CFG1: Intro to CFGs

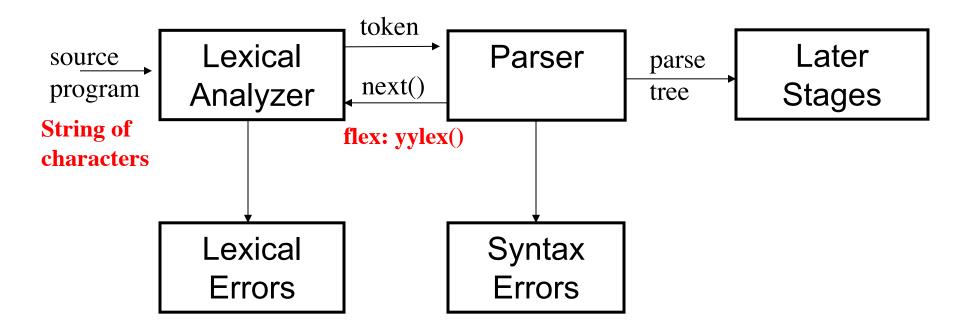
#### **Context-Free Grammars**

CMPT 379: Compilers

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anoopsarkar.github.io/compilers-class

#### Parsing



#### Parsing

- Not all string of tokens are valid programs
- Parser distinguishes between valid and invalid programs
- We need
  - A language for describing valid string of tokens
  - A method for distinguishing valid from invalid programs

 Programming languages have recursive structure

```
• An EXP is ... if EXP then EXP do EXP else end EXP
```

 Context Free Grammars are natural notation for the recursive structures

- A CFG consists of
  - A set of terminals T
  - A set on non-terminals
  - A start symbol S∈N
  - A set of productions  $X \rightarrow Y_1...Y_n$   $X \in N$   $Y_i \in N \cup T \cup \{\epsilon\}$

• 
$$\{(i)^i \mid i \geq 0\}$$

#### **Productions:**

$$S \rightarrow (S)$$

$$S \rightarrow \epsilon$$

$$N = \{S\}$$

$$T = \{ (,) \}$$

- Begin with string that has only start symbol S
- 2. Replace any non-terminal X in the string by the right-hand side of some production  $X \rightarrow Y_1...Y_n$
- 3. Repeat (2) until there is no non-terminals

$$S \to (S)$$

$$S \to \varepsilon$$

$$(S)$$

$$((S))$$

$$((S))$$

#### Language of CFGs

- Let G be a context free grammar with start symbol S, and terminals T
  - The language L(G) of G is:

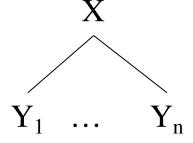
```
\{\alpha_1 \dots \alpha_n | \forall_i \alpha_i \in T \land S \to^* \alpha_1 \dots \alpha_n \}
\{\epsilon, (), (()), ((())), \dots \}
```

#### Derivation and Parse Tree

A derivation is a sequence of productions

$$S \rightarrow \cdots \rightarrow \cdots \rightarrow \cdots \rightarrow \cdots$$

- A derivation can be drawn as a parse tree
  - Start symbol is the tree's root
  - For a production X→Y<sub>1</sub>...Y<sub>n</sub> add
     children Y<sub>1</sub>...Y<sub>n</sub> to node X



## Arithmetic Expressions

- $E \rightarrow E + E$
- $E \rightarrow E * E$
- $E \rightarrow (E)$
- $E \rightarrow -E$
- $E \rightarrow id$

## Derivation for id + id \* id

$$E \rightarrow E + E$$
  
 $E \rightarrow E * E$   
 $E \rightarrow (E)$   
 $E \rightarrow - E$ 

 $E \rightarrow id$ 

$$E \Rightarrow E + E$$

$$\Rightarrow id + E$$

$$\Rightarrow id + E * E$$

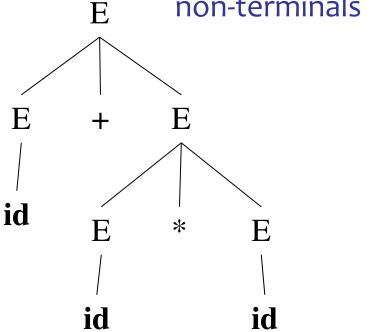
$$\Rightarrow id + id * E$$

$$\Rightarrow id + id * id$$

#### **Leaves nodes:** terminals

#### **Interior nodes:**

non-terminals



# Leftmost derivation for id + id \* id

# Rightmost derivation for id + id \* id

$$E \rightarrow E + E \qquad E \Rightarrow E * E$$

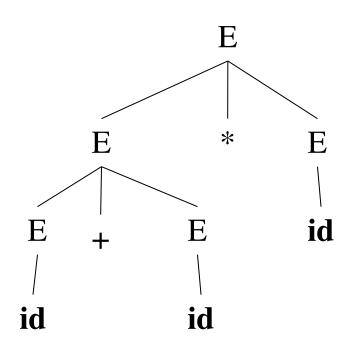
$$E \rightarrow E * E \qquad \Rightarrow E * id$$

$$E \rightarrow (E) \qquad \Rightarrow E + E * id$$

$$E \rightarrow -E \qquad \Rightarrow E + id * id$$

$$E \rightarrow id \qquad \Rightarrow E + id * id$$

$$\Rightarrow id + id * id$$



# Rightmost vs. Leftmost Derivation

- Note that rightmost and leftmost derivations have the same parse tree
  - Every parse tree has a rightmost and a leftmost derivation
  - Important in resolving ambiguity

#### Writing a CFG for a PL

- First write (or read) a reference grammar of what you want to be valid programs
- For now, we only worry about the structure, so the reference grammar might choose to overgenerate in certain cases (e.g. bool x = 20;)
- Convert the reference grammar to a CFG

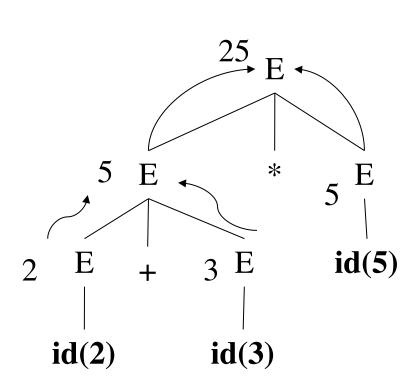
#### Arithmetic Expressions

• E 
$$\rightarrow$$
 E  $+$  E  $\{$  \$\$ = \$1  $+$  \$\$ }  
• E  $\rightarrow$  E  $*$  E  $\{$  \$\$ = \$1  $*$  \$3 }

• 
$$E \rightarrow (E) \{ \$\$ = \$2 \}$$

• 
$$E \rightarrow -E \{ \$\$ = -1 * \$2 \}$$

• 
$$E \rightarrow id \{ \$\$ = \$1 \}$$



#### **CFG** Notation

Normal CFG notation

$$E \rightarrow E * E$$

$$E \rightarrow E + E$$

Backus Naur notation

```
E::= E * E | E + E

(an or-list of right hand sides)

Also:

E = E "*" E | E "+" E
```