LEX5: Regexps to NFA

Lexical Analysis

CMPT 379: Compilers

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anoopsarkar.github.io/compilers-class

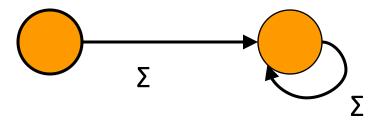
Building a Lexical Analyzer

- Token ⇒ Pattern
- Pattern ⇒ Regular Expression
- Regular Expression ⇒ NFA
- NFA \Rightarrow DFA
- DFA ⇒ Table-driven implementation of DFA

- Converts regexps to equivalent NFA
- Six simple rules
 - Empty language
 - Symbols (Σ)
 - Empty String (ε)
 - Alternation $(r_1 \text{ or } r_2)$
 - Concatenation (r_1 followed by r_2)
 - Repetition (r_1^*)

Used by Ken
Thompson for
pattern-based
search in text
editor QED (1968)

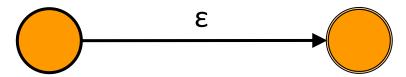
- For the empty language φ
- (optionally include a sinkhole state)



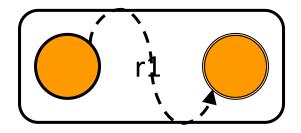
For each symbol x of the alphabet, there is a NFA that accepts it

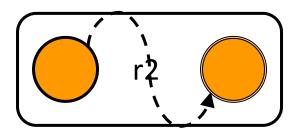


• There is an NFA that accepts only ε

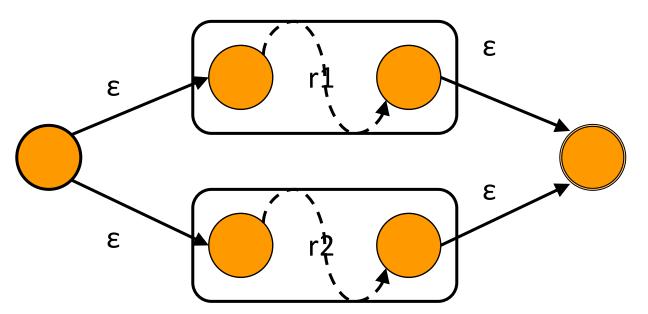


• Given 2 NFAs r_1 , r_2 , there is a NFA that accepts $r_1 \mid r_2$

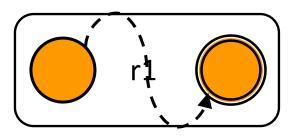


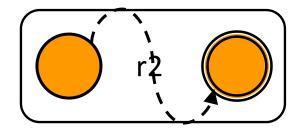


• Given 2 NFAs r_1 , r_2 , there is a NFA that accepts $r_1 \mid r_2$

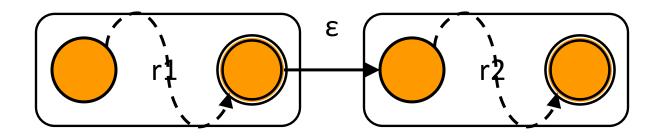


• Given 2 NFAs r_1 , r_2 , there is a NFA that accepts r_1r_2

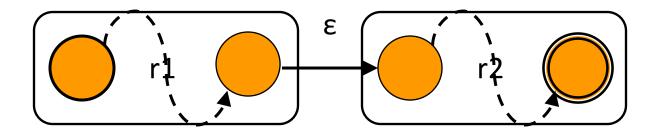




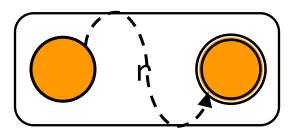
• Given 2 NFAs r_1 , r_2 , there is a NFA that accepts r_1r_2



