

Given the plaintext **[01101101]** and **K<sub>1</sub>: 10100100, K<sub>2</sub>: 01000011**

Functions  $f_K$ , SW, K

- The function  $f_K$  is defined as follows. Let  $P = (L,R)$ , then  $f_K(L,R) = (L \oplus F(R,SK),R)$ .
- The function SW just switches the two halves of the plaintext, so  $SW(L,R) \rightarrow (R,L)$
- The function  $f(P, k)$  takes a four-bit string  $P$  and eight-bit key  $k$  and produces a four-bit output.

Applying the functions, we must perform the following steps:  $IP^{-1} \circ f_{K2} \circ SW \circ f_{K1} \circ IP$

1. Apply the initial Permutation on **[01101101]** and split it into two groups. We have calculated  $IP(P) = \mathbf{1110} \mid \mathbf{0110}$

IP							
2	6	3	1	4	8	5	7

2.  $L_0 = 1110, R_0 = 0110$
3. Find  $L_1$  and  $R_1$ , according the following rules:
  - a)  $L_1 = R_0 \rightarrow 0110$
  - b)  $R_1 = (L_0 \oplus f(R_0, K_1))$

$$(L_0 \oplus f(R_0, K_1))$$

$$(1110 \oplus f(0110 \oplus \mathbf{10100100}))$$

4. Applying the next functions:
  - a)  $F(0110, 10100100) = P_4 \circ S_{Boxes} \circ ((E/P(0110) \oplus 10100100))$

$S_x$		$C_0$	$C_1$	$C_2$	$C_3$
	$R_0$	1	0	3	2
	$R_1$	3	2	1	0
	$R_2$	0	2	1	3
	$R_3$	3	1	3	2

$$(1110 \oplus F(E/P(0110) \oplus \mathbf{10100100}))$$

$$(1110 \oplus F(\mathbf{00111100} \oplus \mathbf{10100100}))$$

$$(1110 \oplus \mathbf{10011000})$$

$$(1110 \oplus \mathbf{1001} \mid \mathbf{1000})$$

$$(S_0 \mid S_1)$$

$$(\mathbf{11} \mid \mathbf{11})$$

$$(1110 \oplus P_4(\mathbf{1111}))$$

E/P							
4	1	2	3	2	3	4	1

$S_y$		$C_0$	$C_1$	$C_2$	$C_3$
	$R_0$	0	1	2	3
	$R_1$	2	0	1	3
	$R_2$	3	0	1	0
	$R_3$	2	1	0	3

5. So now we have the outcome of  $F$  as 1111

$$(1110 \oplus \mathbf{1111})$$

$$(0001)$$

P4			
2	4	3	1

- $f_K(L,R) = (L \oplus F(R,SK),R)$ .
  - $f_K(L,R) = (0001, 0110)$ .
6.  $L_1 = 0001$  and  $R_1 = 0110$
  7. SW just swaps them so  $R_1 = 0001$  and  $L_1 = 0110$
  8. Concatenate  $L$  and  $R = 0110\ 0001$

9. Round # 2: Now do the calculation of  $f_{k2}(L,R) = f(01000011, (01100001) \oplus F(0001, 010000110), 0001))$

$$(0110 \oplus F(E/P(0001) \oplus 01000011)$$

$$(0110 \oplus F(10000010 \oplus 01000011)$$

$$(0110 \oplus 11000001)$$

$$(0110 \oplus 1100 \mid 0001)$$

$$(S_0 \mid S_1)$$

$$(01 \mid 10)$$

$$(0110 \oplus P_4(0110))$$

$$(0110 \oplus 1010)$$

$$(1100)$$

10. So now we have the outcome of F as 1100  
 11.  $f_k(L,R) = (L_1 \oplus F(R_1, K_2), R_1)$   
 12. Calculating we then have  $f_{k2}(L, R) = (1100, 0001)$   
 13.  $L_2 = 1100$  and  $R_2 = 0001$   
 14. Concatenate  $L_2$  and  $R_2 = 11000001$   
 15. perform the  $IP^{-1}$  permutation:

$IP^{-1}$							
4	1	3	5	7	2	8	6

Ciphertext = 01000110

**Steps for Finding  $IP^{-1}$**

IP							
2	6	3	1	4	8	5	7

Original Table (IP)	2	6	3	1	4	8	5	7
Step 1: Add indices	1	2	3	4	5	6	7	8
Step 2: Swap contents and indices	1	2	3	4	5	6	7	8
	2	6	3	1	4	8	5	7
Step 3: Sort based on indices	4	1	3	5	7	2	8	6
	1	2	3	4	5	6	7	8
Inverted Table ( $IP^{-1}$ )	4	1	3	5	7	2	8	6