LR3: SLR(1) Parsing

#### LR Parsing

CMPT 379: Compilers

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#### LR(0) conflicts:

```
S' \rightarrow T
T \rightarrow F
T \rightarrow T * F
T \rightarrow id
T \rightarrow id \mid (T)
F \rightarrow id \mid T;
```

```
11: F \rightarrow id \bullet
F \rightarrow id \bullet = T
Shift/reduce conflict
```

```
1: F \rightarrow id \bullet
T \rightarrow id \bullet
Reduce/Reduce conflict
```

Need more lookahead: SLR(1)

#### FIRST and FOLLOW

$$a \in \text{FIRST}(\alpha) \text{ if } \alpha \Rightarrow^* a\beta$$
  
if  $\alpha \Rightarrow^* \epsilon \text{ then } \epsilon \in \text{FIRST}(\alpha)$   
 $a \in \text{FOLLOW}(A) \text{ if } S \Rightarrow^* \alpha A a\beta$   
 $a \in \text{FOLLOW}(A) \text{ if } S \Rightarrow^* \alpha A \gamma a\beta$   
and  $\gamma \Rightarrow^* \epsilon$ 

#### Example First/Follow

$$S \rightarrow AB$$

$$A \rightarrow c \mid \epsilon$$

$$B \rightarrow cbB \mid ca$$

First(A) = 
$$\{c, \epsilon\}$$
 Follow(A) =  $\{c\}$   
First(B) =  $\{c\}$  Follow(A)  $\cap$   
First(cbB) = First(c) =  $\{c\}$   
First(ca) =  $\{c\}$  Follow(B) =  $\{\$\}$   
First(S) =  $\{c\}$  Follow(S) =  $\{\$\}$ 

#### Example First/Follow

$$S \rightarrow cAa$$
  
 $A \rightarrow cB \mid B$   
 $B \rightarrow bcB \mid \epsilon$   
First(A) = {b, c, \epsilon} Follow(A) = {a}  
First(B) = {b, \epsilon} Follow(B) = {a}  
First(S) = {c} Follow(S) = {\$}

## SLR(1): Simple LR(1) Parsing

$$S' \rightarrow T$$

$$T \rightarrow F \mid T * F \mid C (T)$$

$$F \rightarrow id \mid id ++ \mid (T)$$

$$C \rightarrow id$$

What can the next symbol be when we reduce  $F \rightarrow id$ ?

$$S'\$ \Rightarrow T\$ \Rightarrow F\$ \Rightarrow id\$$$
  $S'\$ \Rightarrow T\$ \Rightarrow T*F\$ \Rightarrow T*id\$ \Rightarrow F*id\$ \Rightarrow id*id\$$ 

$$S'\$ \Rightarrow T\$ \Rightarrow C(T)\$ \Rightarrow C(F)\$ \Rightarrow C(id)\$$$

The top of stack will be id and the next input symbol will be either \$, or \* or )

Follow(F) = 
$$\{ *, ), $ \}$$

## SLR(1): Simple LR(1) Parsing

$$S' \rightarrow T$$

$$T \rightarrow F \mid T * F \mid C (T)$$

$$F \rightarrow id \mid id ++ \mid (T)$$

$$C \rightarrow id$$

What can the next symbol be when we reduce  $C \rightarrow id$ ?

$$S'\$ \Rightarrow T\$ \Rightarrow C(T)\$ \Rightarrow C(F)\$ \Rightarrow C(id) \Rightarrow id(id)\$$$