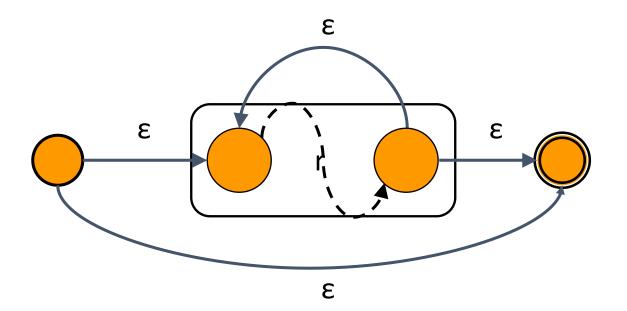
• Given 2 NFAs r_1 , r_2 , there is a NFA that accepts r_1r_2



• Given an NFA for r, there is an NFA that accepts r^*



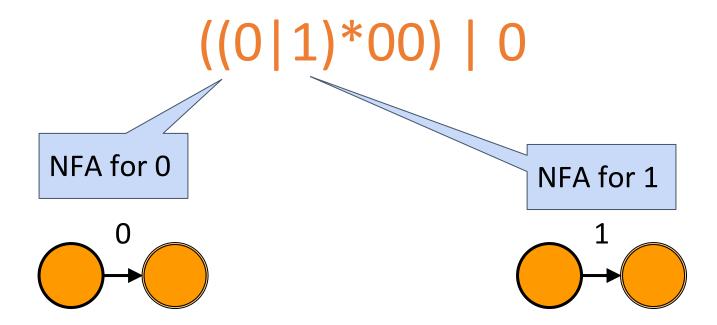
• Given an NFA for r, there is an NFA that accepts r^*

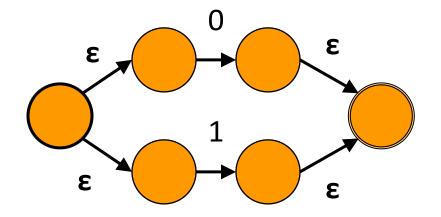


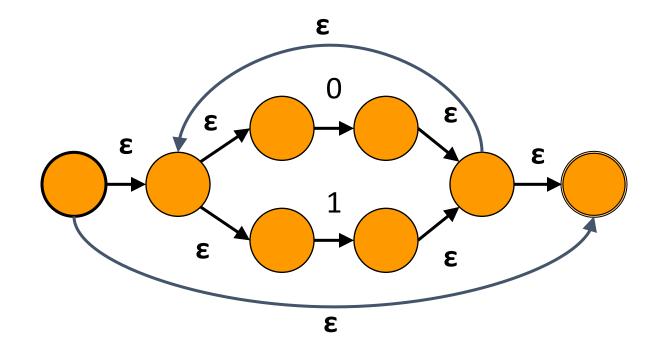
Example

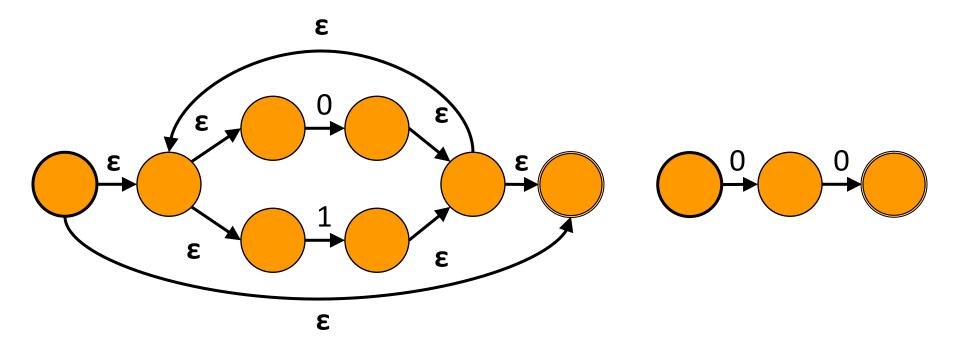
- Set of all binary strings that are divisible by four (include 0 in this set)
- Defined by the regexp: ((0|1)*00) | 0
- Apply Thompson's Rules to create an NFA

