ALU Design A.5

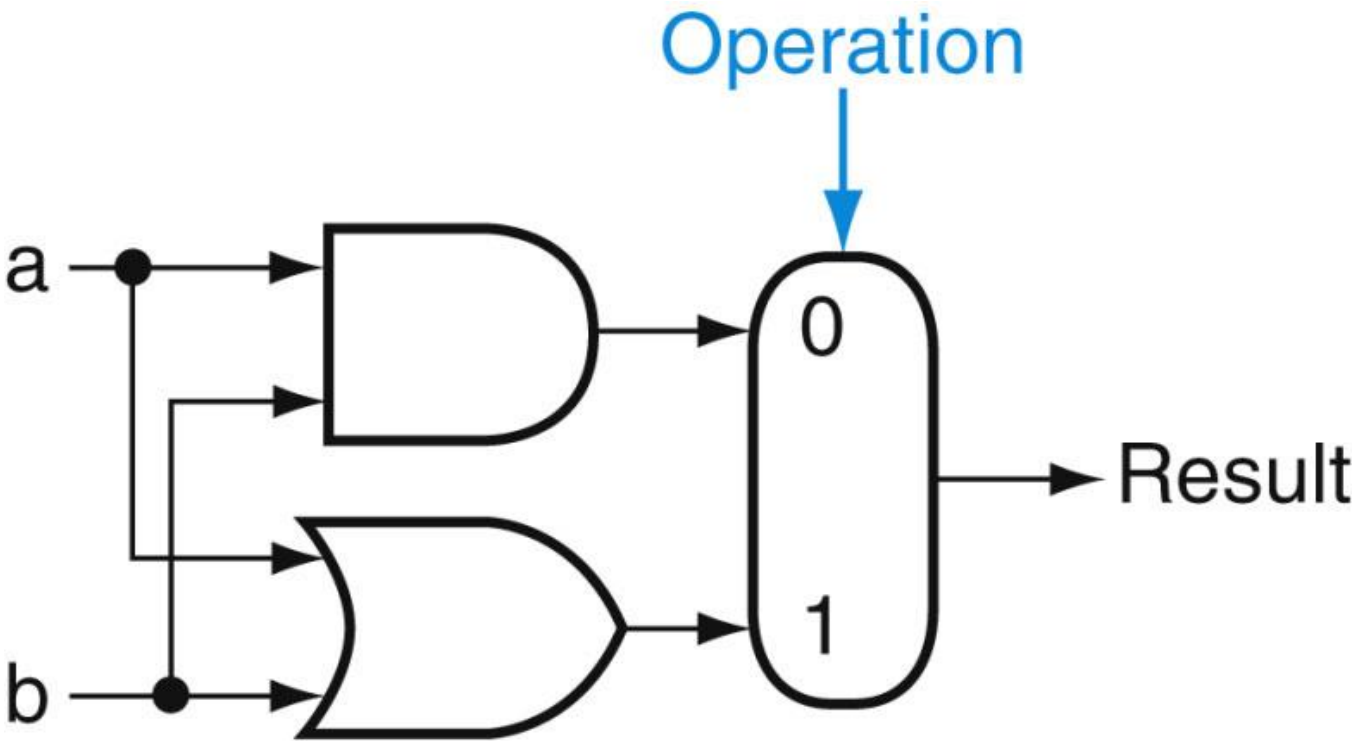


FIGURE A.5.1 The 1-bit logical unit for AND and OR.

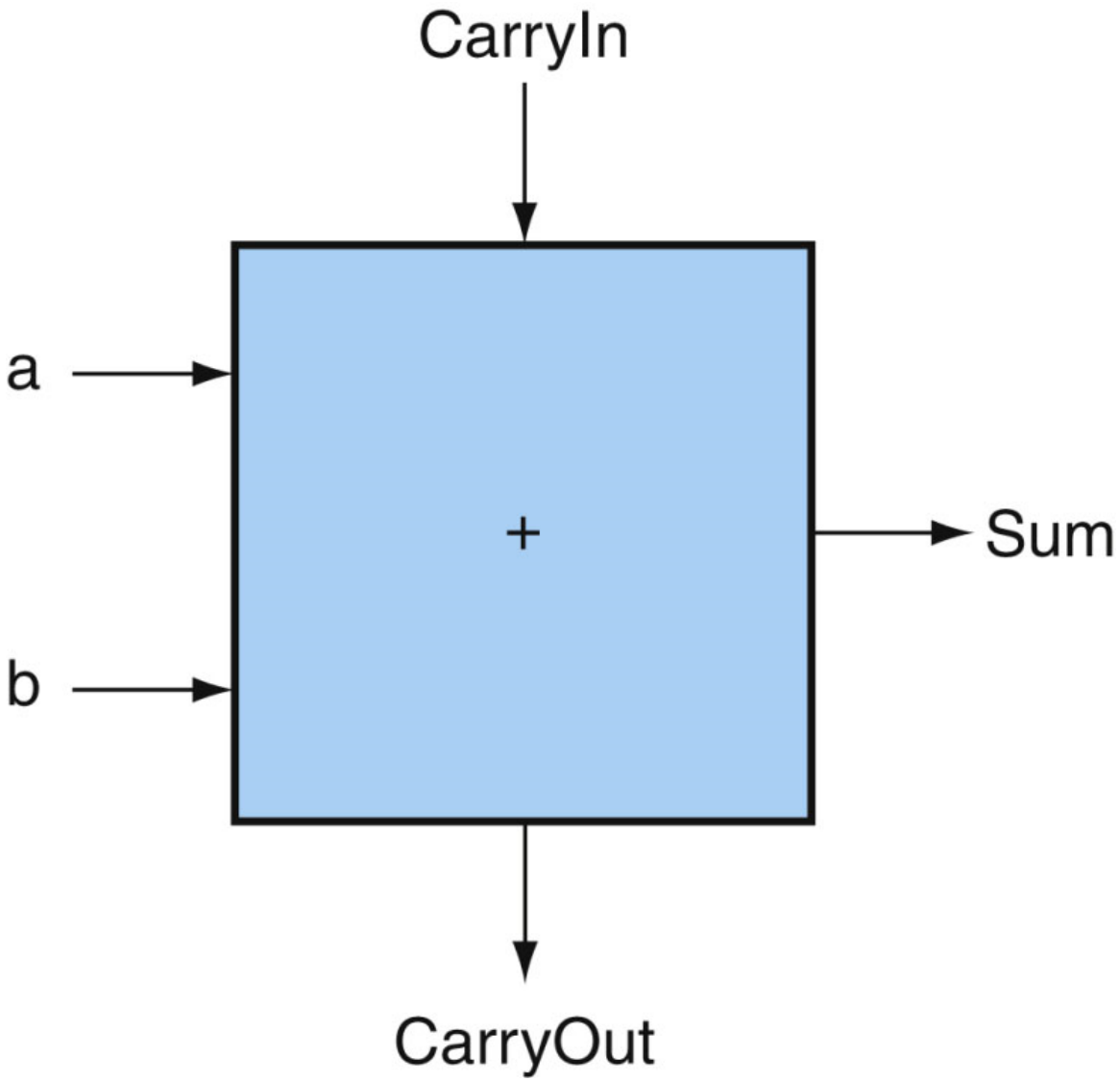


FIGURE A.5.2 A 1-bit adder. This adder is called a full adder; it is also called a (3,2) adder because it has 3 inputs and 2 outputs. An adder with only the a and b inputs is called a (2,2) adder or half-adder.

Inputs			Outputs		Comments
a	b	CarryIn	CarryOut	Sum	
0	0	0	0	0	$0 + 0 + 0 = 00_{two}$
0	0	1	0	1	$0 + 0 + 1 = 01_{two}$
0	1	0	0	1	$0 + 1 + 0 = 01_{two}$
0	1	1	1	0	$0 + 1 + 1 = 10_{two}$
1	0	0	0	1	$1 + 0 + 0 = 01_{two}$
1	0	1	1	0	$1 + 0 + 1 = 10_{two}$
1	1	0	1	0	$1 + 1 + 0 = 10_{two}$
1	1	1	1	1	$1 + 1 + 1 = 11_{two}$

FIGURE A.5.3 Input and output specification for a 1-bit adder.

Inputs		
a	b	CarryIn
0	1	1
1	0	1
1	1	0
1	1	1

FIGURE A.5.4 Values of the inputs when CarryOut is a 1.

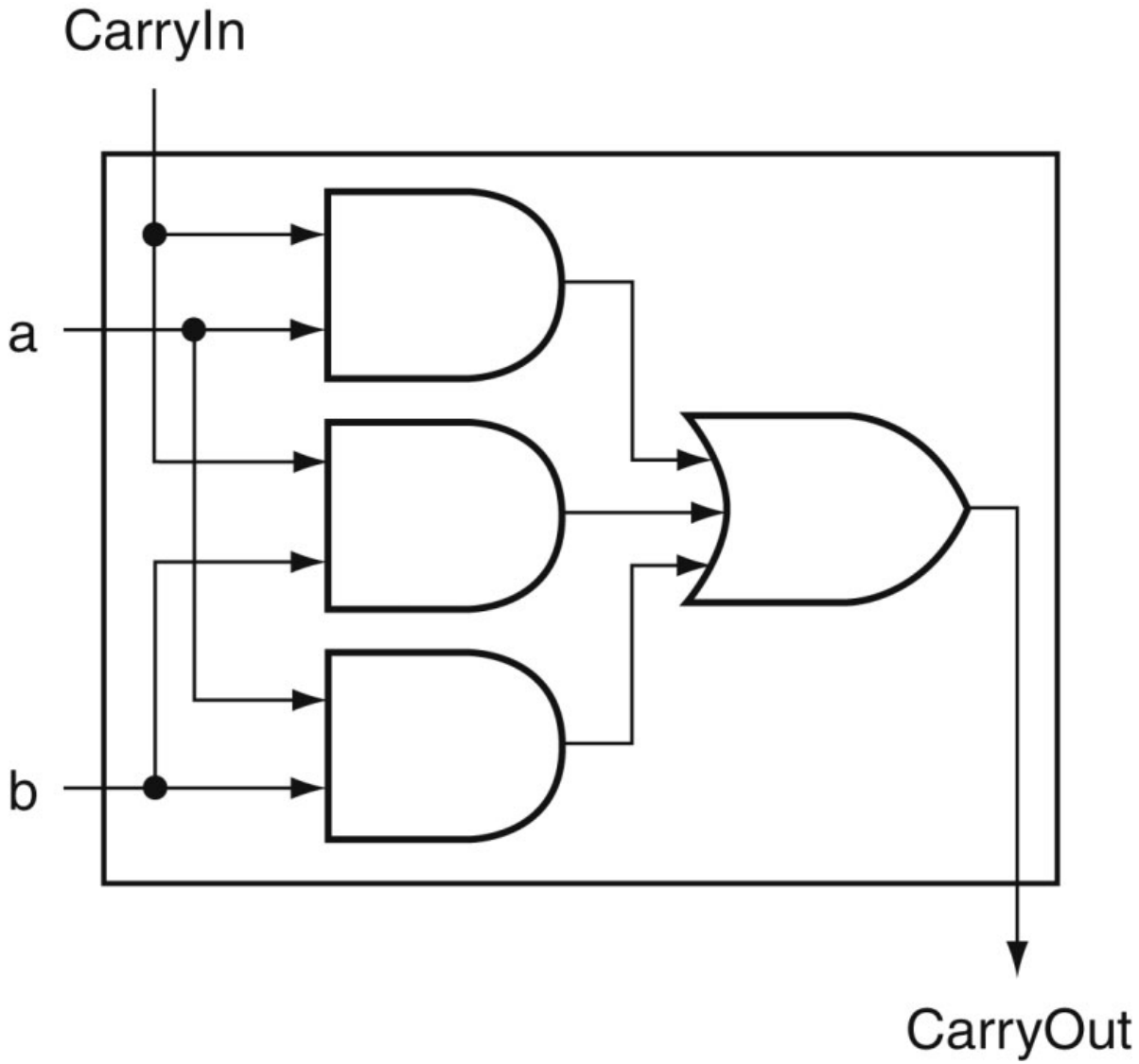


FIGURE A.5.5 Adder hardware for the CarryOut signal. The rest of the adder hardware is the logic for the Sum output given in the equation on this page.

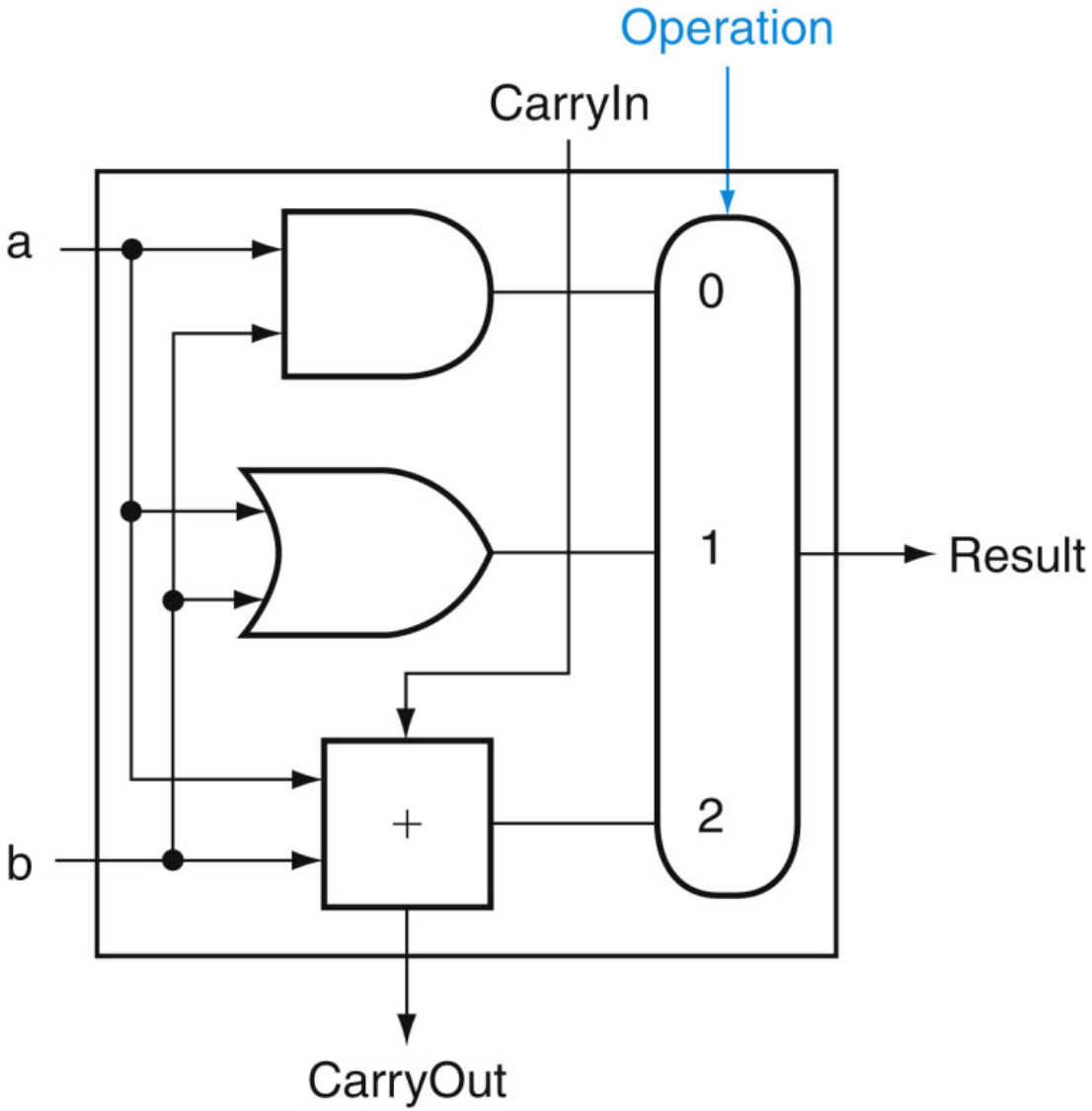


FIGURE A.5.6 A 1-bit ALU that performs AND, OR, and addition (see Figure B.5.5).

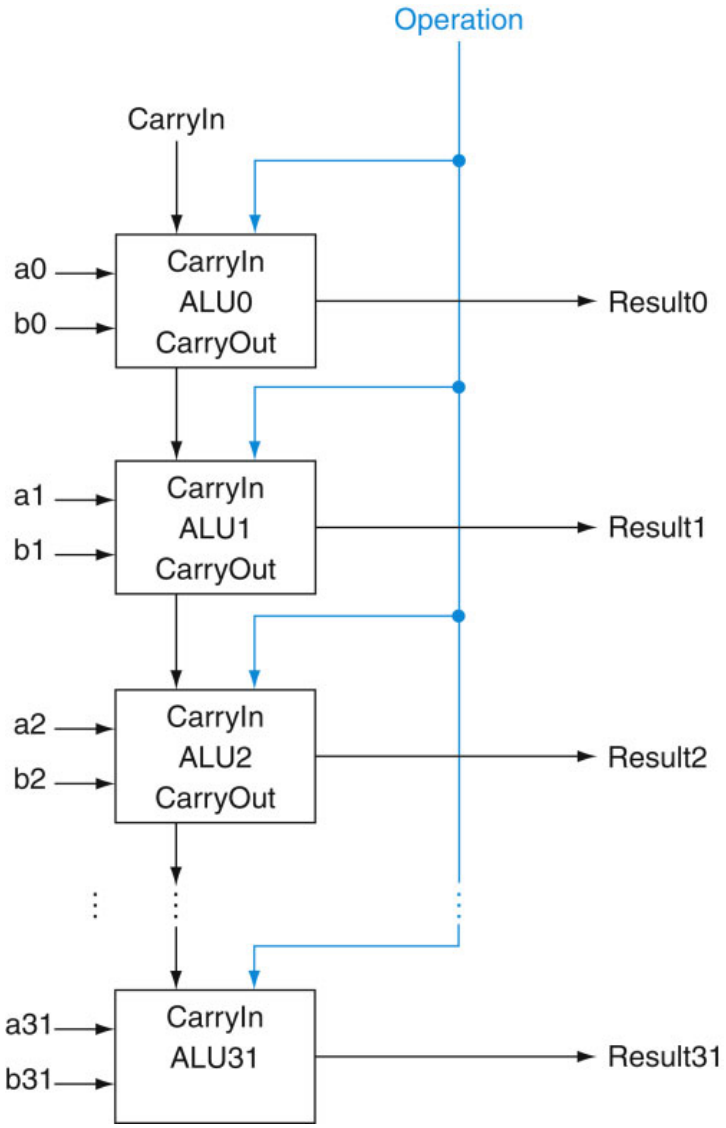


FIGURE A.5.7 A 32-bit ALU constructed from 32 1-bit ALUs. CarryOut of the less significant bit is connected to the CarryIn of the more significant bit. This organization is called ripple carry.

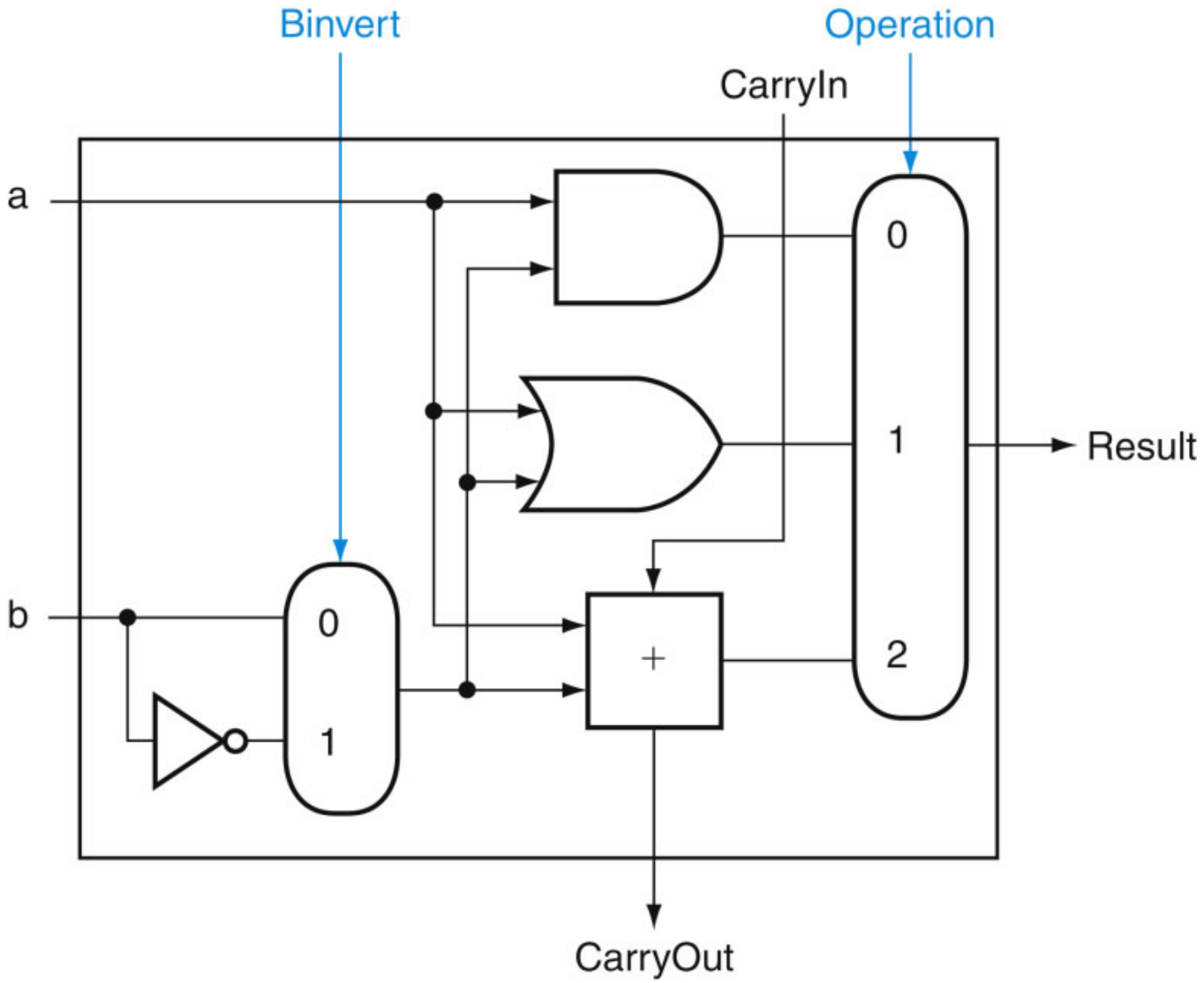


FIGURE A.5.8 A 1-bit ALU that performs AND, OR, and addition on a and b or a and b. By selecting (Binvert 5 1) and setting CarryIn to 1 in the least significant bit of the ALU, we get two's comple-ment subtraction of b from a instead of addition of b to a.

