

# Top-down Parsing

CMPT 379: Compilers

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# Parsing - Roadmap

- Parser:
  - decision procedure: builds a parse tree
- Top-down vs. bottom-up
- LL(1) – Deterministic Parsing
  - recursive-descent
  - table-driven
- LR(k) – Deterministic Parsing
  - LR(0), SLR(1), LR(1), LALR(1)
- Parsing arbitrary CFGs – Polynomial time parsing

# Top-Down vs. Bottom Up

Grammar:  $S \rightarrow A B$

Input String: ccbca

$A \rightarrow c \mid \varepsilon$

$B \rightarrow cbB \mid ca$

Top-Down/leftmost		Bottom-Up/rightmost	
$S \Rightarrow AB$	$S \rightarrow AB$	$ccbca \Leftarrow Acbca$	$A \rightarrow c$
$\Rightarrow cB$	$A \rightarrow c$	$\Leftarrow AcbB$	$B \rightarrow ca$
$\Rightarrow ccbB$	$B \rightarrow cbB$	$\Leftarrow AB$	$B \rightarrow cbB$
$\Rightarrow ccbca$	$B \rightarrow ca$	$\Leftarrow S$	$S \rightarrow AB$

# Leftmost derivation for **id + id \* id**

**$E \rightarrow E + E$**

**$E \rightarrow E * E$**

**$E \rightarrow ( E )$**

**$E \rightarrow - E$**

**$E \rightarrow \text{id}$**

$E \Rightarrow E + E$

$\Rightarrow \text{id} + E$

$\Rightarrow \text{id} + E * E$

$\Rightarrow \text{id} + \text{id} * E$

$\Rightarrow \text{id} + \text{id} * \text{id}$

$E \Rightarrow_{\text{lm}}^* \text{id} + E * E$

# Predictive Top-Down Parser

- Knows which production to choose based on single lookahead symbol
- Need LL(1) grammars
  - First L: reads input Left to right
  - Second L: produce Leftmost derivation
  - 1: one symbol of lookahead
- Cannot have left-recursion
- Must be left-factored (no left-factors)
- Not all grammars can be made LL(1)

# LL(1) Parser

- In recursive-descent
  - for each non-terminal and input token, many choices of production to use
  - Backtracking to remove bad choices
- In LL(1)
  - for each non-terminal and each token, only one production

$S \rightarrow^* \omega A \beta$  and next input token:  $t$

$A \rightarrow \alpha$  is the only production

$\omega \alpha \beta$

# Left Factoring

- Consider this grammar
  - $E \rightarrow T + E \mid T$
  - $T \rightarrow id \mid id * T \mid ( E )$
- Hard to predict because
  - For  $T$  two productions start with  $id$
  - For  $E$  it is not clear how to predict
- The grammar should be left-factored
  - Remove common prefixes from multiple productions for each non-terminal

# Left Factoring

- In general, for rules

$$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \dots \mid \alpha\beta_n \mid \gamma$$

- Left factoring is achieved by the following grammar transformation:

$$A \rightarrow \alpha A' \mid \gamma$$

$$A' \rightarrow \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$$



# Left Factoring

- Recall the grammar
  - $E \rightarrow T + E \mid T$
  - $T \rightarrow \text{id} \mid \text{id} * T \mid ( E )$
- Factor out common prefixes for productions
  - $E \rightarrow T X$
  - $X \rightarrow + E \mid \varepsilon$
  - $T \rightarrow \text{id} Y \mid ( E )$
  - $Y \rightarrow * T \mid \varepsilon$

# Predictive Parsing Table

- Can be specified via 2D tables
  - One dimension for current (leftmost) non-terminal to expand
  - One dimension for next token
  - Each table entry contains one production

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow \text{id } Y$
6	$Y \rightarrow * T$
7	$Y \rightarrow \epsilon$

	+	*	(	)	id	\$
E			$T X$		$T X$	
X	$+ E$			$\epsilon$		$\epsilon$
T			$( E )$		$\text{id } Y$	
Y	$\epsilon$	$* T$		$\epsilon$		$\epsilon$