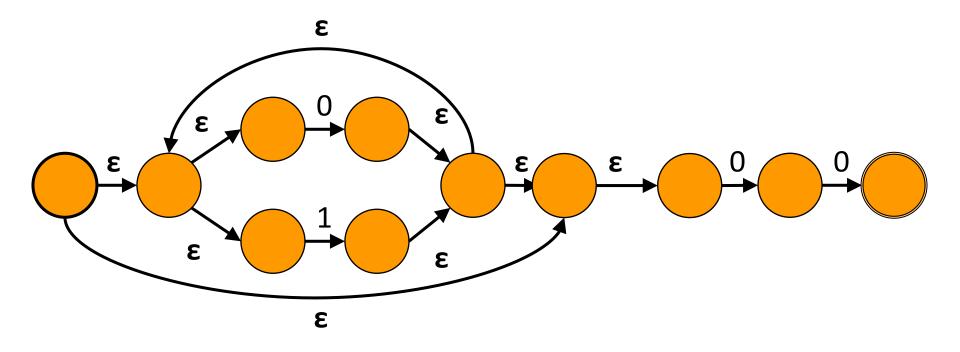
Basic Blocks 0 and 1

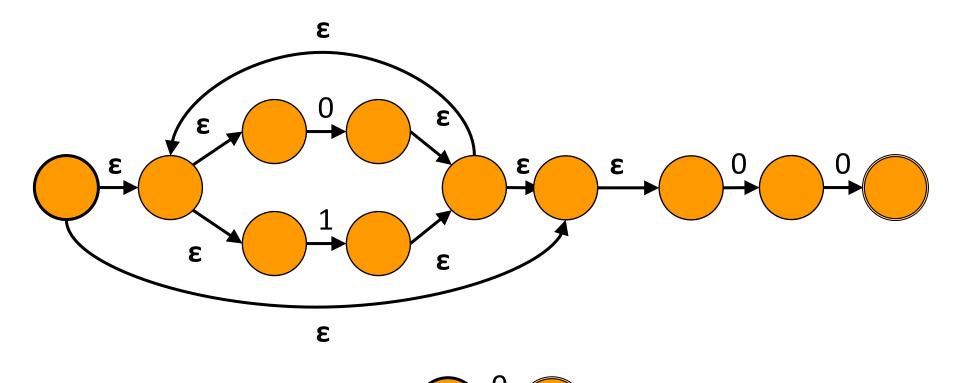


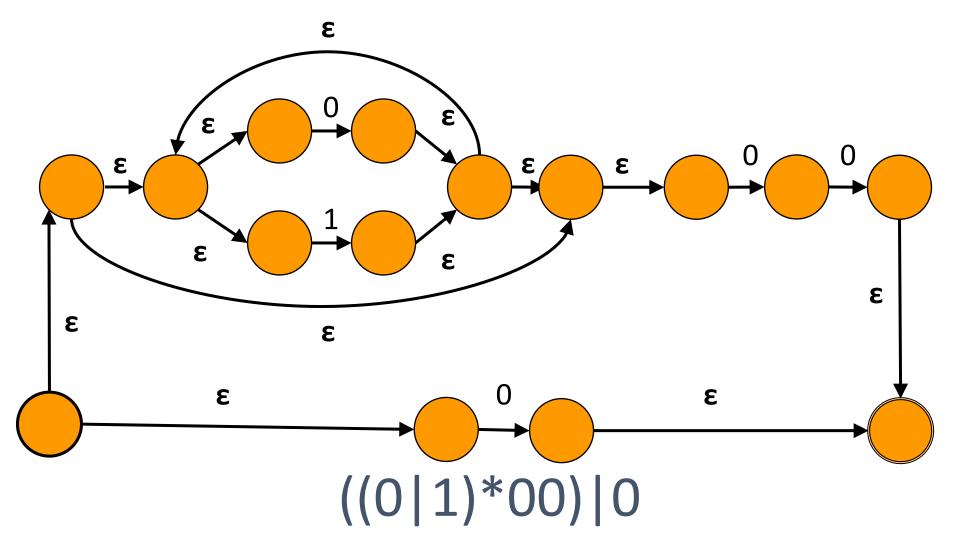












Converts regexps to NFA

Thompson's construction

Build NFA recursively from the regexp tree

n7

n6

(a(a|b))c

aab | .c.

