LR4: LR(1) Parsing

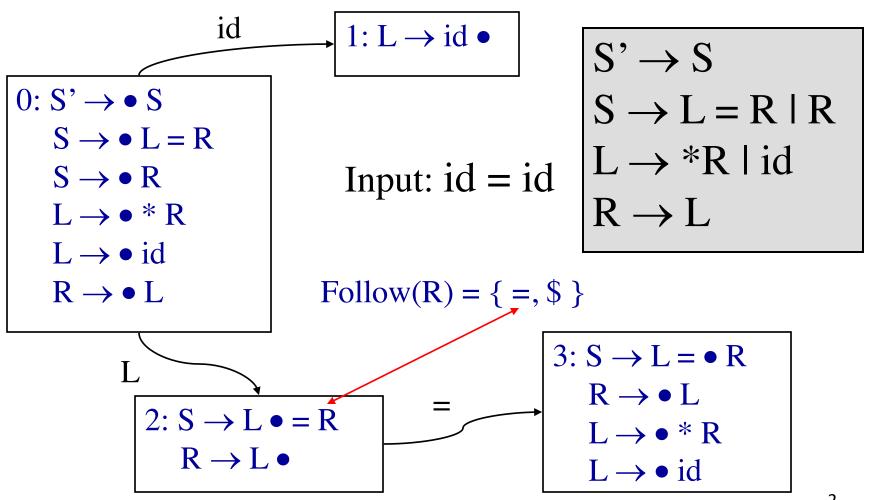
#### LR Parsing

CMPT 379: Compilers

Instructor: Anoop Sarkar

anoopsarkar.github.io/compilers-class

#### SLR limitation: lack of context

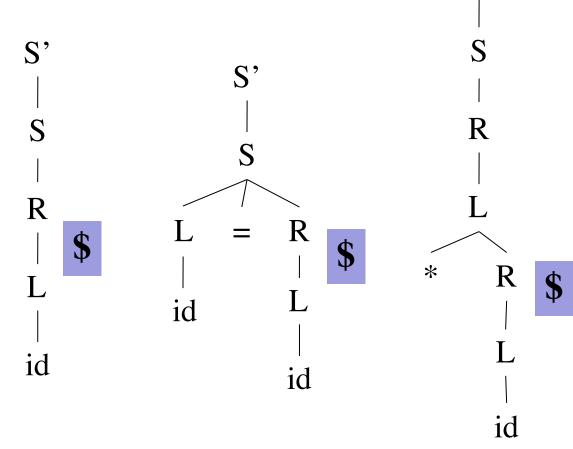


$$S' \rightarrow S$$
  
 $S \rightarrow L = R \mid R$   
 $L \rightarrow *R \mid id$   
 $R \rightarrow L$ 

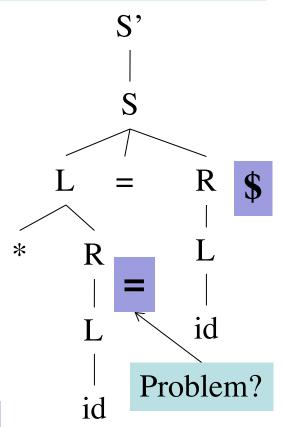
$$Follow(R) = \{ =, \$ \}$$

$$2: S \to L \bullet = R$$

$$R \to L \bullet$$



Find all lookaheads for reduce  $R \rightarrow L \bullet$ 



No!  $R \rightarrow L \bullet$  reduce and  $S \rightarrow L \bullet = R$  do not co-occur due to the  $L \rightarrow *R$  rule

## Solution: Canonical LR(1)

- Extend definition of configuration
  - Remember lookahead
- New closure method
- Extend definition of Successor

## LR(1) Configurations

- [A  $\rightarrow \alpha$ • $\beta$ , a] for a  $\in$  T is valid for a viable prefix  $\delta \alpha$  if there is a rightmost derivation S  $\Rightarrow$ \*  $\delta A \eta \Rightarrow$ \*  $\delta \alpha \beta \eta$  and  $(\eta = a \gamma)$  or  $(\eta = \epsilon)$
- Notation: [A  $\rightarrow \alpha \bullet \beta$ , a/b/c]
  - if [A → α•β, a], [A → α•β, b], [A → α•β, c] are valid configurations