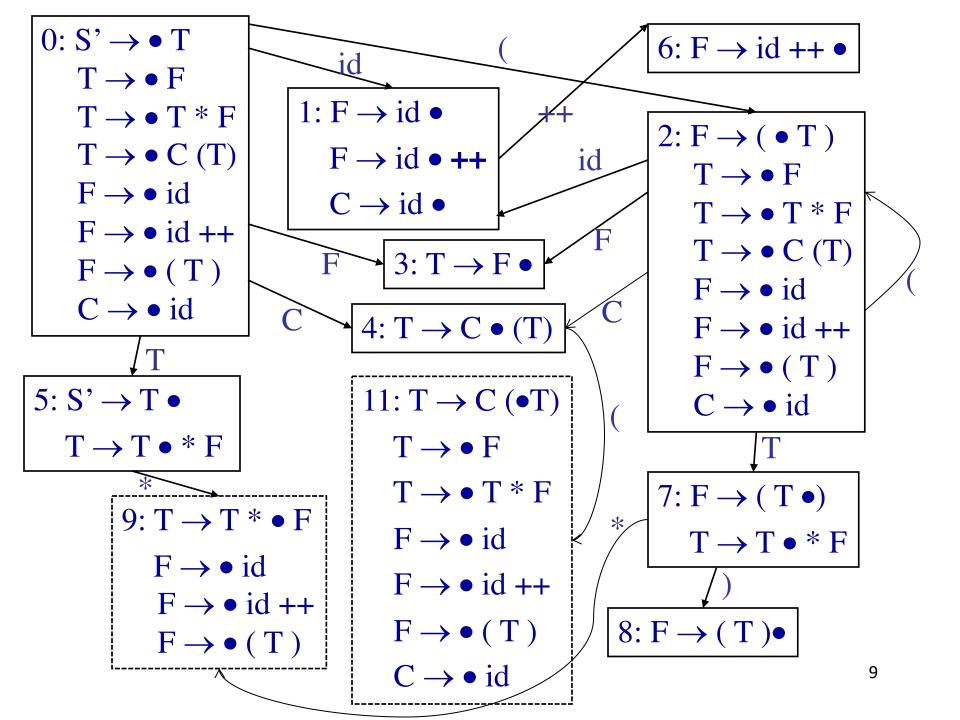
$$Follow(C) = \{ ( \}$$

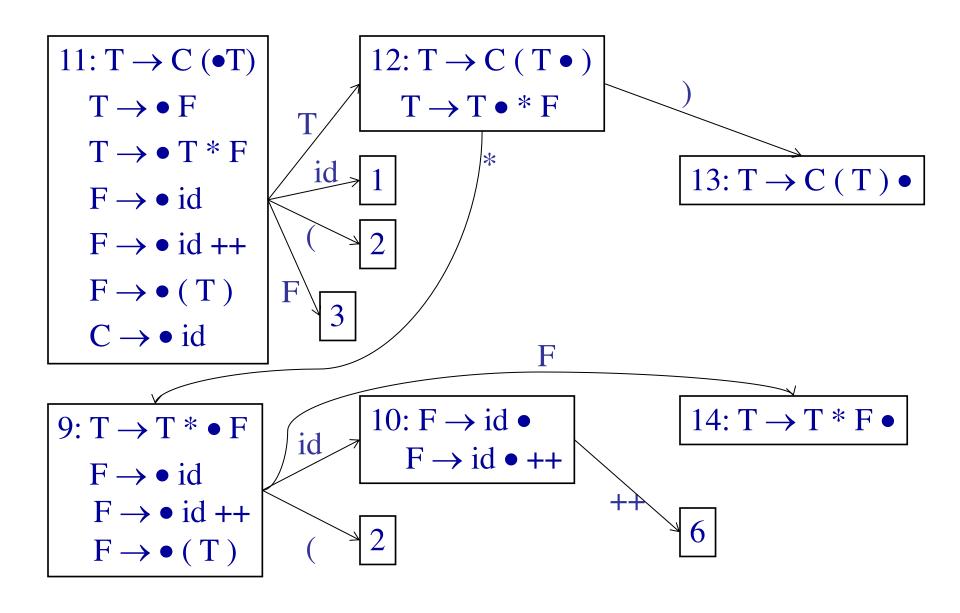
#### SLR(1): Simple LR(1) Parsing

```
0: S' \rightarrow \bullet T
                                                           S' \rightarrow T
     T \rightarrow \bullet F
                                                           T \rightarrow F \mid T * F \mid C (T)
     T \rightarrow \bullet T * F
     T \rightarrow \bullet C (T)
                                                           F \rightarrow id \mid id ++ \mid (T)
                                          id
     F \rightarrow \bullet id
                                                           C \rightarrow id
     F \rightarrow \bullet id ++
     F \rightarrow \bullet (T)
                                        1: F \rightarrow id \bullet
                                                                            Follow(F) = \{ *, ), \$ \}
     C \rightarrow \bullet id
                                            F \rightarrow id \bullet ++
                                                                            Follow(C) = \{ ( \} 
                                            C \rightarrow id \bullet
```

action[1,\*]= action[1,)] = action[1,\$] = Reduce 
$$F \rightarrow id$$
  
action[1,(] = Reduce  $C \rightarrow id$   
action[1,++] = Shift

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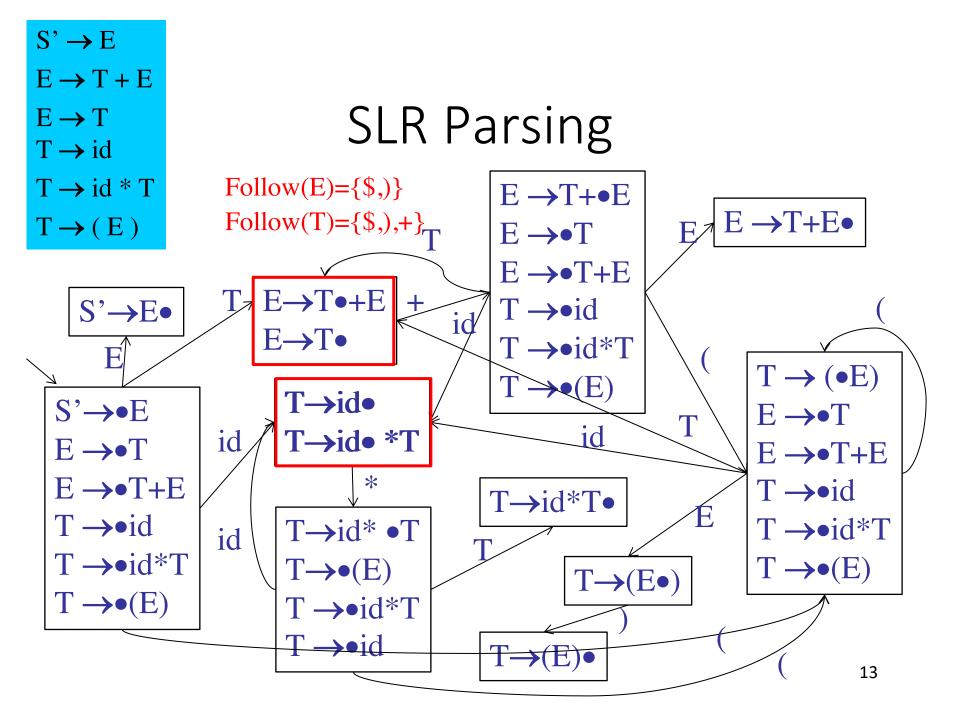
| ŀ | <b>Productions</b>                    |  |  |
|---|---------------------------------------|--|--|
| 1 | $T \rightarrow F$                     |  |  |
| 2 | $T \rightarrow T^*F$                  |  |  |
| 3 | $T \rightarrow C(T)$                  |  |  |
| 4 | $F \rightarrow id$                    |  |  |
| 5 | $F \rightarrow id ++$                 |  |  |
| 6 | $\mathbf{F} \rightarrow (\mathbf{T})$ |  |  |
| 7 | $C \rightarrow id$                    |  |  |