Input is the tree in postfix

Post-order traversal of the regexp tree

n1 = nfa(a)

n2 = nfa(a)

n3 = nfa(b)

n4= nfa(n2, n3, |)

n5 = nfa(n1, n4, .)

n6= nfa(c)

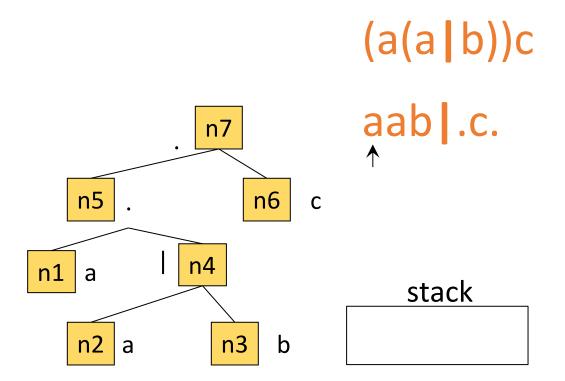
n7= nfa(n5, n6, .)

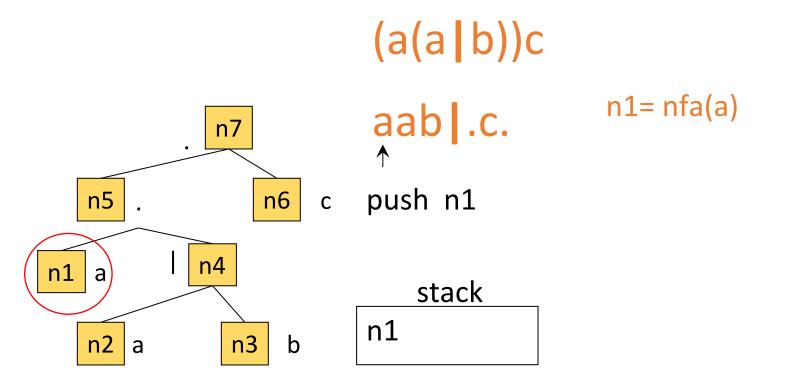


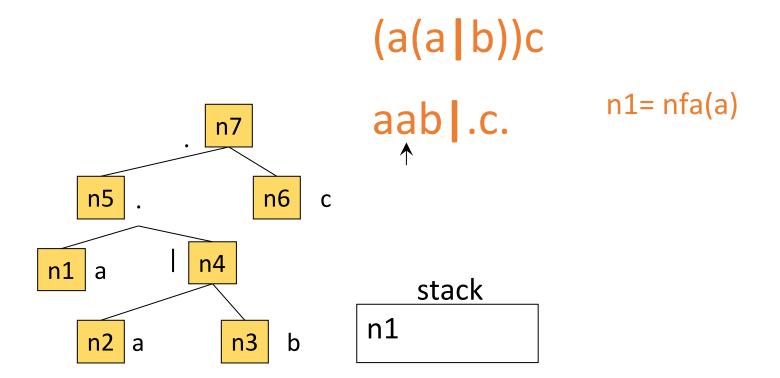
n4

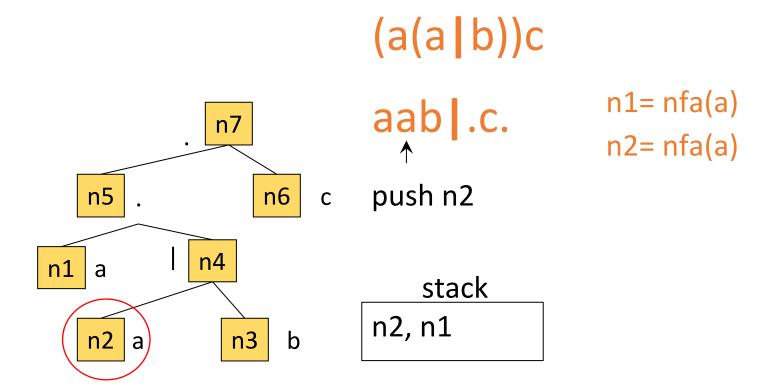
n5

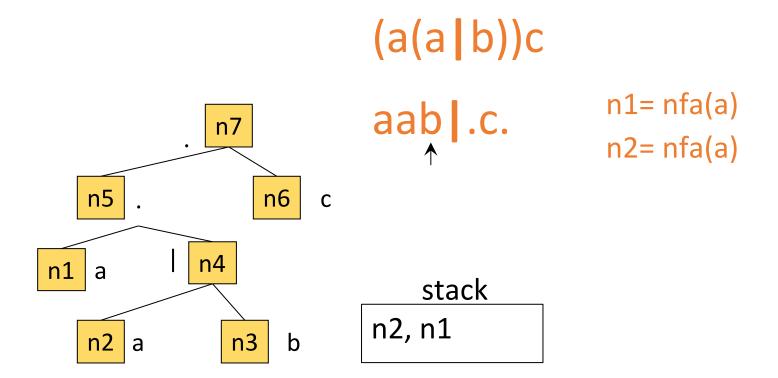
n1

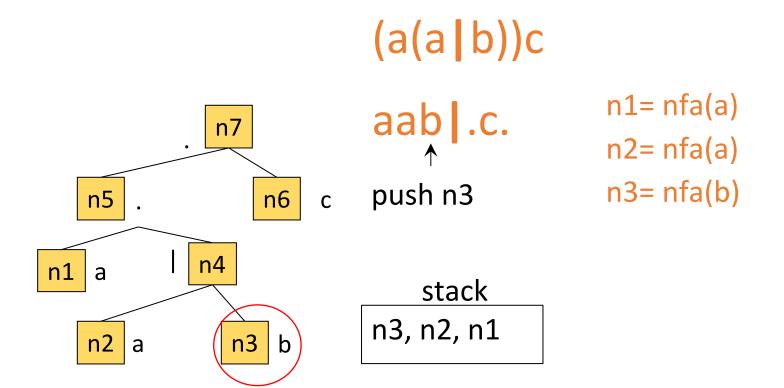