## LR(1) Configurations

$$S \rightarrow B B$$
  
  $B \rightarrow a B \mid b$ 

$$S \Rightarrow BB \Rightarrow BaB \Rightarrow Bab$$
  
 $\Rightarrow aBab \Rightarrow aaBab \Rightarrow aaaBab$ 

- $S \Rightarrow^*_{rm} aaBab \Rightarrow_{rm} aaaBab$
- Item [B → a B, a] is valid for viable prefix
- $S \Rightarrow^*_{rm} BaB \Rightarrow_{rm} BaaB \leftarrow \begin{bmatrix} In BaB \Rightarrow BaaB \text{ the string} \\ aB \text{ is the handle (rhs of B)} \end{bmatrix}$
- Also, item [B → a B, \$] is valid for viable prefix Baa

$$S \Rightarrow BB \Rightarrow BaB \Rightarrow BaaB$$

#### LR(1) Closure

#### Closure property:

- If  $[A \rightarrow \alpha \bullet B\beta, a]$  is in set, then  $[B \rightarrow \bullet \gamma, b]$  is in set if  $b \in First(\beta a)$
- Compute as fixed point
- Only include contextually valid lookaheads to guide reducing to B

#### Starting Configuration

- Augment Grammar with S' just like for LR(0), SLR(1)
- Initial configuration set is

