

Context-Free Grammars

CMPT 379: Compilers

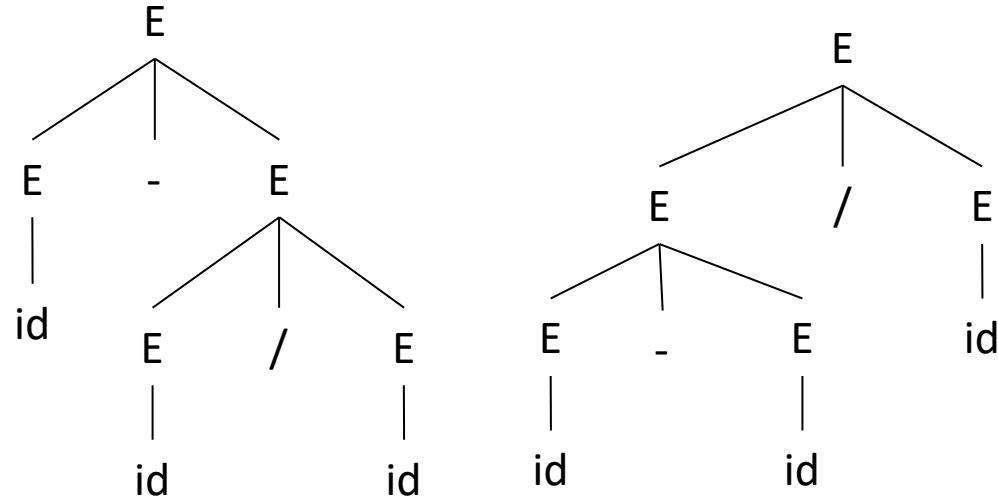
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anoopsarkar.github.io/compilers-class

Ambiguity

- r1 $E \rightarrow E - E$
- r2 $E \rightarrow E / E$
- r3 $E \rightarrow (E)$
- r4 $E \rightarrow id$

id - id / id



Ambiguity

- Grammar is ambiguous if more than one parse tree is possible for some sentences
 - There is more than one leftmost (or rightmost) derivations
- Ambiguity is not acceptable in programming languages
 - Leaves meaning of some programs ill-defined
 - Unfortunately, it's undecidable to check whether a given CFG is ambiguous
 - Some CFLs are inherently ambiguous (do not have an unambiguous CFG)

Ambiguity

- Handle ambiguity:
 - Rewrite the grammar unambiguously
 - Augment parser by enforcing precedence and associativity

- Consider the original ambiguous grammar:

$E \rightarrow E - E$ $E \rightarrow E / E$

$E \rightarrow (E)$ $E \rightarrow \mathbf{id}$

- How can we change the grammar to get only one tree for the input string: **id - id / id**

Precedence

- Original ambiguous grammar:

$$\bullet E \rightarrow E - E \quad E \rightarrow E / E$$

$$\bullet E \rightarrow (E) \quad E \rightarrow \text{id}$$

- Use different non-terminals for each

Precedence level: (start from lowest level)

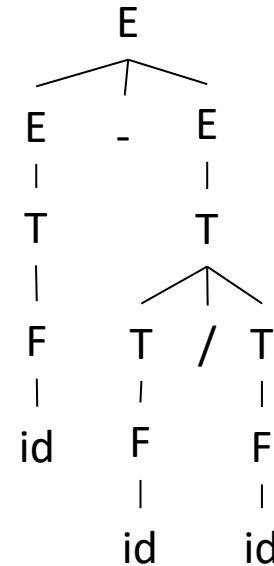
$$\bullet E \rightarrow E - E \quad E \rightarrow T$$

$$\bullet T \rightarrow T / T \quad T \rightarrow F$$

$$\bullet F \rightarrow \text{id} \quad F \rightarrow (E)$$

- Input: id - id / id

Q: Using this CFG write down two leftmost derivations for input string id-id-id



Associativity

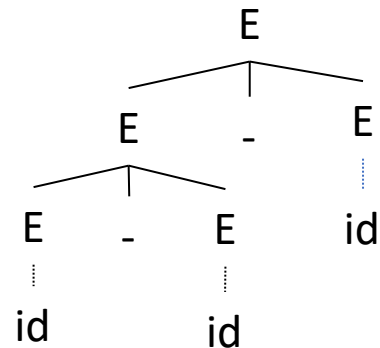
- Grammar captures operator precedence

- $E \rightarrow E - E$ $E \rightarrow T$
- $T \rightarrow T / T$ $T \rightarrow F$
- $F \rightarrow \text{id}$ $F \rightarrow (E)$

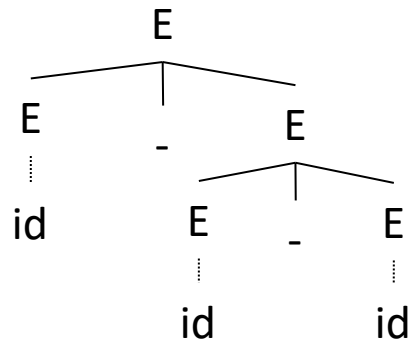
- Still ambiguous!!