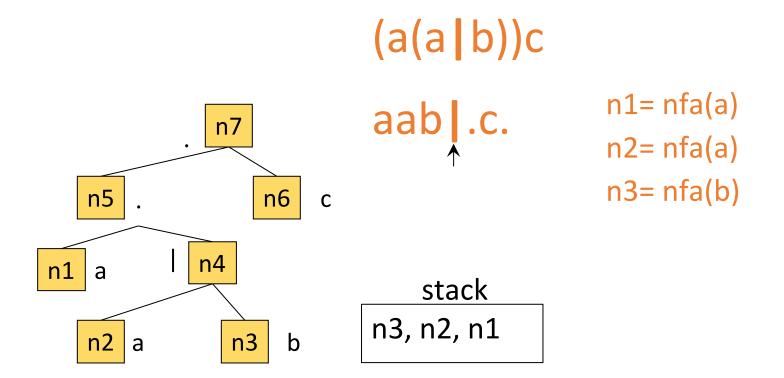


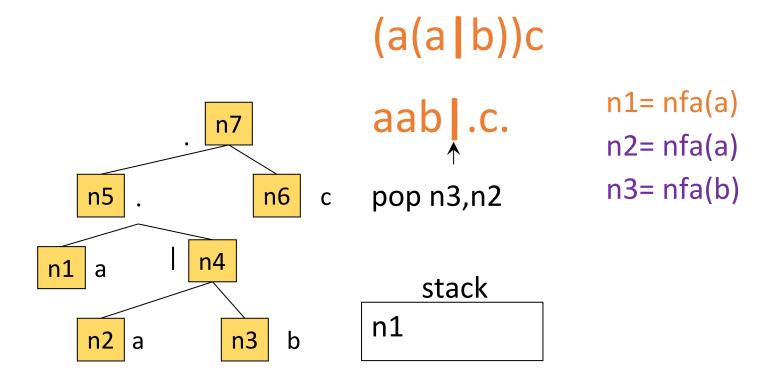


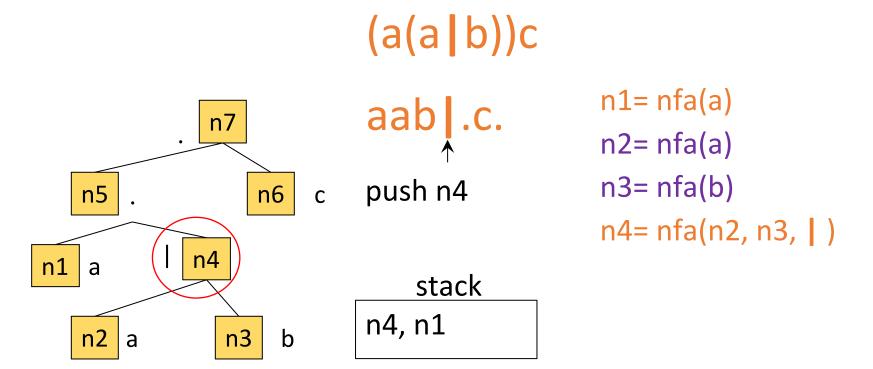


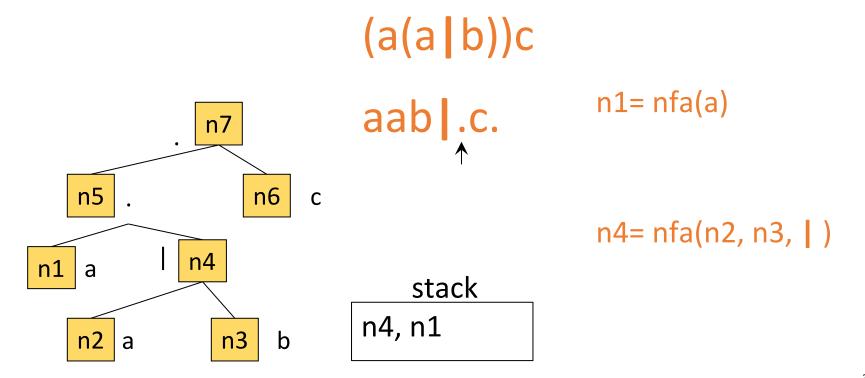