# Predictive Parsing Table

- Consider  $[E, id]$  entry
  - When current non-terminal is  $E$  and the next input is  $id$ , use production  $E \rightarrow T X$

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow id Y$
6	$Y \rightarrow * T$
7	$Y \rightarrow \epsilon$

	+	*	(	)	id	\$
E			$T X$		$T X$	
X	$+ E$			$\epsilon$		$\epsilon$
T			$( E )$		$id Y$	
Y	$\epsilon$	$* T$		$\epsilon$		$\epsilon$

# Predictive Parsing Table

- Consider  $[Y, +]$  entry
  - When current non-terminal is  $Y$  and the next input is  $+$ , get rid of  $Y$
  - $Y$  can be followed by  $+$  only if  $Y \rightarrow \epsilon$

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow \text{id } Y$
6	$Y \rightarrow * T$
7	$Y \rightarrow \epsilon$

	$+$	$*$	$($	$)$	id	$\$$
E			$T X$		$T X$	
X	$+ E$			$\epsilon$		$\epsilon$
T			$( E )$		$\text{id } Y$	
Y	$\epsilon$	$* T$		$\epsilon$		$\epsilon$

# Predictive Parsing Table

- Blank entries indicate error situations
- Consider  $[E, *]$  entry
  - There is no way to derive a string starting with  $*$  from non-terminal  $E$

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow \text{id } Y$
6	$Y \rightarrow * T$
7	$Y \rightarrow \epsilon$

	+	*	(	)	id	\$
E			$T X$		$T X$	
X	$+ E$			$\epsilon$		$\epsilon$
T			$( E )$		$\text{id } Y$	
Y	$\epsilon$	$* T$		$\epsilon$		$\epsilon$

# Predictive Parsing

- Method similar to recursive descent, except
  - For each non-terminal  $S$
  - We look at the next token  $a$
  - And chose the production shown at entry  $[S,a]$
- We use a stack to keep track of pending non-terminals (frontier of parse tree)
- We reject when we encounter an error state
- We accept when we encounter end-of-input and empty stack

# Table-Driven Parsing

```
stack.push($); stack.push(S);  
a = input.read();
```

```
forever do begin
```

```
    X = stack.peek();
```

```
    if X = a and a = $ then return SUCCESS;
```

```
    elseif X = a and a != $ then
```

```
        stack.pop(X); a = input.read();
```

```
    elseif X != a and  $X \in N$  and  $M[X, a]$  not empty then
```

```
        stack.pop(X);
```

```
        stack.push( $M[X, a]$ ); /*  $M[X, a] = Y_1 \dots Y_n$  */  
        else ERROR!
```

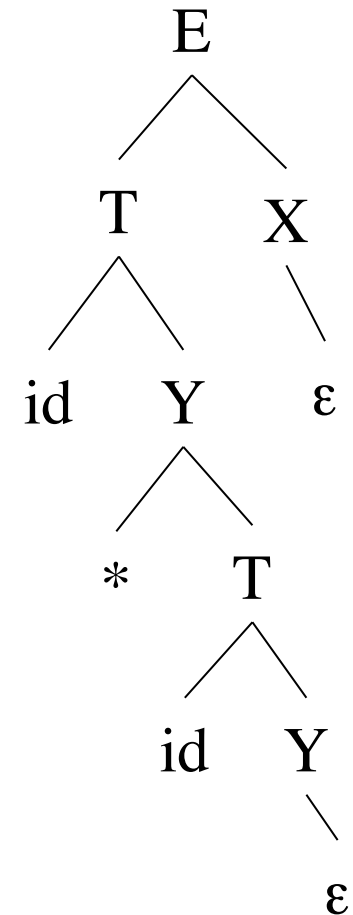
```
end
```

**Stack: to keep track  
of pending non-terminals  
in the derivation  
(leaves in parse tree)**

# Trace “id\*id”

	+	*	(	)	id	\$
E			<b>T X</b>		<b>T X</b>	
X	<b>+ E</b>			$\epsilon$		$\epsilon$
T			<b>( E )</b>		<b>id Y</b>	
Y	$\epsilon$	<b>* T</b>		$\epsilon$		$\epsilon$

