LR3: SLR(1) Parsing

LR Parsing

CMPT 379: Compilers

Instructor: Anoop Sarkar

anoopsarkar.github.io/compilers-class

LR(o) conflicts:

```
S' \rightarrow T
T \rightarrow F
T \rightarrow T * F
T \rightarrow id
F \rightarrow id \mid (T)
F \rightarrow id = T;
```

```
11: F \rightarrow id \bullet
F \rightarrow id \bullet = T
Shift/reduce conflict
```

```
1: F → id •

T → id •

Reduce/Reduce conflict
```

Need more lookahead: SLR(1)

FIRST and FOLLOW

$$a \in \text{FIRST}(\alpha) \text{ if } \alpha \Rightarrow^* a\beta$$

if $\alpha \Rightarrow^* \epsilon \text{ then } \epsilon \in \text{FIRST}(\alpha)$
 $a \in \text{FOLLOW}(A) \text{ if } S \Rightarrow^* \alpha A a\beta$
 $a \in \text{FOLLOW}(A) \text{ if } S \Rightarrow^* \alpha A \gamma a\beta$
and $\gamma \Rightarrow^* \epsilon$

Example First/Follow

$$S \to AB$$
$$A \to c \mid \epsilon$$

$$First(A) = \{c, \epsilon\}$$

$$First(B) = \{c\}$$

$$First(cbB) =$$

$$First(ca) = \{c\}$$

$$First(S) = \{c\}$$

$$Follow(A) = \{c\}$$

$$Follow(A) \cap$$

$$First(c) = \{c\}$$

$$Follow(B) = \{\$\}$$

$$Follow(S) = \{\$\}$$

Example First/Follow

$$S \rightarrow cAa$$

$$A \rightarrow cB \mid B$$

$$B \rightarrow bcB \mid \epsilon$$

First(A) =
$$\{b, c, \epsilon\}$$
 Follow(A) = $\{a\}$
First(B) = $\{b, \epsilon\}$ Follow(B) = $\{a\}$
First(S) = $\{c\}$ Follow(S) = $\{\$\}$

SLR(1): Simple LR(1) Parsing

$$S' \rightarrow T$$
 $T \rightarrow F \mid T * F \mid C (T)$
 $F \rightarrow id \mid id ++ \mid (T)$
 $C \rightarrow id$

What can the next symbol be when we reduce $F \rightarrow id$?

$$S'\$ \Rightarrow T\$ \Rightarrow F\$ \Rightarrow id\underline{\$}$$
 $S'\$ \Rightarrow T\$ \Rightarrow T*F\$ \Rightarrow T*id\$ \Rightarrow$ $F*id\$ \Rightarrow id\underline{*}id\$$

$$S'\$ \Rightarrow T\$ \Rightarrow C(T)\$ \Rightarrow C(F)\$ \Rightarrow C(id)\$$$

The top of stack will be id and the next input symbol will be either \$, or * or)

$$Follow(F) = \{ *,), \$ \}$$

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SLR(1): Simple LR(1) Parsing

$$S' \rightarrow T$$
 $T \rightarrow F \mid T * F \mid C (T)$
 $F \rightarrow id \mid id ++ \mid (T)$
 $C \rightarrow id$

What can the next symbol be when we reduce $C \rightarrow id$?

$$S'\$ \Rightarrow T\$ \Rightarrow C(T)\$ \Rightarrow C(F)\$ \Rightarrow C(id) \Rightarrow id\underline{(id)}\$$$

$$Follow(C) = \{ (\}$$

SLR(1): Simple LR(1) Parsing

```
0: S' \to \bullet T
T \to \bullet F
T \to \bullet T * F
T \to \bullet C (T)
F \to \bullet id
F \to \bullet id ++
F \to \bullet (T)
C \to \bullet id
```

```
S' \rightarrow T
T \rightarrow F \mid T * F \mid C (T)
F \rightarrow id \mid id ++ \mid (T)
C \rightarrow id
```