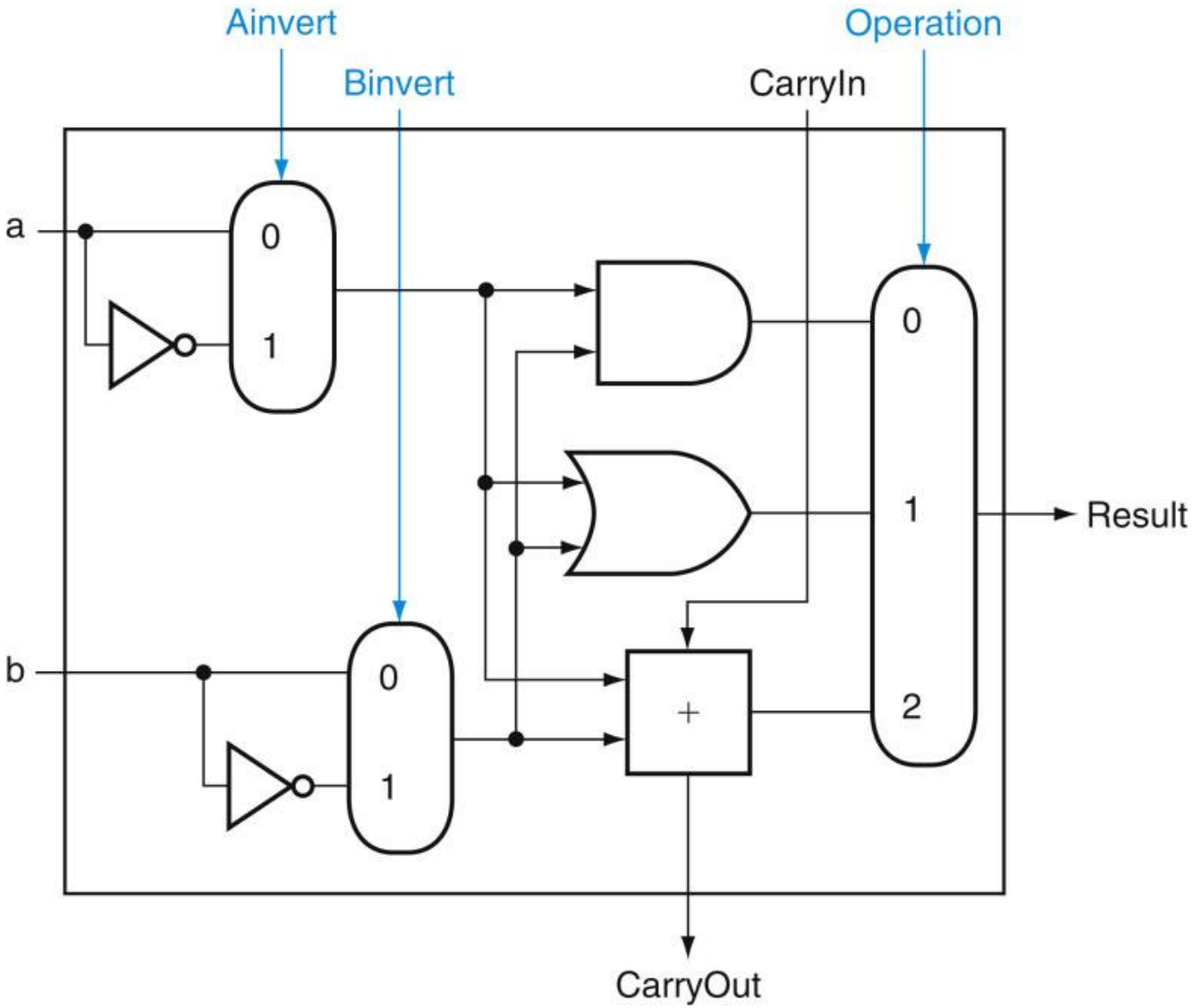
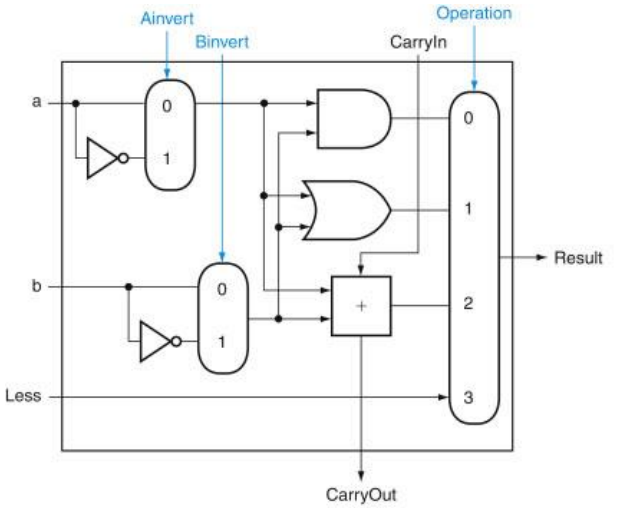


FIGURE A.5.9 A 1-bit ALU that performs AND, OR, and addition on a and b or a and b. By selecting (Ainvert 5 1) and (Binvert 5 1), we get a NOR b instead of a AND b.



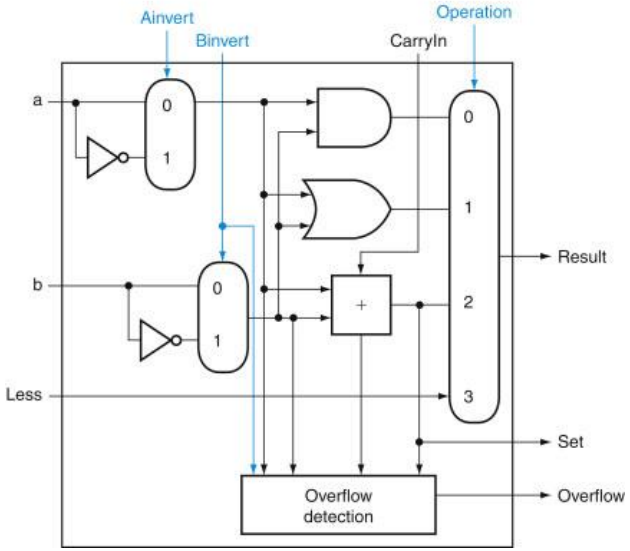


FIGURE A.5.10 (Top) A 1-bit ALU that performs AND, OR, and addition on a and b or b , and (bottom) a 1-bit ALU for the most significant bit. The top drawing includes a direct input that is connected to perform the set on less than operation (see Figure A.5.11); the bottom has a direct output from the adder for the less than comparison called Set. (See Exercise A.24 at the end of this appendix to see how to calculate overflow with fewer inputs.)

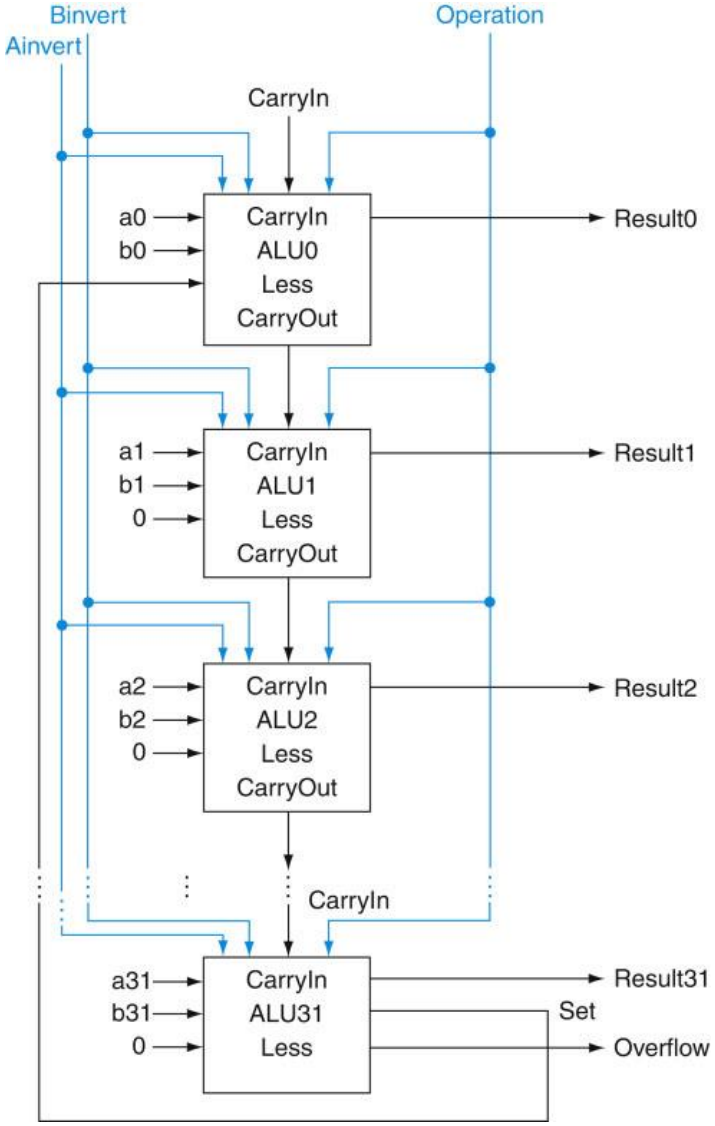


FIGURE A.5.11 A 32-bit ALU constructed from the 31 copies of the 1-bit ALU in the top of Figure A.5.10 and one 1-bit ALU in the bottom of that figure. The Less inputs are connected to 0 except for the least significant bit, which is connected to the Set output of the most significant bit. If the ALU performs a 2 b and we select the input 3 in the multiplexor in Figure A.5.10, then Result 5 0 … 001 if a , b, and Result 5 0 … 000 otherwise.

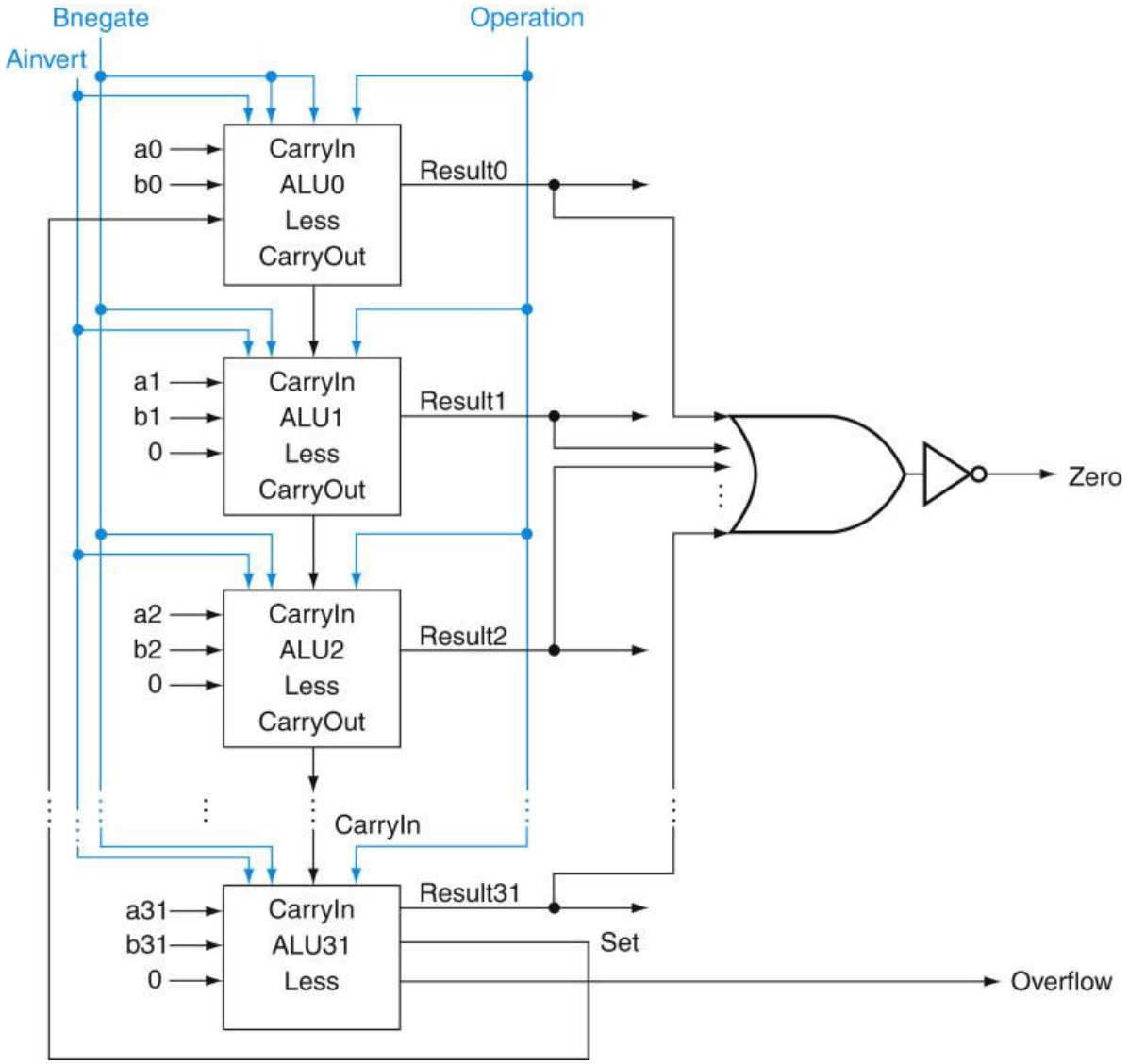


FIGURE A.5.12 The final 32-bit ALU. This adds a Zero detector to Figure A.5.11.

ALU control lines	Function
0000	AND
0001	OR
0010	add
0110	subtract

FIGURE A.5.13 The values of the three ALU control lines, Bnegate, and Operation, and the corresponding ALU operations.

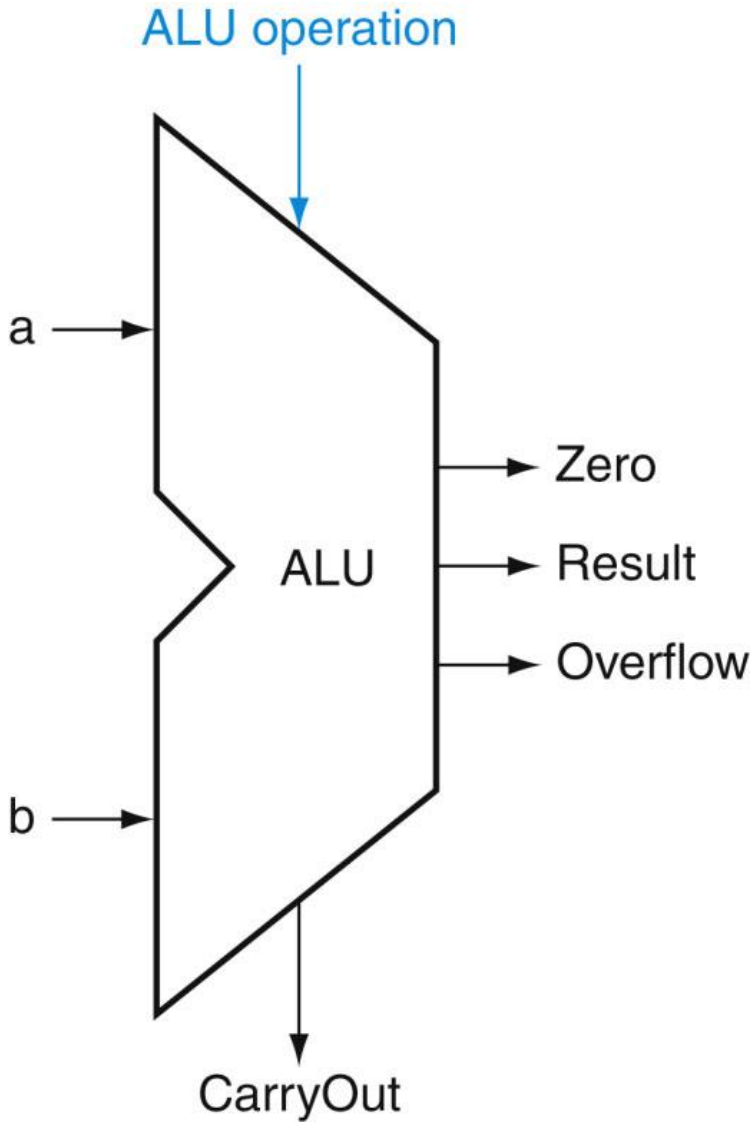


FIGURE A.5.14 The symbol commonly used to represent an ALU, as shown in Figure A.5.12. This symbol is also used to represent an adder, so it is normally labeled either with ALU or Adder.

Chapter 4

The Processor

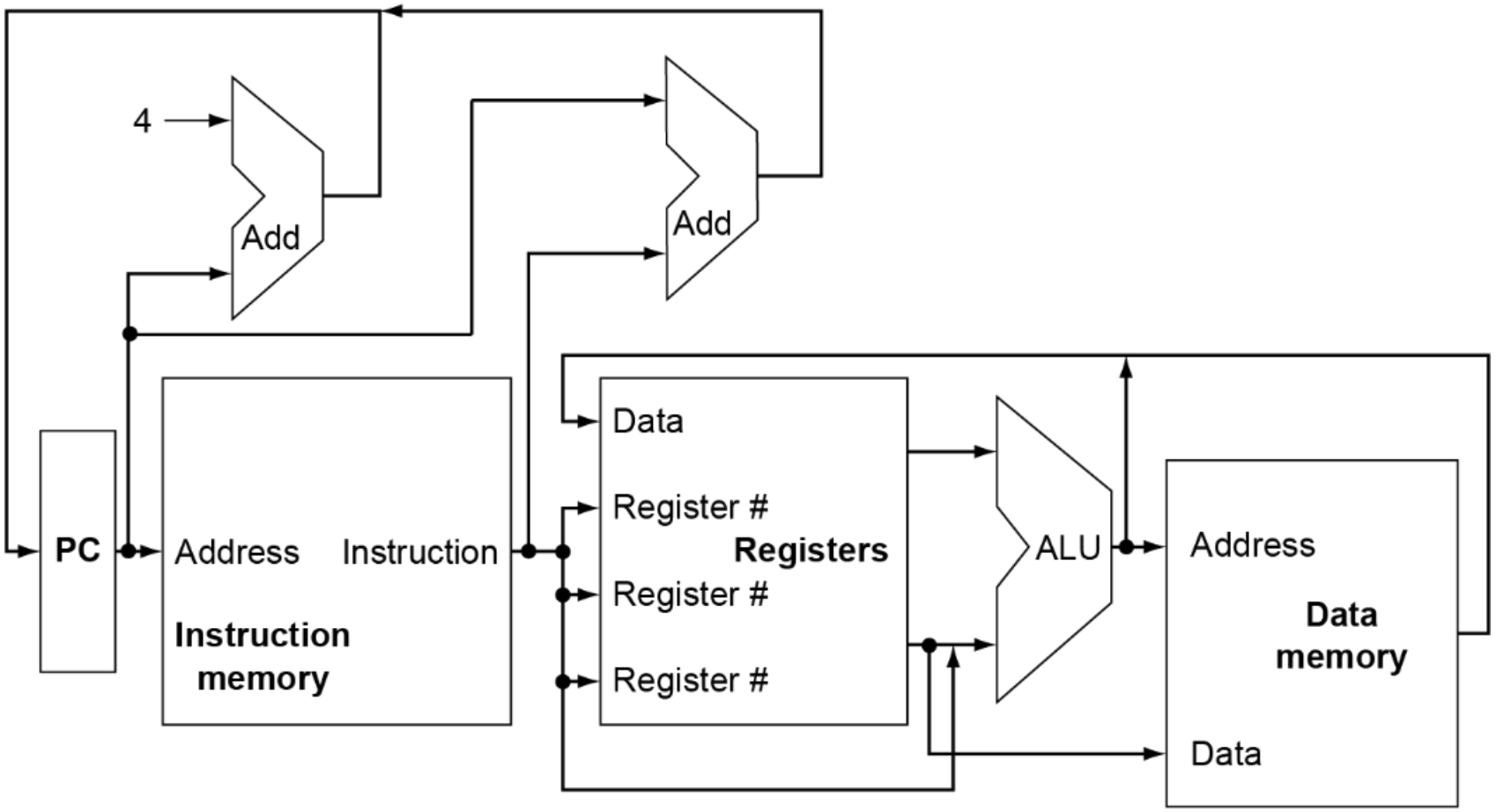
Introduction

- CPU performance factors
  - Instruction count
    - Determined by ISA and compiler
  - CPI and Cycle time
    - Determined by CPU hardware
- We will examine two RISC-V implementations
  - A simplified version
  - A more realistic pipelined version
- Simple subset, shows most aspects
  - Memory reference: `ld`, `sd`
  - Arithmetic/logical: `add`, `sub`, `and`, `or`
  - Control transfer: `beq`