Stack	Input	Action
E \$	id*id\$	<b>T X</b>
T X \$	id*id\$	<b>id Y</b>
id Y X \$	id*id\$	<b>terminal</b>
Y X \$	*id\$	<b>* T</b>
* T X \$	*id\$	<b>terminal</b>
T X \$	id\$	<b>id Y</b>
id Y X \$	id\$	<b>terminal</b>
Y X \$	\$	$\epsilon$
X \$	\$	$\epsilon$
\$	\$	<b>Accept!</b>





# Predictive Parsing table

- Given a grammar produce the predictive parsing table
- We need to know for all rules  $A \rightarrow \alpha \mid \beta$  the lookahead symbol
- Based on the lookahead symbol the table can be used to pick which rule to push onto the stack
- This can be done using two sets: FIRST and FOLLOW

# Predictive Parsing Table

- For Nonterminal  $A$ , rule  $A \rightarrow \alpha$ , and the token  $t$ ,  $M[A, t] = \alpha$  in two cases:
  - If  $\alpha \Rightarrow^* t \beta$ 
    - $\alpha$  can derive a  $t$  in the first position
    - We say that  $t \in \text{First}(\alpha)$
  - $A \rightarrow \alpha$  and  $\alpha \Rightarrow^* \varepsilon$  and  $S \Rightarrow^* \beta A t \delta$ 
    - Useful if stack has  $A$ , input is  $t$  and  $A$  cannot derive  $t$
    - In this case only option is to get rid of  $A$  (by  $\alpha \Rightarrow^* \varepsilon$ )
      - Can work only if  $t$  can follow  $A$  in at least on derivation
    - We say  $t \in \text{Follow}(A)$

# FIRST and FOLLOW

$a \in \text{FIRST}(\alpha)$  if  $\alpha \Rightarrow^* a\beta$

if  $\alpha \Rightarrow^* \epsilon$  then  $\epsilon \in \text{FIRST}(\alpha)$

$a \in \text{FOLLOW}(A)$  if  $S \Rightarrow^* \alpha A a \beta$

$a \in \text{FOLLOW}(A)$  if  $S \Rightarrow^* \alpha A \gamma a \beta$

and  $\gamma \Rightarrow^* \epsilon$

# Conditions for LL(1)

- Necessary conditions:
  - no ambiguity
  - no left recursion
  - Left factored grammar
- A grammar  $G$  is LL(1) if - whenever
$$A \rightarrow \alpha \mid \beta$$
  1.  $\text{First}(\alpha) \cap \text{First}(\beta) = \emptyset$
  2.  $\alpha \Rightarrow^* \epsilon$  implies  $\neg(\beta \Rightarrow^* \epsilon)$
  3.  $\alpha \Rightarrow^* \epsilon$  implies  $\text{First}(\beta) \cap \text{Follow}(A) = \emptyset$

# ComputeFirst( $\alpha$ : string of symbols)

```
// assume  $\alpha = X_1 X_2 X_3 \dots X_n$ 
if  $X_1 \in T$  then First[ $\alpha$ ] := { $X_1$ }
else begin
   $i := 1$ ; First[ $\alpha$ ] := ComputeFirst( $X_1$ ) \ { $\epsilon$ };
  while  $X_i \Rightarrow^* \epsilon$  do begin
    if  $i < n$  then
      First[ $\alpha$ ] := First[ $\alpha$ ]  $\cup$  ComputeFirst( $X_{i+1}$ ) \ { $\epsilon$ };
    else
      First[ $\alpha$ ] := First[ $\alpha$ ]  $\cup$  { $\epsilon$ };
     $i := i + 1$ ;
  end
end
```

