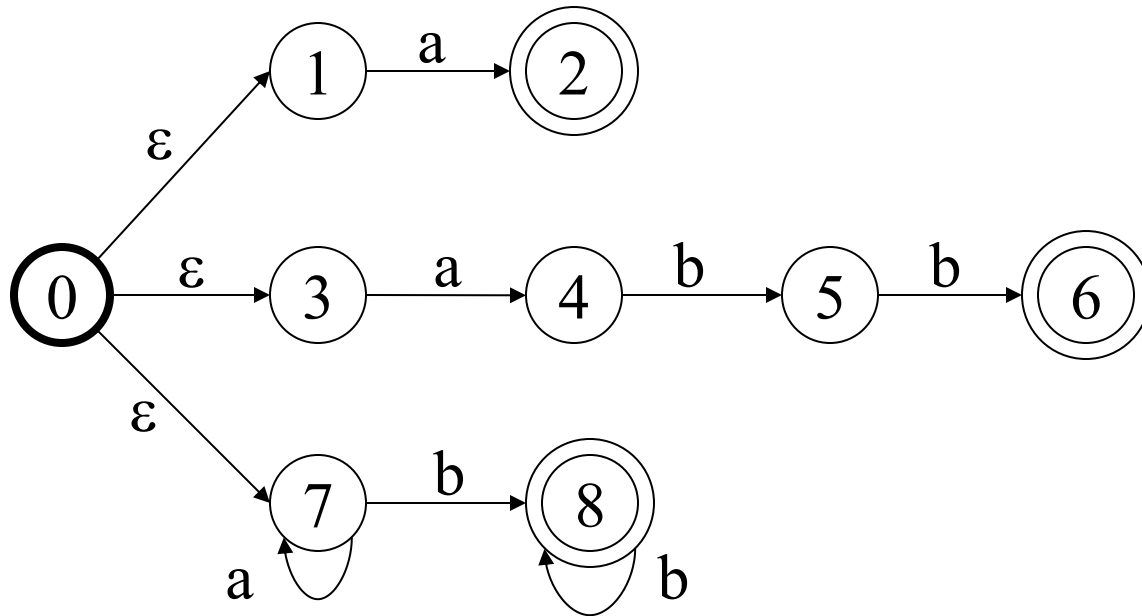
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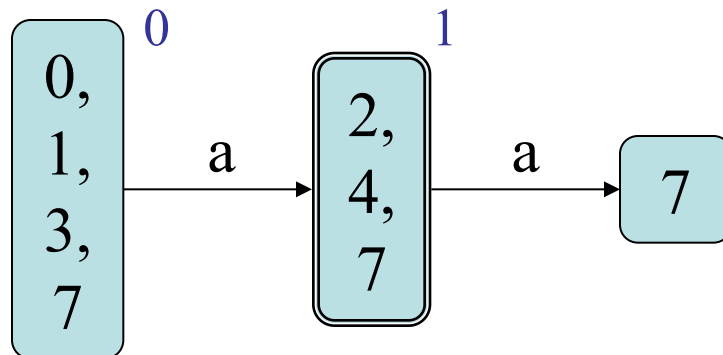
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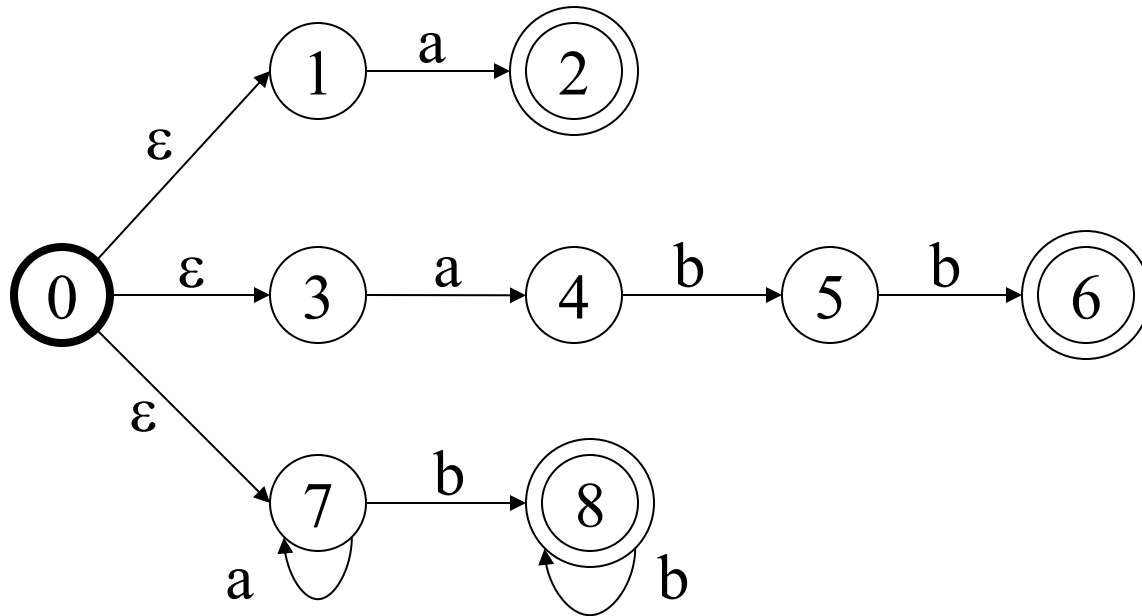
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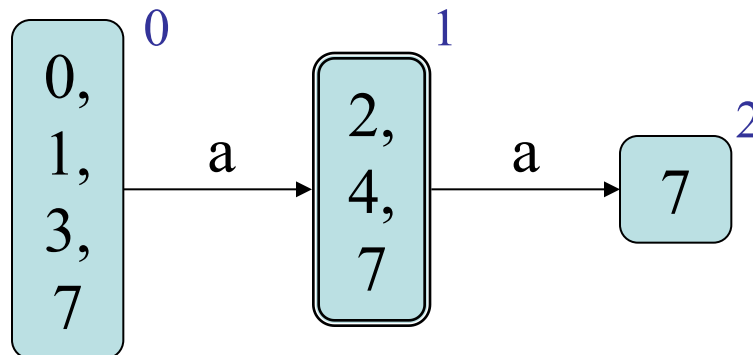
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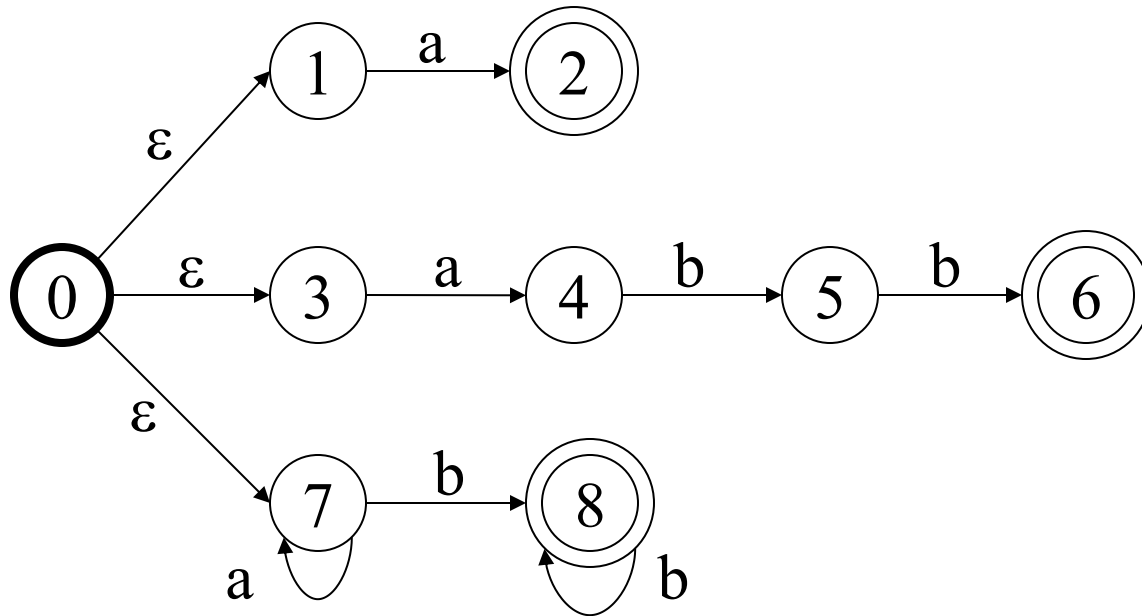
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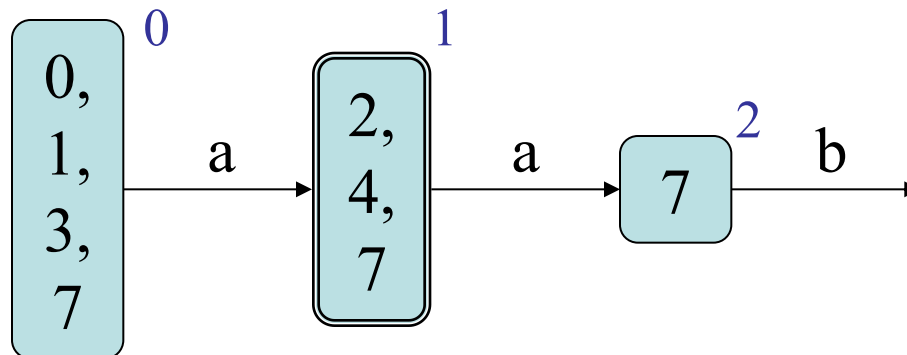
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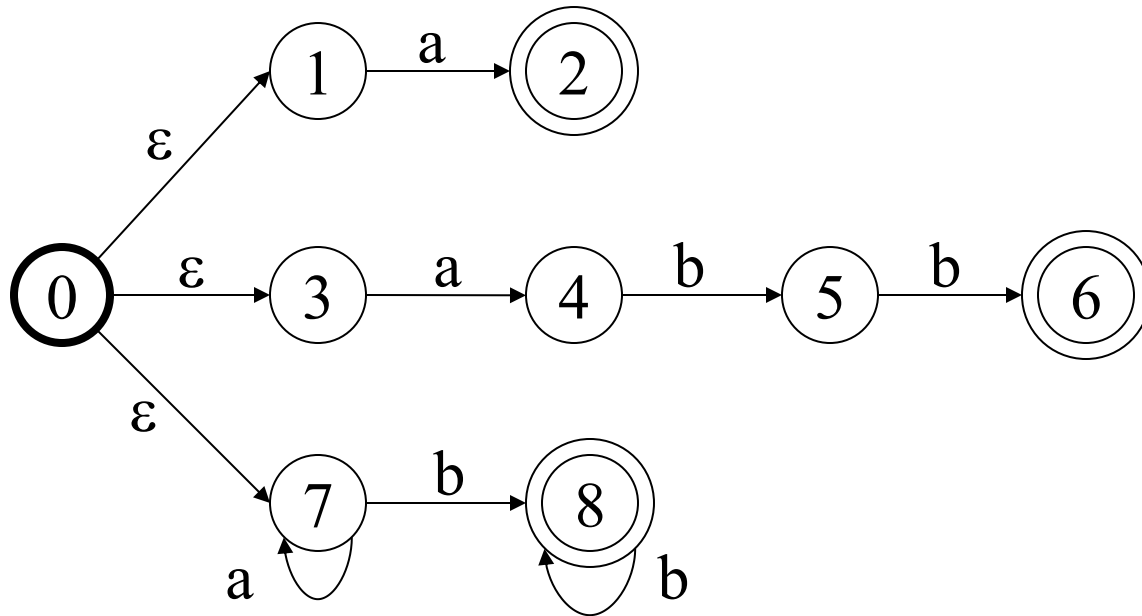