- Consider: **id - id - id**
- "-" is left associative
- Operations are grouped from left to right

5-3-2



(5-3)-2



5-(3-2)

Recursion

- Grammar is **recursive** in nonterminal X if:
 - $X \Rightarrow^+ \dots X \dots$
 - \Rightarrow^+ means in one or more steps, X derives a sequence of symbols that includes X
- Grammar is **left recursive** in X if:
 - $X \Rightarrow^+ X \dots$
 - In one or more steps, X derives a sequence of symbols that **starts** with X
- Grammar is **right recursive** in X if:
 - $X \Rightarrow^+ \dots X$
 - In one or more steps, X derives a sequence of symbols that **ends** with X

Fix Associativity

- Left and right recursive in non-terminals E and T

- $E \rightarrow E - E$ $E \rightarrow T$
- $T \rightarrow T / T$ $T \rightarrow F$
- $F \rightarrow \mathbf{id}$ $F \rightarrow (E)$

- Express operator associativity:

- For left associativity use left recursion
- For right associativity use right recursion

- Unambiguous grammar

- $E \rightarrow E - T$ $E \rightarrow T$
- $T \rightarrow T / F$ $T \rightarrow F$
- $F \rightarrow \mathbf{id}$ $F \rightarrow (E)$

Q: Using this CFG write down all possible leftmost derivations for each input string below:

1. $\mathbf{id-id-id}$
2. $\mathbf{id-id/id}$
3. $\mathbf{(id-id)/id}$

Precedence and Associativity

- Original ambiguous grammar:

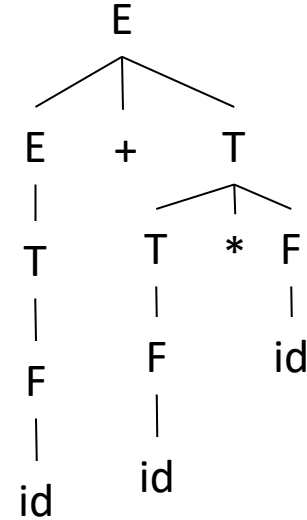
- $E \rightarrow E + E$ $E \rightarrow E * E$
- $E \rightarrow (E)$ $E \rightarrow - E$
- $E \rightarrow \text{id}$

- Unambiguous grammar:

- $E \rightarrow E + T$ $T \rightarrow T * F$
- $E \rightarrow T$ $T \rightarrow F$
- $F \rightarrow (E)$
- $F \rightarrow \text{id}$

$F \rightarrow - E$

- Input: $\text{id} + \text{id} * \text{id}$



Warning! Is this unambiguous?
Check derivations for $-\text{id} + \text{id}$

Q: Compare
with $F \rightarrow - F$

Dangling else ambiguity

- Original Grammar (ambiguous)

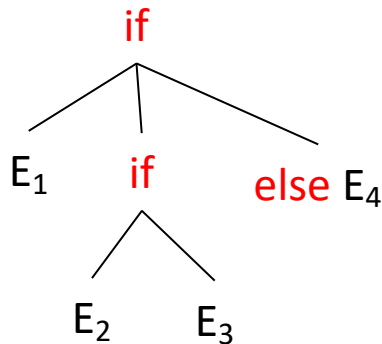
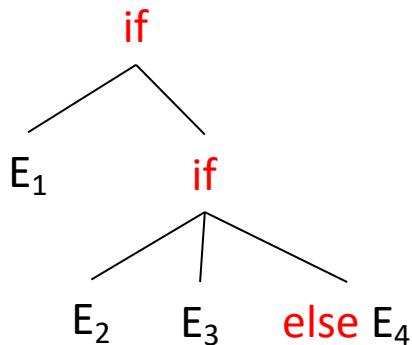
Stmt \rightarrow if Expr then Stmt else Stmt

Stmt \rightarrow if Expr then Stmt

Stmt \rightarrow Other

- if E₁ then if E₂ then E₃ else E₄

else matches the closest
unmatched then



Dangling else ambiguity

- Original Grammar (ambiguous)