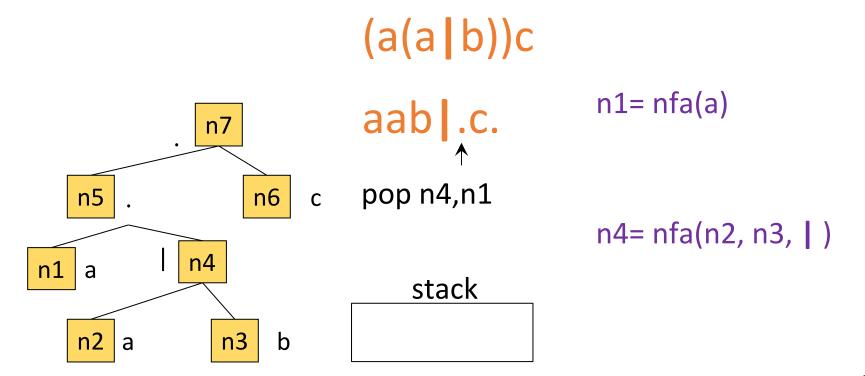


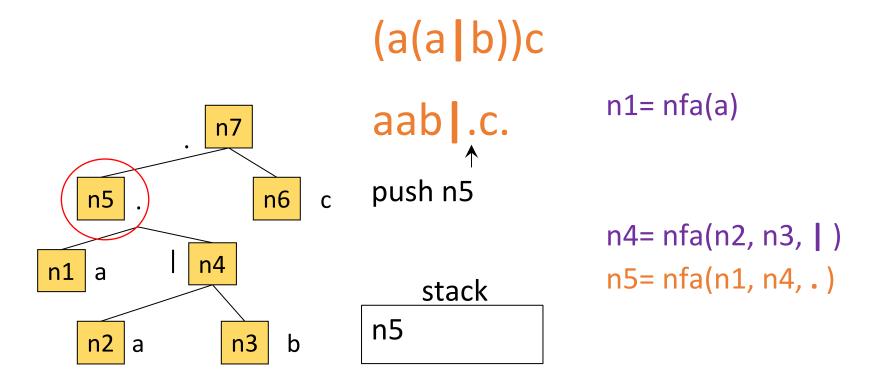


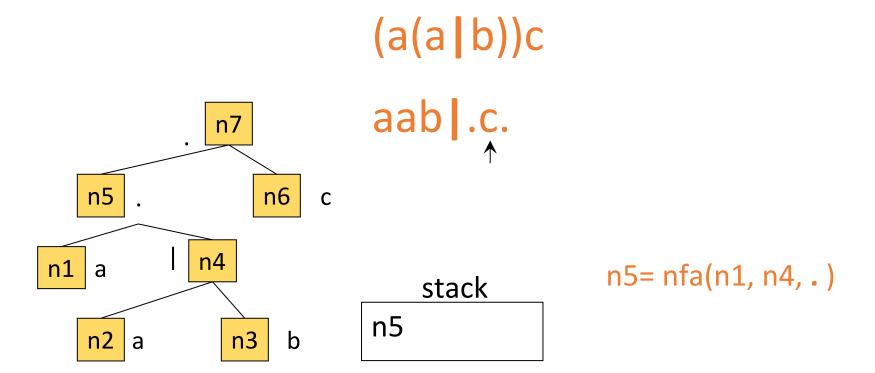


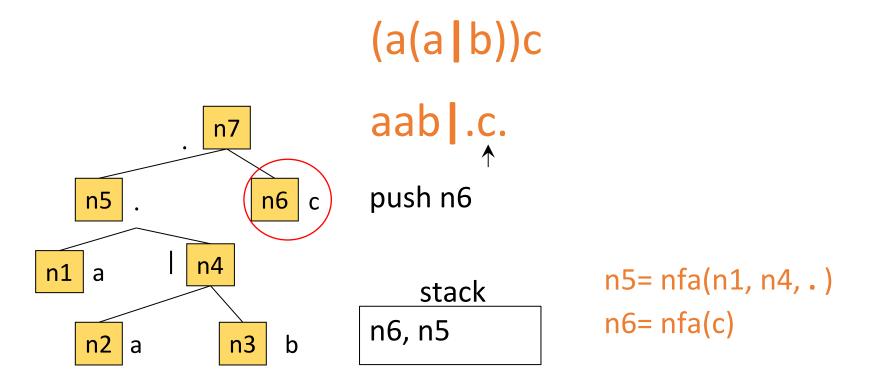


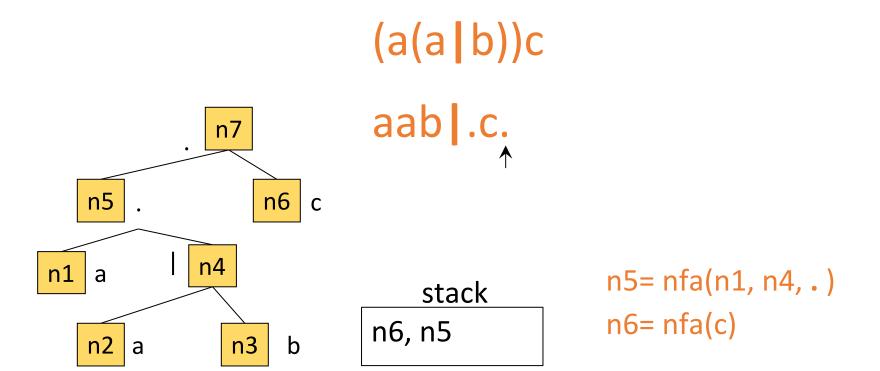