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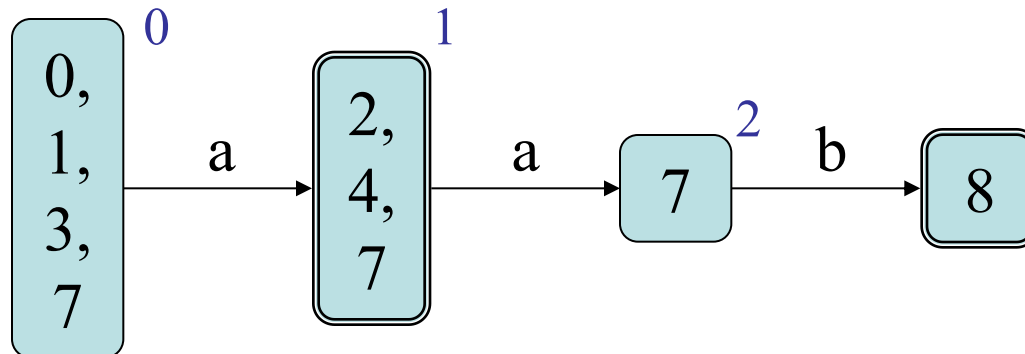
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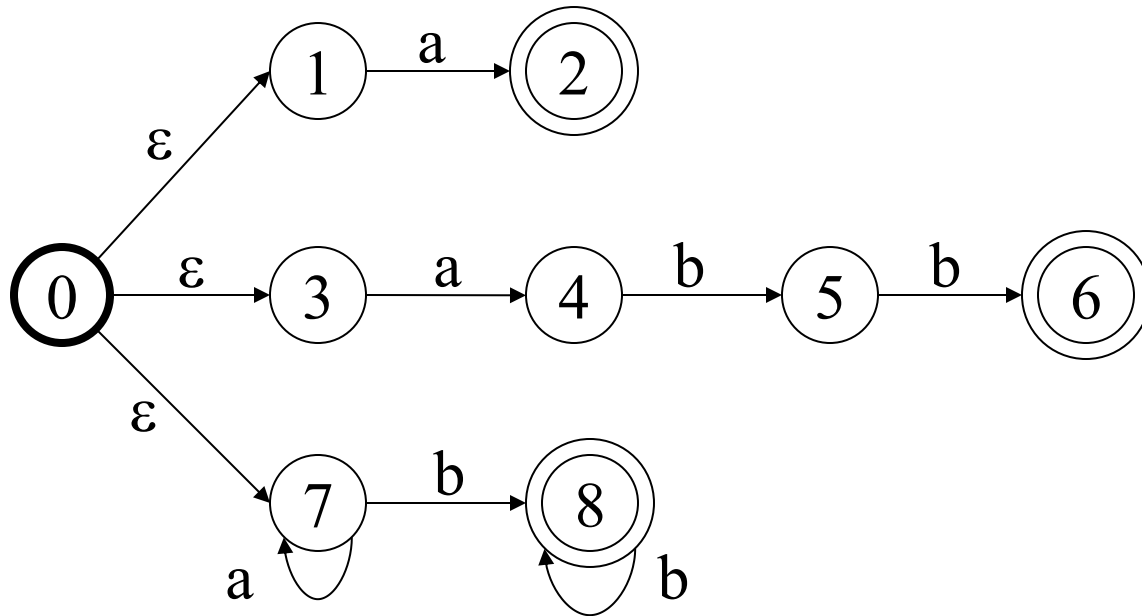
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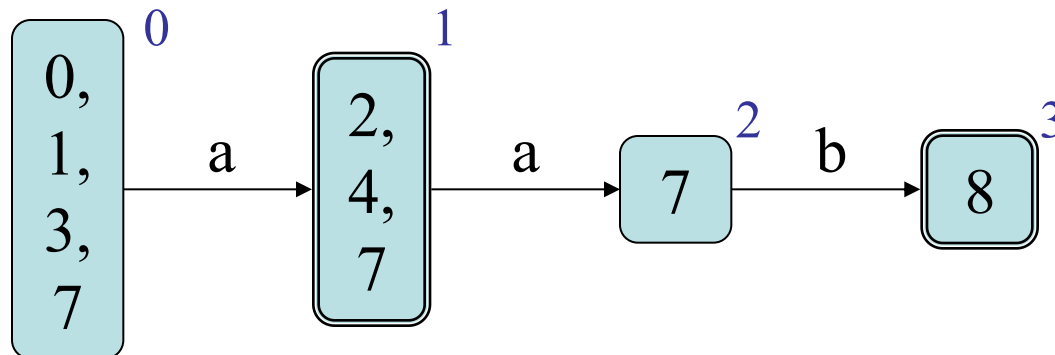
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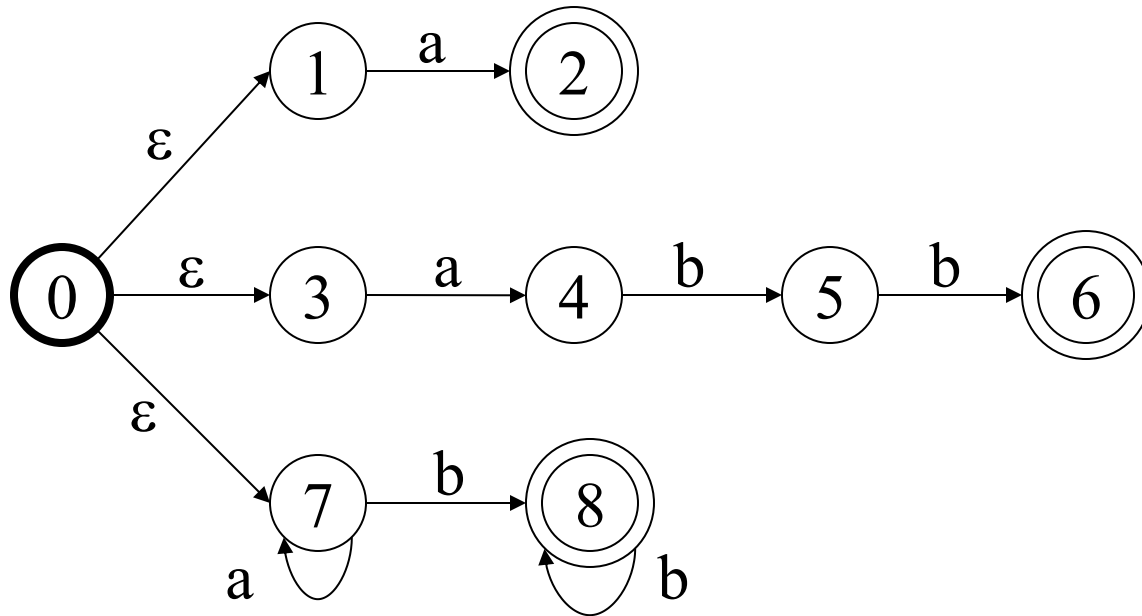
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$_0a_1a_2b_3a_4$



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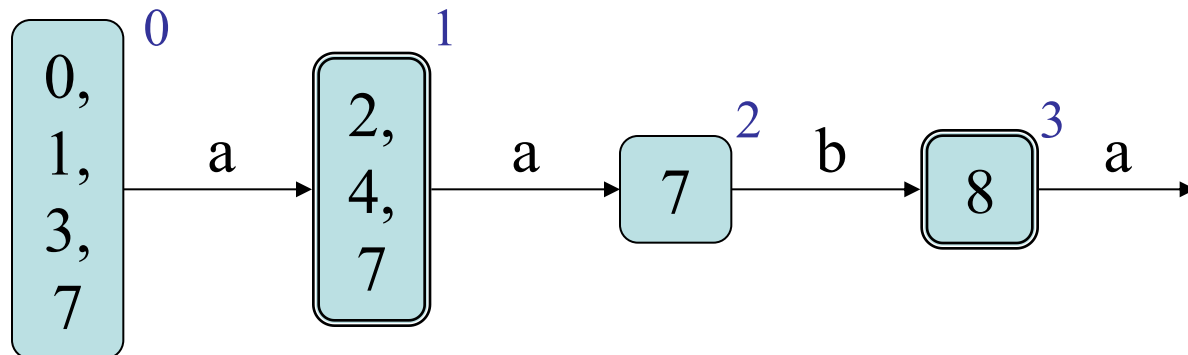
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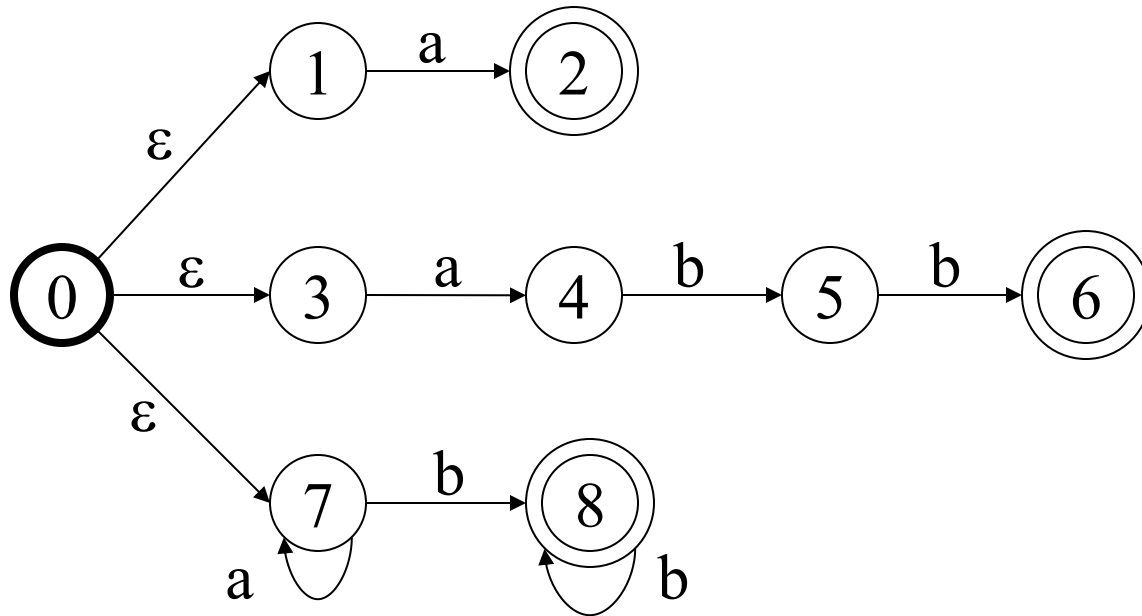