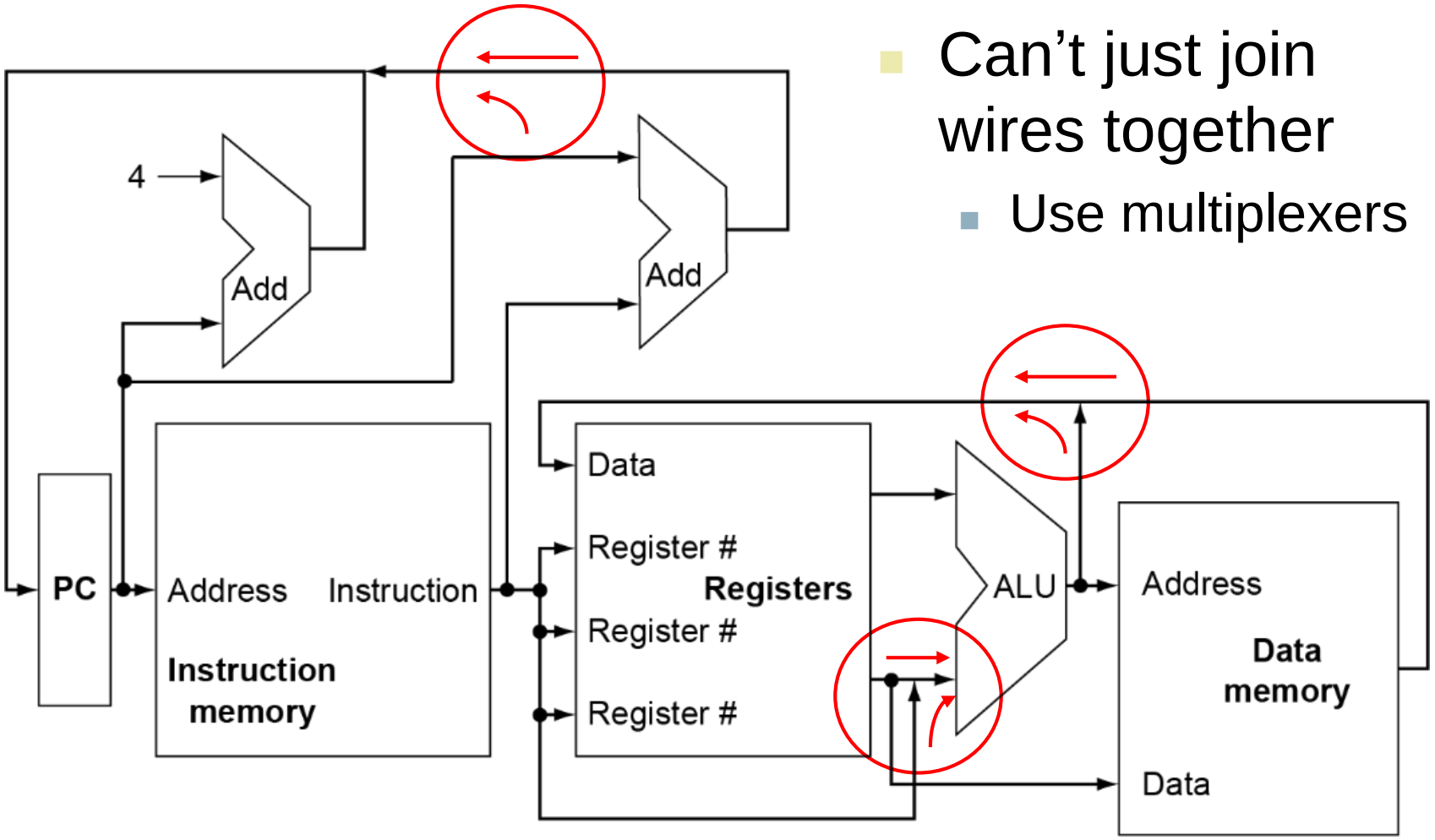
Instruction Execution

- PC → instruction memory, fetch instruction
- Register numbers → register file, read registers
- Depending on instruction class
  - Use ALU to calculate
    - Arithmetic result
    - Memory address for load/store
    - Branch comparison
  - Access data memory for load/store
  - PC ← target address or PC + 4

CPU Overview

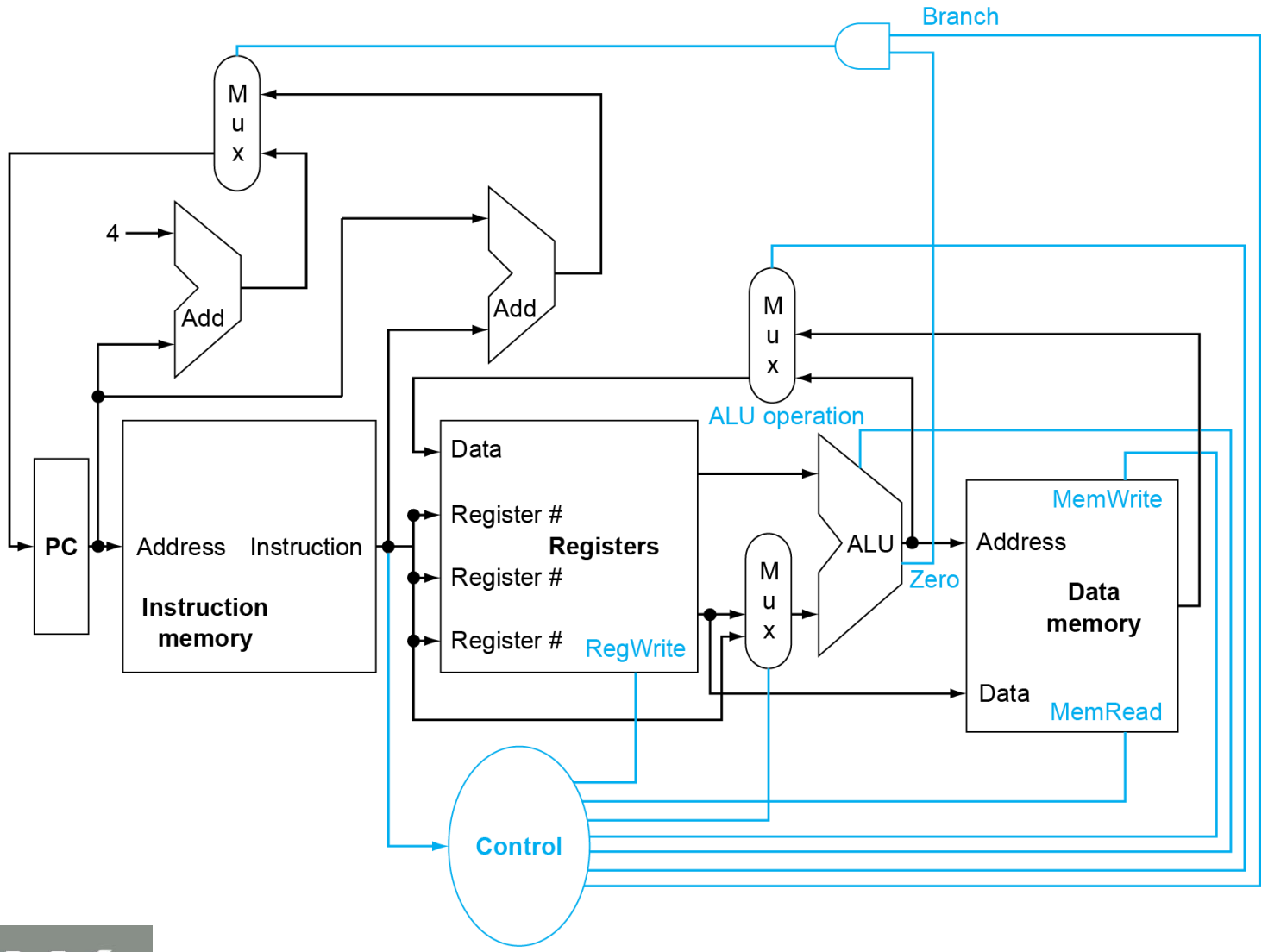


Multiplexers



- Can't just join wires together
  - Use multiplexers

Control

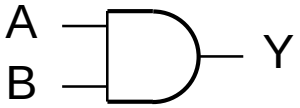

Branch
M
u
x
4
Add
Add
M
u
x
ALU operation
PC
Address
Instruction
Instruction
memory
Data
Register #
Registers
Register #
Register #
RegWrite
M
u
x
ALU
Zero
MemWrite
Address
Data
memory
Data
MemRead
Control

Logic Design Basics

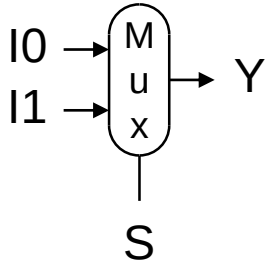
- Information encoded in binary
  - Low voltage = 0, High voltage = 1
  - One wire per bit
  - Multi-bit data encoded on multi-wire buses
- Combinational element
  - Operate on data
  - Output is a function of input
- State (sequential) elements
  - Store information

Combinational Elements

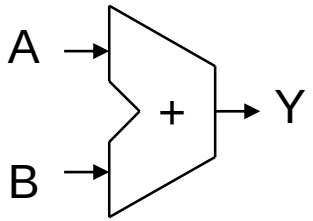
- AND-gate
  - Y = A & B



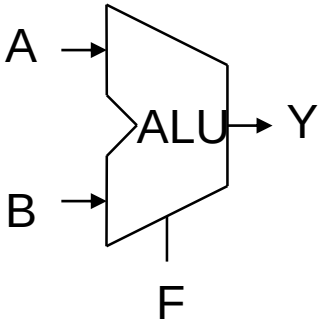
- Multiplexer
  - Y = S ? I1 : I0



- Adder
  - Y = A + B

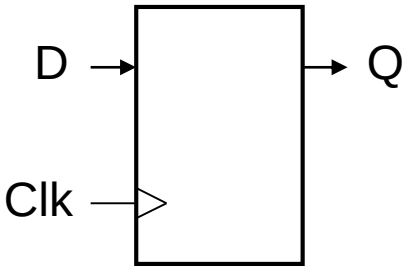


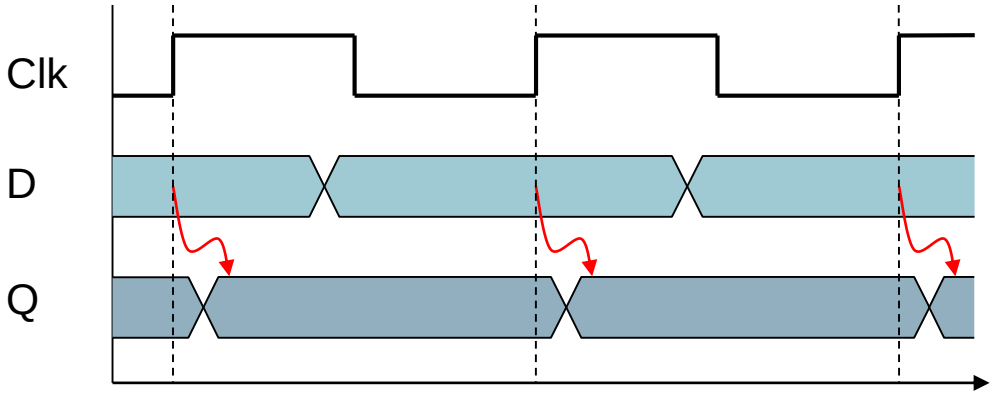
- Arithmetic/Logic Unit
  - Y = F(A, B)



Sequential Elements

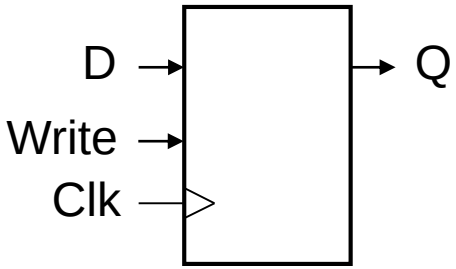
- Register: stores data in a circuit
  - Uses a clock signal to determine when to update the stored value
  - Edge-triggered: update when Clk changes from 0 to 1

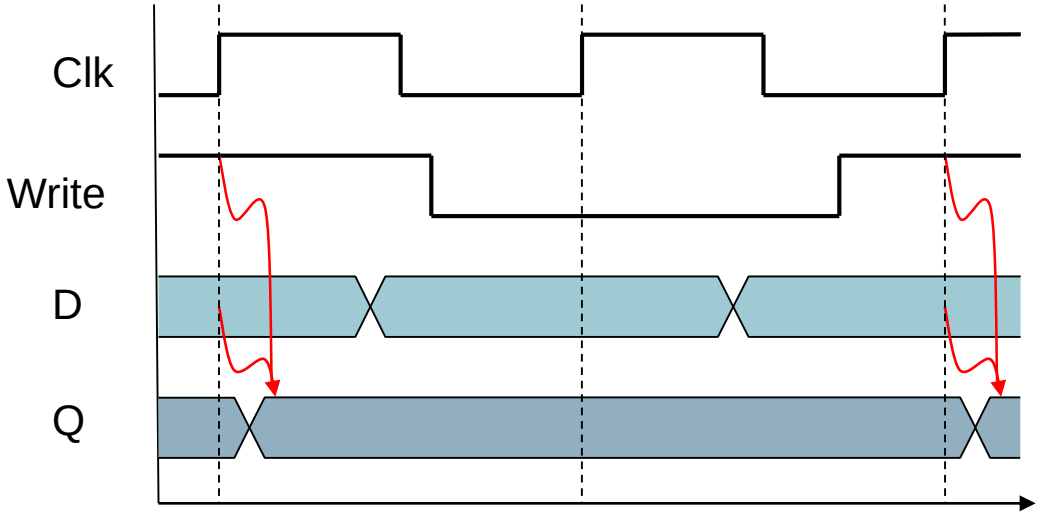




Sequential Elements

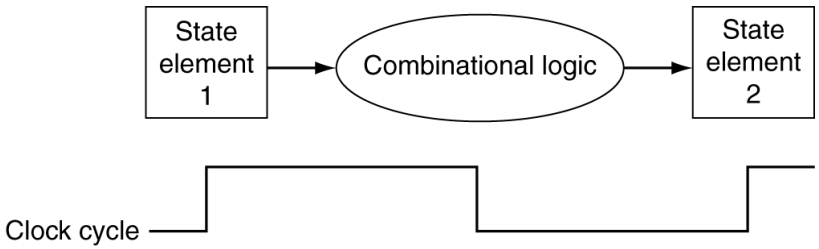
- Register with write control
  - Only updates on clock edge when write control input is 1
  - Used when stored value is required later

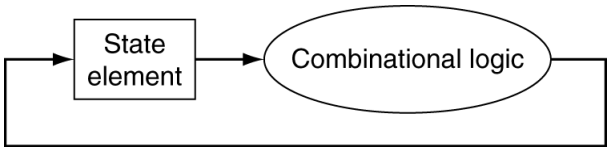




Clocking Methodology

- Combinational logic transforms data during clock cycles
  - Between clock edges
  - Input from state elements, output to state element
  - Longest delay determines clock period

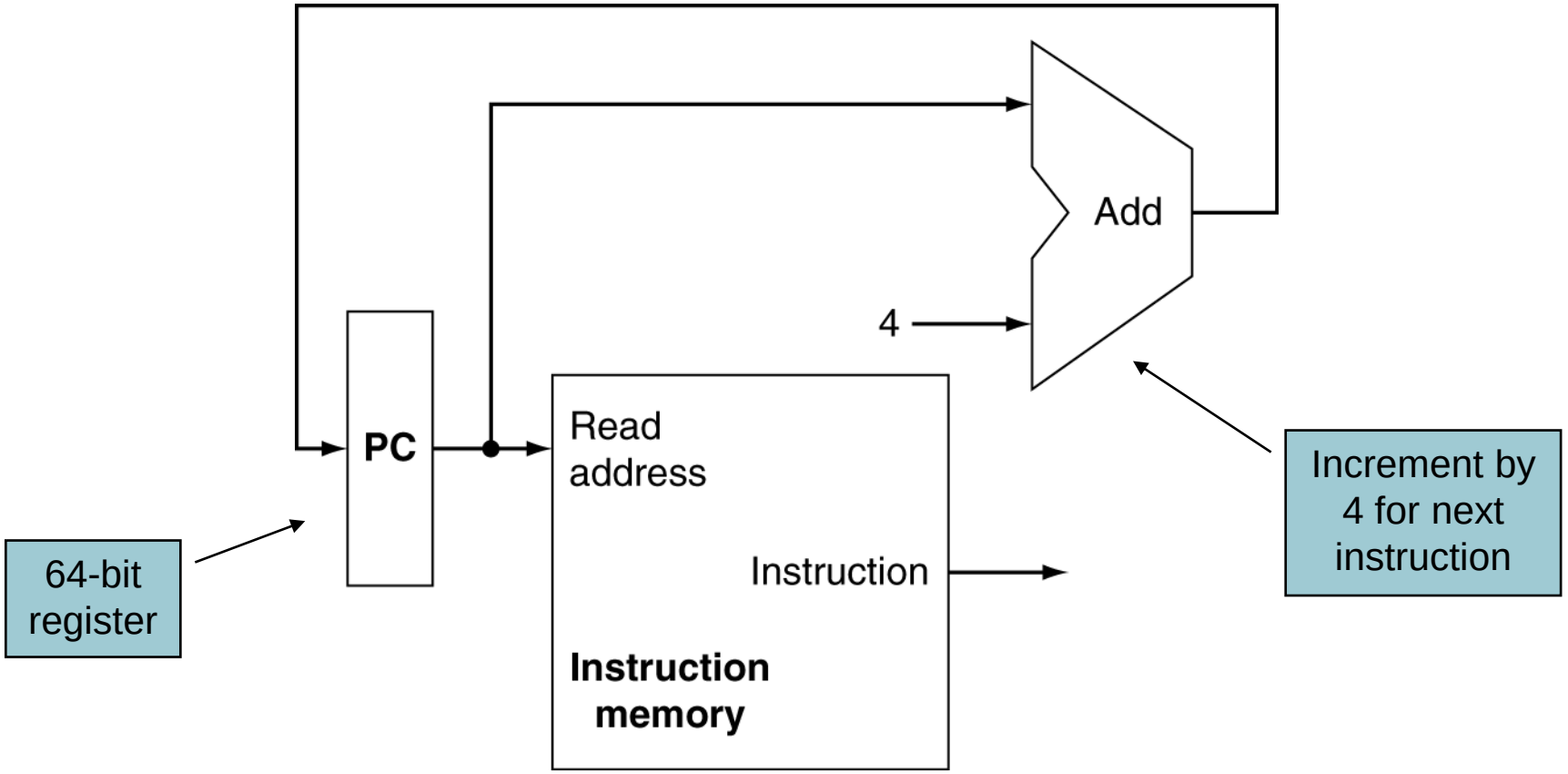




Building a Datapath

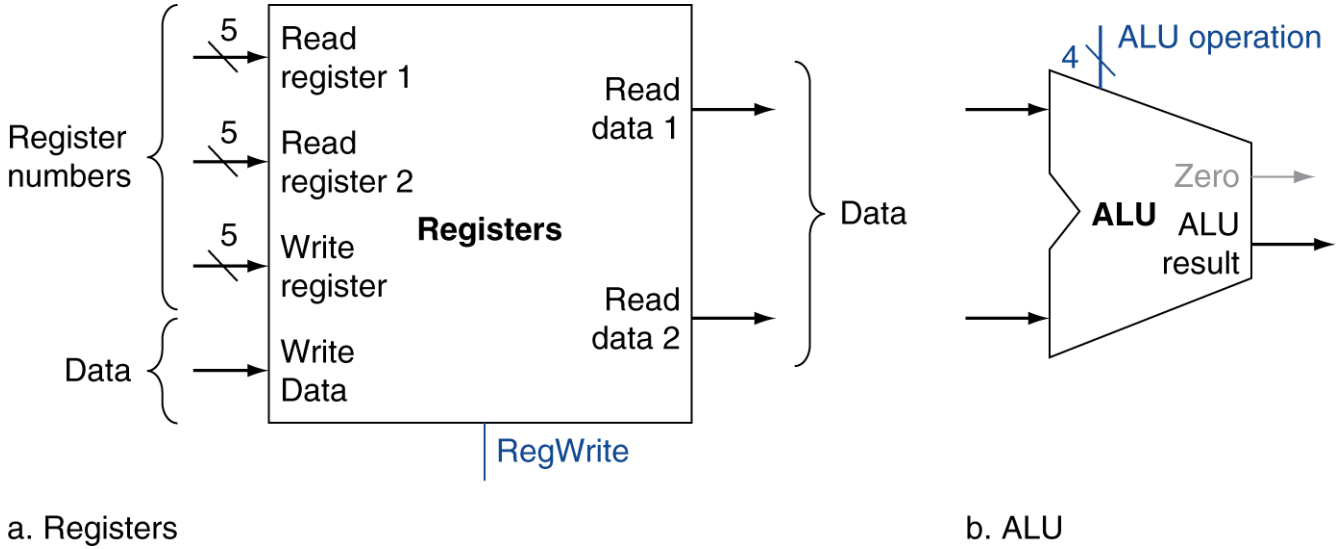
- Datapath
  - Elements that process data and addresses in the CPU
    - Registers, ALUs, mux's, memories, …
- We will build a RISC-V datapath incrementally
  - Refining the overview design

Instruction Fetch



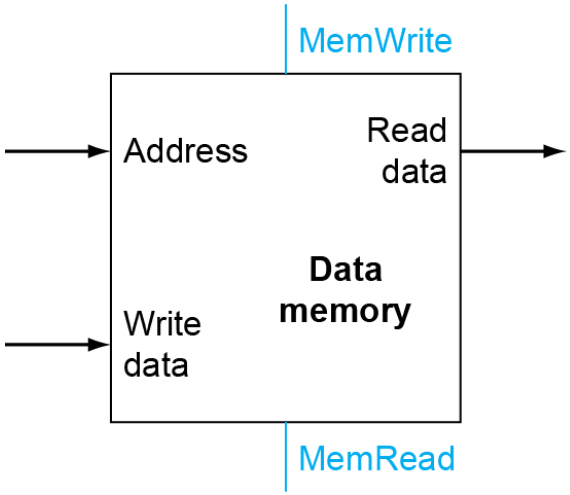
R-Format Instructions

- Read two register operands
- Perform arithmetic/logical operation
- Write register result