|    | *          | (   | )   | id  | ++         | \$ | T  | F  | C |
|----|------------|-----|-----|-----|------------|----|----|----|---|
| 0  |            | S2  |     | S1  |            |    | 5  | 3  | 4 |
| 1  | R4         | R7  | R4  |     | S2         | R4 |    |    |   |
| 2  |            | S2  |     | S1  |            |    | 7  | 3  | 4 |
| 3  | R1         |     | R1  |     |            | R1 |    |    |   |
| 4  |            | S11 |     |     |            |    |    |    |   |
| 5  | <b>S</b> 9 |     |     |     |            | A  |    |    |   |
| 6  | R5         |     | R5  |     |            | R5 |    |    |   |
| 7  | S9         |     | S8  |     |            |    |    |    |   |
| 8  | R6         |     | R6  |     |            | R6 |    |    |   |
| 9  |            | S2  |     | S10 |            |    |    | 14 |   |
| 1  | R4         |     | R4  |     | <b>S</b> 6 | R4 |    |    |   |
| 0  |            |     |     |     |            |    |    |    |   |
| 11 |            | S2  |     | S1  |            |    | 12 | 3  |   |
| 1  | <b>S</b> 9 |     | S13 |     |            |    |    |    |   |
| 2  |            |     |     |     |            |    |    |    |   |
| 1  | R3         |     | R3  |     |            | R3 |    |    |   |
| 3  |            |     |     |     |            |    |    |    |   |
| 1  | R2         |     | R2  |     |            | R2 |    |    |   |

#### If there is still conflicts under These rules, grammar is not SLR

#### **SLR Parsing**

- Assume:
  - Stack contains  $\alpha$  and next input is t
  - DFA on input  $\alpha$  terminates in state s
- Reduce by  $X \rightarrow \beta$  if
  - − s contains item  $X \rightarrow \beta \bullet$
  - $-t \in Follow(X)$
- Shift if
  - s contains item X→ β tω
  - If  $X \rightarrow \beta$  is in s then t cannot be in Follow(X)