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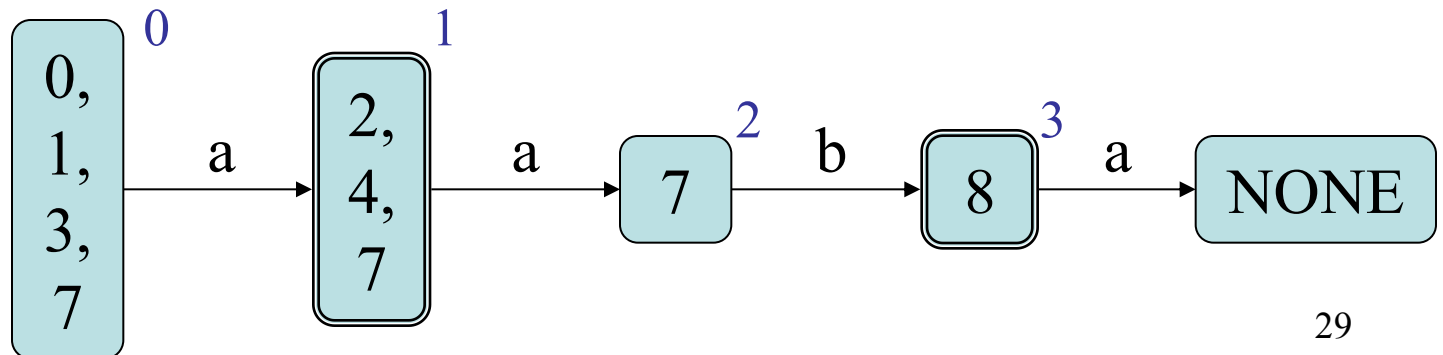
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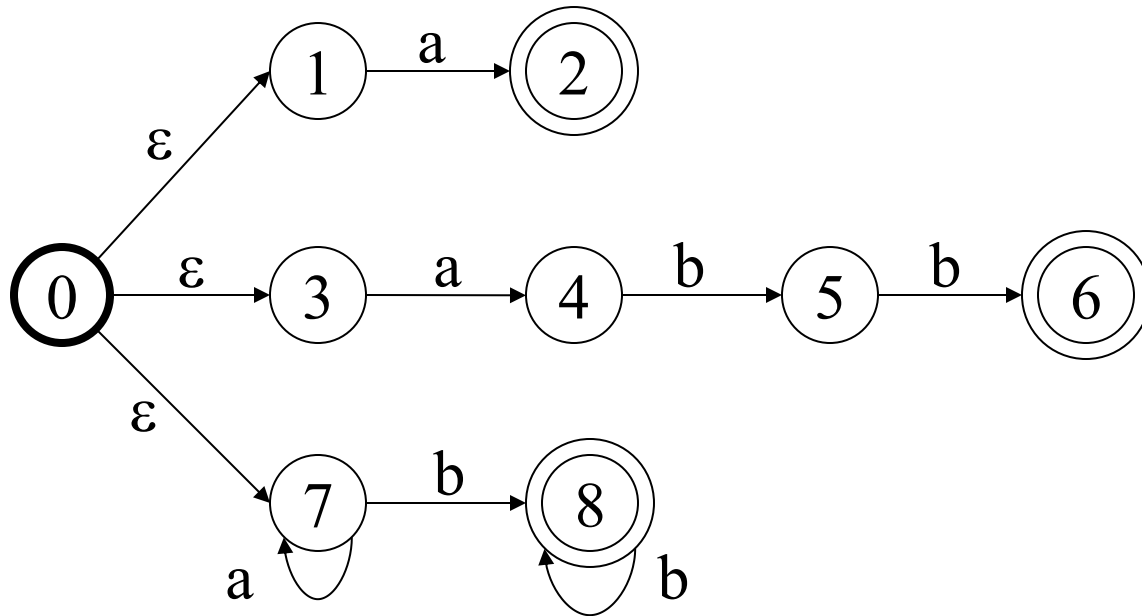
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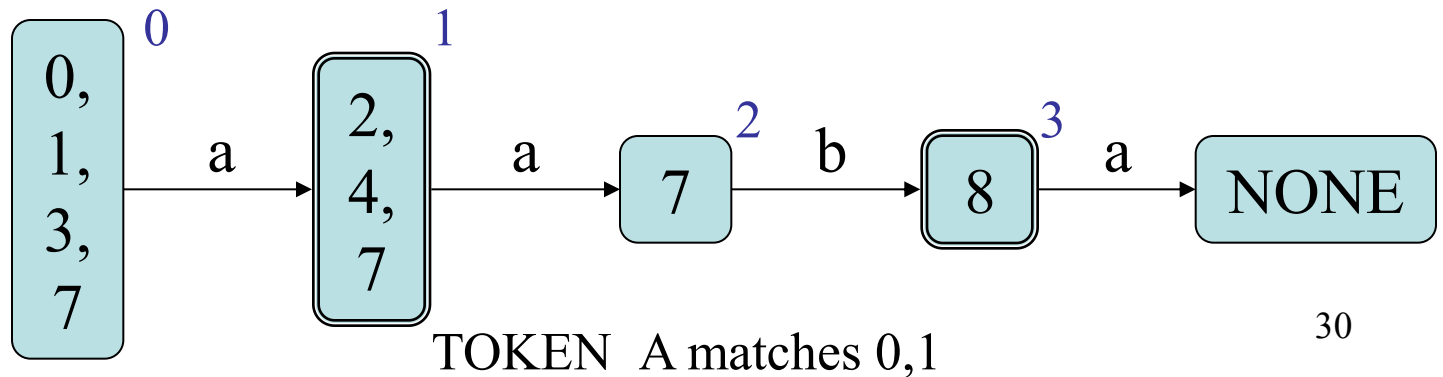
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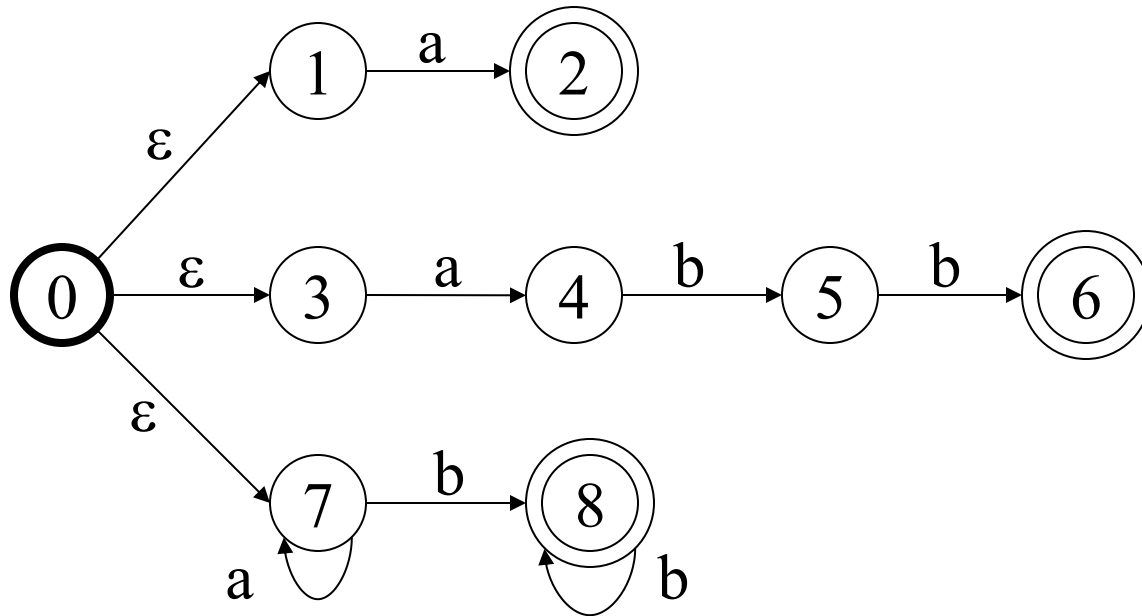
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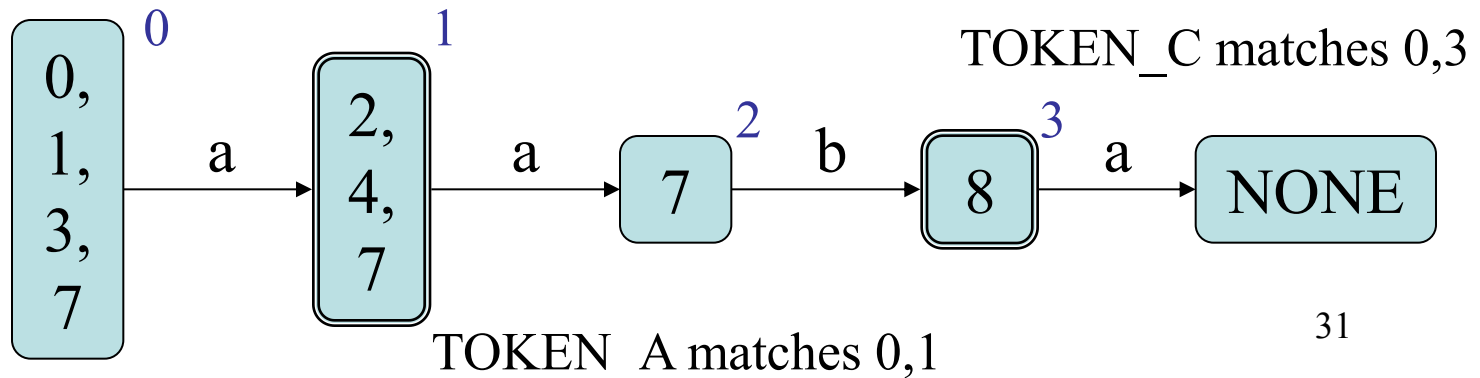
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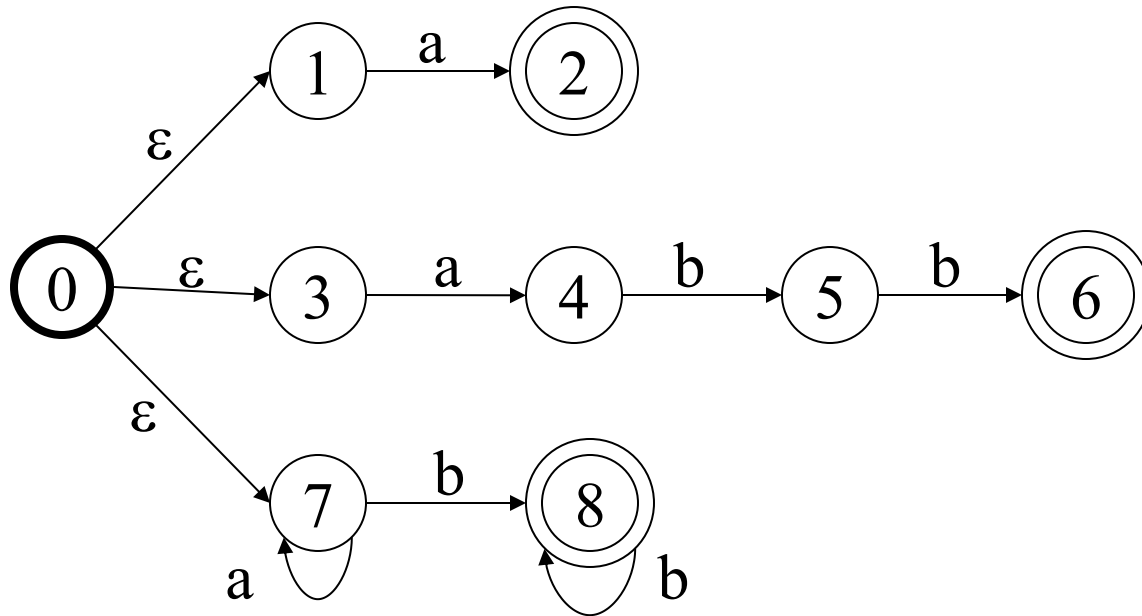
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Lexical Analysis using NFAs