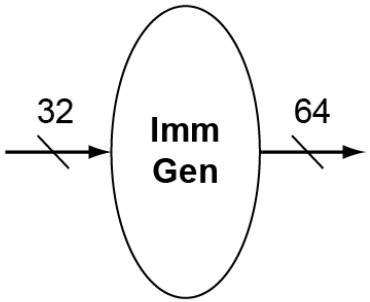


Load/Store Instructions

- Read register operands
- Calculate address using 12-bit offset
  - Use ALU, but sign-extend offset
- Load: Read memory and update register
- Store: Write register value to memory



a. Data memory unit

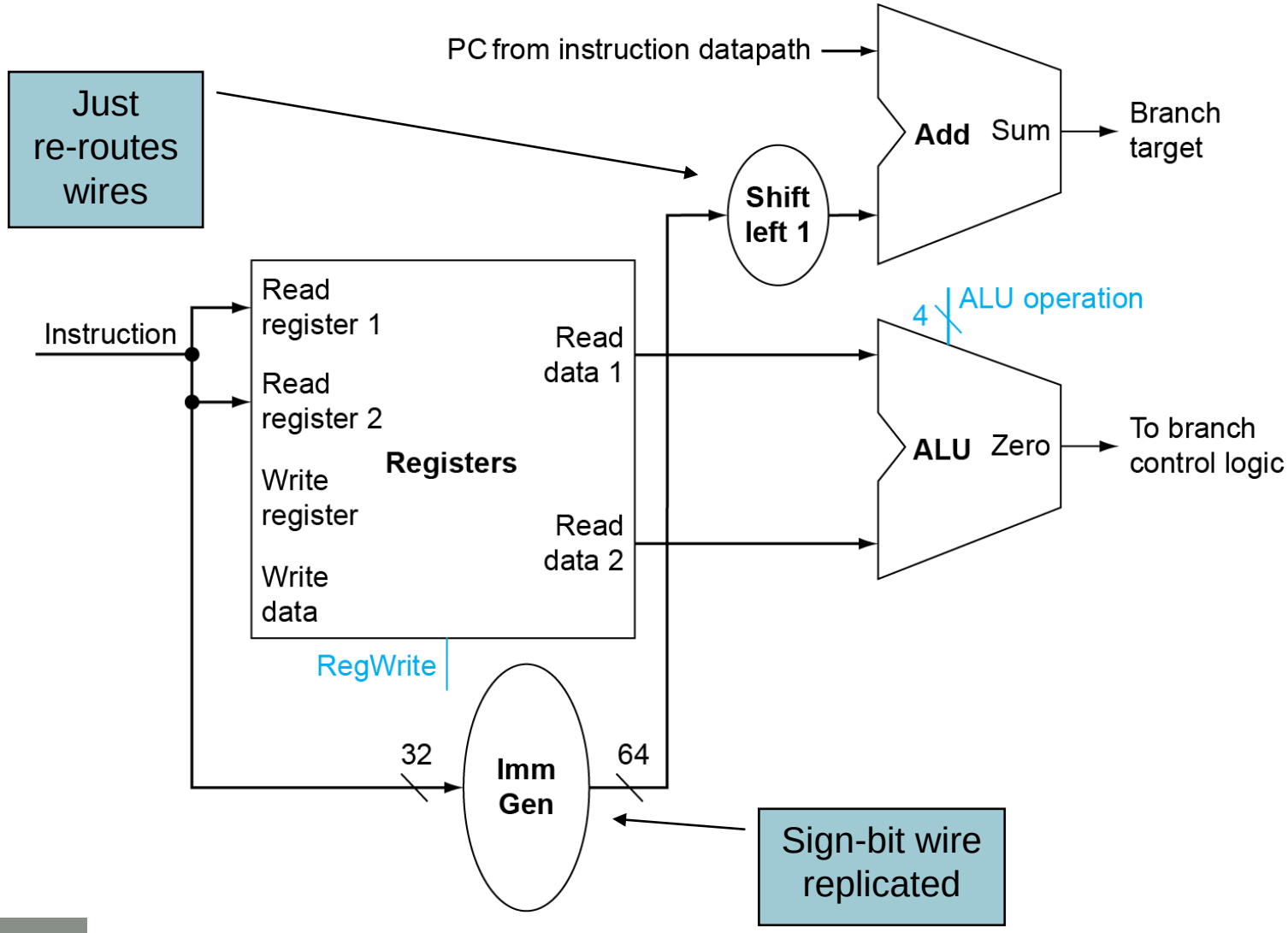


b. Immediate generation unit

Branch Instructions

- Read register operands
- Compare operands
  - Use ALU, subtract and check Zero output
- Calculate target address
  - Sign-extend displacement
  - Shift left 1 place (halfword displacement)
  - Add to PC value

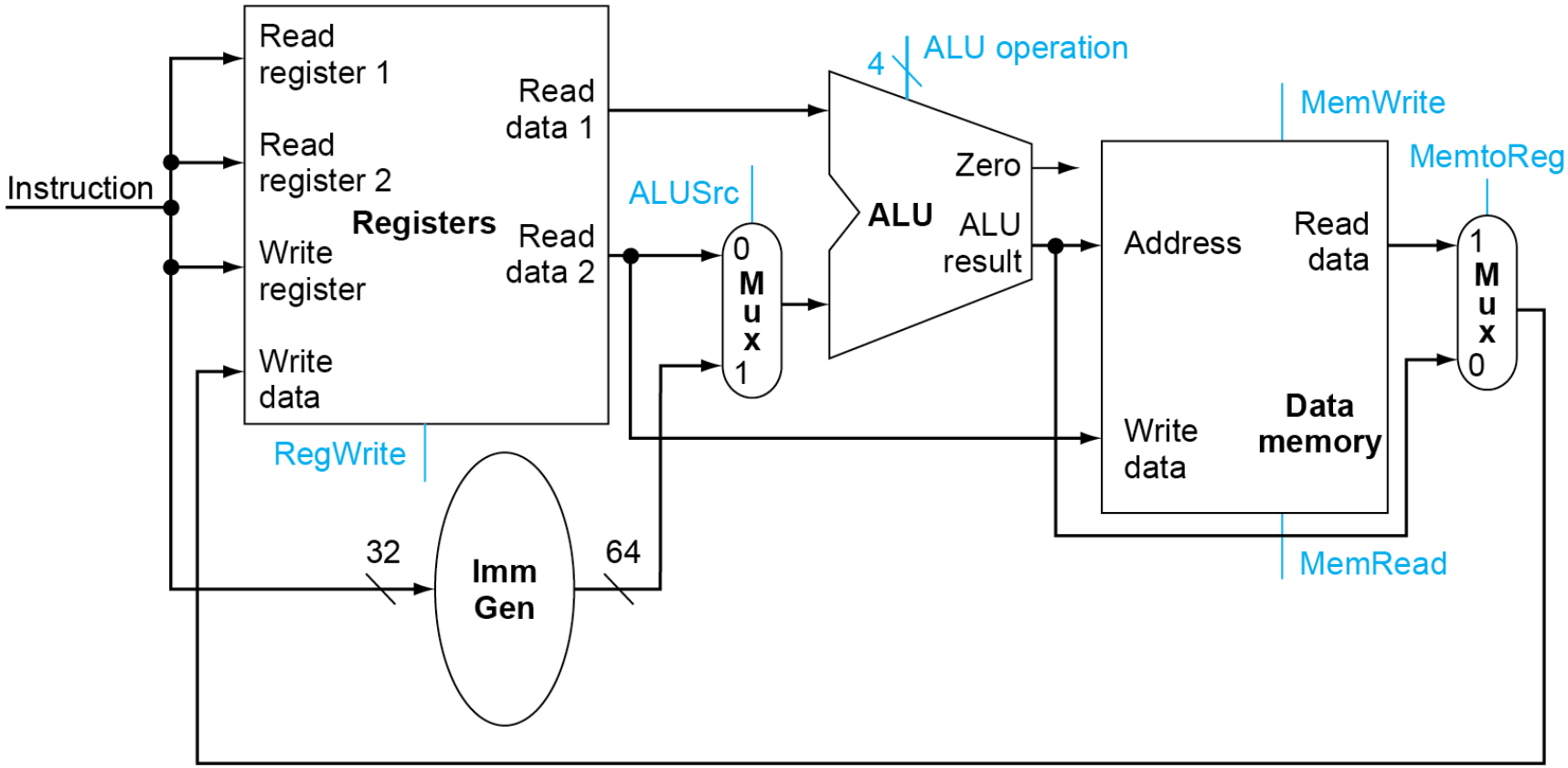
Branch Instructions



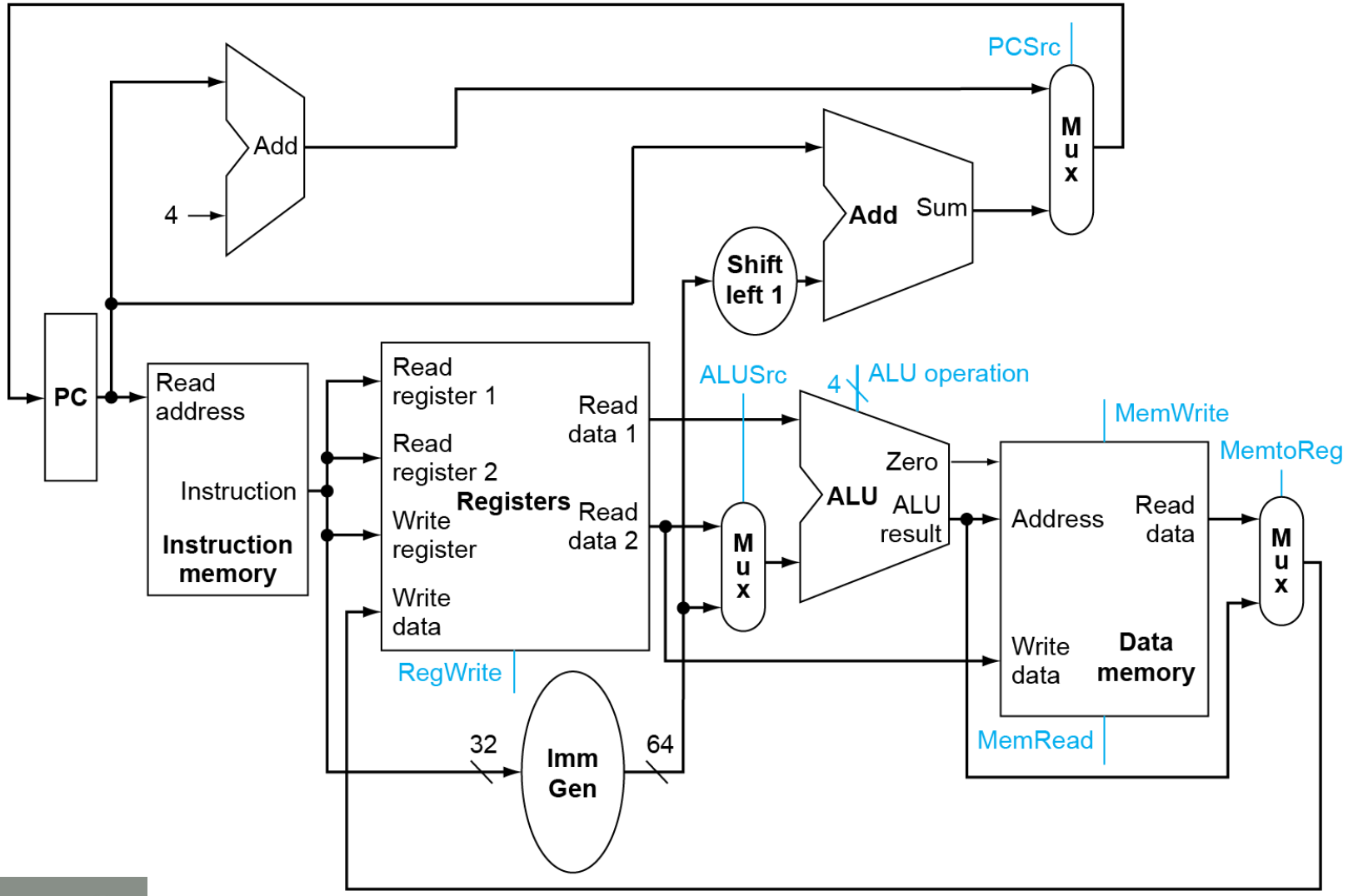
Composing the Elements

- First-cut data path does an instruction in one clock cycle
  - Each datapath element can only do one function at a time
  - Hence, we need separate instruction and data memories
- Use multiplexers where alternate data sources are used for different instructions

R-Type/Load/Store Datapath



Full Datapath



ALU Control

- ALU used for
  - Load/Store: F = add
  - Branch: F = subtract
  - R-type: F depends on opcode

ALU control	Function
0000	AND
0001	OR
0010	add
0110	subtract

ALU Control

- Assume 2-bit ALUOp derived from opcode
  - Combinational logic derives ALU control

opcode	ALUOp	Operation	Opcode field	ALU function	ALU control
ld	00	load register	XXXXXXXXXXX	add	0010
sd	00	store register	XXXXXXXXXXX	add	0010
beq	01	branch on equal	XXXXXXXXXXX	subtract	0110
R-type	10	add	100000	add	0010
		subtract	100010	subtract	0110
		AND	100100	AND	0000
		OR	100101	OR	0001

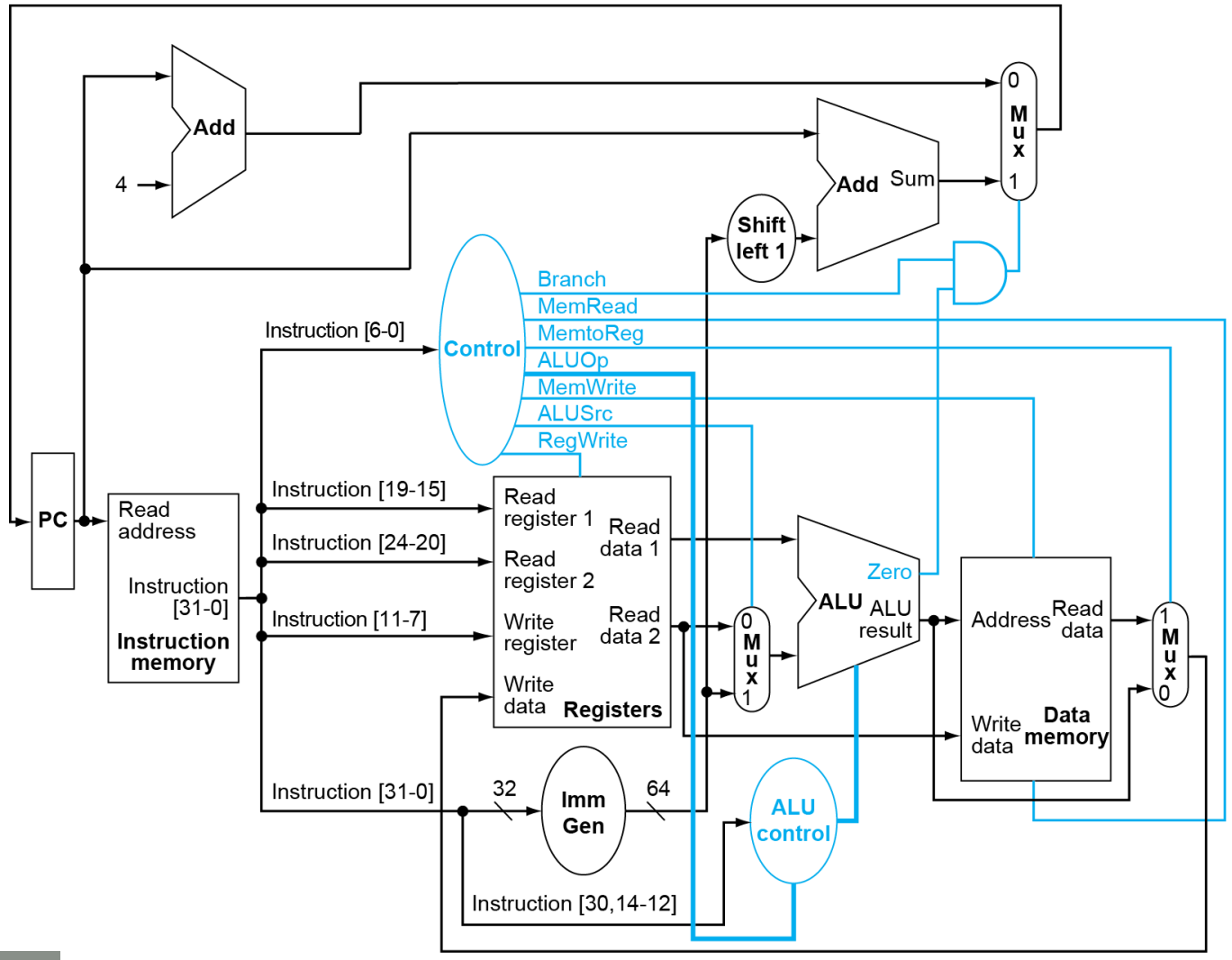
The Main Control Unit

- Control signals derived from instruction

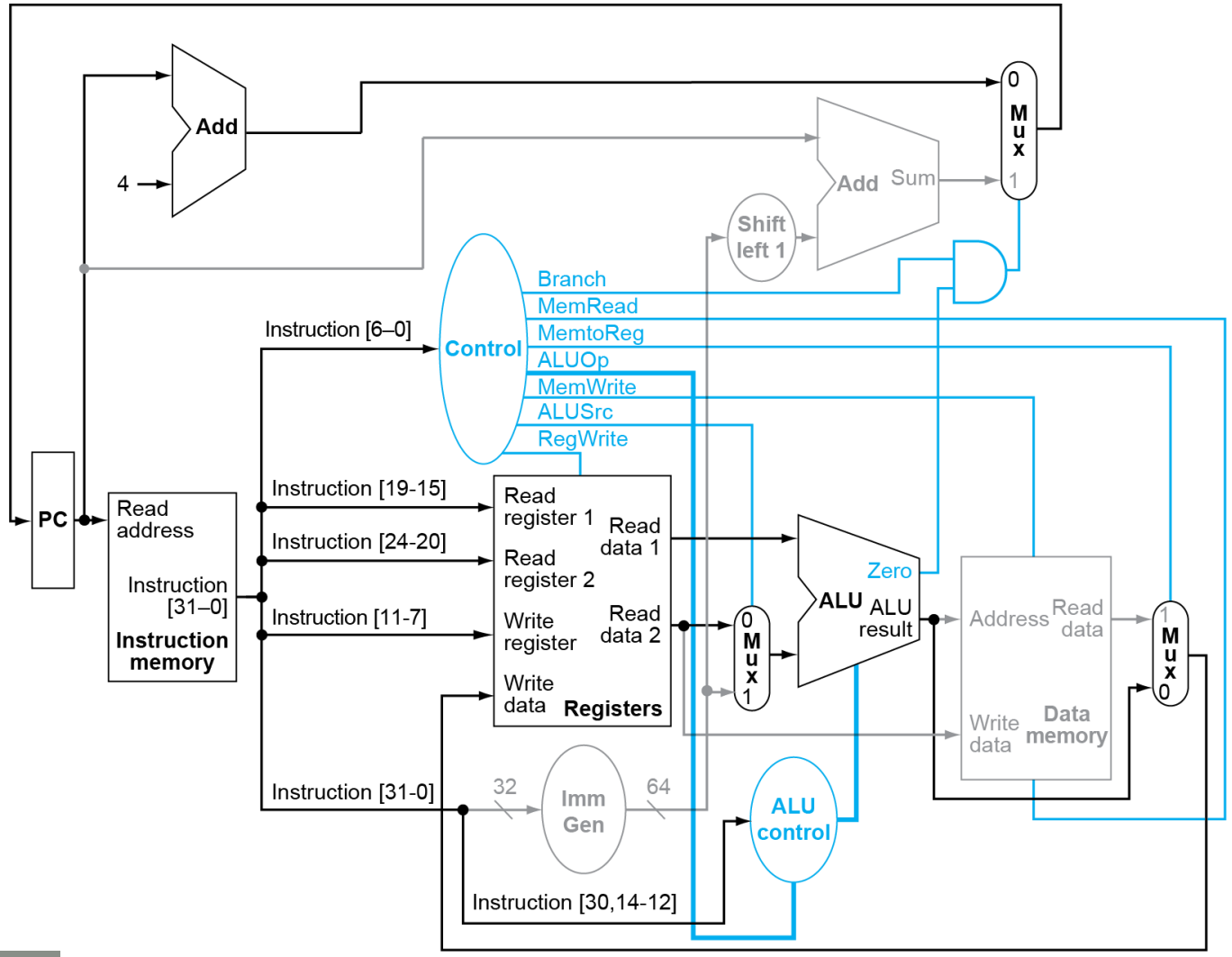
Name (Bit position)	Fields 31:25	24:20	19:15	14:12	11:7	6:0
(a) R-type	funct7	rs2	rs1	funct3	rd	opcode
(b) I-type	immediate[11:0]		rs1	funct3	rd	opcode
(c) S-type	immed[11:5]	rs2	rs1	funct3	immed[4:0]	opcode
(d) SB-type	immed[12,10:5]	rs2	rs1	funct3	immed[4:1,11]	opcode

ALUOp		Funct7 field							Funct3 field			
ALUOp1	ALUOp0	I[31]	I[30]	I[29]	I[28]	I[27]	I[26]	I[25]	I[14]	I[13]	I[12]	Operation
0	0	X	X	X	X	X	X	X	X	X	X	0010
X	1	X	X	X	X	X	X	X	X	X	X	0110
1	X	0	0	0	0	0	0	0	0	0	0	0010
1	X	0	1	0	0	0	0	0	0	0	0	0110
1	X	0	0	0	0	0	0	0	1	1	1	0000
1	X	0	0	0	0	0	0	0	1	1	0	0001