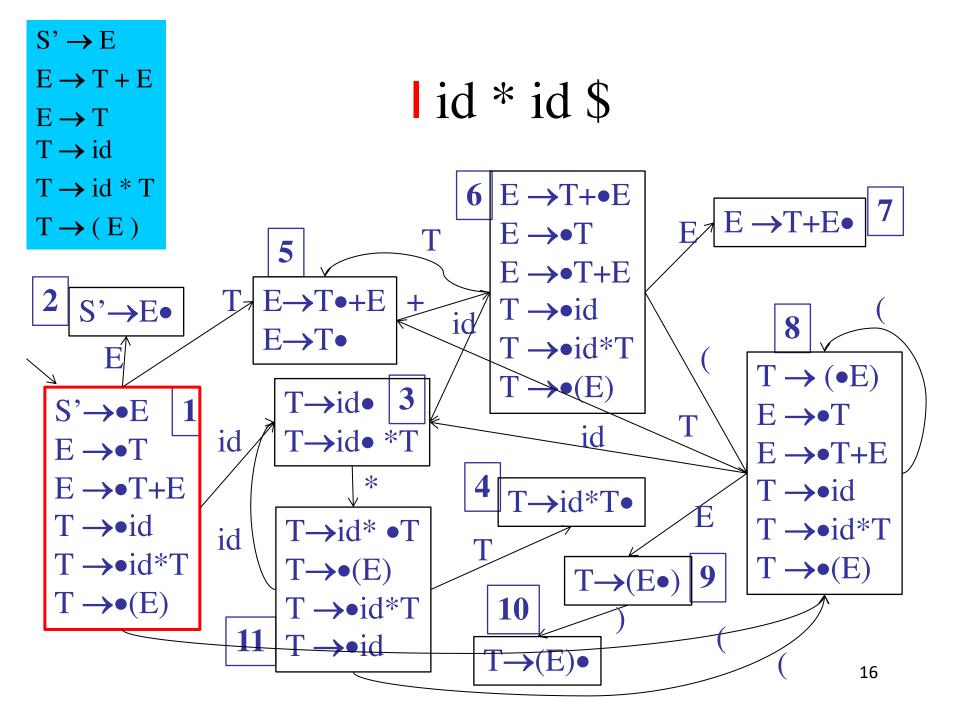


#### **SLR Parsing**

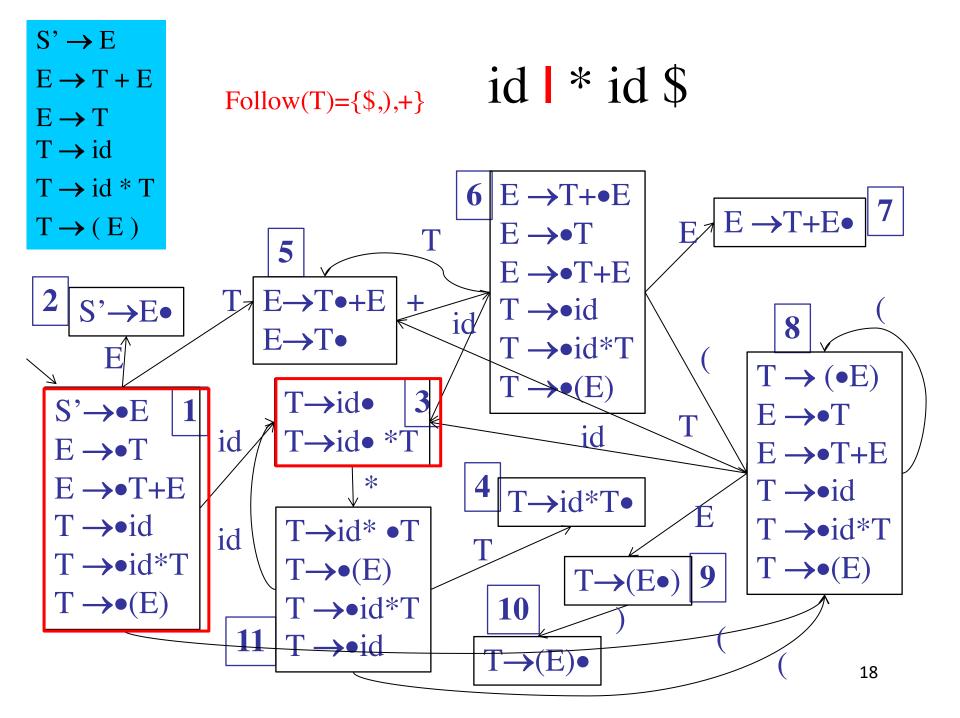
- Let M be DFA for viable prefixes of G
- Let  $|x_1...x_n|$  be initial configuration
- Repeat until configuration is \$|\$
  - Let  $\alpha \mid \omega$  be current configuration
  - Run M on current stack α
  - If M rejects  $\alpha$ , report parsing error
    - Stack  $\alpha$  is not a viable prefix
  - If M accepts  $\alpha$  with items I, let a be the next input
    - Shift  $[X \rightarrow \beta \bullet a \gamma] \in I$
    - Reduce if  $[X \to \beta \bullet] \in I$  and  $a \in Follow(X)$
    - Report parsing error if neither applies

If there is any conflict in the last step (more than two valid action), grammar is not SLR(k) in practice k=1

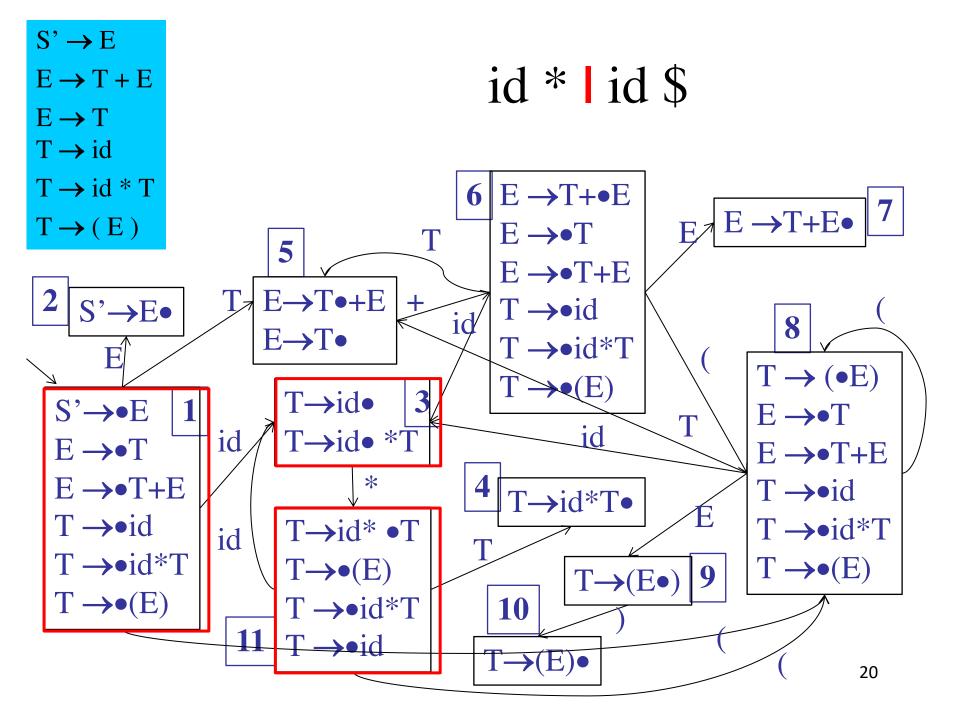
| configuration | DFA halt state | Action |
|---------------|----------------|--------|
| (Stacklinput) |                |        |
| l id * id \$  |                |        |
|               |                |        |
|               |                |        |
|               |                |        |
|               |                |        |
|               |                |        |
|               |                |        |