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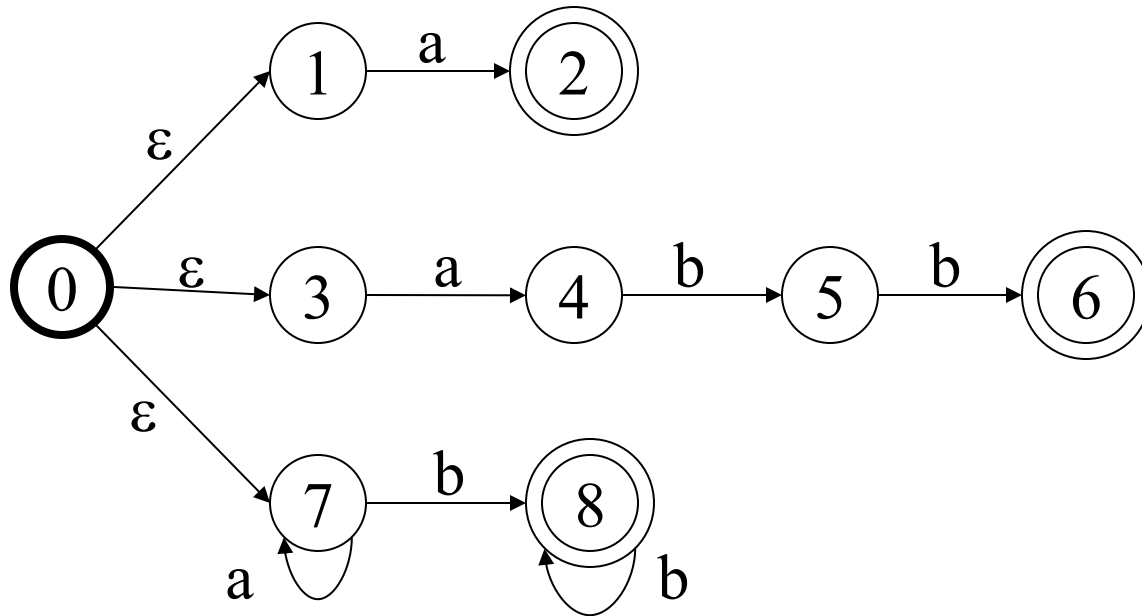
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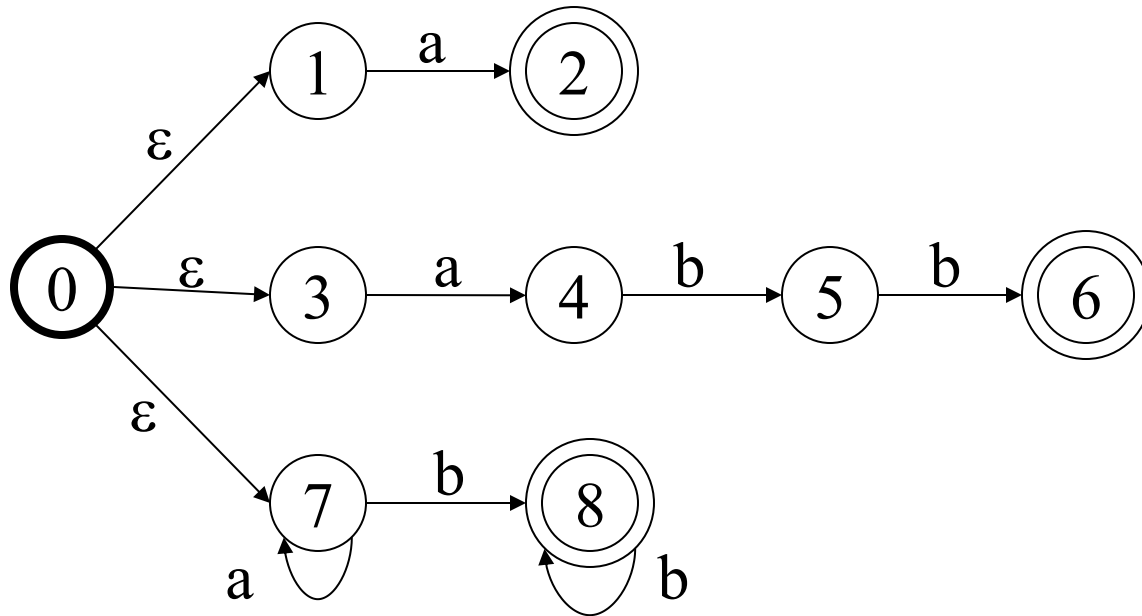
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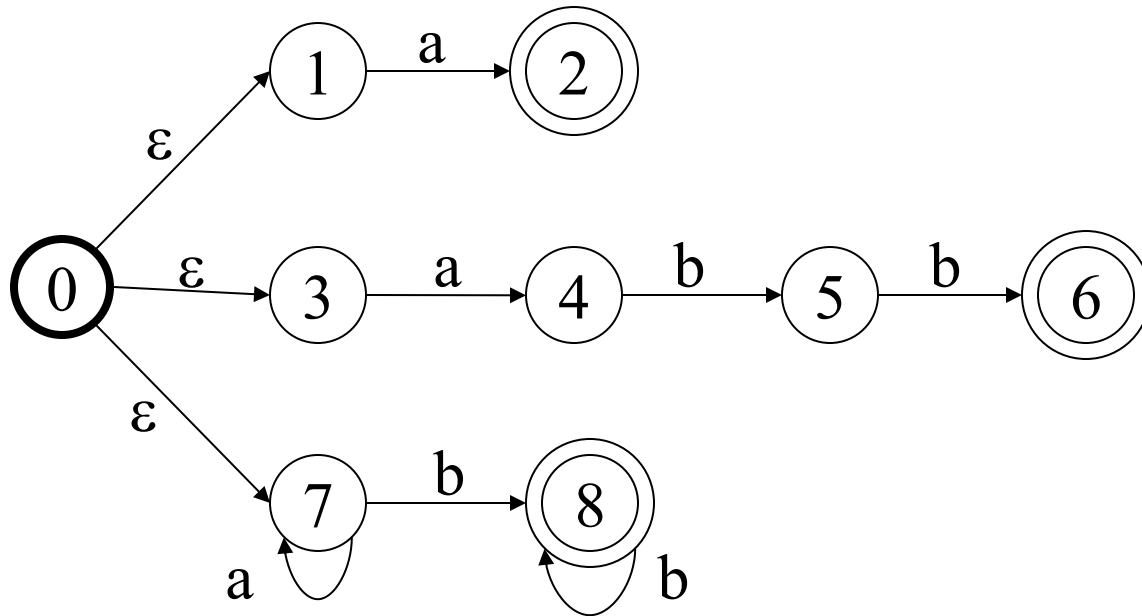
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³

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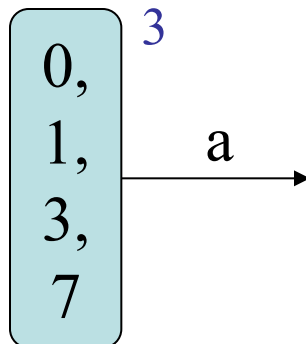
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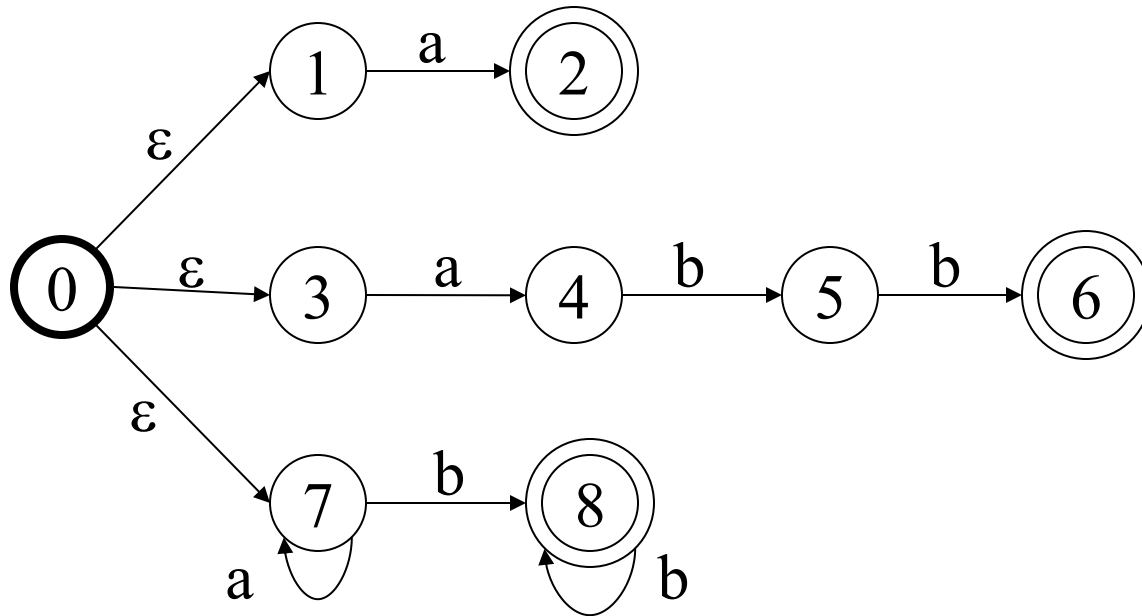
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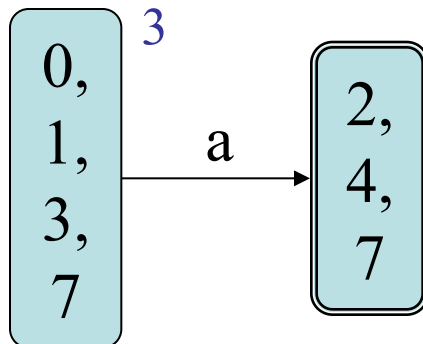