1:
$$F \rightarrow id \bullet$$

$$F \rightarrow id \bullet ++$$

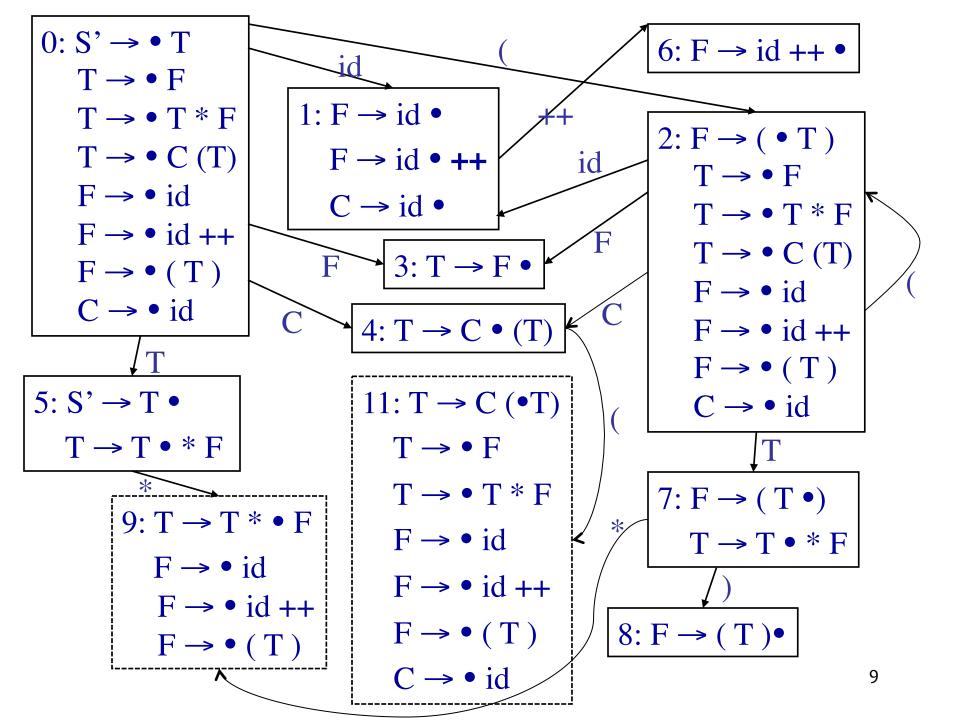
$$C \rightarrow id \bullet$$

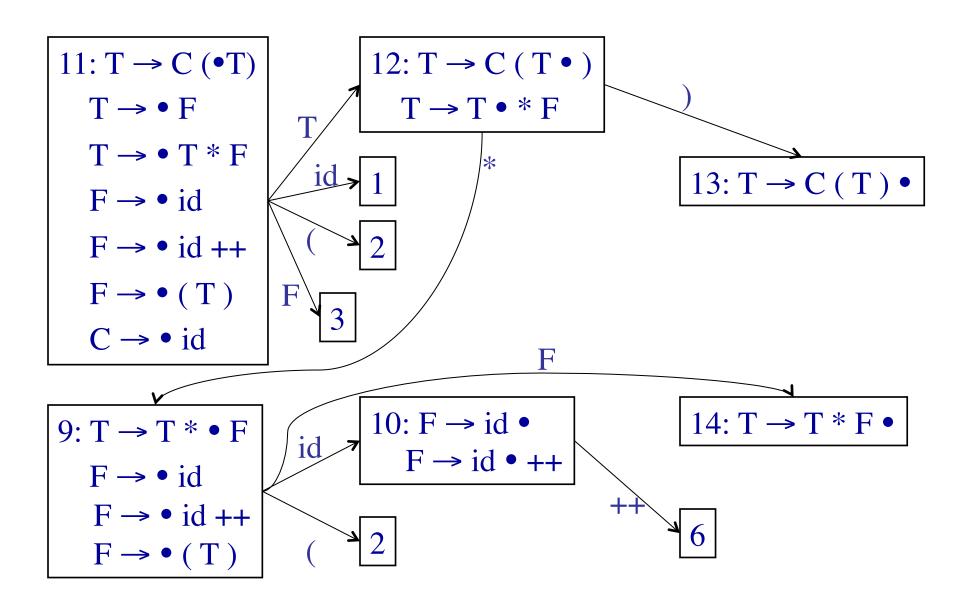
Follow(F) =
$$\{ *,), $ \}$$

Follow(C) = $\{ (\}$

action[1,*]= action[1,*] = action[1,\$] = Reduce
$$F \rightarrow id$$

action[1,(] = Reduce $C \rightarrow id$
action[1,++] = Shift



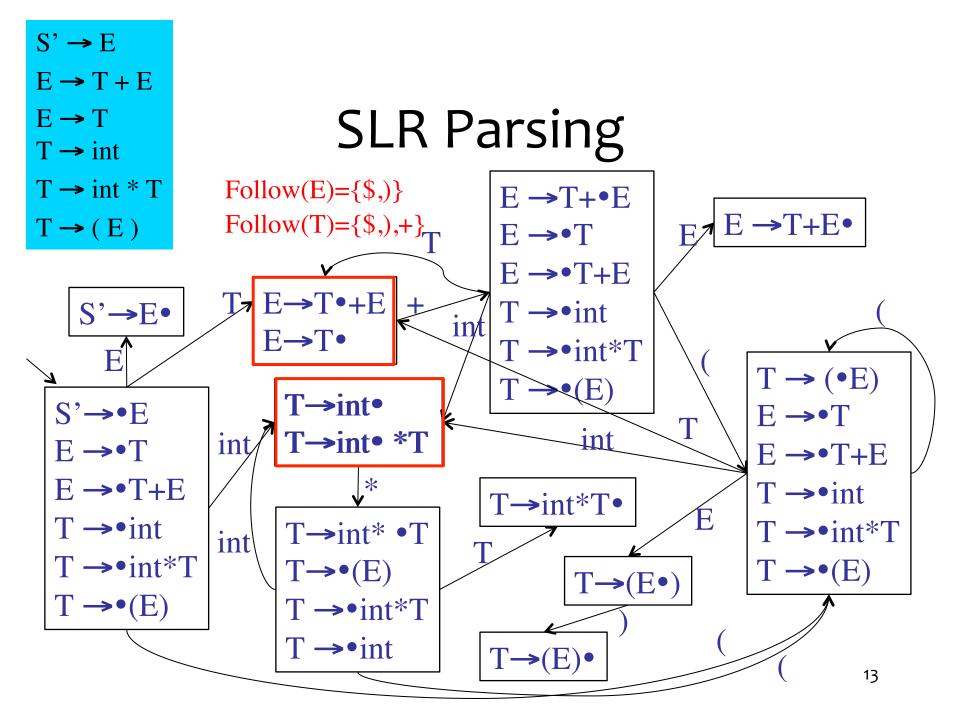


	Productions			
1	$T \rightarrow F$			
2	T → T*F			
3	$T \rightarrow C(T)$			
4	$F \rightarrow id$			
5	F → id ++			
6	$\mathbf{F} \rightarrow (\mathbf{T})$			
7	$C \rightarrow id$			

	*	()	id	++	\$	T	F	С
0		S2		S 1			5	3	4
1	R4	R7	R4		S2	R4			
2		S2		S 1			7	3	4
3	R1		R1			R1			
4		S 11							
5	S9					A			
6	R5		R5			R5			
7	S9		S8						
8	R6		R6			R6			
9		S2		S10				14	
10	R4		R4		S6	R4			
11		S2		S1			12	3	
12	S 9		S13						
13	R3		R3			R3			
14	R2		R2			R2			

SLR Parsing

- Assume:
 - Stack contains α and next input is t
 - DFA on input α terminates in state s
- Reduce by $X \rightarrow \beta$ if
 - s contains item X → β •
 - $-t \in Follow(X)$
- Shift if
 - s contains item X→ β tω
 - If $X \rightarrow \beta$ is in s then t cannot be in Follow(X)