Recursion in computing FIRST  
causes problems when faced with  
recursive grammar rules

# ComputeFirst; modified

```
foreach  $X \in T$  do First[X] := {X};  
foreach  $p \in P : X \rightarrow \epsilon$  do First[X] := { $\epsilon$ };  
repeat foreach  $X \in N, p : X \rightarrow Y_1 Y_2 Y_3 \dots Y_n$  do  
  begin  $i := 1$ ;  
    while  $Y_i \Rightarrow^* \epsilon$  and  $i \leq n$  do begin  
      First[X] := First[X]  $\cup$  First[ $Y_i$ ] \ { $\epsilon$ };  
       $i := i + 1$ ;  
    end  
    if  $i = n + 1$  then First[X] := First[X]  $\cup$  { $\epsilon$ };  
until no change in First[X] for any X;
```

# ComputeFirst; modified

```
foreach  $X \in T$  do First[X] := X;  
foreach  $p \in P : X \rightarrow \epsilon$  do First[X] := { $\epsilon$ };  
repeat foreach  $X \in N, p : X \rightarrow Y_1 Y_2 Y_3 \dots Y_n$  do  
  begin  $i := 1$ ;  
    while  $Y_i \Rightarrow^*$  do  
      First[X] := F  
       $i := i + 1$ ;  
    end  
  if  $i = n + 1$  then First[X] := First[X]  $\cup \{\epsilon\}$ ;  
until no change in First[X] for any X;
```

Non-recursive FIRST computation  
works with left-recursive grammars.  
Computes a fixed point for FIRST[X]  
for all non-terminals X in the grammar.  
But this algorithm is very inefficient.

# First Sets

$\text{First}(+) = \{+\}$

$\text{First}(\ast) = \{\ast\}$

$\text{First}(\text{'('}) = \{\text{'('}\}$

$\text{First}(\text{'('}) = \{\text{'('}\}$

$\text{First}(\text{id}) = \{\text{id}\}$

$\text{First}(E) = ?$

$\text{First}(T) \subseteq \text{First}(E)$

$\text{First}(T) = \{\text{id}, \text{'('}\}$

$\text{First}(E) = \{\text{id}, \text{'('}\}$

$\text{First}(X) = \{+, \epsilon\}$

$\text{First}(Y) = \{\ast, \epsilon\}$

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow \text{id } Y$
6	$Y \rightarrow \ast T$
7	$Y \rightarrow \epsilon$



# Follow Sets

- Algorithm sketch
  1. Add  $\$$  to  $\text{Follow}(S)$
  2. For each production  $A \rightarrow \alpha X \beta$ 
    - Add  $\text{First}(\beta) - \{\epsilon\}$  to  $\text{Follow}(X)$
  3. For each  $A \rightarrow \alpha X \beta$  where  $\epsilon \in \text{First}(\beta)$ 
    - Add  $\text{Follow}(A)$  to  $\text{Follow}(X)$
- Repeat steps 2-3 until no follow set grows

# ComputeFollow

```
Follow(S) := {$};  
repeat  
  foreach  $p \in P$  do  
    case  $p = A \rightarrow \alpha B \beta$  begin  
      Follow[B] := Follow[B]  $\cup$  ComputeFirst( $\beta$ ) \  $\{\epsilon\}$ ;  
      if  $\epsilon \in \text{First}(\beta)$  then  
        Follow[B] := Follow[B]  $\cup$  Follow[A];  
      end  
    case  $p = A \rightarrow \alpha B$   
      Follow[B] := Follow[B]  $\cup$  Follow[A];  
until no change in any Follow[N]
```

# Follow Sets. Example

$\text{Follow}(E) \subseteq \text{Follow}(X)$   
 $\text{Follow}(X) \subseteq \text{Follow}(E)$   
 $\text{First}(X) - \{\epsilon\} \subseteq \text{Follow}(T)$   
 $\text{Follow}(E) \subseteq \text{Follow}(T)$   
 $\text{Follow}(Y) \subseteq \text{Follow}(T)$   
 $\text{Follow}(T) \subseteq \text{Follow}(Y)$