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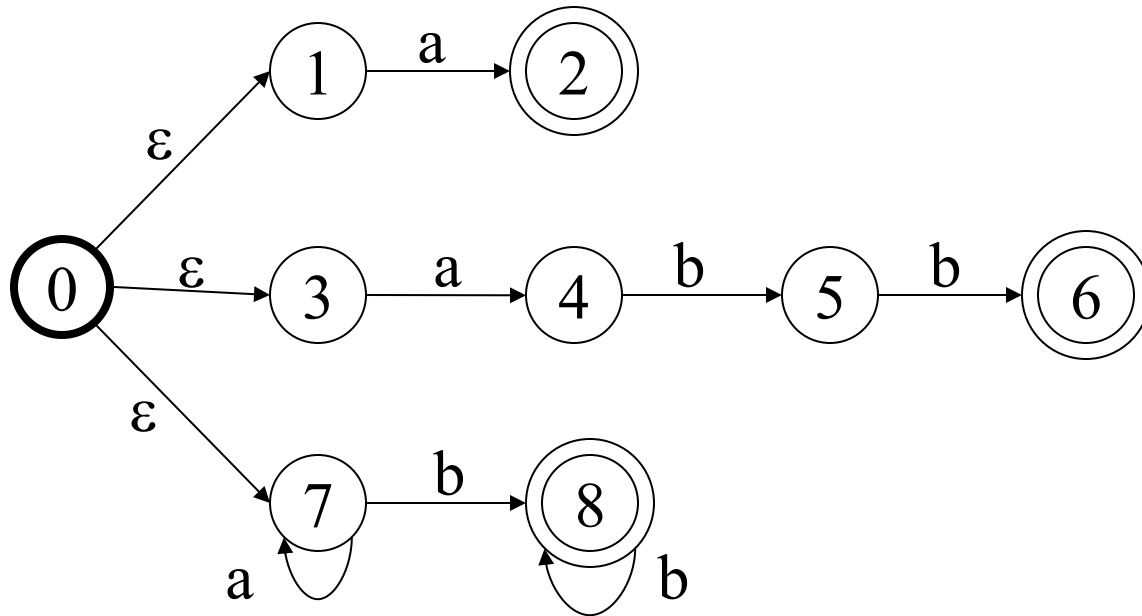
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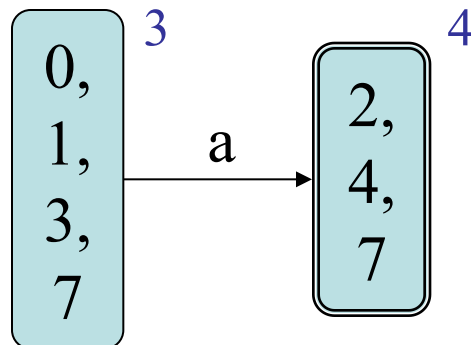
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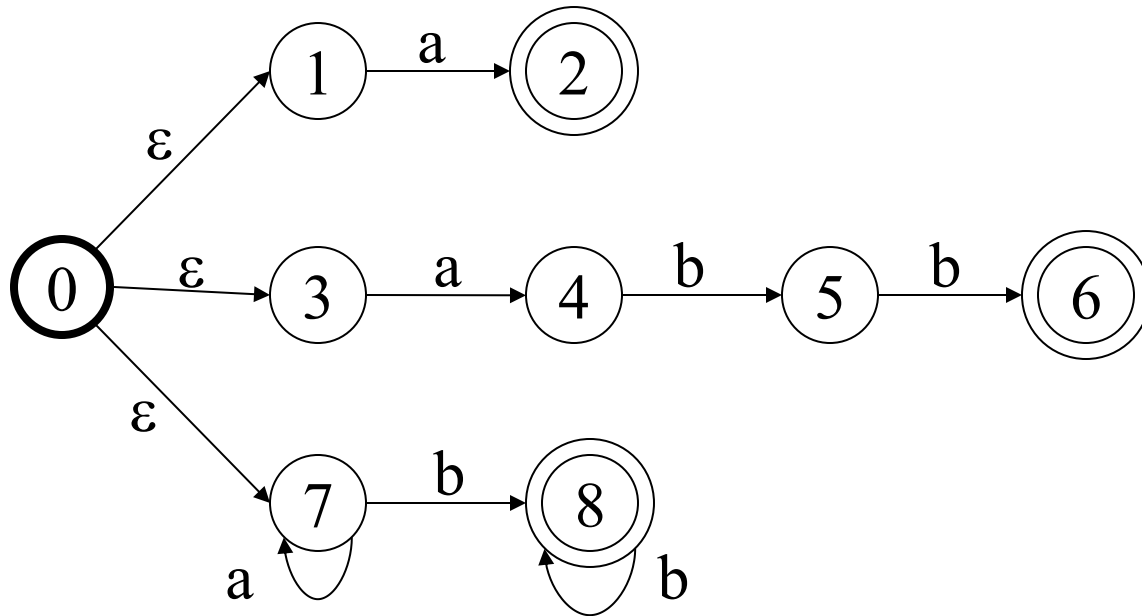
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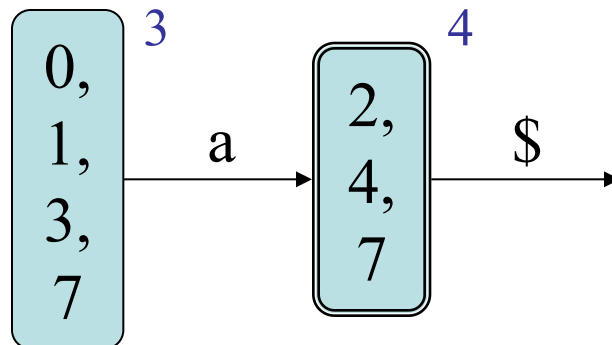
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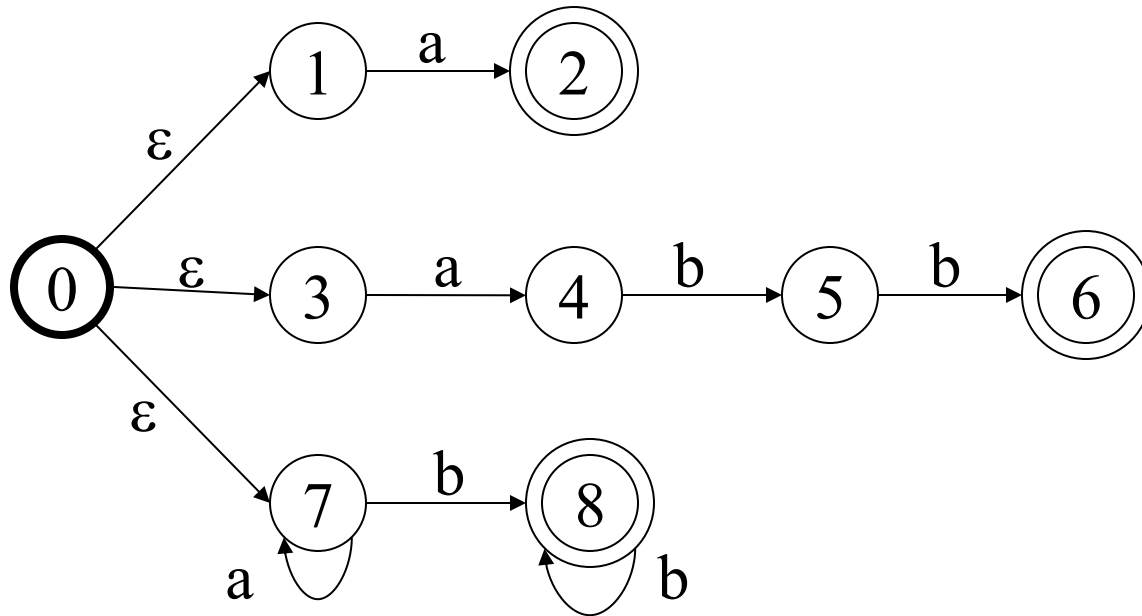
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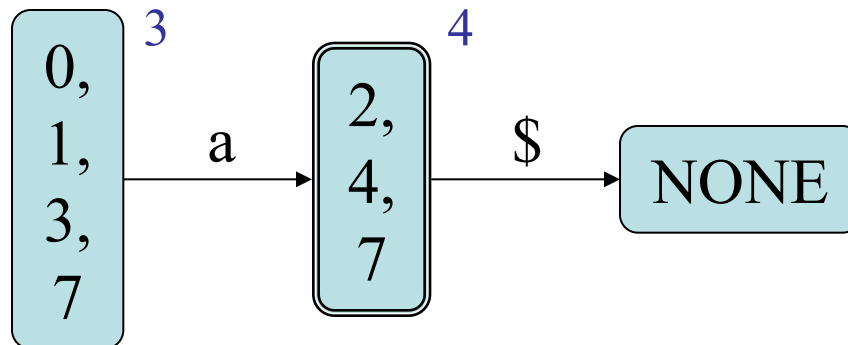
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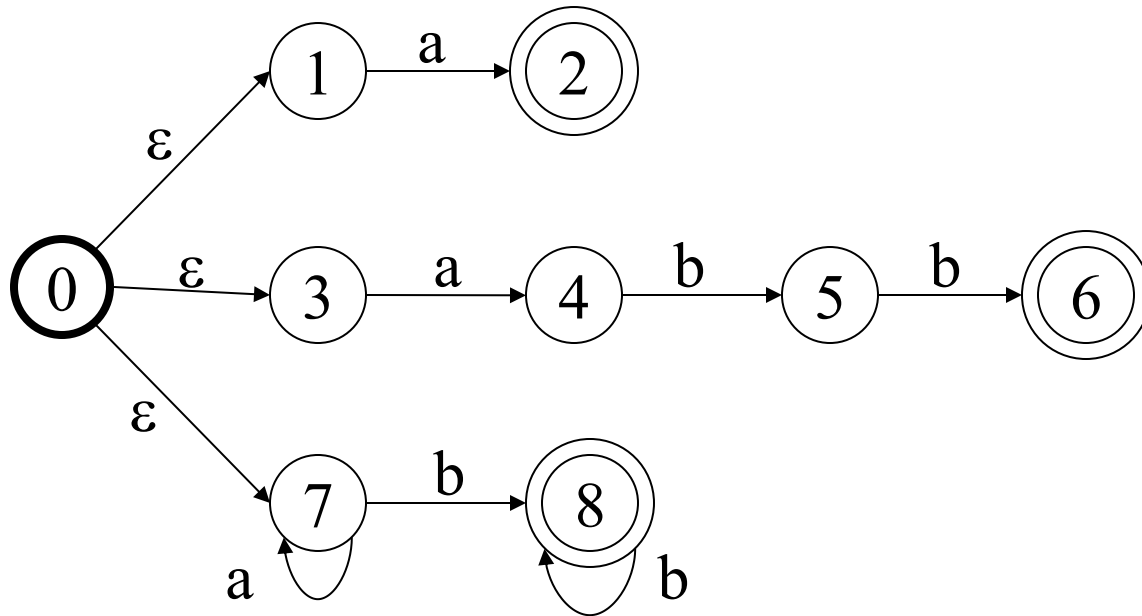