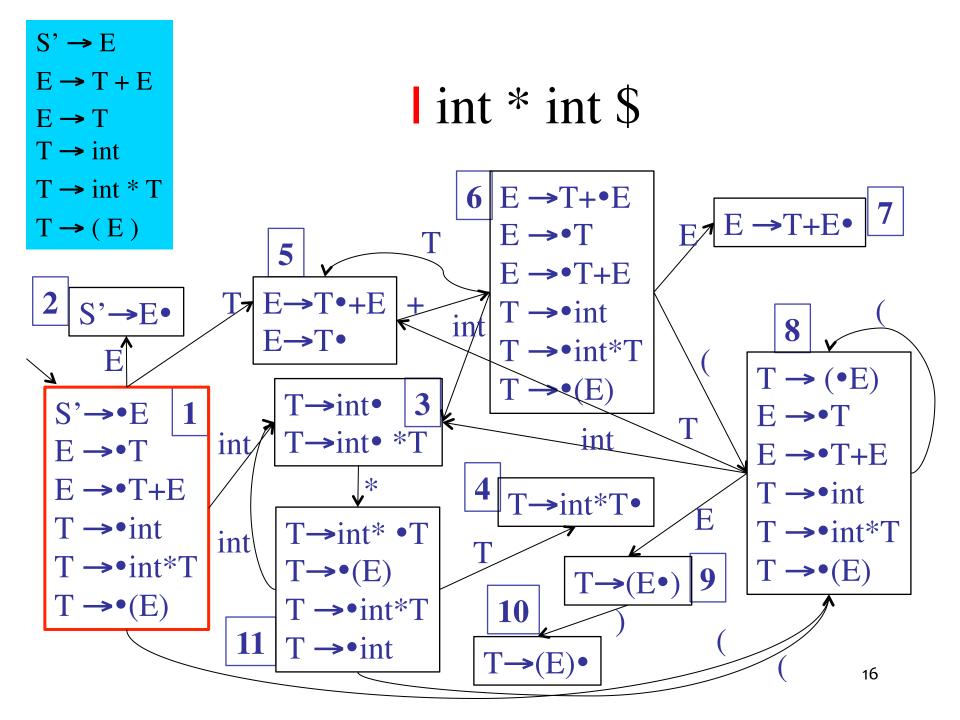


SLR Parsing

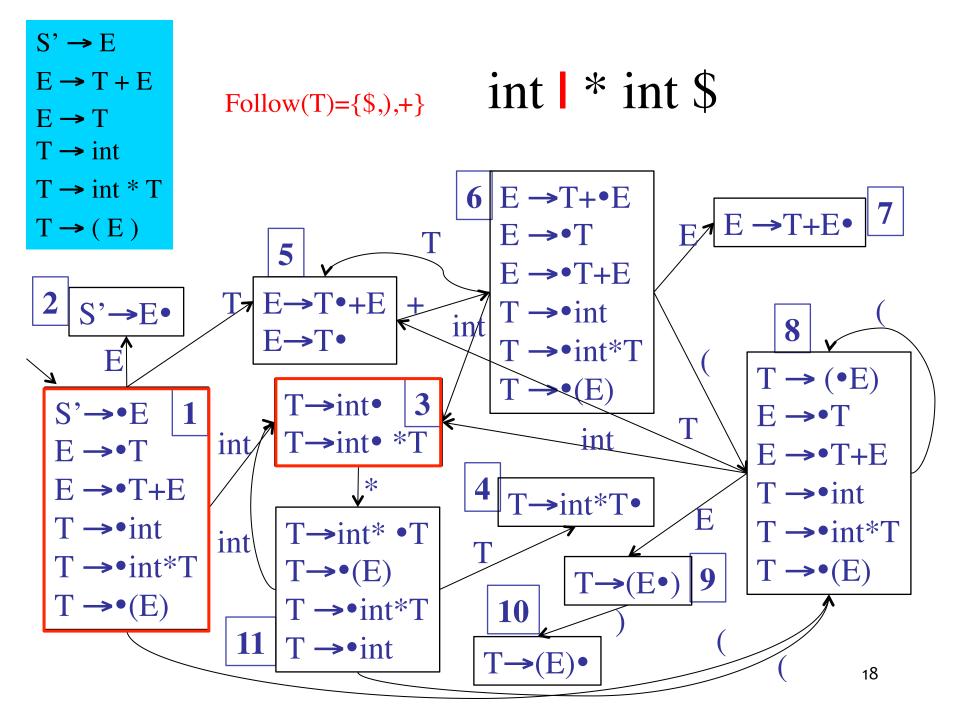
- Let M be DFA for viable prefixes of G
- Let $|x_1...x_n|$ \$ be initial configuration
- Repeat until configuration is S \$
 - Let $\alpha \mid \omega$ be current configuration
 - Run M on current stack α
 - If M rejects α , report parsing error
 - Stack α is not a viable prefix
 - If M accepts α with items I, let a be the next input
 - Shift $[X \rightarrow \beta \bullet a \gamma] \in I$
 - Reduce if $[X \to \beta \bullet] \in I$ and $a \in Follow(X)$
 - Report parsing error if neither applies

If there is any conflict in the last step (more than two valid action), grammar is not SLR(k) in practice k=1

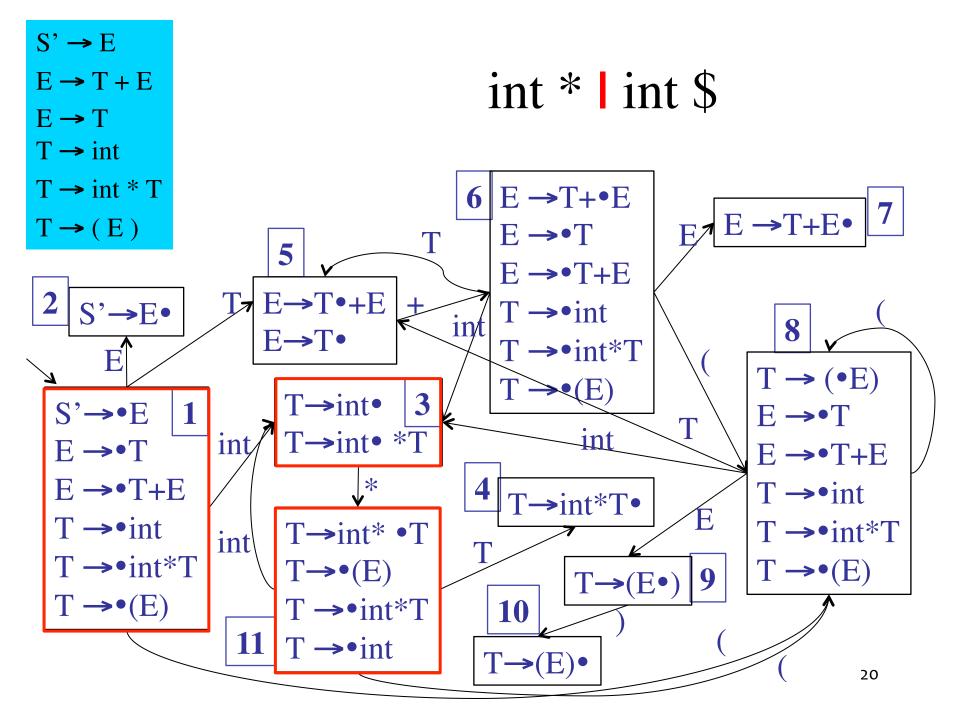
configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$		