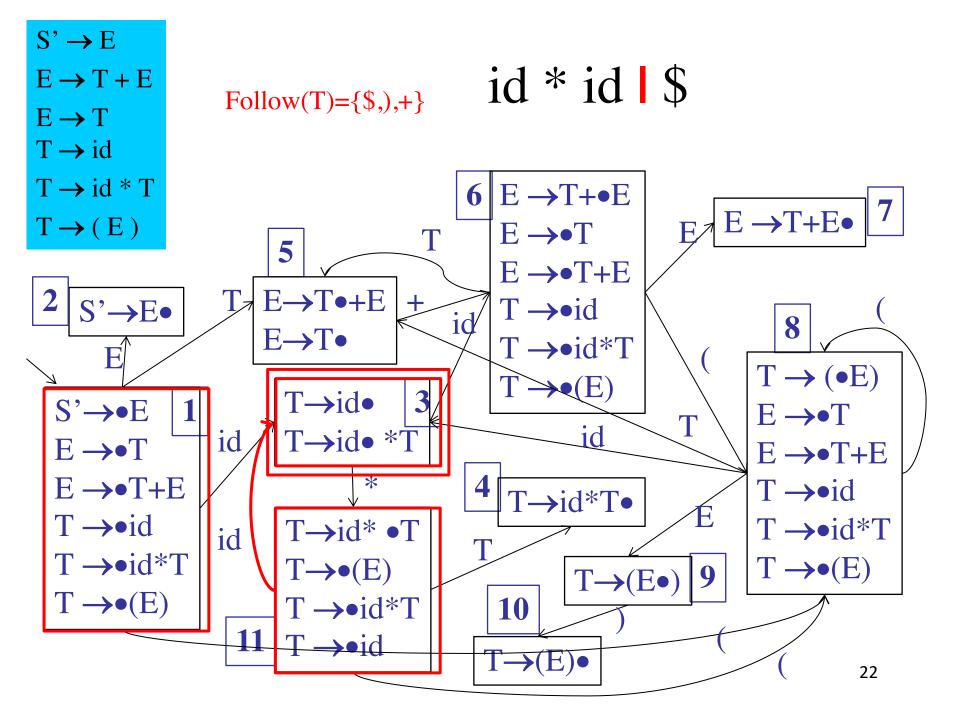
| configuration | DFA halt state | Action |
|---------------|----------------|--------|
| (Stacklinput) |                |        |
| l id * id \$  | 1              | Shift  |
| id I * id \$  |                |        |
|               |                |        |
|               |                |        |
|               |                |        |
|               |                |        |
|               |                |        |



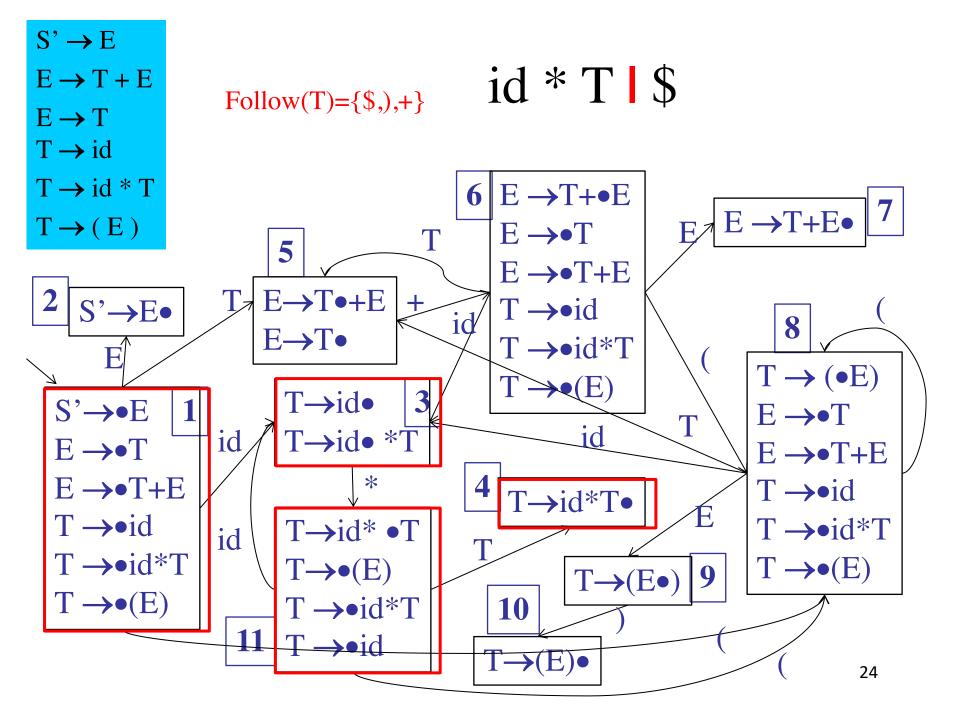
| configuration | DFA halt state         | Action |
|---------------|------------------------|--------|
| (Stacklinput) |                        |        |
| l id * id \$  | 1                      | Shift  |
| id I * id \$  | $3 * \notin Follow(T)$ | Shift  |
| id * I id \$  |                        |        |
|               |                        |        |
|               |                        |        |
|               |                        |        |
|               |                        |        |
|               |                        |        |