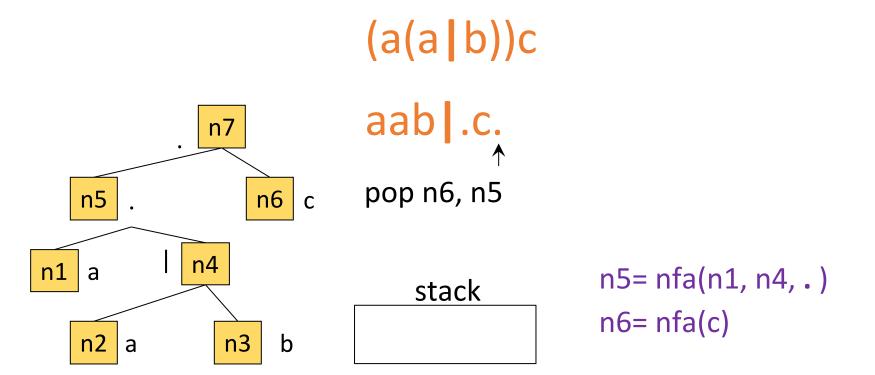


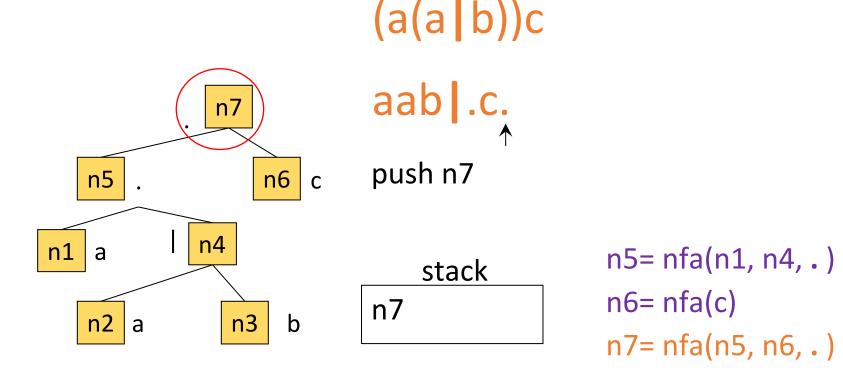


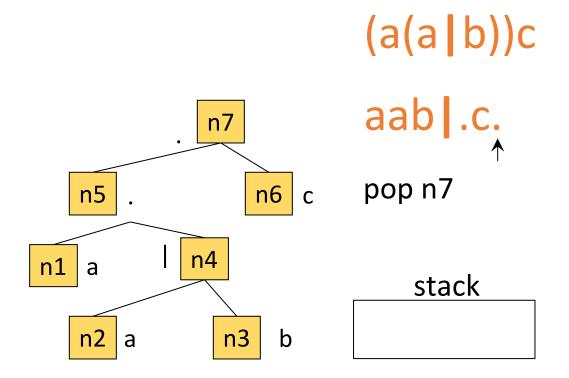












$$n7 = nfa(n5, n6, .)$$

Q: Use Thompson's construction to build an NFA for (0|1)(0|1)*