$$I = closure([S' \rightarrow \bullet S, \$])$$

# Example: closure( $[S' \rightarrow \bullet S, \$]$ )

$$[S' \rightarrow \bullet S, \$]$$

$$[S \rightarrow \bullet L = R, \$]$$

$$[S \rightarrow \bullet R, \$]$$

$$[L \rightarrow \bullet * R, =]$$

$$[L \rightarrow \bullet id, =]$$

$$[R \rightarrow \bullet L, \$]$$

$$[L \rightarrow \bullet *R, \$]$$

$$[L \rightarrow \bullet id, \$]$$

$$S' \rightarrow S$$

$$S \rightarrow L = R \mid R$$

$$L \rightarrow *R \mid id$$

$$R \rightarrow L$$

$$S' \rightarrow \bullet S, \$$$

$$S \rightarrow \bullet L = R, \$$$

$$S \rightarrow \bullet R, \$$$

$$L \rightarrow \bullet * R, =/$$$

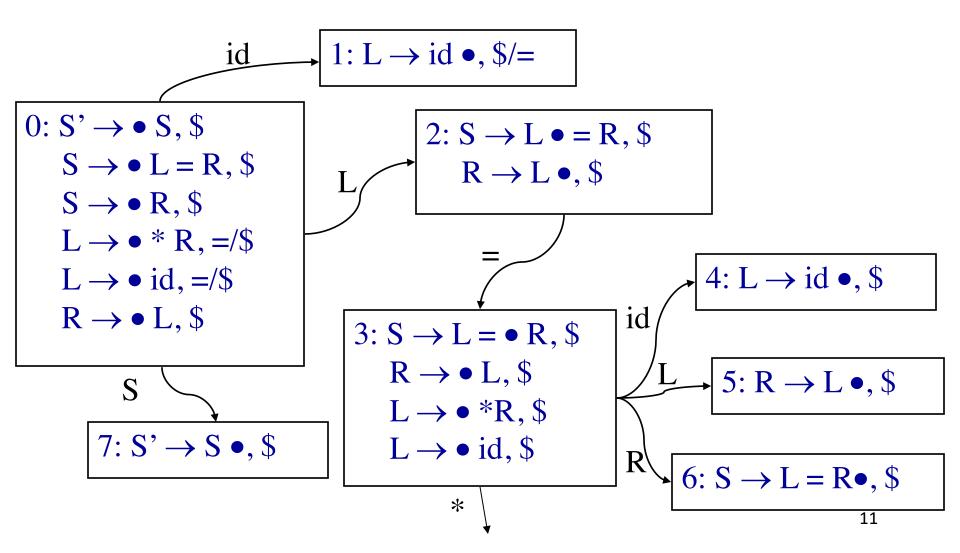
$$L \rightarrow \bullet id, =/$$

$$R \rightarrow \bullet L, \$$$

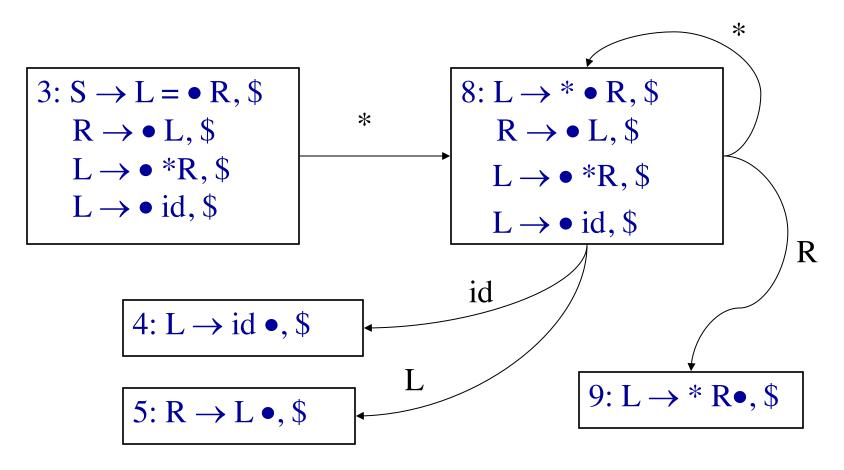
## LR(1) Successor(C, X)

- Let  $I = [A \rightarrow \alpha \bullet B\beta, a]$  or  $[A \rightarrow \alpha \bullet b\beta, a]$
- Successor(I, B) = closure([A  $\rightarrow \alpha$ B •  $\beta$ , a])
- Successor(I, b) = closure([A  $\rightarrow \alpha b \bullet \beta, a]$ )

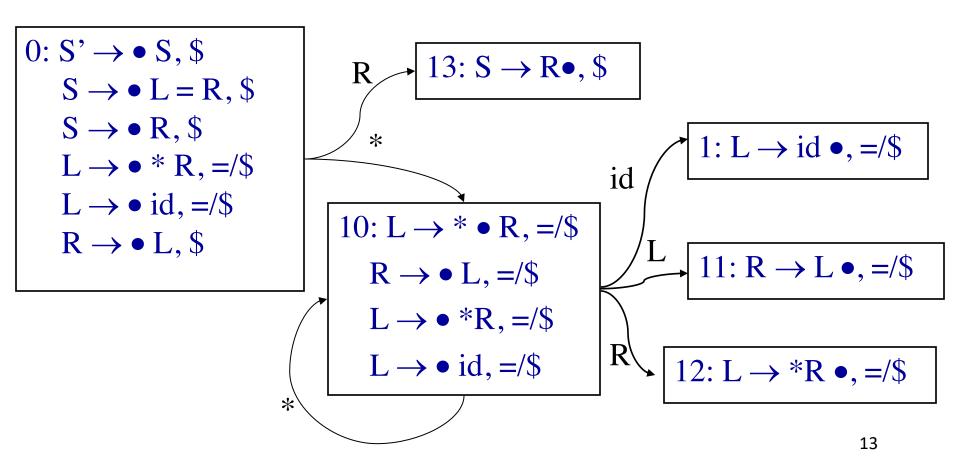
# LR(1) Example



#### LR(1) Example (contd)



# LR(1) Example (contd)



<b>Productions</b>					
1	$S \rightarrow L = R$				
2	$S \rightarrow R$				
3	$L \rightarrow R$				
4	$L \rightarrow id$				
5	$R \rightarrow L$				

	id	=	*	\$	S	L	R
0	<b>S</b> 1		S10		7	2	13
1		R4		R4			
2		<b>S</b> 3		R5			
3	S4		<b>S</b> 8			5	6
4				R4			
5				R5			
6				R1			
7				Acc			
8	<b>S</b> 4		<b>S</b> 8			5	9
9				R3			
10	<b>S</b> 1		S10			11	12
11		R5		R5			
12		R3		R3			
13				R2			

#### LR(1) Construction

1. Construct  $F = \{I_0, I_1, ... I_n\}$ 2. a) if  $[A \rightarrow \alpha \bullet, a] \in I_i$  and A != S'then action[i, a] := reduce A  $\rightarrow \alpha$ b) if  $[S' \rightarrow S \bullet, \S] \in I_i$ then action[i, \$] := accept c) if  $[A \rightarrow \alpha \bullet a\beta, b] \in I_i$  and Successor $(I_i, a)=I_i$ then action[i, a] := shift i 3. if Successor( $I_i$ , A) =  $I_i$  then goto[i, A] := j