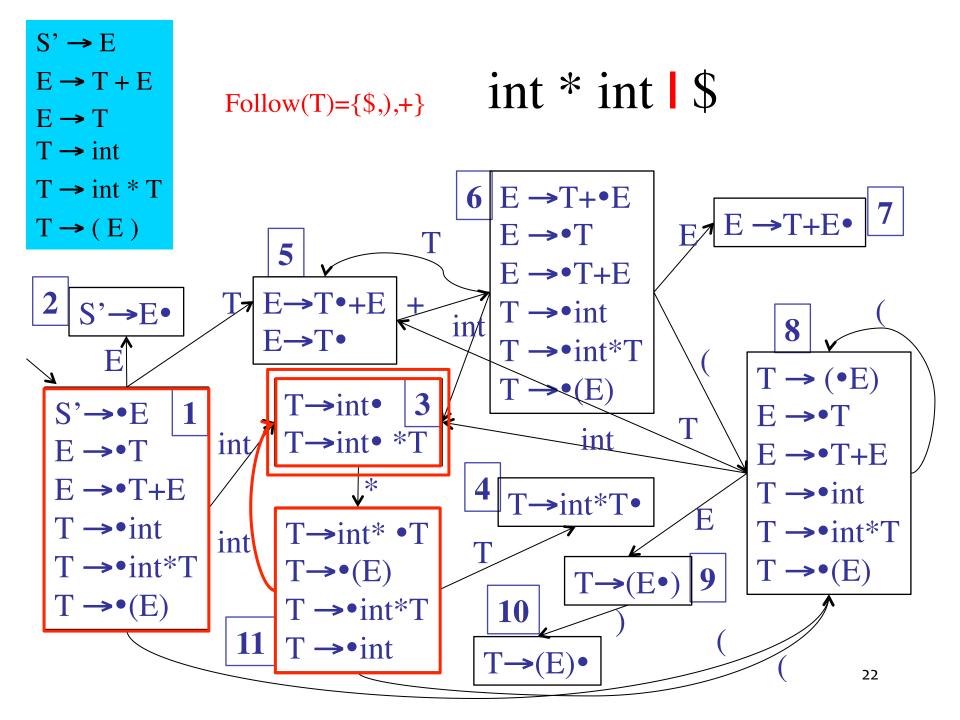
configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int * int \$		



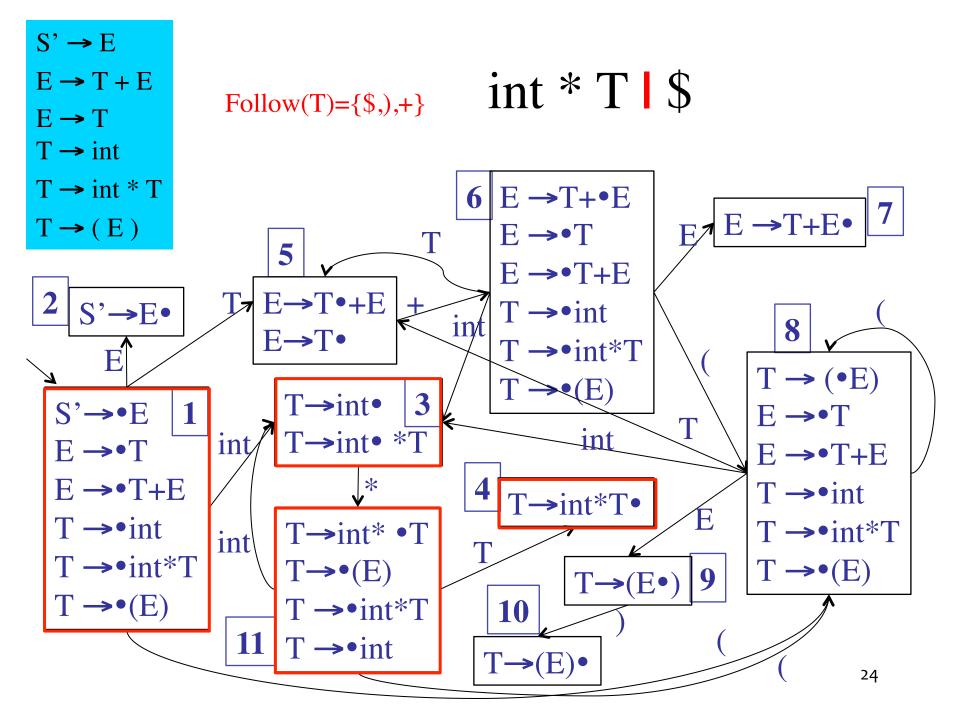
configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int * int \$	3 * ∉ Follow(T)	Shift
int * int \$		