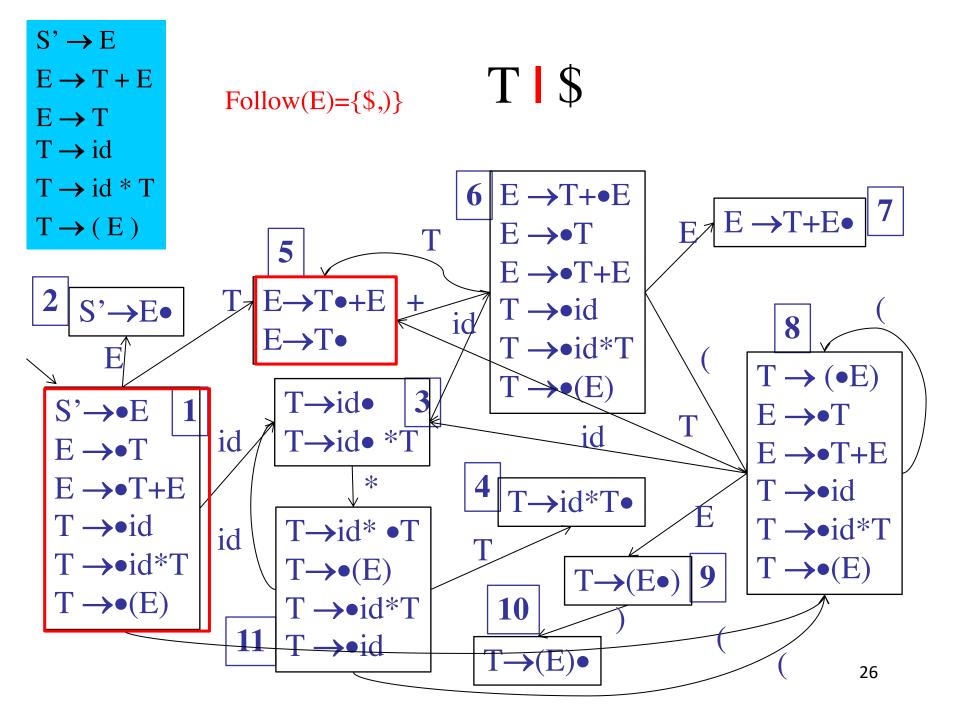
| configuration | DFA halt state         | Action |
|---------------|------------------------|--------|
| (Stacklinput) |                        |        |
| l id * id \$  | 1                      | Shift  |
| id I * id \$  | $3 * \notin Follow(T)$ | Shift  |
| id * I id \$  | 11                     | Shift  |
| id * id   \$  |                        |        |
|               |                        |        |
|               |                        |        |
|               |                        |        |
|               |                        |        |



| configuration | DFA halt state               | Action        |  |
|---------------|------------------------------|---------------|--|
| (Stacklinput) |                              |               |  |
| l id * id \$  | 1                            | Shift         |  |
| id   * id \$  | $3 * \notin Follow(T)$       | Shift         |  |
| id * I id \$  | 11                           | Shift         |  |
| id * id   \$  | $3  \$ \in \text{Follow}(T)$ | Reduce T → id |  |
| id * T   \$   |                              |               |  |
|               |                              |               |  |
|               |                              |               |  |
|               |                              |               |  |

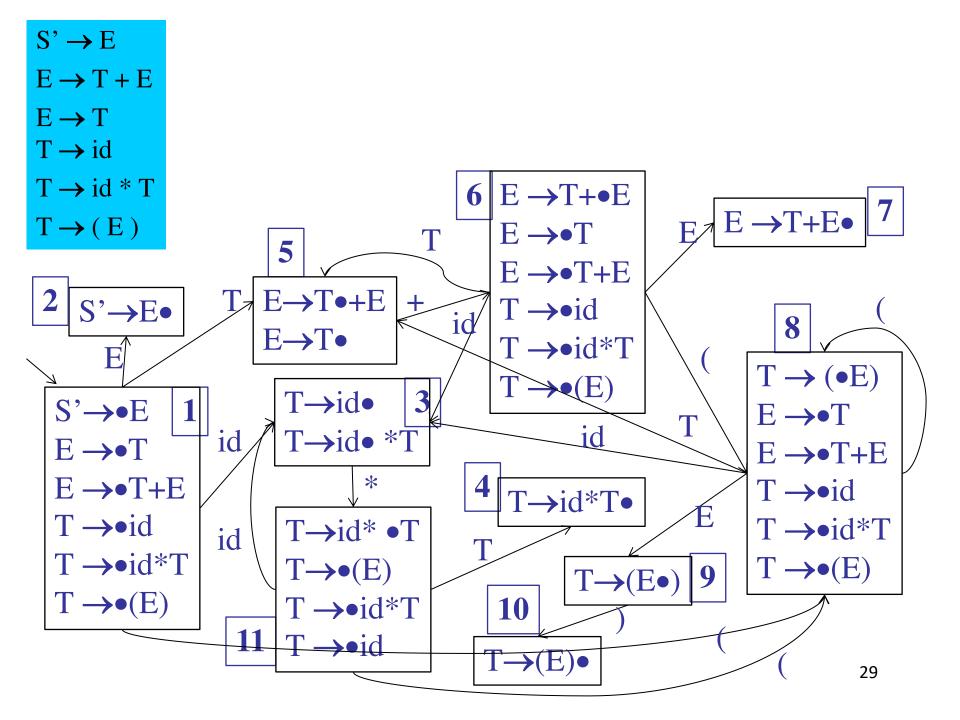


| configuration | DFA halt state              | Action                        |
|---------------|-----------------------------|-------------------------------|
| (Stacklinput) |                             |                               |
| l id * id \$  | 1                           | Shift                         |
| id I * id \$  | 3 * ∉ Follow(T)             | Shift                         |
| id * I id \$  | 11                          | Shift                         |
| id * id   \$  | $3 \qquad \$ \in Follow(T)$ | Reduce T → id                 |
| id * T   \$   | $4 \qquad \$ \in Follow(T)$ | Reduce T $\rightarrow$ id * T |
| T   \$        |                             |                               |
|               |                             |                               |
|               |                             |                               |



| configuration | DFA halt state              | Action                        |
|---------------|-----------------------------|-------------------------------|
| (Stacklinput) |                             |                               |
| l id * id \$  | 1                           | Shift                         |
| id I * id \$  | $3 * \notin Follow(T)$      | Shift                         |
| id * I id \$  | 11                          | Shift                         |
| id * id   \$  | $3 \qquad \$ \in Follow(T)$ | Reduce T → id                 |
| id * T   \$   | $4 \qquad \$ \in Follow(T)$ | Reduce T $\rightarrow$ id * T |
| TI\$          | $5  \$ \in Follow(E)$       | Reduce E→T                    |
| EI\$          |                             |                               |
|               |                             |                               |