$\text{Follow}(E) = \{\$, )\}$   
 $\text{Follow}(X) = \{\$, )\}$   
 $\text{Follow}(T) = \{+, \$, )\}$   
 $\text{Follow}(Y) = \{+, \$, )\}$   
 $\text{Follow}('(') = \{ (, \text{id} \}$   
 $\text{Follow}(')') = \{+, \$, )\}$   
 $\text{Follow}(+) = \{ (, \text{id} \}$   
 $\text{Follow}(*) = \{ (, \text{id} \}$   
 $\text{Follow}(\text{id}) = \{*, +, \$, )\}$

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow \text{id } Y$
6	$Y \rightarrow * T$
7	$Y \rightarrow \epsilon$

# Building the Parse Table

- Compute First and Follow sets
- For each production  $A \rightarrow \alpha$ 
  - For each  $t \in \text{First}(\alpha)$ 
    - $M[A, t] = \alpha$
  - If  $\epsilon \in \text{First}(\alpha)$ , for each  $t \in \text{Follow}(A)$ 
    - $M[A, t] = \alpha$
  - If  $\epsilon \in \text{First}(\alpha)$  and  $\$ \in \text{Follow}(\alpha)$ 
    - $M[A, \$] = \alpha$
  - All undefined entries are errors

# Predictive Parsing Table

$\text{First}(T) = \{\text{id}, '('\}$   
 $\text{First}(X) = \{+, \epsilon\}$   
 $\text{First}(Y) = \{*, \epsilon\}$   
 $\text{First}(E) = \{\text{id}, '('\}$

$\text{Follow}(E) = \{\$, )\}$   
 $\text{Follow}(X) = \{\$, )\}$   
 $\text{Follow}(T) = \{+, \$, )\}$   
 $\text{Follow}(Y) = \{+, \$, )\}$

Productions	
1	$E \rightarrow T X$
2	$X \rightarrow \epsilon$
3	$X \rightarrow + E$
4	$T \rightarrow ( E )$
5	$T \rightarrow \text{id } Y$
6	$Y \rightarrow * T$
7	$Y \rightarrow \epsilon$

	+	*	(	)	id	\$
E			<b>T X</b>		<b>T X</b>	
X	<b>+ E</b>			<b><math>\epsilon</math></b>		<b><math>\epsilon</math></b>
T			<b>( E )</b>		<b>id Y</b>	
Y	<b><math>\epsilon</math></b>	<b>* T</b>		<b><math>\epsilon</math></b>		<b><math>\epsilon</math></b>

# Example First/Follow

$$S \rightarrow AB$$

$$A \rightarrow c \mid \varepsilon$$

Not an LL(1) grammar

$$B \rightarrow cbB \mid ca$$

$$\text{First}(A) = \{c, \varepsilon\}$$

$$\text{Follow}(A) = \{c\}$$

$$\text{First}(B) = \{c\}$$

$$\text{Follow}(A) \cap$$

$$\text{First}(cbB) =$$

$$\text{First}(c) = \{c\}$$

$$\text{First}(ca) = \{c\}$$

$$\text{Follow}(B) = \{\$ \}$$

$$\text{First}(S) = \{c\}$$

$$\text{Follow}(S) = \{\$ \}$$

# Converting to LL(1)

$$S \rightarrow AB$$

$$A \rightarrow c \mid \varepsilon$$

$$B \rightarrow cbB \mid ca$$

Note that grammar  
is regular:  $c? (cb)^* ca$

$c (c b c b \dots c b) c a$   
 $(c b c b \dots c b) c a$



$c c (b c b \dots c b c) a$   
 $c (b c b \dots c b c) a$

same as:

$c c? (bc)^* a$

$$S \rightarrow cAa$$

$$A \rightarrow cB \mid B$$

$$B \rightarrow bcB \mid \varepsilon$$

# Verifying LL(1) using F/F sets

$$S \rightarrow cAa$$

$$A \rightarrow cB \mid B$$

$$B \rightarrow bcB \mid \varepsilon$$

$$\text{First}(A) = \{b, c, \varepsilon\}$$

$$\text{Follow}(A) = \{a\}$$

$$\text{First}(B) = \{b, \varepsilon\}$$

$$\text{Follow}(B) = \{a\}$$

$$\text{First}(S) = \{c\}$$

$$\text{Follow}(S) = \{\$ \}$$



# Building the Parse Table

- Compute First and Follow sets
- For each production  $A \rightarrow \alpha$ 
  - foreach  $a \in \text{First}(\alpha)$  add  $A \rightarrow \alpha$  to  $M[A,a]$
  - If  $\epsilon \in \text{First}(\alpha)$  add  $A \rightarrow \alpha$  to  $M[A,b]$  for each  $b$  in  $\text{Follow}(A)$
  - If  $\epsilon \in \text{First}(\alpha)$  add  $A \rightarrow \alpha$  to  $M[A,\$]$  if  $\$ \in \text{Follow}(\alpha)$
  - All undefined entries are errors

# Predictive Parsing Table

Productions	
1	$T \rightarrow F T'$
2	$T' \rightarrow \epsilon$
3	$T' \rightarrow * F T'$
4	$F \rightarrow \text{id}$
5	$F \rightarrow ( T )$

$\text{FIRST}(T) = \{\text{id}, ( \}$   
 $\text{FIRST}(T') = \{*, \epsilon\}$   
 $\text{FIRST}(F) = \{\text{id}, ( \}$

$\text{FOLLOW}(T) = \{\$, )\}$   
 $\text{FOLLOW}(T') = \{\$, )\}$   
 $\text{FOLLOW}(F) = \{*, \$, )\}$

	*	(	)	id	\$
T		$T \rightarrow F T'$		$T \rightarrow F T'$	
T'	$T' \rightarrow * F T'$		$T' \rightarrow \epsilon$		$T' \rightarrow \epsilon$
F		$F \rightarrow ( T )$		$F \rightarrow \text{id}$	

# Revisit conditions for LL(1)

- A grammar  $G$  is LL(1) iff - whenever  $A \rightarrow \alpha \mid \beta$ 
  1.  $\text{First}(\alpha) \cap \text{First}(\beta) = \emptyset$
  2.  $\alpha \Rightarrow^* \varepsilon$  implies  $\neg(\beta \Rightarrow^* \varepsilon)$
  3.  $\alpha \Rightarrow^* \varepsilon$  implies  $\text{First}(\beta) \cap \text{Follow}(A) = \emptyset$
- No more than one entry per table field

# Error Handling

- Reporting & Recovery
  - Report as soon as possible
  - Suitable error messages
  - Resume after error
  - Avoid cascading errors
- Phrase-level vs. Panic-mode recovery

# Panic-Mode Recovery

- Skip tokens until *synchronizing set* is seen
  - Follow(A)
    - garbage or missing things after
  - Higher-level start symbols
  - First(A)
    - garbage before
  - Epsilon
    - if nullable
  - Pop/Insert terminal
    - “auto-insert”
- Add “synch” actions to table

# Summary so far

- LL(1) grammars, necessary conditions
  - No left recursion
  - Left-factored
- Not all languages can be generated by LL(1) grammar
- LL(1) – Parsing:  $O(n)$  time complexity
  - recursive-descent and table-driven predictive parsing
- LL(1) grammars can be parsed by simple predictive recursive-descent parser
  - Alternative: table-driven top-down parser

# Extra Slides

# ComputeFirst on Left-recursive Grammars

- ComputeFirst as defined earlier loops on left-recursive grammars
- Here is an alternative algorithm for ComputeFirst
  1. Compute non left-recursive cases of FIRST
  2. Create a graph of recursive cases where FIRST of a non-terminal depends on another non-terminal
  3. Compute Strongly Connected Components (SCC)
  4. Compute FIRST starting from root of SCC to avoid cycles