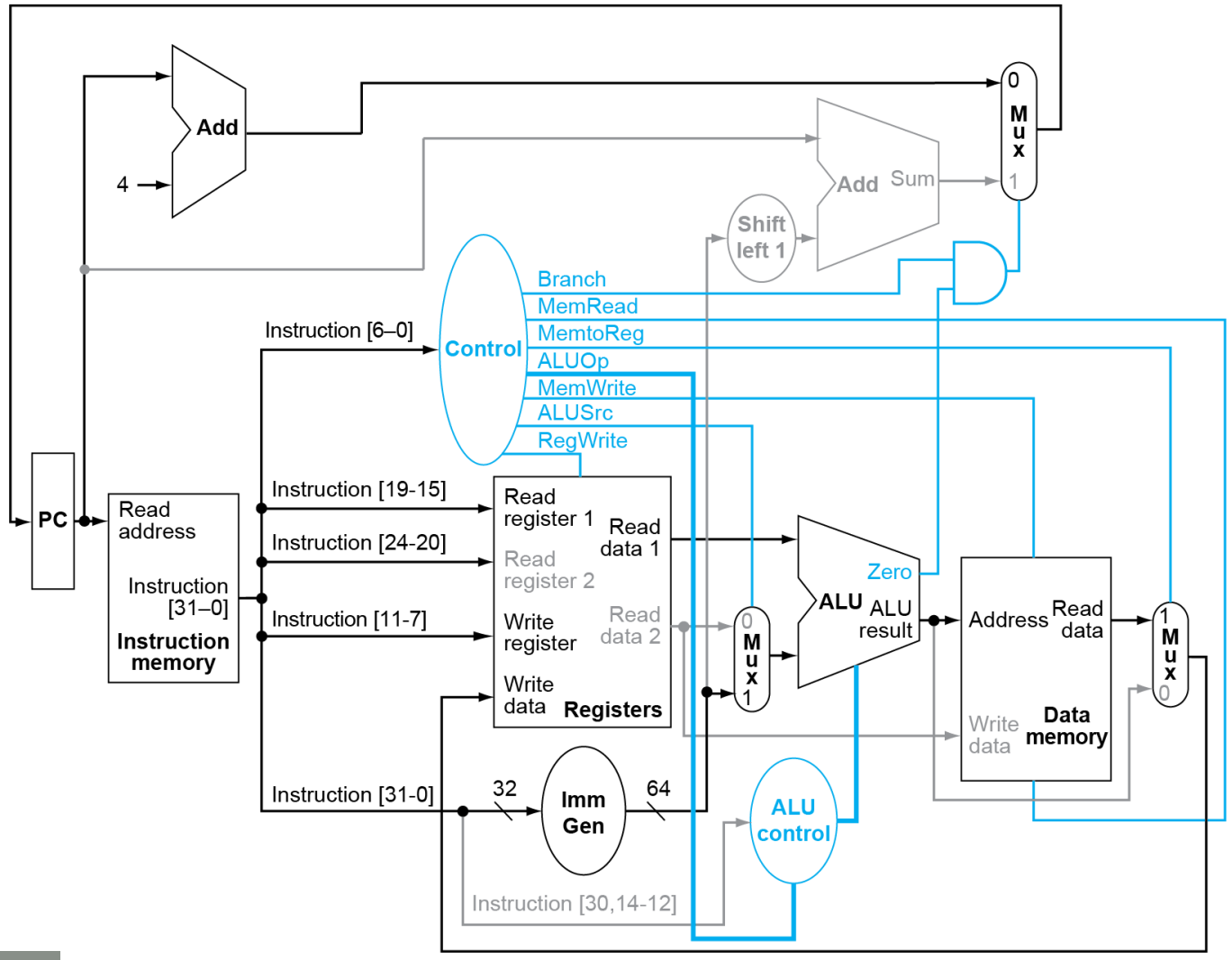
Datapath With Control



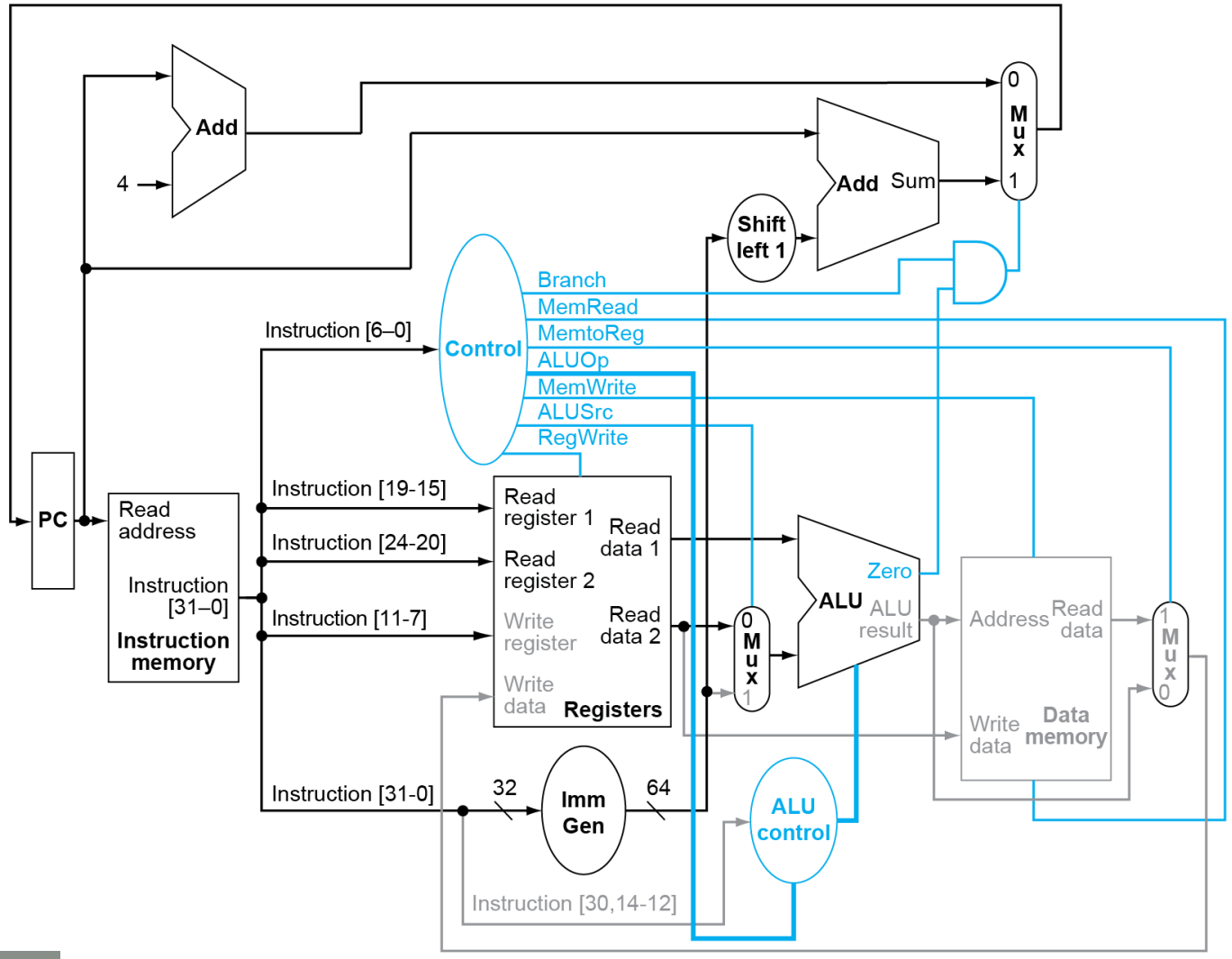
R-Type Instruction



Load Instruction



BEQ Instruction

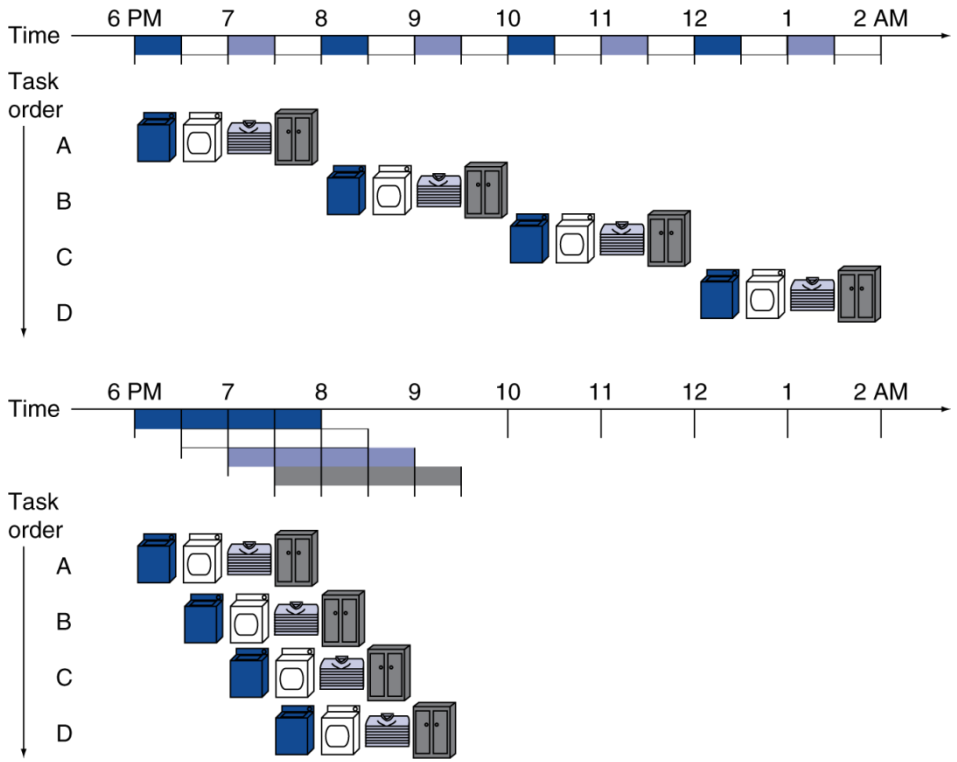


Performance Issues

- Longest delay determines clock period
  - Critical path: load instruction
  - Instruction memory → register file → ALU → data memory → register file
- Not feasible to vary period for different instructions
- Violates design principle
  - Making the common case fast
- We will improve performance by pipelining

Pipelining Analogy

- Pipelined laundry: overlapping execution
  - Parallelism improves performance



- Four loads:
  - Speedup
    = 8/3.5 = 2.3
- Non-stop:
  - Speedup
    = 2n/(0.5n + 1.5) ≈ 4
    = number of stages

RISC-V Pipeline

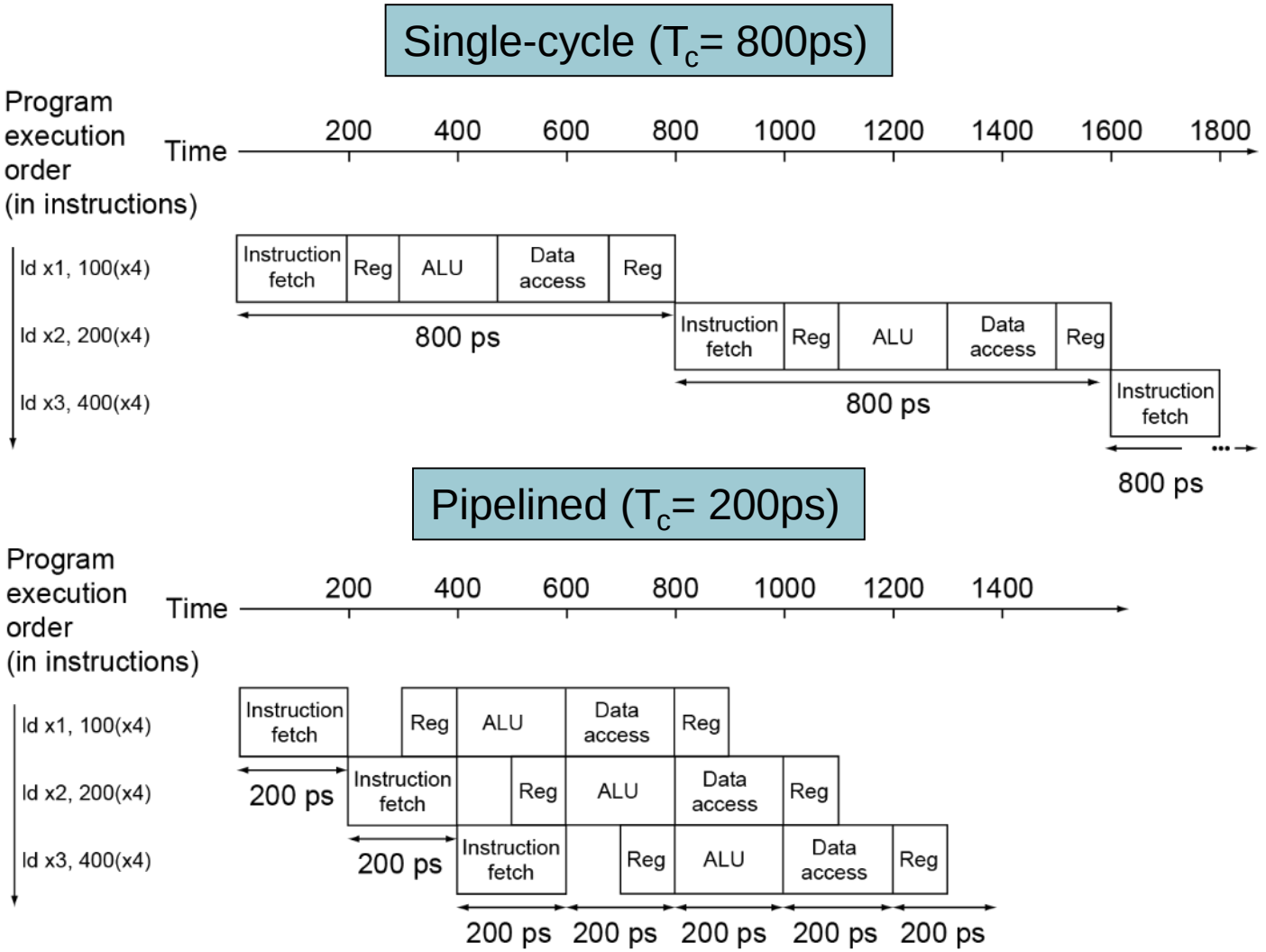
- Five stages, one step per stage
  1. IF: Instruction fetch from memory
  2. ID: Instruction decode & register read
  3. EX: Execute operation or calculate address
  4. MEM: Access memory operand
  5. WB: Write result back to register

Pipeline Performance

- Assume time for stages is
  - 100ps for register read or write
  - 200ps for other stages
- Compare pipelined datapath with single-cycle datapath

Instr	Instr fetch	Register read	ALU op	Memory access	Register write	Total time
ld	200ps	100 ps	200ps	200ps	100 ps	800ps
sd	200ps	100 ps	200ps	200ps		700ps
R-format	200ps	100 ps	200ps		100 ps	600ps
beq	200ps	100 ps	200ps			500ps

Pipeline Performance



Pipeline Speedup

- If all stages are balanced
  - i.e., all take the same time
  - Time between instructions$_{\text{pipelined}}$
    = $\dfrac{\text{Time between instructions}_{\text{nonpipelined}}}{\text{Number of stages}}$
- If not balanced, speedup is less
- Speedup due to increased throughput
  - Latency (time for each instruction) does not decrease

Pipelined Performance: Speed-Up Ratio

Given:

- *A pipeline of **K** stages*
- *Number of tasks (instructions, cars): **n***
- *Total time required to execute each task: t_n*
- *Execution time of each pipeline segment: t_p*
- *Execution time: (number of tasks) x (time/task)*

- ***Non-pipelined execution:*** $n.t_n$

- ***Pipelined execution:***
- *Execution time of first task* $(k.t_p)$ +
- *Execution time of remaining tasks* $(n-1).t_p$

$$= (k + n-1).t_p$$

Speed-up Ratio:
un-pipelined execution / pipelined execution

$$S = n.t_n / (k + n-1).t_p$$

If n >>>> k -1

$$S = n.t_n / n.t_p$$

$$S = t_n / t_p$$

$$S = k.t_p / t_p$$

$$S = k \text{ (Number of the pipeline stages)}$$

A Numerical Example

Given:

- *A pipeline of **K** = 4 stages*
- *Number of tasks **n = 100***
- *Execution time of each time segment: t_p = 20 ns*
- *Execution time of one task: $t_n = k. t_p = 20 .4 = 80$ ns*
- *Execution time: (number of tasks) x (time/task)*

- ***Non-pipelined execution:*** *$n.t_n = 100 . 80 = 8000$ ns.*

- ***Pipelined execution:***
- *Execution time of first task* $(k.t_p)$ +
- *Execution time of remaining tasks* $(n-1).t_p$

$$= (k + n-1).t_p = (4 + 100 -1). 20$$
$$= 2060$$

Speed-up Ratio:

un-pipelined execution / pipelined execution

$$S = 8000\ ns \,/\, 2060\ ns$$
$$= 3.88$$

If n = 10000 >>>> 4 - 1

$$S = 10000 \,.\, 80 \,/\, (4 + 10000 - 1)\ \ (20)$$
$$S = 4$$

MIPS:

Million Instruction Per Second

Un-Pipelined Case :

MIPS **=** *100 Instructions / 8000 ns.* 10^6

= 12.5

Pipelined Case :

MIPS **=** *100 Instructions / 2060 ns.* 10^6

~ = 50

CPI (Un-Pipelined) = ?

CPI (Ideal pipeline) = ?

Pipelining and ISA Design

- RISC-V ISA designed for pipelining
  - All instructions are 32-bits
    - Easier to fetch and decode in one cycle
    - c.f. x86: 1- to 17-byte instructions
  - Few and regular instruction formats
    - Can decode and read registers in one step
  - Load/store addressing
    - Can calculate address in 3rd stage, access memory in 4th stage

Hazards

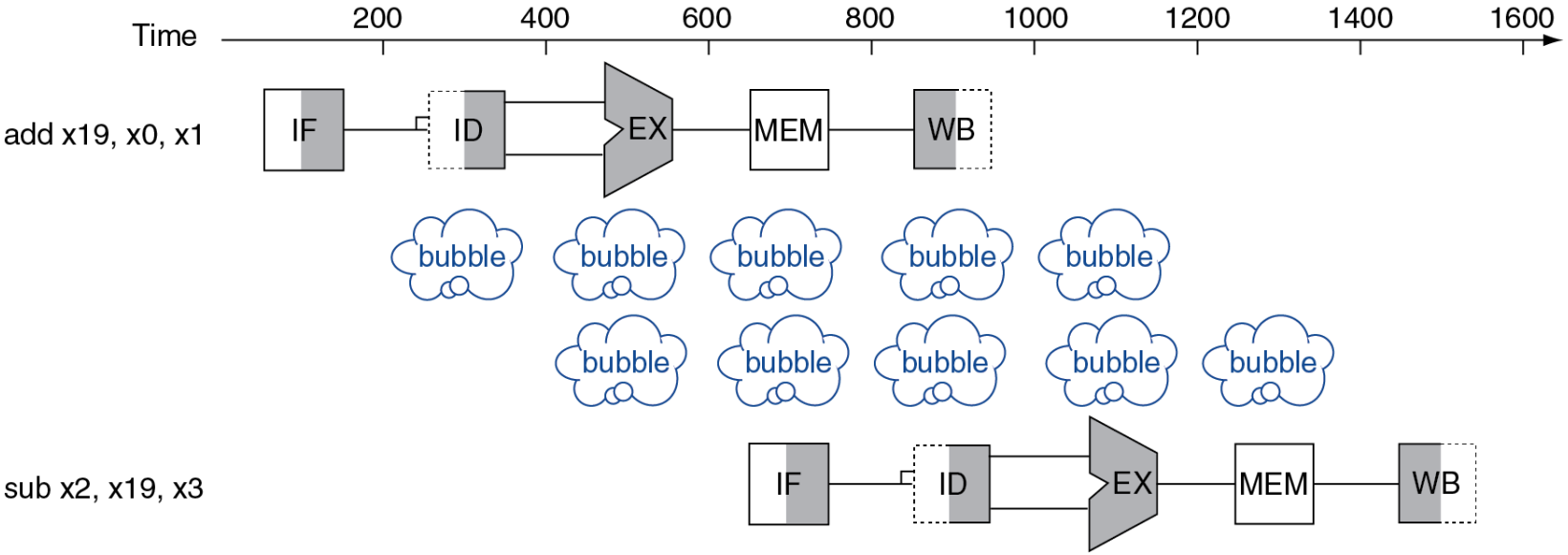
- Situations that prevent starting the next instruction in the next cycle
- Structural hazards
  - A required resource is busy
- Data hazard
  - Need to wait for previous instruction to complete its data read/write
- Control hazard
  - Deciding on control action depends on previous instruction

Structural Hazards

- Conflict for use of a resource
- In RISC-V pipeline with a single memory
  - Load/store requires data access
  - Instruction fetch would have to *stall* for that cycle
    - Would cause a pipeline “bubble”
- Hence, pipelined datapaths require separate instruction/data memories
  - Or separate instruction/data caches

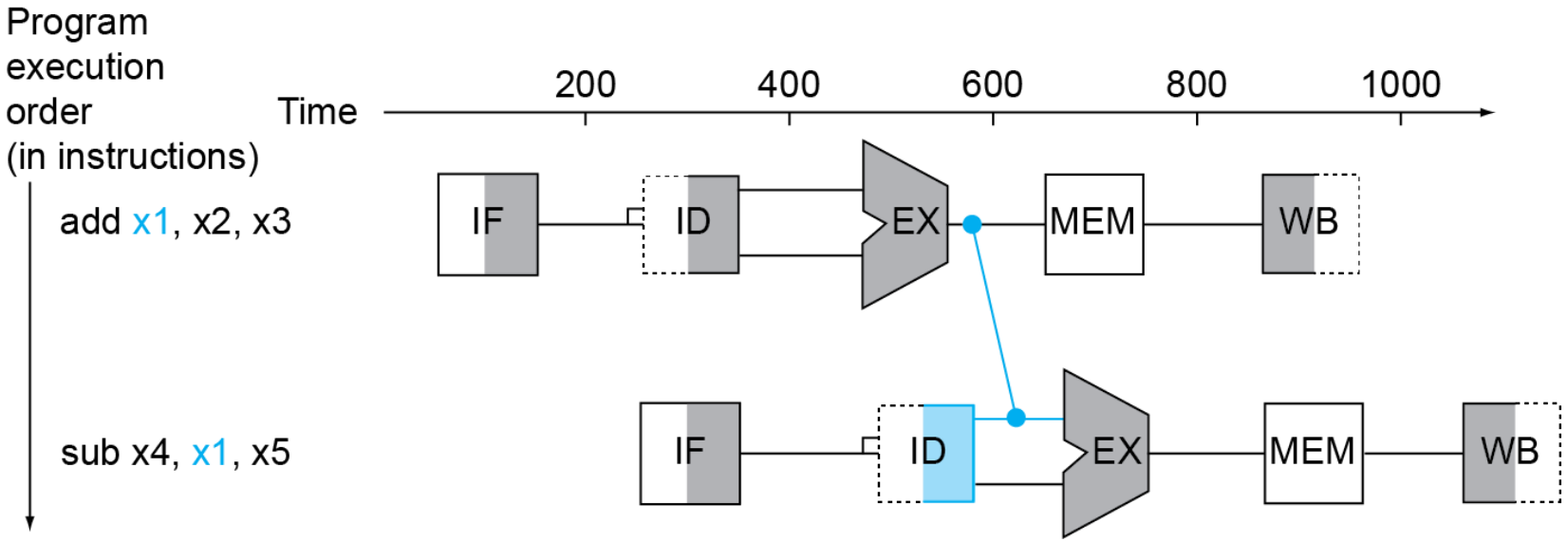
Data Hazards

- An instruction depends on completion of data access by a previous instruction
  - `add  x19, x0, x1`
    `sub  x2, x19, x3`



