$g_A: \ \omega_{0a} = \omega(k) + \mathrm{i}\mathrm{i}\delta$