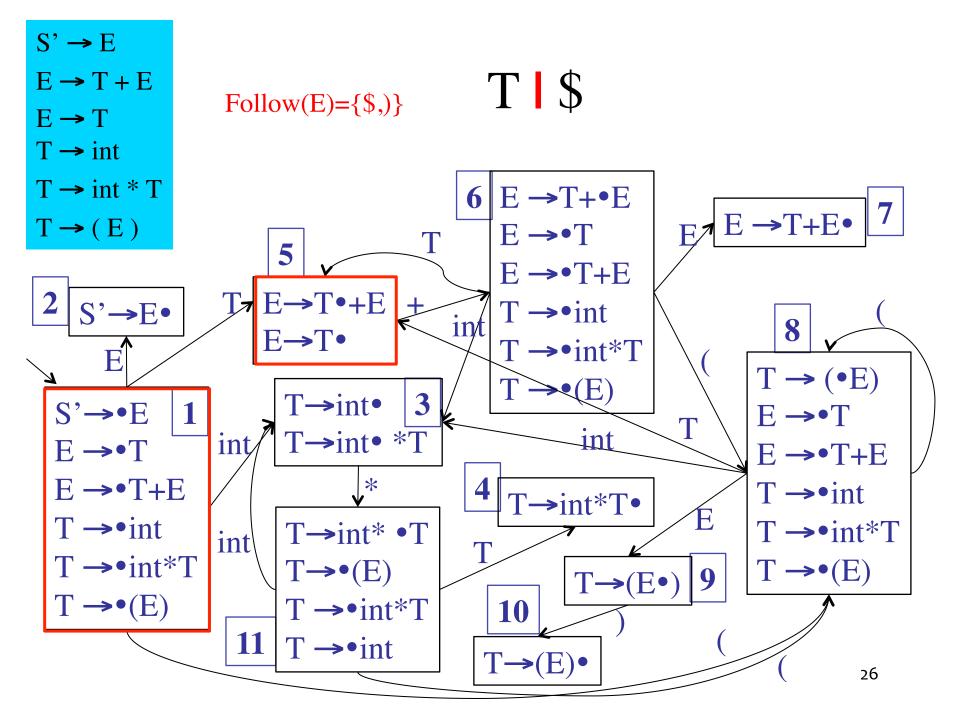
configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int * int \$	3 * ∉ Follow(T)	Shift
int * int \$	11	Shift
int * int \$		



configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int * int \$	$3 * \notin Follow(T)$	Shift
int * int \$	11	Shift
int * int \$	$3 \$ \in \text{Follow}(T)$	Reduce $T \rightarrow int$
int * T \$		

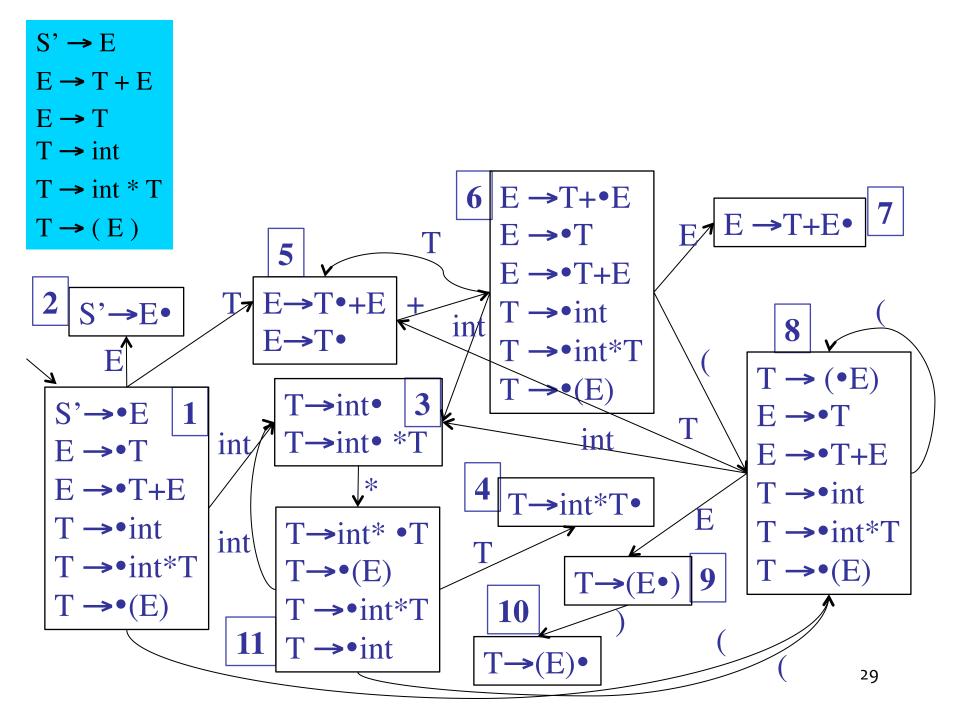


configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int * int \$	3 * ∉ Follow(T)	Shift
int * int \$	11	Shift
int * int \$	$3 \$ \in \text{Follow}(T)$	Reduce $T \rightarrow int$
int * T \$	$4 \qquad \$ \in Follow(T)$	Reduce $T \rightarrow int * T$
T \$		



configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int * int \$	3 * ∉ Follow(T)	Shift
int * int \$	11	Shift
int * int \$	$3 \$ \in \text{Follow}(T)$	Reduce $T \rightarrow int$
int * T \$	$4 \qquad \$ \in Follow(T)$	Reduce $T \rightarrow int * T$
T \$	$5 \$ \in Follow(E)$	Reduce E→T
EI\$		

configuration	DFA halt state	Action
(Stacklinput)		
l int * int \$	1	Shift
int I * int \$	3 * ∉ Follow(T)	Shift
int * int \$	11	Shift
int * int \$	$3 \$ \in \text{Follow}(T)$	Reduce $T \rightarrow int$
int * T \$	$4 \qquad \$ \in Follow(T)$	Reduce $T \rightarrow int * T$
TI\$	$5 \$ \in Follow(T)$	Reduce E→T
EI\$		Accept



Constructing SLR states

- Begin with item S'→•S, calculate related items (closure)
- Determine following states: what states can be reached on a single input token or non-terminal (GOTO)
- Construct closure of each resulting states

SLR(1) Construction

```
    Construct F = {I₀, I₁, ... Iո}
    a) if {A → α•} ∈ Iᵢ and A!= S'
        then action[i, b] := reduce A → α
        for all b ∈ Follow(A)
    b) if {S' → S•} ∈ Iᵢ
        then action[i, $] := accept
    c) if {A → α•aβ} ∈ Iᵢ and Successor(Iᵢ, a) = Iᵢ
        then action[i, a] := shift j
    if Successor(Iᵢ, A) = Iᵢ then goto[i, A] := j
```

SLR(1) Construction (cont'd)

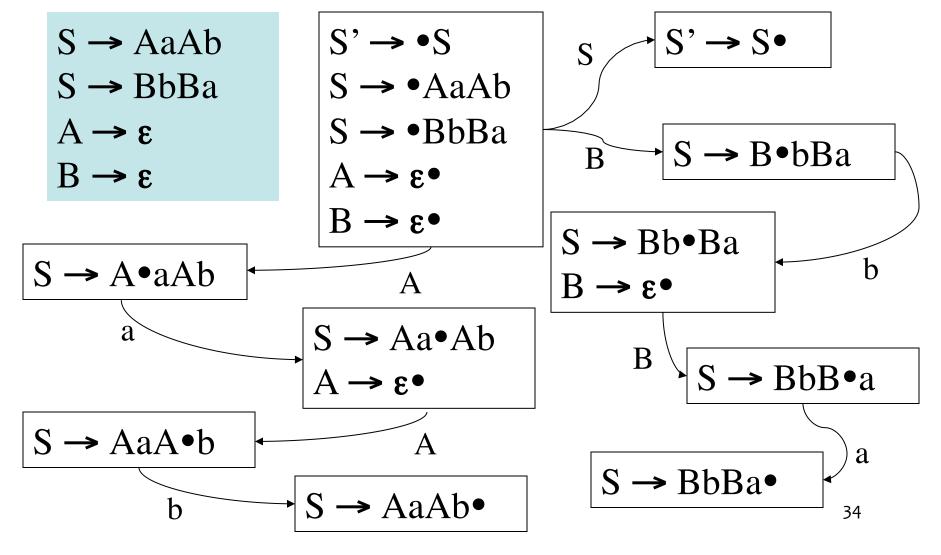
- 4. All entries not defined are errors
- 5. Make sure I_0 is the initial state
- Note: SLR(1) only reduces
 {A → α•} if lookahead in Follow(A)
- Shift and reduce items or more than one reduce item can be in the same configuration set as long as lookaheads are disjoint