| configuration | DFA halt state              | Action                        |
|---------------|-----------------------------|-------------------------------|
| (Stacklinput) |                             |                               |
| l id * id \$  | 1                           | Shift                         |
| id   * id \$  | $3 * \notin Follow(T)$      | Shift                         |
| id * I id \$  | 11                          | Shift                         |
| id * id   \$  | $3  \$ \in Follow(T)$       | Reduce T → id                 |
| id * T   \$   | $4 \qquad \$ \in Follow(T)$ | Reduce T $\rightarrow$ id * T |
| TI\$          | $5  \$ \in Follow(T)$       | Reduce E→T                    |
| EI\$          |                             | Accept                        |
|               |                             |                               |



#### Constructing SLR states

- Begin with item S'→•S, calculate related items (closure)
- Determine following states: what states can be reached on a single input token or non-terminal (GOTO)
- Construct closure of each resulting states

#### SLR(1) Construction

```
    Construct F = {I₀, I₁, ...Iո}
    a) if {A → α•} ∈ Iᵢ and A!= S'
        then action[i, b] := reduce A → α
        for all b ∈ Follow(A)
    b) if {S' → S•} ∈ Iᵢ
        then action[i, $] := accept
    c) if {A → α•aβ} ∈ Iᵢ and Successor(Iᵢ, a) = Iᵢ
        then action[i, a] := shift j
    if Successor(Iᵢ, A) = Iᵢ then goto[i, A] := j
```

#### SLR(1) Construction (cont'd)

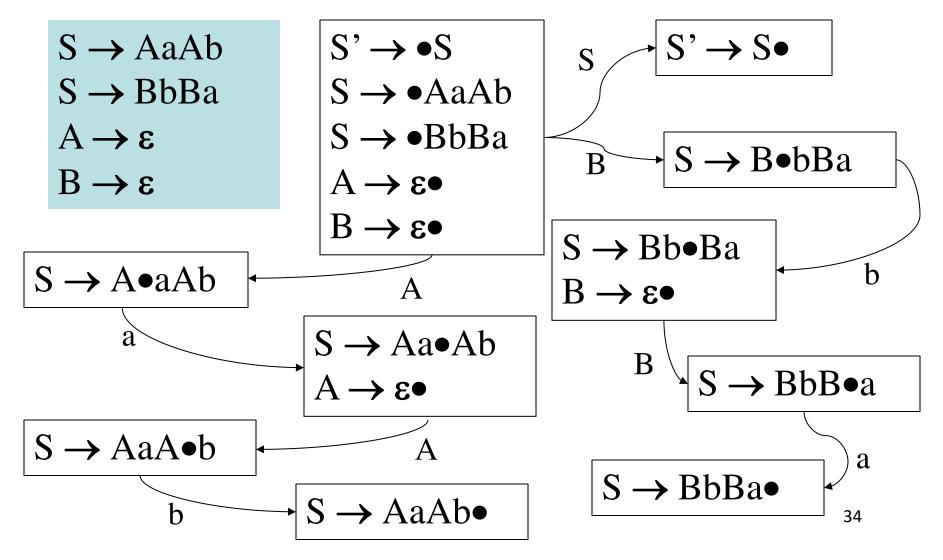
- 4. All entries not defined are errors
- 5. Make sure  $I_0$  is the initial state
- Note: SLR(1) only reduces
   {A → α•} if lookahead in Follow(A)
- Shift and reduce items or more than one reduce item can be in the same configuration set as long as lookaheads are disjoint

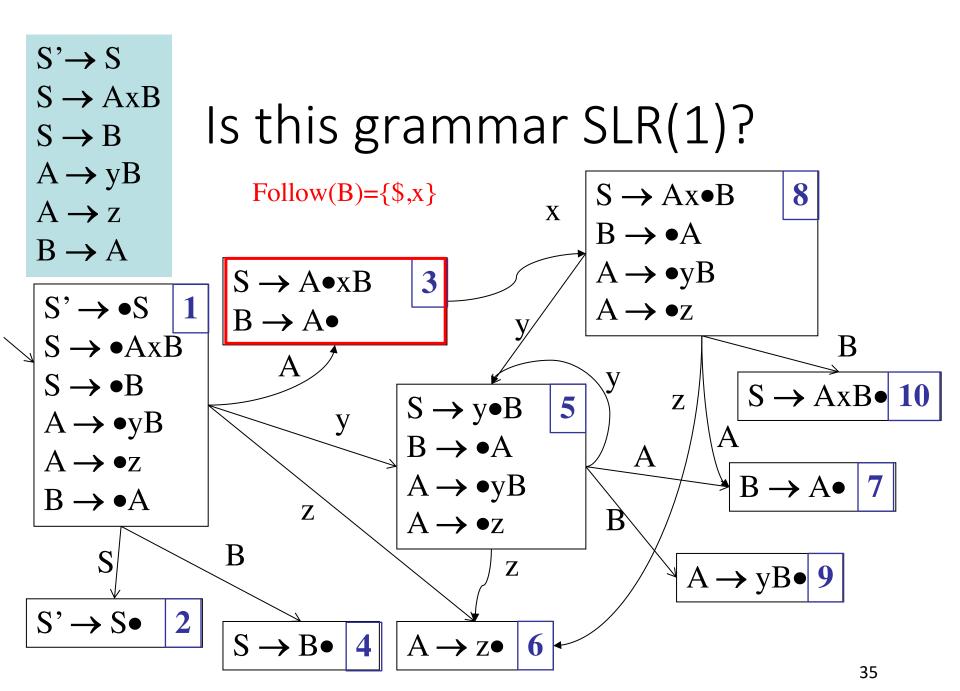
#### SLR(1) Conditions

- A grammar is SLR(1) if for each configuration set:
  - For any item {A →  $\alpha \bullet x\beta$ : x ∈ T} there is no {B →  $\gamma \bullet$ : x ∈ Follow(B)}
  - For any two items {A →  $\alpha$ •} and {B →  $\beta$ •} Follow(A)  $\cap$  Follow(B) =  $\emptyset$