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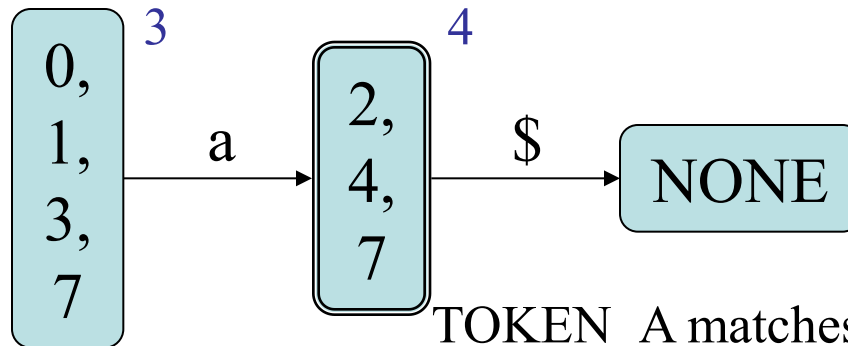
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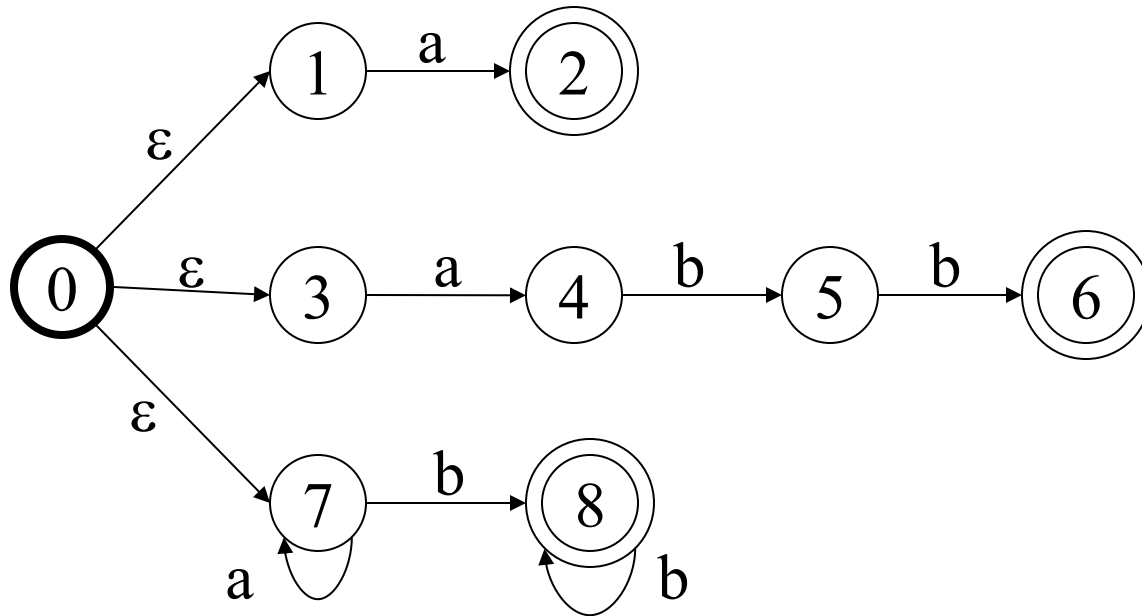
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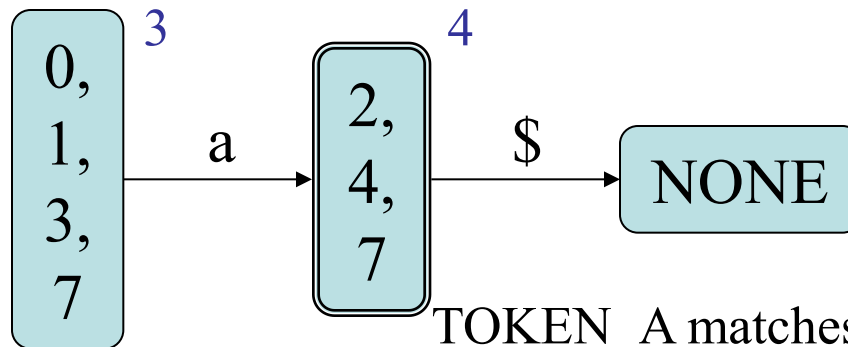
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Input: aaba

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Output:

TOKEN_C aab [0,3]

TOKEN_A a [3,4]

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- Each token is defined using a regexp r_i
- Merge all regexps into one big regexp
 - $R = (r_1 \mid r_2 \mid \dots \mid r_n)$
- Convert R to an NFA, then DFA, then minimize
 - remember orig NFA final states with each DFA state

Lexical Analyzer using DFAs

- The DFA recognizer has to find the *longest leftmost match* for a token
 - continue matching and report the last final state reached once DFA simulation cannot continue
 - e.g. longest match: `<print>` and not `<pr>`, `<int>`
 - e.g. leftmost match: for input string `aabaaaaab` the regexp `a+b` will match `aab` and not `aaaaab`

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 - e.g. leftmost match: for input string `aabaaaaab` the regexp `a+b` will match `aab` and not `aaaaab`
- If two patterns match the same token, pick the one that was listed earlier in R
 - e.g. prefer final state (in the original NFA) of r_2 over r_3

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- Implementing r_1/r_2 : match r_1 when followed by r_2

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- The lexical analyzer matches $r_1 \& r_2$ up to position q in the input
- But remembers the position p in the input where r_1 matched but not r_2
- Reset to start state and start from position p

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\Rightarrow Lexical Analyzer (multiple patterns)