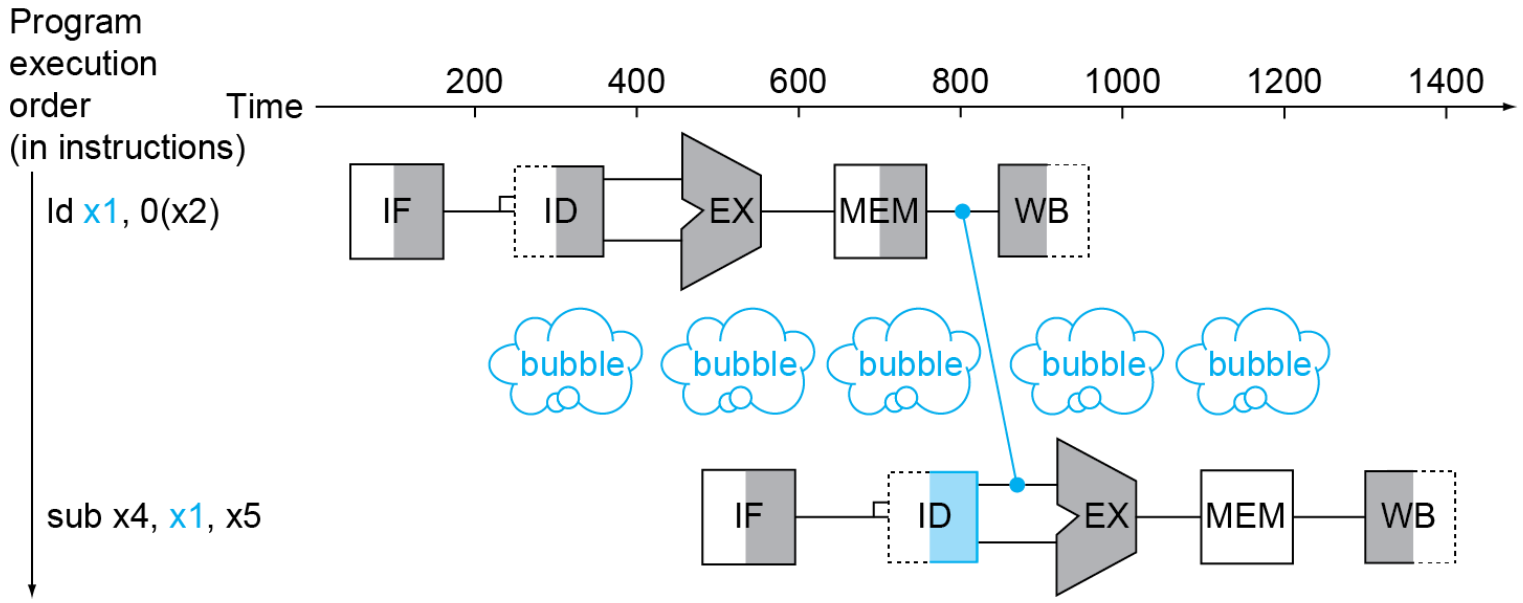
Forwarding (aka Bypassing)

- Use result when it is computed
  - Don’t wait for it to be stored in a register
  - Requires extra connections in the datapath



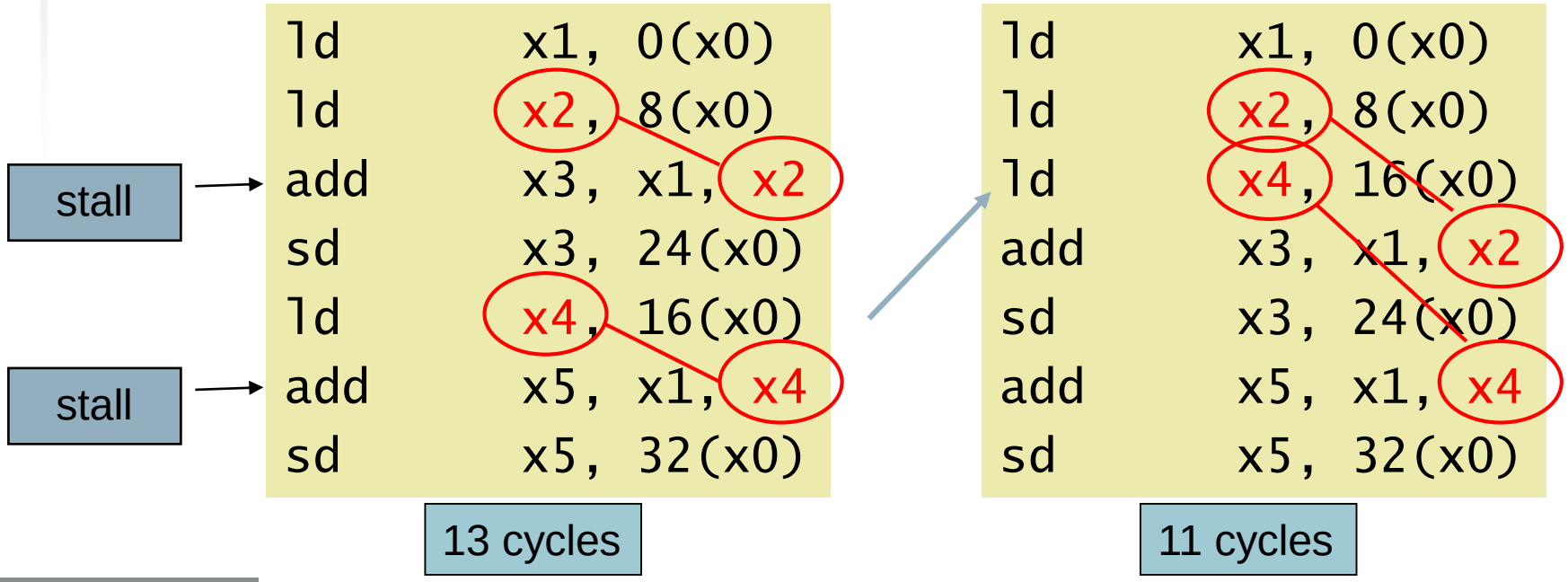
Load-Use Data Hazard

- Can’t always avoid stalls by forwarding
  - If value not computed when needed
  - Can’t forward backward in time!



Code Scheduling to Avoid Stalls

- Reorder code to avoid use of load result in the next instruction
- C code for `a = b + e; c = b + f;`

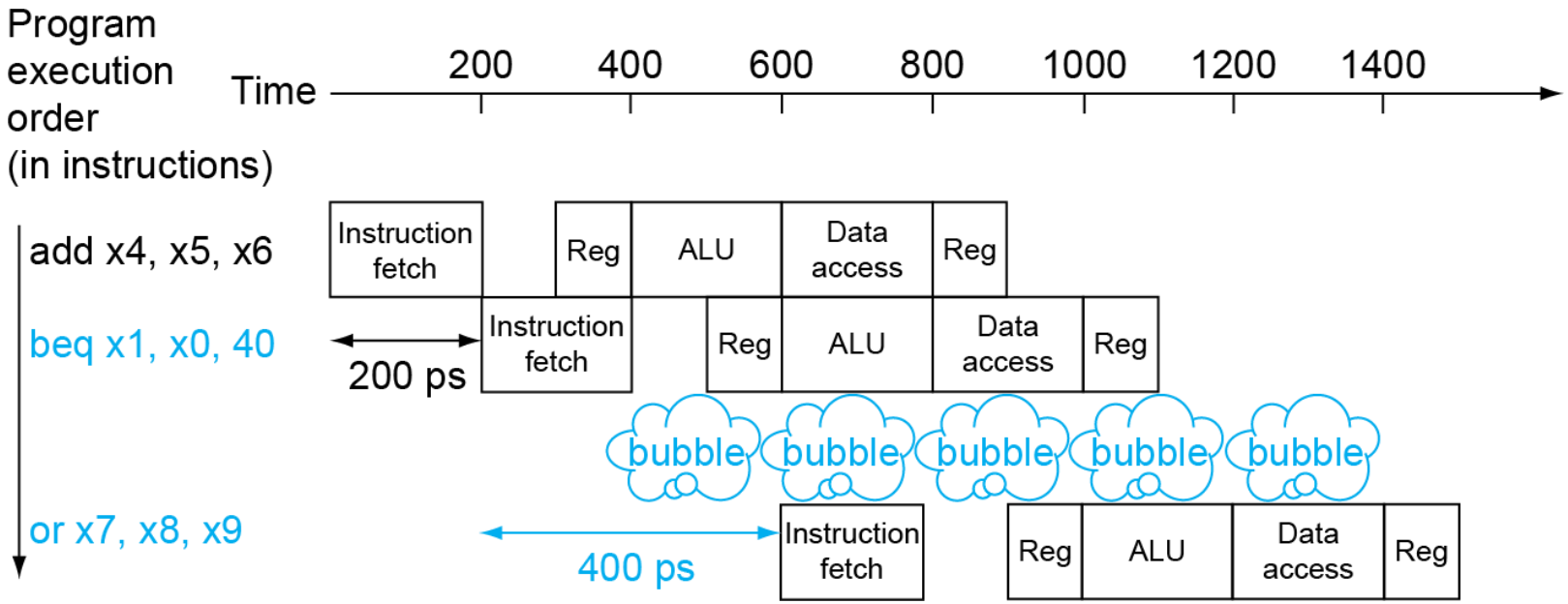


Control Hazards

- Branch determines flow of control
  - Fetching next instruction depends on branch outcome
  - Pipeline can’t always fetch correct instruction
    - Still working on ID stage of branch
- In RISC-V pipeline
  - Need to compare registers and compute target early in the pipeline
  - Add hardware to do it in ID stage

Stall on Branch

- Wait until branch outcome determined before fetching next instruction



Branch Prediction

- Longer pipelines can't readily determine branch outcome early
  - Stall penalty becomes unacceptable
- Predict outcome of branch
  - Only stall if prediction is wrong
- In RISC-V pipeline
  - Can predict branches not taken
  - Fetch instruction after branch, with no delay

More-Realistic Branch Prediction

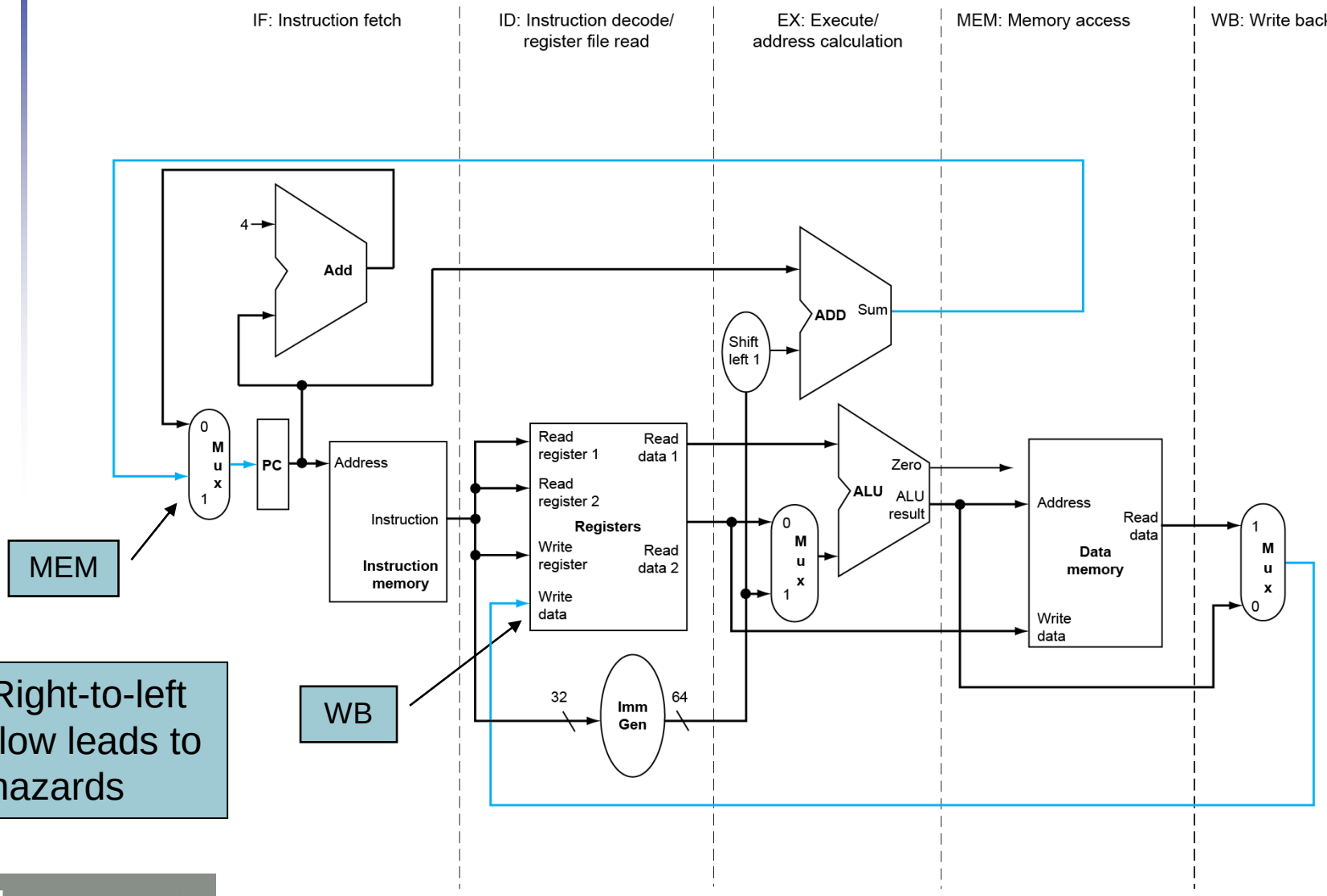
- Static branch prediction
  - Based on typical branch behavior
  - Example: loop and if-statement branches
    - Predict backward branches taken
    - Predict forward branches not taken
- Dynamic branch prediction
  - Hardware measures actual branch behavior
    - e.g., record recent history of each branch
  - Assume future behavior will continue the trend
    - When wrong, stall while re-fetching, and update history

Pipeline Summary

The BIG Picture

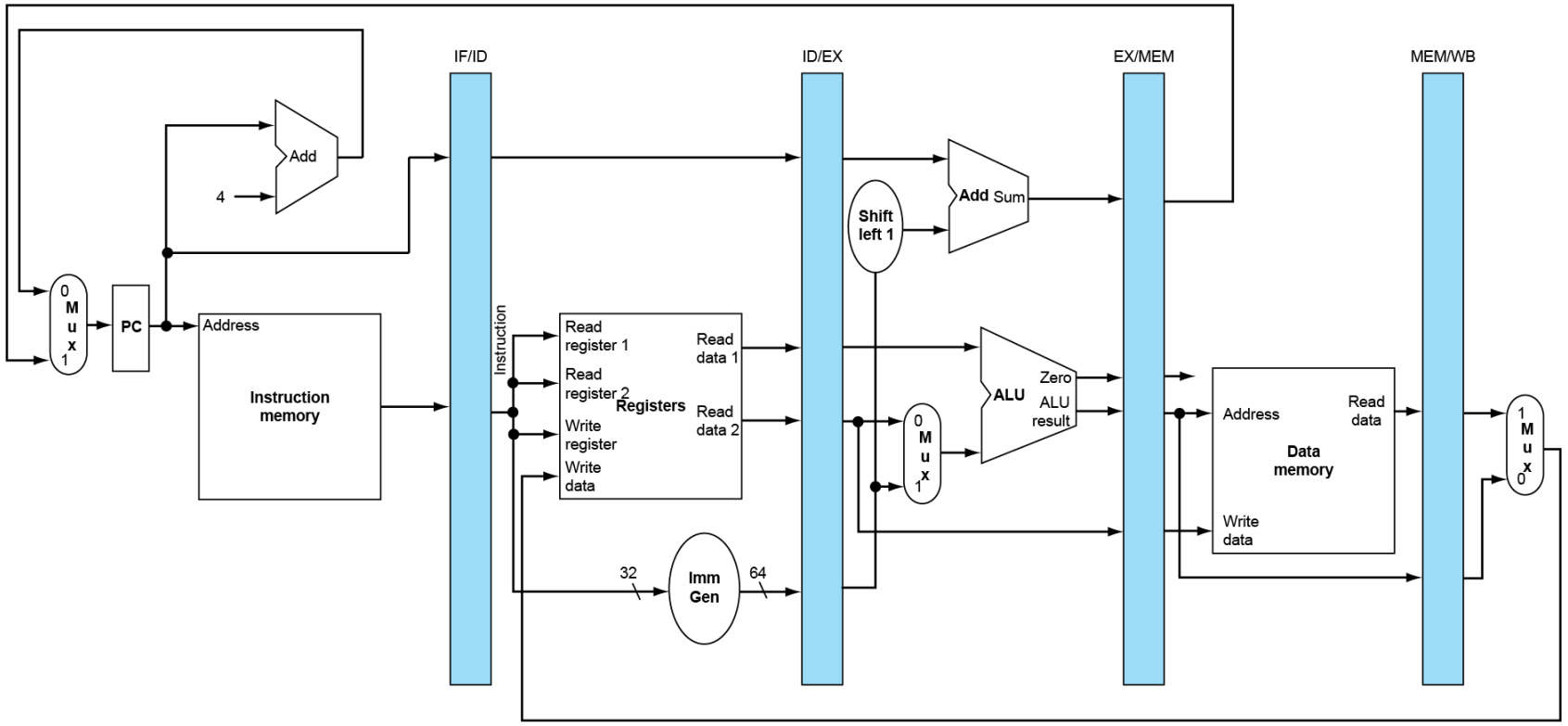
- Pipelining improves performance by increasing instruction throughput
  - Executes multiple instructions in parallel
  - Each instruction has the same latency
- Subject to hazards
  - Structure, data, control
- Instruction set design affects complexity of pipeline implementation

RISC-V Pipelined Datapath



Pipeline registers

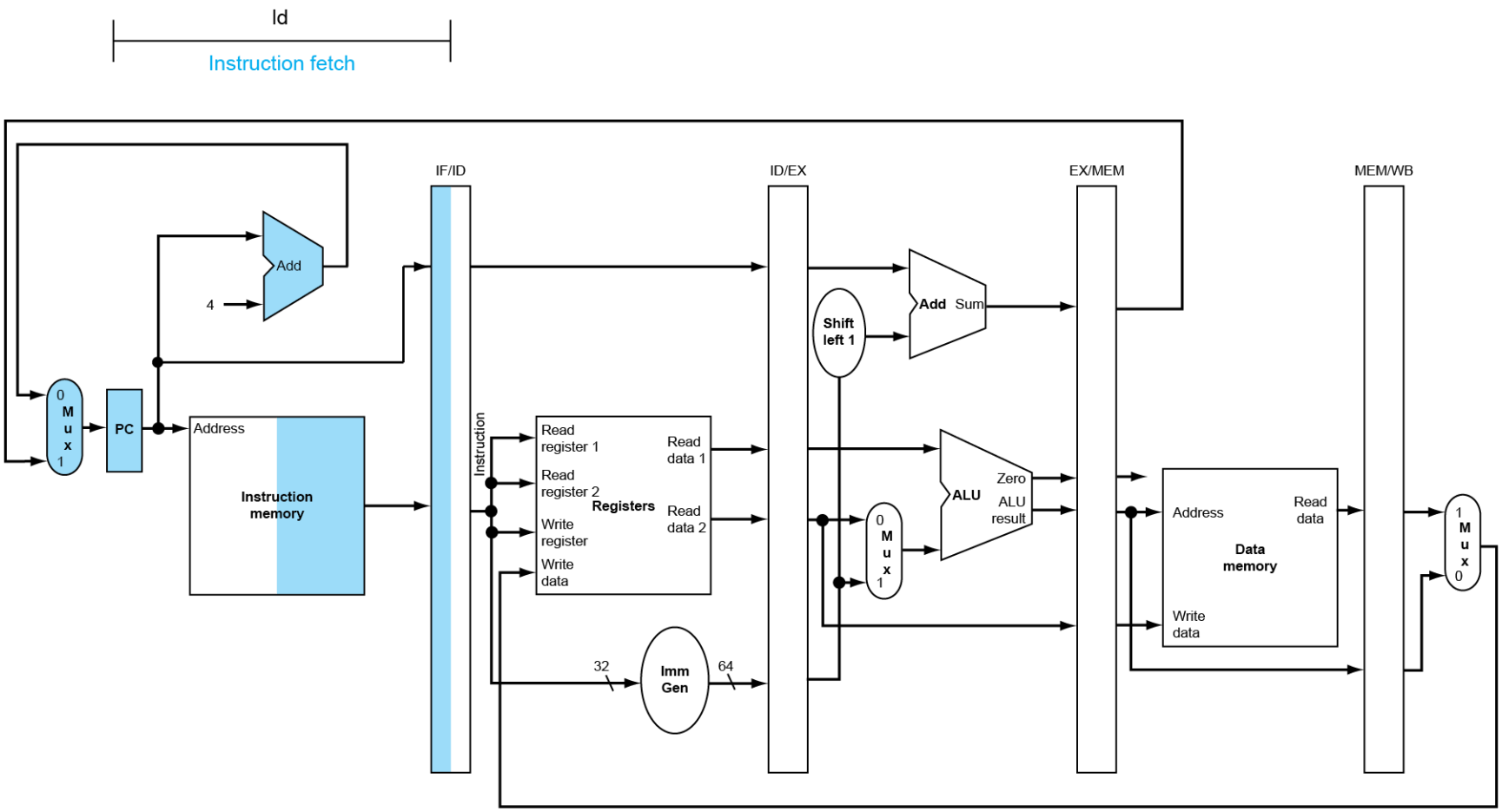
- Need registers between stages
  - To hold information produced in previous cycle