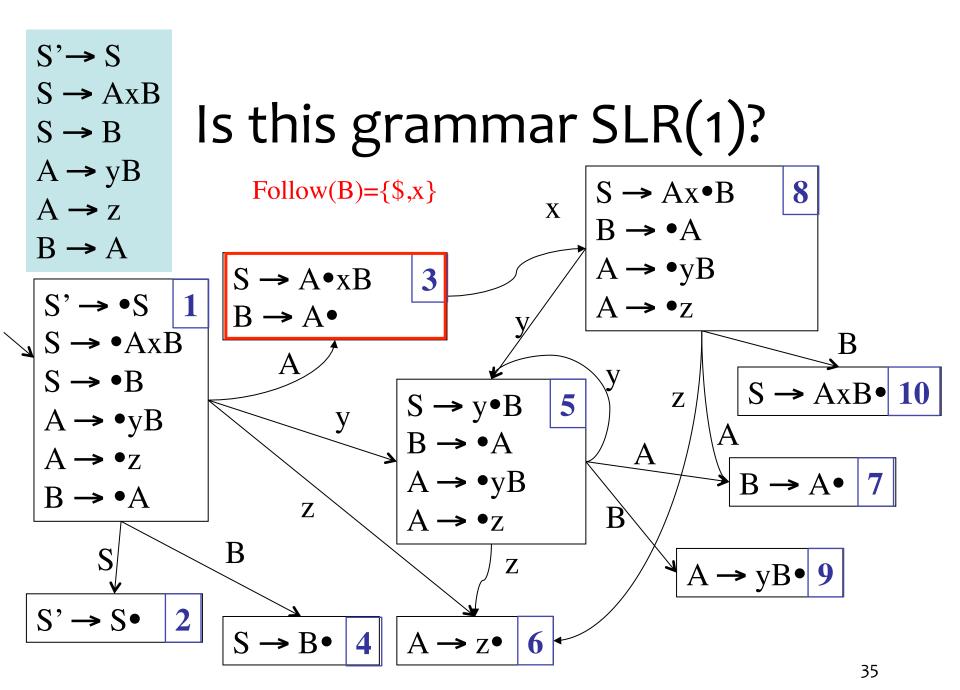
SLR(1) Conditions

- A grammar is SLR(1) if for each configuration set:
 - For any item {A → α •xβ: x ∈ T} there is no {B → γ •: x ∈ Follow(B)}
 - For any two items {A → α •} and {B → β •} Follow(A) ∩ Follow(B) = Ø

LR(o) Grammars \subseteq SLR(1) Grammars

Is this grammar SLR(1)?





- 1) $S \rightarrow AxB$
- 2) $S \rightarrow B$
- $3) A \rightarrow yB$
- $4) A \rightarrow z$
- 5) $B \rightarrow A$

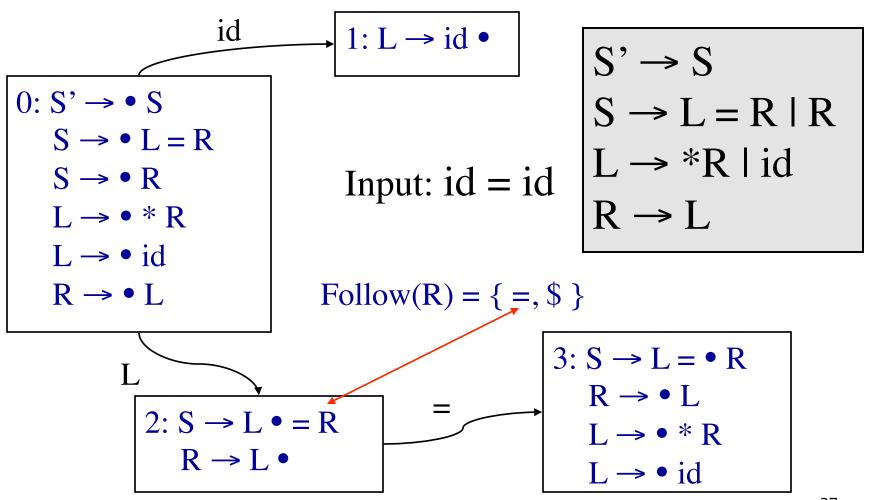
Grammar is not SLR

Reduce is a bad choice

SLR Parsing Table

	X	y	Z	\$	S	A	В
1		S5	S 6		2	3	4
2				ACC!			
3	S8,R5			R5			
4				R2			
5		S5	S 6			7	9
6	R4			R4			
7	R5			R5			
8		S5	S 6			7	10
9	R3			R3			
10				R1			

SLR limitation: lack of context



$$S' \rightarrow S$$

 $S \rightarrow L = R \mid R$
 $L \rightarrow *R \mid id$
 $R \rightarrow L$

S'

R

id

\$

id

$$Follow(R) = \{ =, \$ \}$$

2:
$$S \rightarrow L \bullet = R$$

 $R \rightarrow L \bullet$

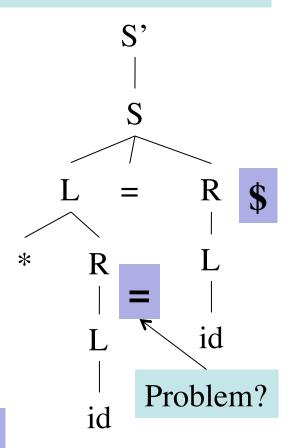
R

id

\$

S'

Find all lookaheads for reduce $R \rightarrow L$ •



No! $R \rightarrow L \bullet$ reduce and $S \rightarrow L \bullet = R$ do not co-occur due to the $L \rightarrow *R$ rule

Solution: Canonical LR(1)

- Extend definition of configuration
 - Remember lookahead
- New closure method
- Extend definition of Successor

LR(1) Parsing

- Limit introduced by SLR parsing in using Follow set to decide reductions
- Idea: augment LR items with 1 character lookahead [B → A•, \$] making an LR(1) item
 - Reduce to B only if lookahead token is \$
- More accurate than just Follow set
- Similar to SLR parsing just use LR(1) items rather than LR(0) items