Stmt \rightarrow if Expr then Stmt else Stmt

Stmt \rightarrow if Expr then Stmt

Stmt \rightarrow Other

else matches the closest
unmatched then

- Unambiguous grammar

Stmt \rightarrow MatchedStmt /*all then are matched*/

Stmt \rightarrow UnmatchedStmt /*some then are unmatched*/

MatchedStmt \rightarrow if Expr then MatchedStmt else MatchedStmt

MatchedStmt \rightarrow Other

UnmatchedStmt \rightarrow if Expr then Stmt

UnmatchedStmt \rightarrow if Expr then MatchedStmt else UnmatchedStmt

Dangling else ambiguity

- Check unambiguous dangling-else grammar with the following inputs:
 - if Expr then if Expr then Other else Other
 - if Expr then if Expr then Other else Other else Other
 - if Expr then if Expr then Other else if Expr then Other else Other

Precedence and Associativity Declaration

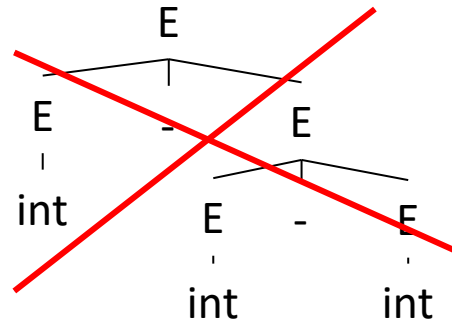
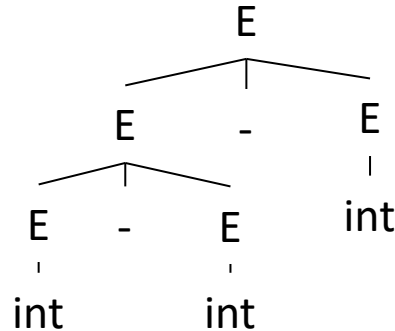
- Impossible to automatically convert an ambiguous grammar to an unambiguous one
- Used with care, potentially ambiguous grammars can be useful:
 - Allows a grammar that is easier to read for humans
 - However it needs disambiguation mechanisms like precedence & associativity

Precedence and Associativity Declaration

- Instead of re-writing the grammar
 - Use the more natural (ambiguous) grammar
 - Along with disambiguation declarations
- Most tools allow **precedence and associativity declaration** to disambiguate grammars

Associativity Declaration

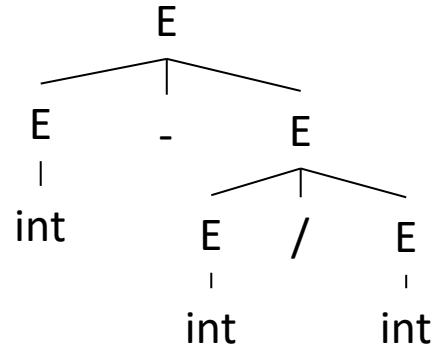
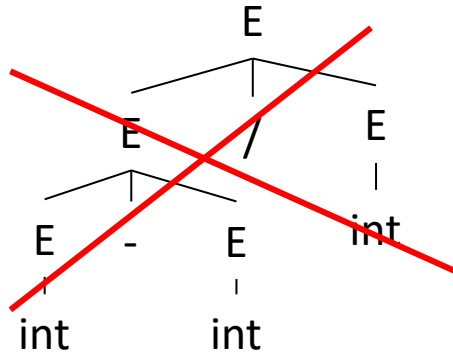
- Consider the grammar:
 - $E \rightarrow E - E \mid \text{int}$
- Ambiguous: two parse trees $\text{int} - \text{int} - \text{int}$



- Left associativity declaration: `%left -`

Precedence Declaration

- Consider the grammar:
 - $E \rightarrow E - E \mid E / E \mid \text{int}$
- Ambiguous: two parse trees $\text{int} - \text{int} / \text{int}$



- Precedence declaration: $\%left -$ lower priority
 $\%left /$ higher priority

Extra Slides

Other Ambiguous Grammars

- Consider the grammar

$$\begin{aligned} R \rightarrow & R \text{ '}' R \\ & | R R \\ & | R \text{ '*' } \\ & | \text{ '(' } R \text{ ')' } \\ & | a \\ & | b \end{aligned}$$

- What does this grammar generate?
- What is the parse tree for $a \mid b^*a$
- Is this grammar ambiguous?