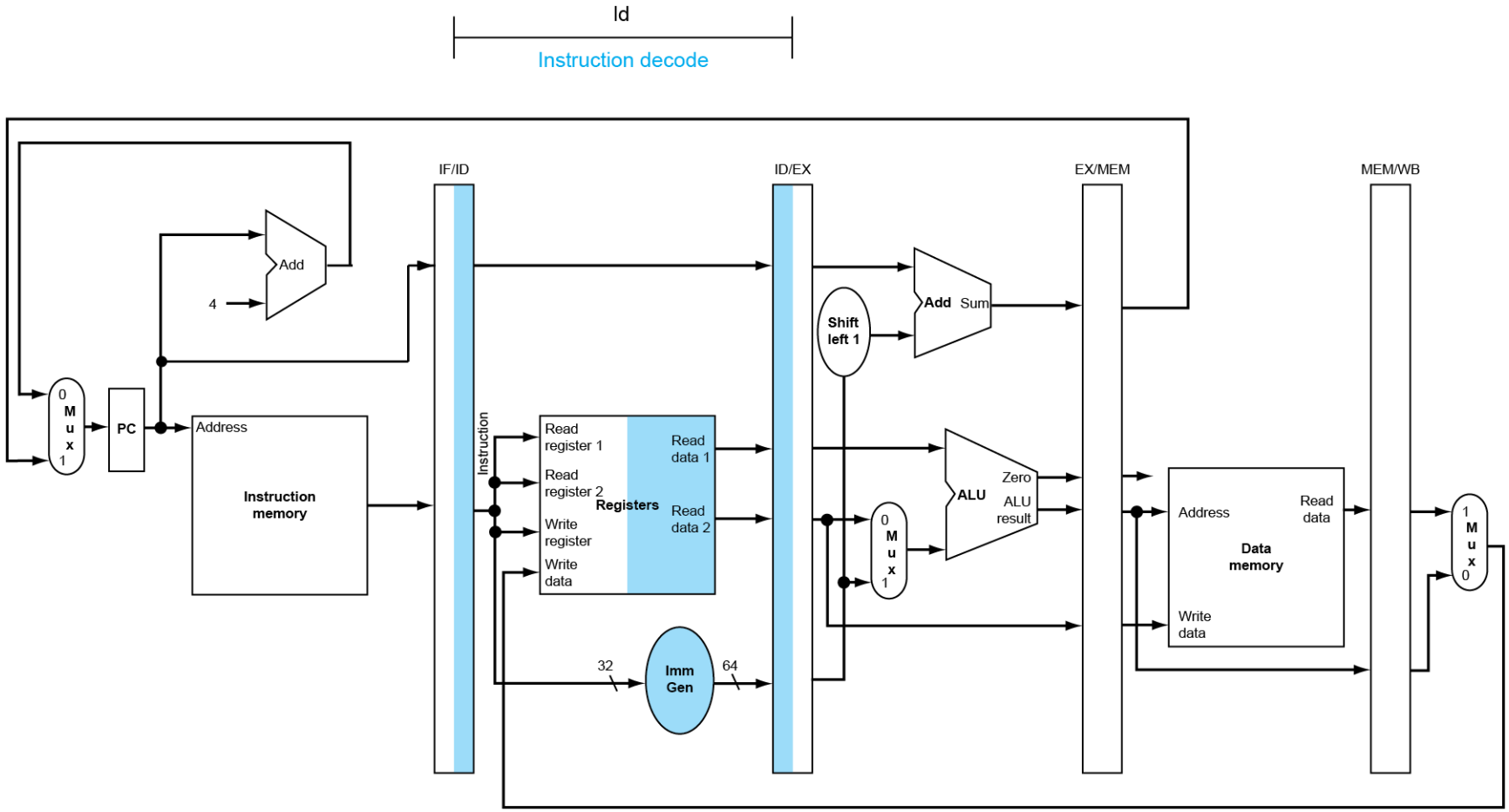
Pipeline Operation

- Cycle-by-cycle flow of instructions through the pipelined datapath
  - “Single-clock-cycle” pipeline diagram
    - Shows pipeline usage in a single cycle
    - Highlight resources used
  - c.f. “multi-clock-cycle” diagram
    - Graph of operation over time
- We’ll look at “single-clock-cycle” diagrams for load & store

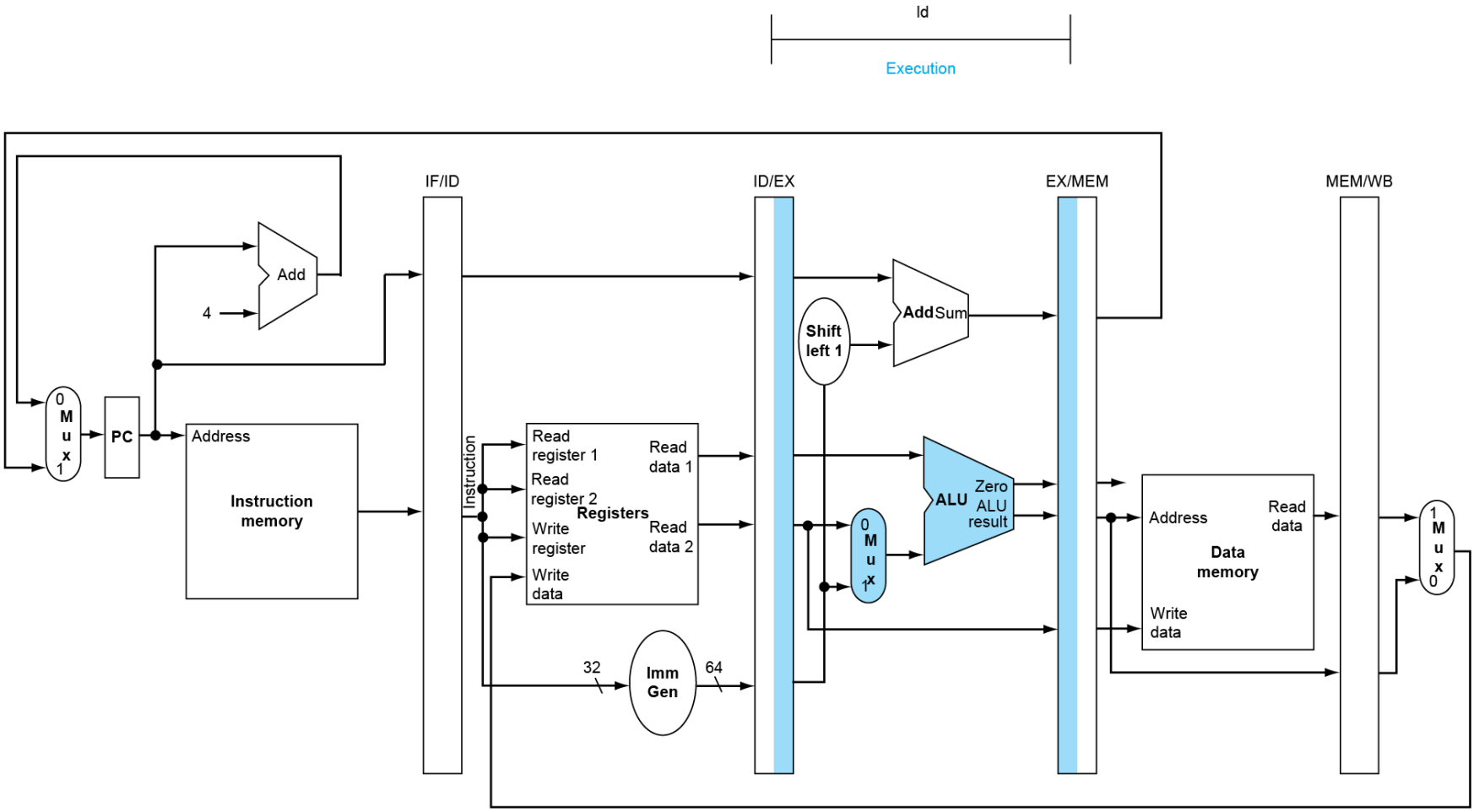
IF for Load, Store, …



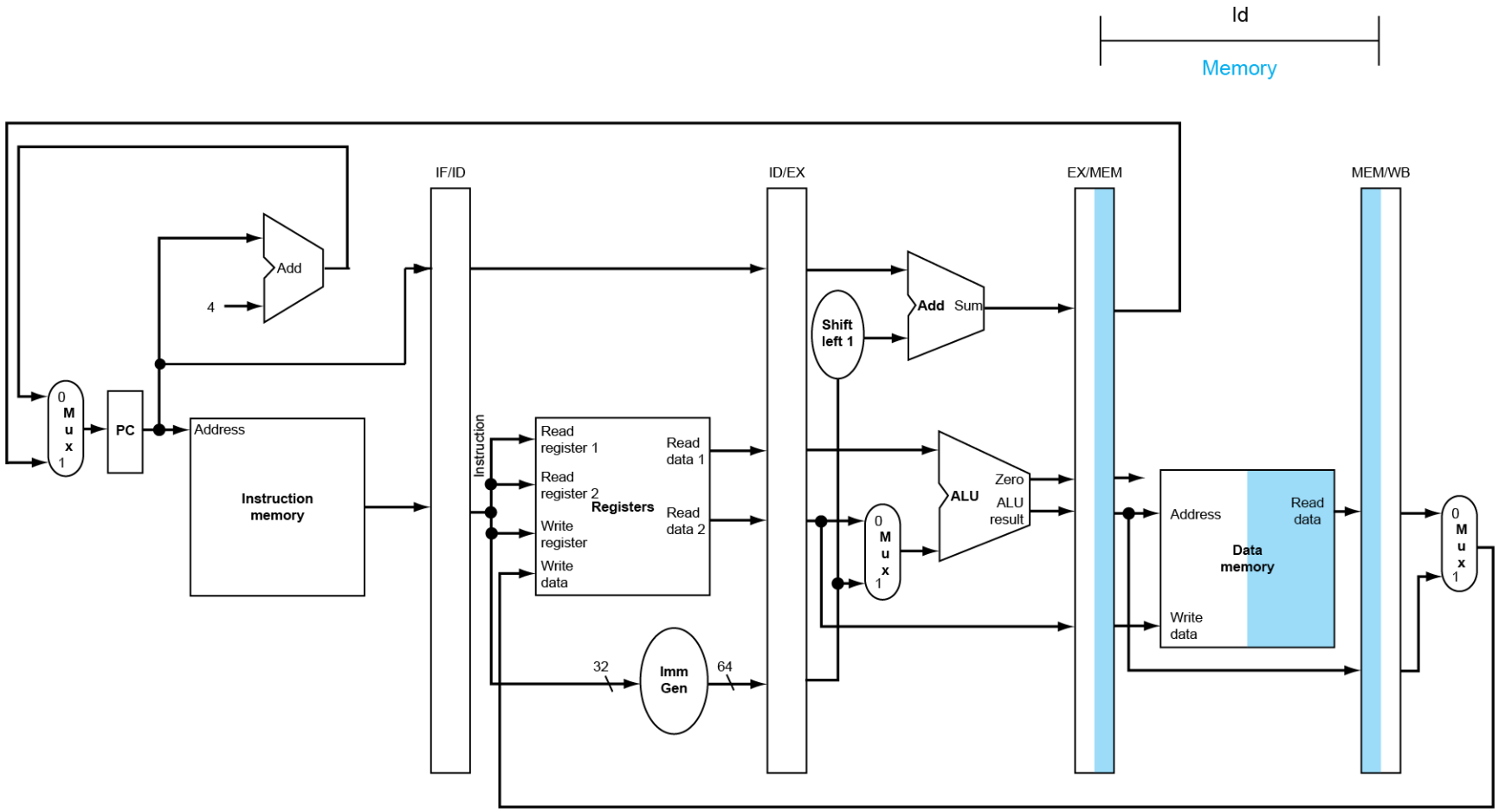
ID for Load, Store, …



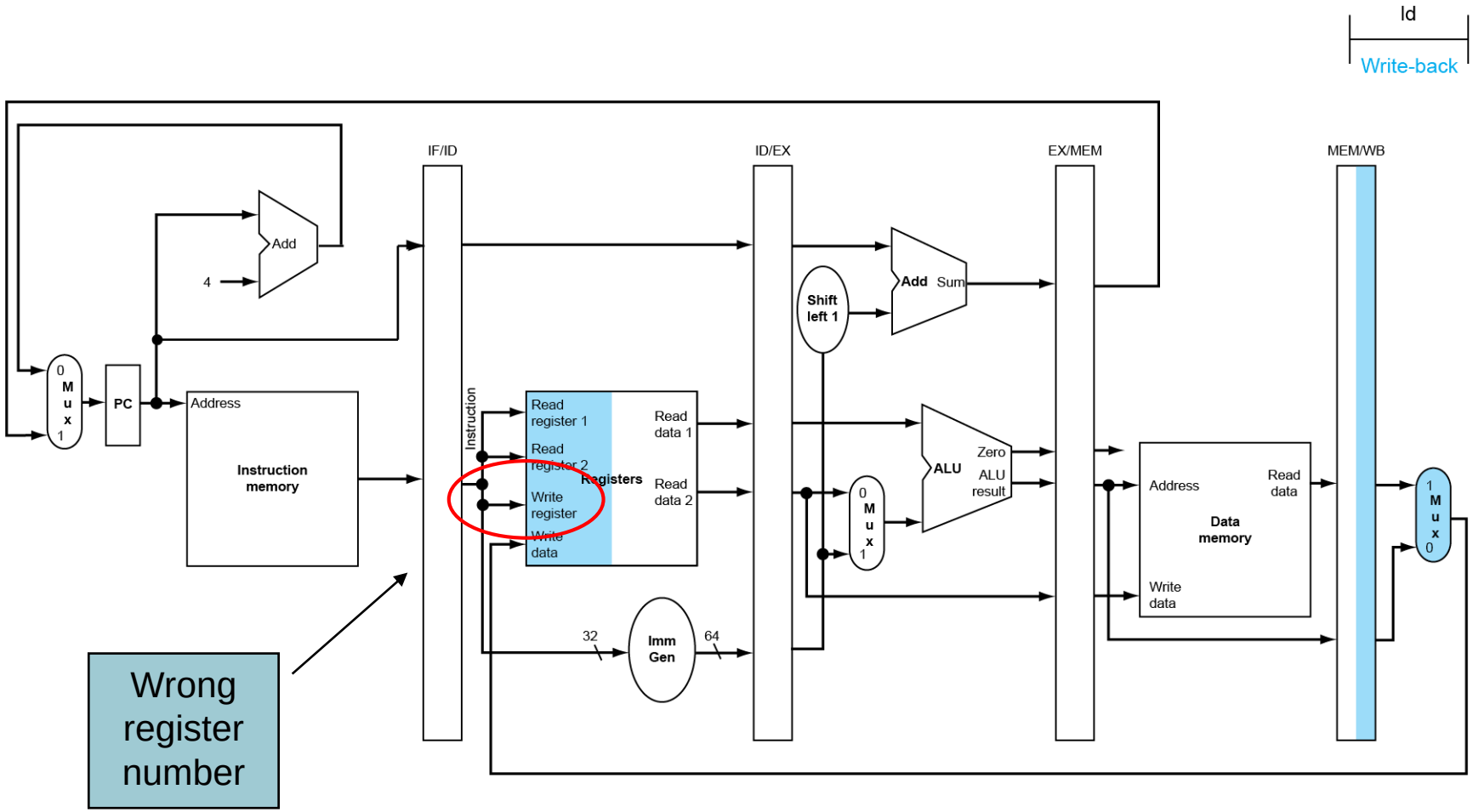
EX for Load


ld
Execution
IF/ID
ID/EX
EX/MEM
MEM/WB
Add
4
0
M
u
x
1
PC
Address
Instruction memory
Instruction
Read register 1
Read register 2
Registers
Write register
Write data
Read data 1
Read data 2
32
Imm Gen
64
Shift left 1
Add
Sum
0
M
u
x
1
ALU
Zero
ALU result
Address
Read data
Data memory
Write data
1
M
u
x
0

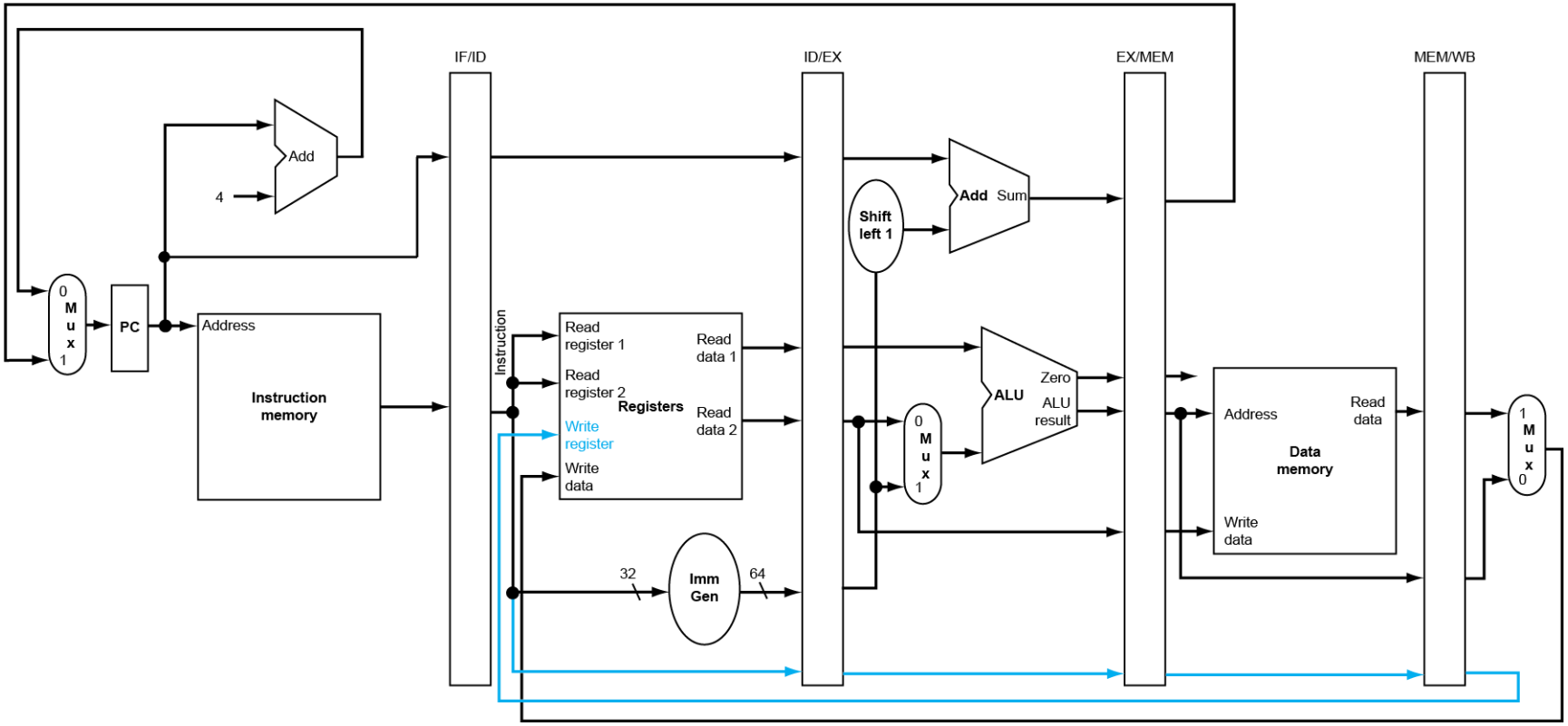
MEM for Load


ld
Memory
IF/ID
ID/EX
EX/MEM
MEM/WB
Add
4
0
M
u
x
1
PC
Address
Instruction memory
Instruction
Read register 1
Read register 2
Registers
Write register
Write data
Read data 1
Read data 2
32
Imm Gen
64
Shift left 1
Add
Sum
ALU
Zero
ALU result
Address
Data memory
Read data
Write data