LR(0) Grammars ⊂ SLR(1) Grammars

# Is this grammar SLR(1)?





- 1)  $S \rightarrow AxB$
- 2)  $S \rightarrow B$
- $3) A \rightarrow yB$
- $4) A \rightarrow z$
- 5)  $B \rightarrow A$

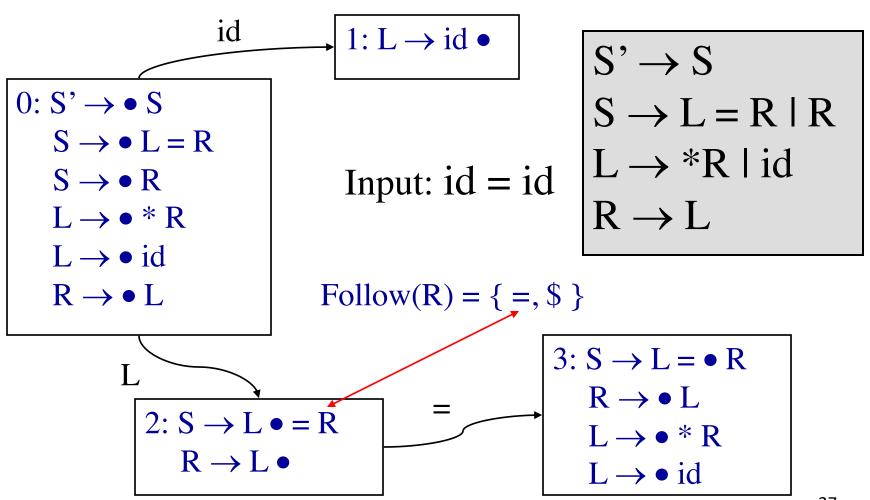
#### Grammar is not SLR

Reduce is a bad choice

## SLR Parsing Table

|    | х     | у  | Z  | \$   | S | Α | В  |
|----|-------|----|----|------|---|---|----|
| 1  |       | S5 | S6 |      | 2 | 3 | 4  |
| 2  |       |    |    | ACC! |   |   |    |
| 3  | S8,R5 |    |    | R5   |   |   |    |
| 4  |       |    |    | R2   |   |   |    |
| 5  |       | S5 | S6 |      |   | 7 | 9  |
| 6  | R4    |    |    | R4   |   |   |    |
| 7  | R5    |    |    | R5   |   |   |    |
| 8  |       | S5 | S6 |      |   | 7 | 10 |
| 9  | R3    |    |    | R3   |   |   |    |
| 10 |       |    |    | R1   |   |   |    |

#### SLR limitation: lack of context



$$S' \rightarrow S$$
  
 $S \rightarrow L = R \mid R$   
 $L \rightarrow *R \mid id$   
 $R \rightarrow L$ 

S'

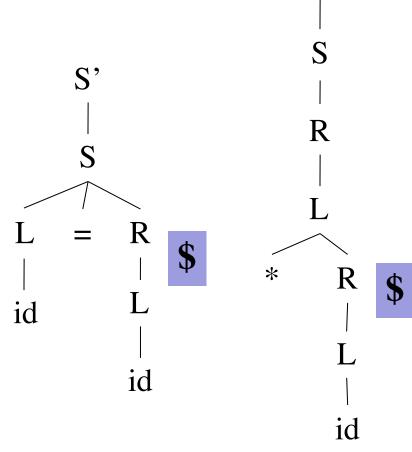
R

id

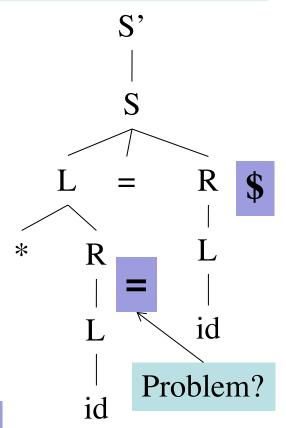
$$Follow(R) = \{ =, \$ \}$$

$$2: S \to L \bullet = R$$

$$R \to L \bullet$$



Find all lookaheads for reduce  $R \rightarrow L \bullet$ 



No!  $R \rightarrow L \bullet$  reduce and  $S \rightarrow L \bullet = R$  do not co-occur due to the  $L \rightarrow *R$  rule

#### Solution: Canonical LR(1)

- Extend definition of configuration
  - Remember lookahead
- New closure method
- Extend definition of Successor

#### LR(1) Parsing

- Limit introduced by SLR parsing in using Follow set to decide reductions
- Idea: augment LR items with 1 character lookahead [B → A•, \$] making an LR(1) item
  - Reduce to B only if lookahead token is \$
- More accurate than just Follow set
- Similar to SLR parsing just use LR(1) items rather than LR(0) items