Dangling else ambiguity

- Original Grammar (ambiguous)

Stmt \rightarrow if Expr then Stmt else Stmt

Stmt \rightarrow if Expr then Stmt

Stmt \rightarrow Other

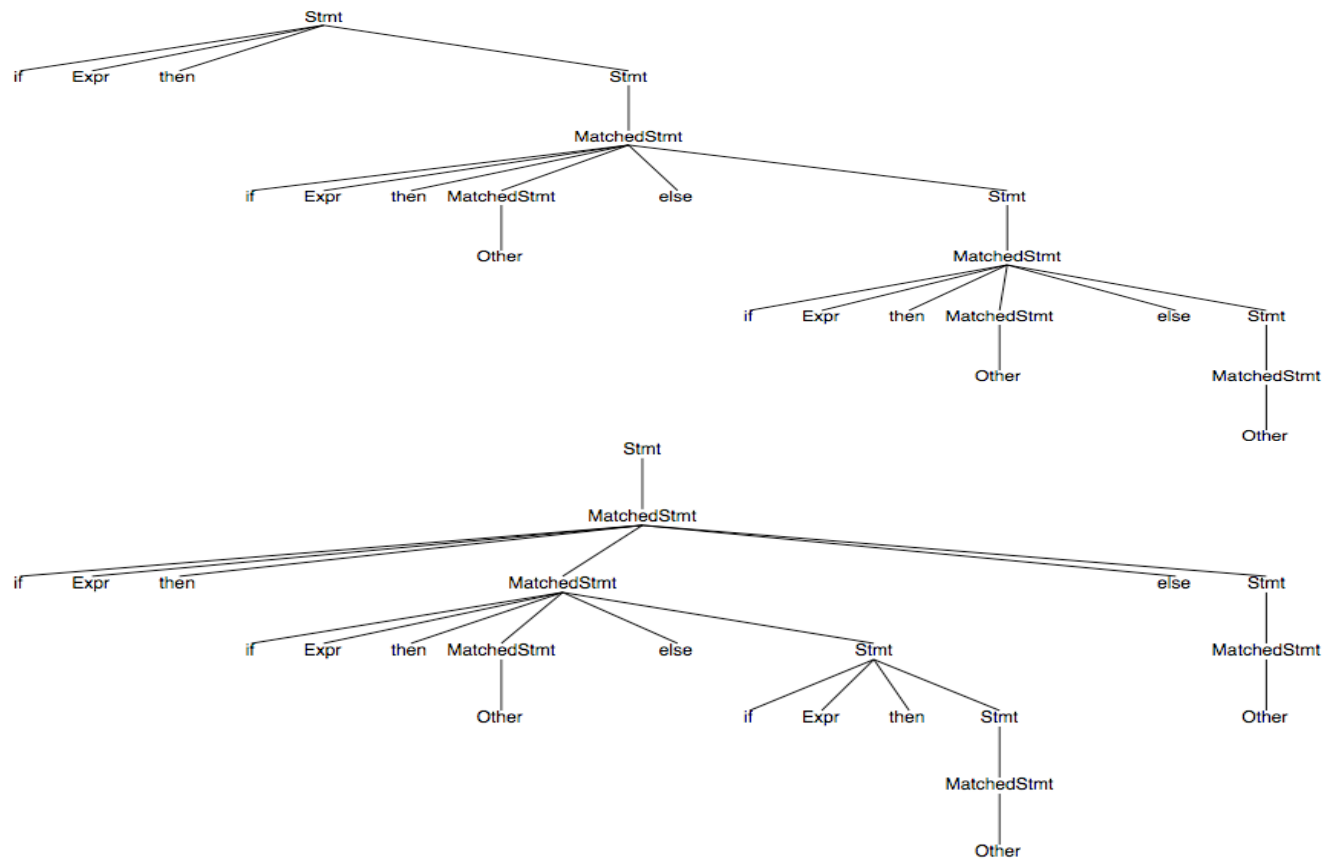
- Modified Grammar (unambiguous?)

Stmt \rightarrow if Expr then Stmt

Stmt \rightarrow MatchedStmt

MatchedStmt \rightarrow if Expr then MatchedStmt else Stmt

MatchedStmt \rightarrow Other



Dangling else ambiguity

- Modified Grammar (check for ambiguity)

Stmt \rightarrow MatchedStmt

Stmt \rightarrow UnmatchedStmt

MatchedStmt \rightarrow **if** Expr **then** MatchedStmt **else** MatchedStmt

MatchedStmt \rightarrow Other

UnmatchedStmt \rightarrow **if** Expr **then** Stmt

UnmatchedStmt \rightarrow **if** Expr **then** MatchedStmt **else** UnmatchedStmt