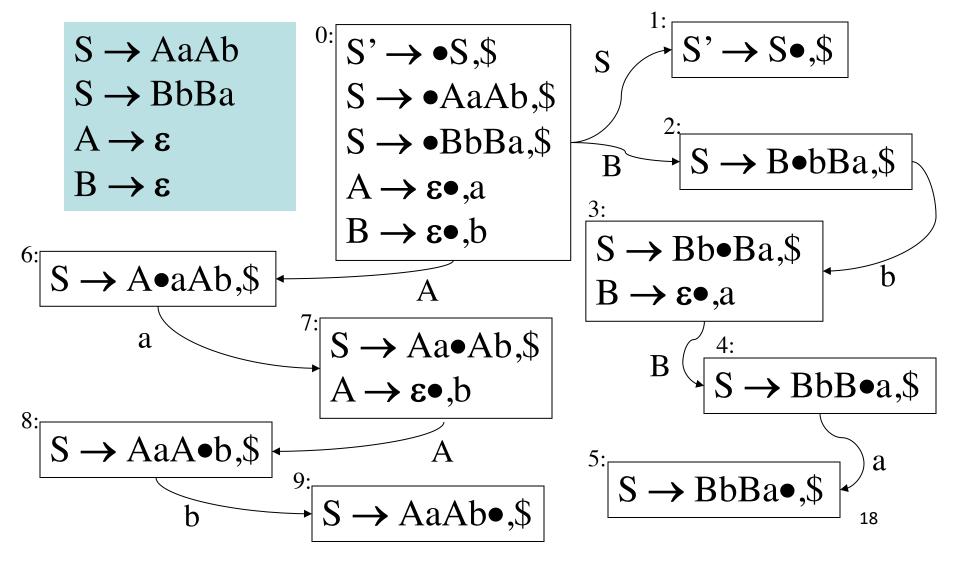
# LR(1) Construction (cont'd)

- 4. All entries not defined are errors
- 5. Make sure  $I_0$  is the initial state
- Note: LR(1) only reduces using A  $\rightarrow \alpha$  for [A  $\rightarrow \alpha$ •, a] if a follows
- LR(1) states remember context by virtue of lookahead
- Possibly many states!
  - LALR(1) combines some states

#### LR(1) Conditions

- A grammar is LR(1) if for each configuration set (itemset) the following holds:
  - For any item [A → α•xβ, a] with x ∈ T there is no [B →  $\gamma$ •, x]
  - For any two complete items [A  $\rightarrow \gamma \bullet$ , a] and [B  $\rightarrow \beta \bullet$ , b] then a != b.
- Grammars:
  - $LR(0) \subset SLR(1) \subset LR(1) \subset LR(k)$
- Languages expressible by grammars:
  - $LR(0) \subset SLR(1) \subset LR(1) = LR(k)$

# Set-of-items with Epsilon rules

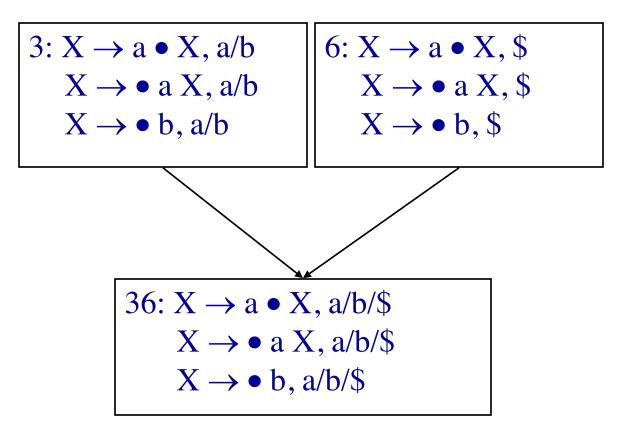


#### Canonical LR(1) Recap

- LR(1) uses left context, current handle and lookahead to decide when to reduce or shift
- Most powerful parser so far
- LALR(1) is practical simplification with fewer states

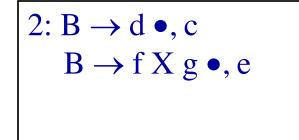
#### Merging States in LALR(1)

- $S' \rightarrow S$   $S \rightarrow XX$   $X \rightarrow aX$  $X \rightarrow b$
- Same CoreSet
- Different lookaheads



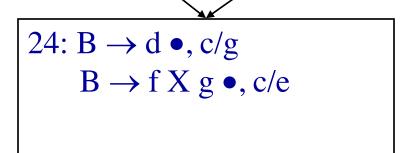
#### R/R conflicts when merging

• 
$$B \rightarrow d$$
  
 $B \rightarrow f X g$   
 $X \rightarrow ...$ 



 $\begin{array}{c} 4: B \to d \bullet, g \\ B \to f X g \bullet, c \end{array}$ 

 If R/R conflicts are introduced, grammar is not LALR(1)!



## LALR(1)

- LALR(1) Condition:
  - Merging in this way does not introduce reduce/reduce conflicts
  - Shift/reduce can't be introduced
- Merging brute force or step-by-step
- More compact than canonical LR, like SLR(1)
- More powerful than SLR(1)
  - Not always merge to full Follow Set