# ComputeFirst on Left-recursive Grammars

- Each Strongly Connected Component can have recursion
- But the connections between SCC means that (by defn) what we have now is a directed acyclic graph – hence without left recursion
- Unlike top-down LL parsing, bottom-up LR parsing allows left-recursive grammars, so this algorithm is useful for LR parsing

# ComputeFirst on Left-recursive Grammars

- $S \rightarrow BD \mid D$
- $D \rightarrow d \mid Sd$

$\text{FIRST}_0[A] := \{a\}$

$\text{FIRST}_0[C] := \{\}$

$\text{FIRST}_0[B] := \{b\}$

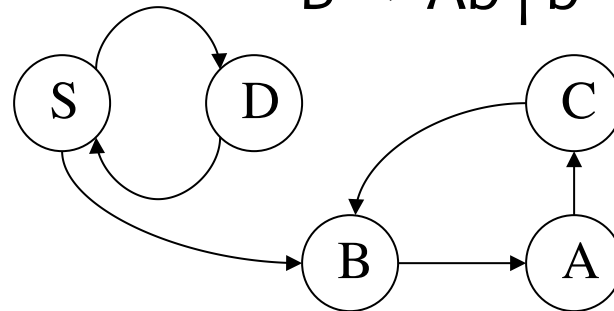
$\text{FIRST}_0[S] := \{b, d\}$

$\text{FIRST}_0[D] := \{d\}$

- $A \rightarrow CB \mid a$

- $C \rightarrow Bb \mid \varepsilon$

- $B \rightarrow Ab \mid b$



Compute  
Strongly  
Connected  
Components

2 SCCs: e.g. consider B-A-C

$\text{FIRST}[B] := \text{FIRST}_0[B] + \text{ComputeFirst}(A)$

$\text{FIRST}[A] := \text{FIRST}_0[A] + \text{ComputeFirst}(C)$

$\text{FIRST}[A] := \text{FIRST}[A] + \text{FIRST}_0[B]$

$\text{FIRST}[C] := \text{FIRST}_0[C] + \text{FIRST}_0[B]$

$\text{FIRST}[C] := \text{FIRST}[C] + \{\varepsilon\}$

# Examples

$S \rightarrow A B C$

$A \rightarrow a \mid \varepsilon$

$B \rightarrow b B \mid \varepsilon$

$C \rightarrow c \mid \varepsilon$

Is this LL(1)?

$S \rightarrow F$

$F \rightarrow A ( B ) \mid B A$

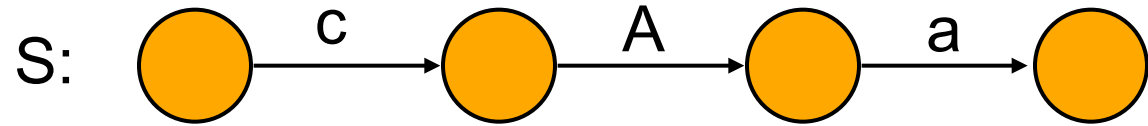
$A \rightarrow x \mid y$

$B \rightarrow a B \mid b B \mid \varepsilon$

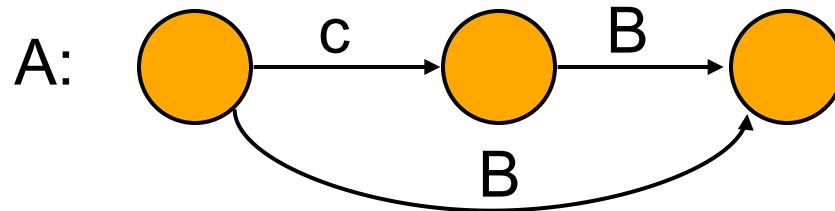
Is this LL(1)?

# Transition Diagram

$S \rightarrow cAa$



$A \rightarrow cB \mid B$



$B \rightarrow bcB \mid \epsilon$