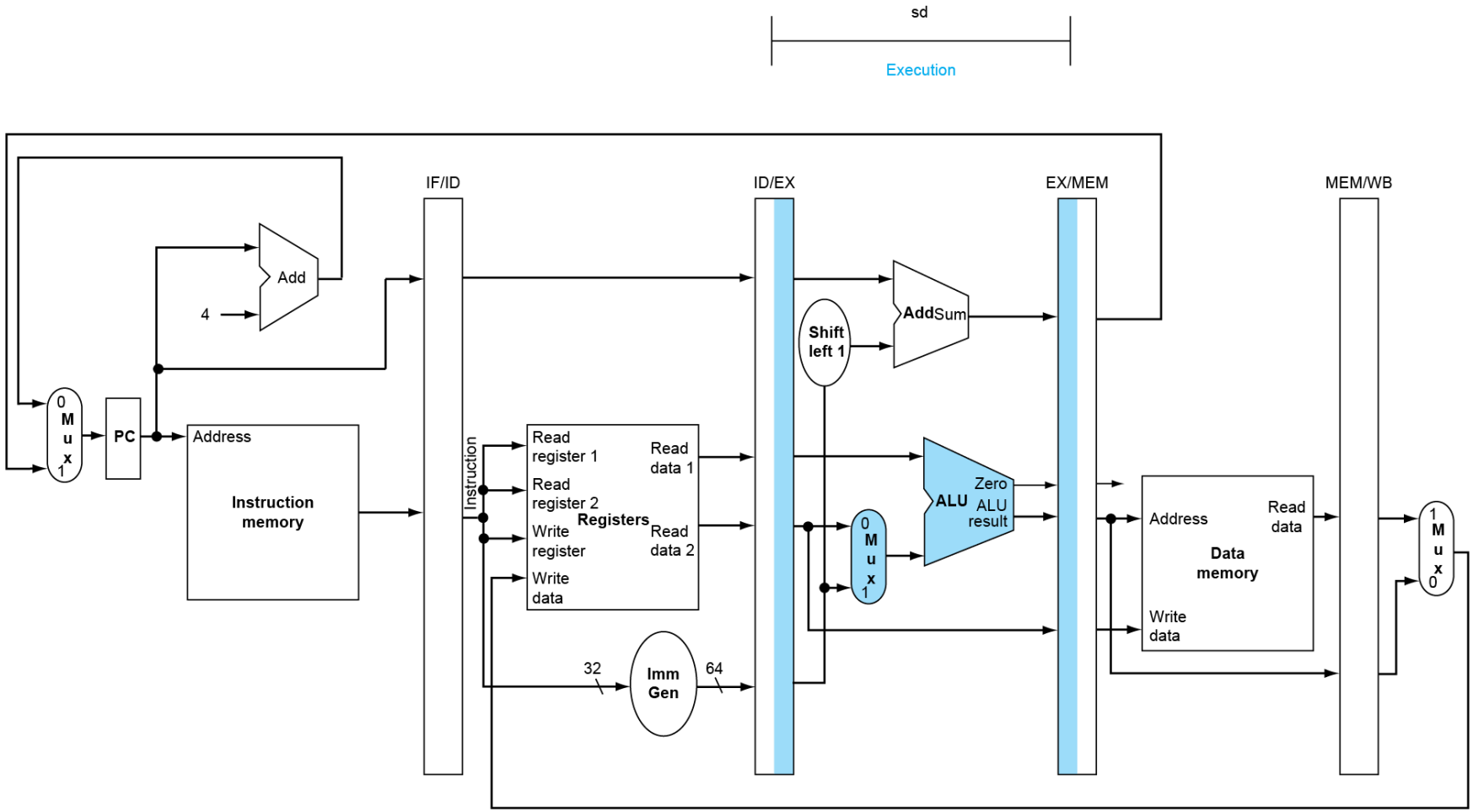
WB for Load


ld
Write-back
IF/ID
ID/EX
EX/MEM
MEM/WB
Add
4
M
u
x
0
1
PC
Address
Instruction memory
Instruction
Read register 1
Read register 2
Registers
Write register
Write data
Read data 1
Read data 2
Shift left 1
Add
Sum
ALU
Zero
ALU result
Address
Read data
Data memory
Write data
32
Imm Gen
64
Wrong register number

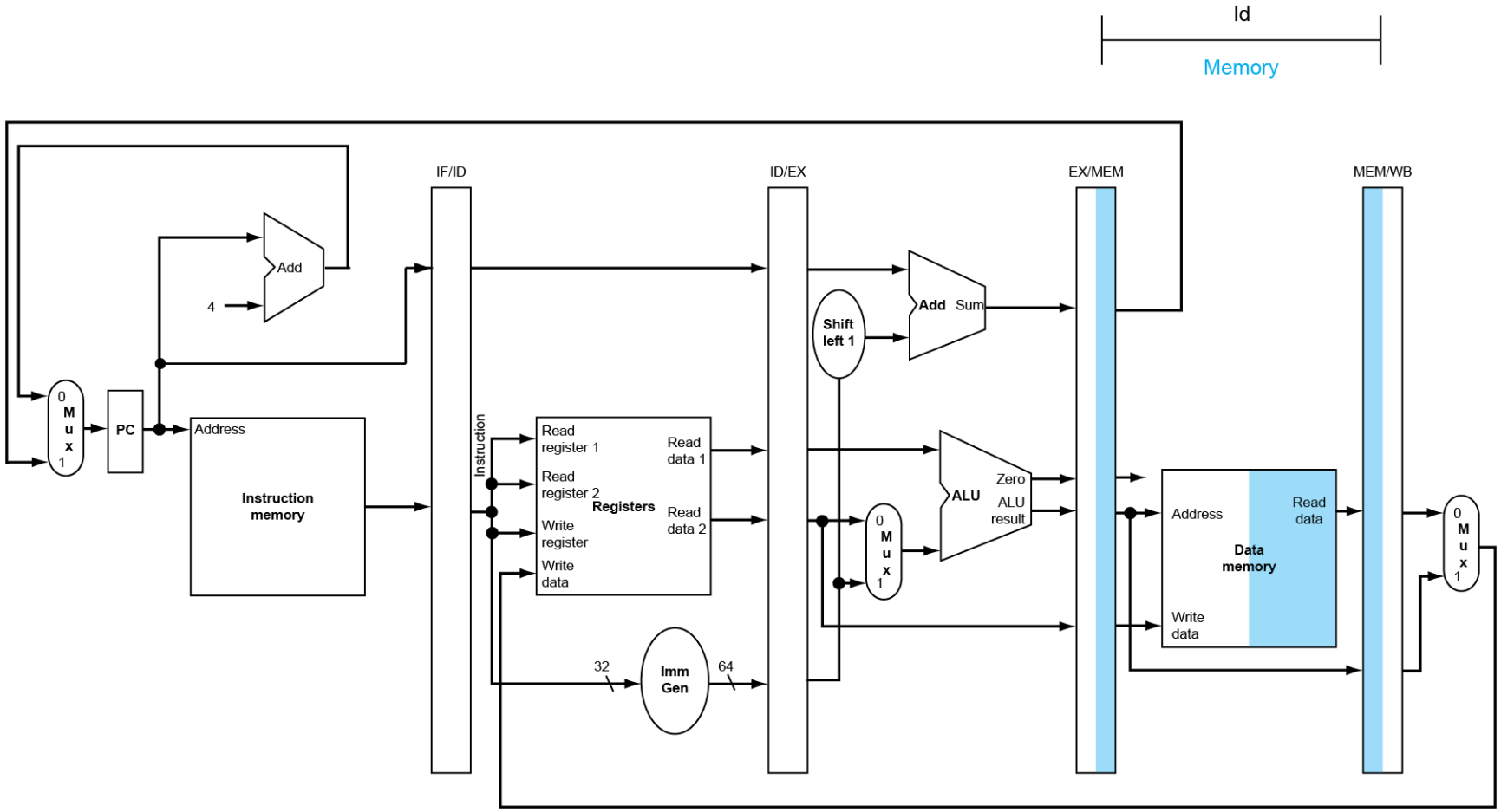
Corrected Datapath for Load



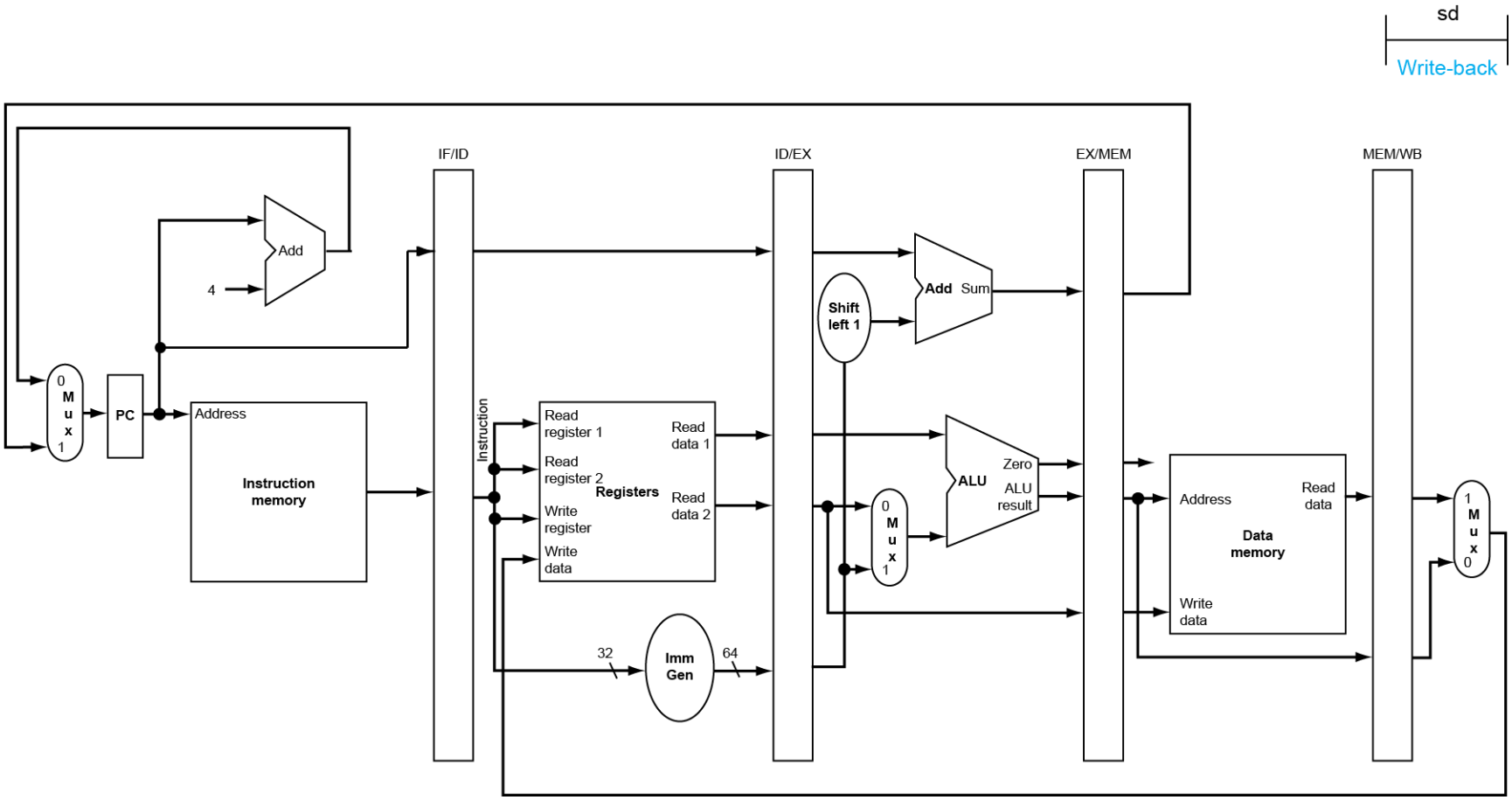
EX for Store


sd
Execution
IF/ID
ID/EX
EX/MEM
MEM/WB
Add
4
0
M
u
x
1
PC
Address
Instruction memory
Instruction
Read register 1
Read register 2
Registers
Write register
Write data
Read data 1
Read data 2
32
Imm Gen
64
Shift left 1
AddSum
ALU
Zero
ALU result
Address
Read data
Data memory
Write data
1
M
u
x
0

MEM for Store

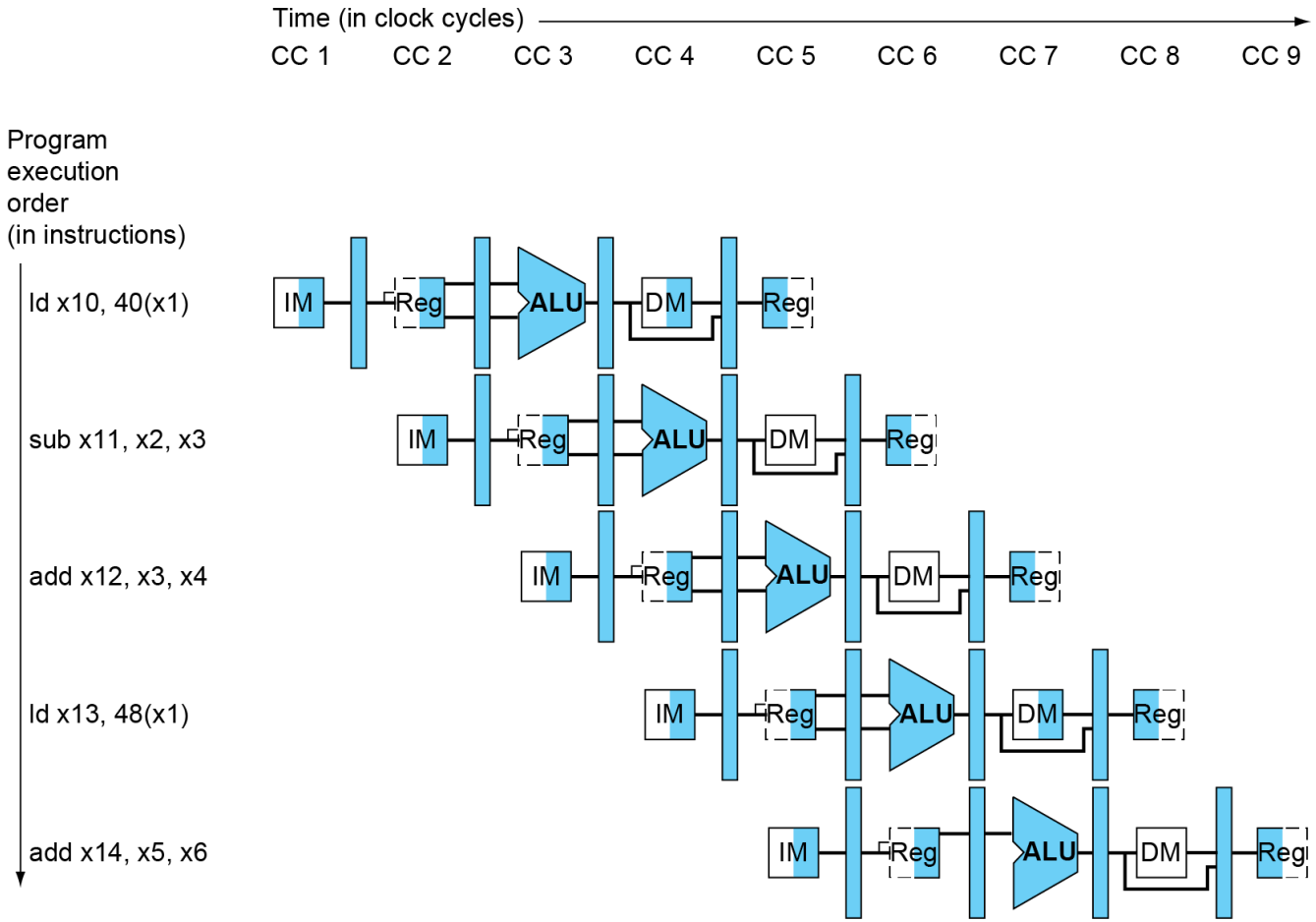


WB for Store


sd
Write-back
IF/ID
ID/EX
EX/MEM
MEM/WB
Add
4
M
u
x
0
1
PC
Address
Instruction memory
Instruction
Read register 1
Read register 2
Registers
Write register
Write data
Read data 1
Read data 2
Shift left 1
Add
Sum
ALU
Zero
ALU result
32
Imm Gen
64
Address
Data memory
Read data
Write data

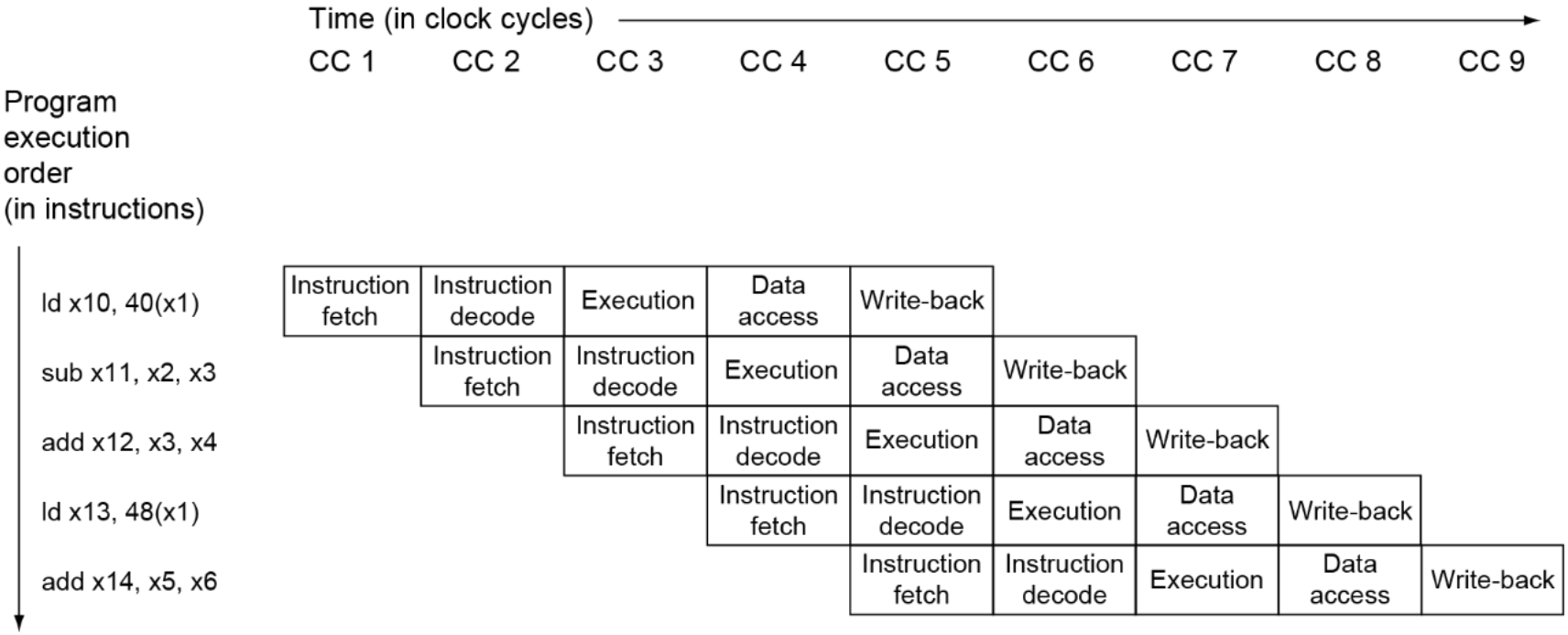
Multi-Cycle Pipeline Diagram

- Form showing resource usage



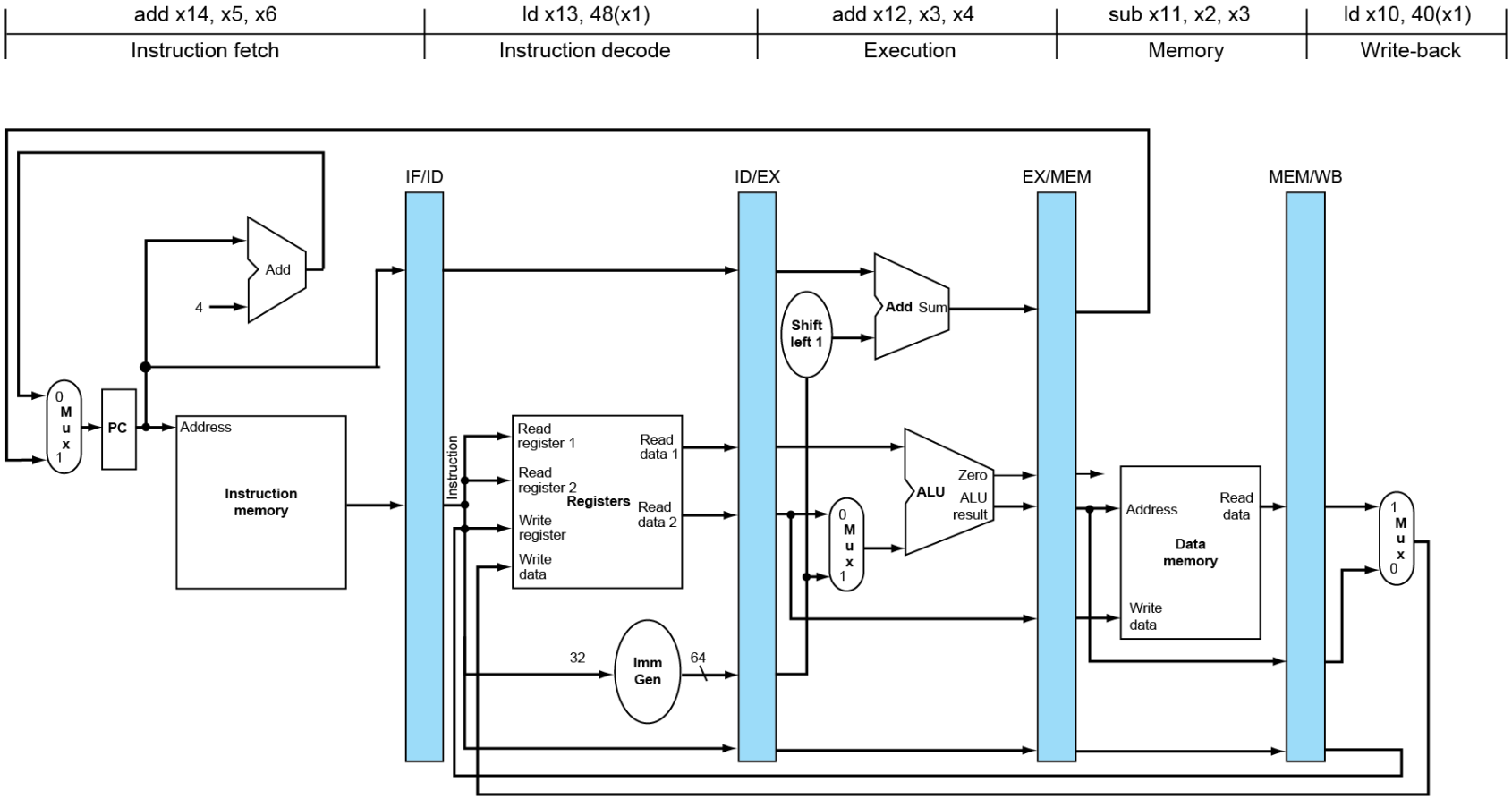
Multi-Cycle Pipeline Diagram

- Traditional form

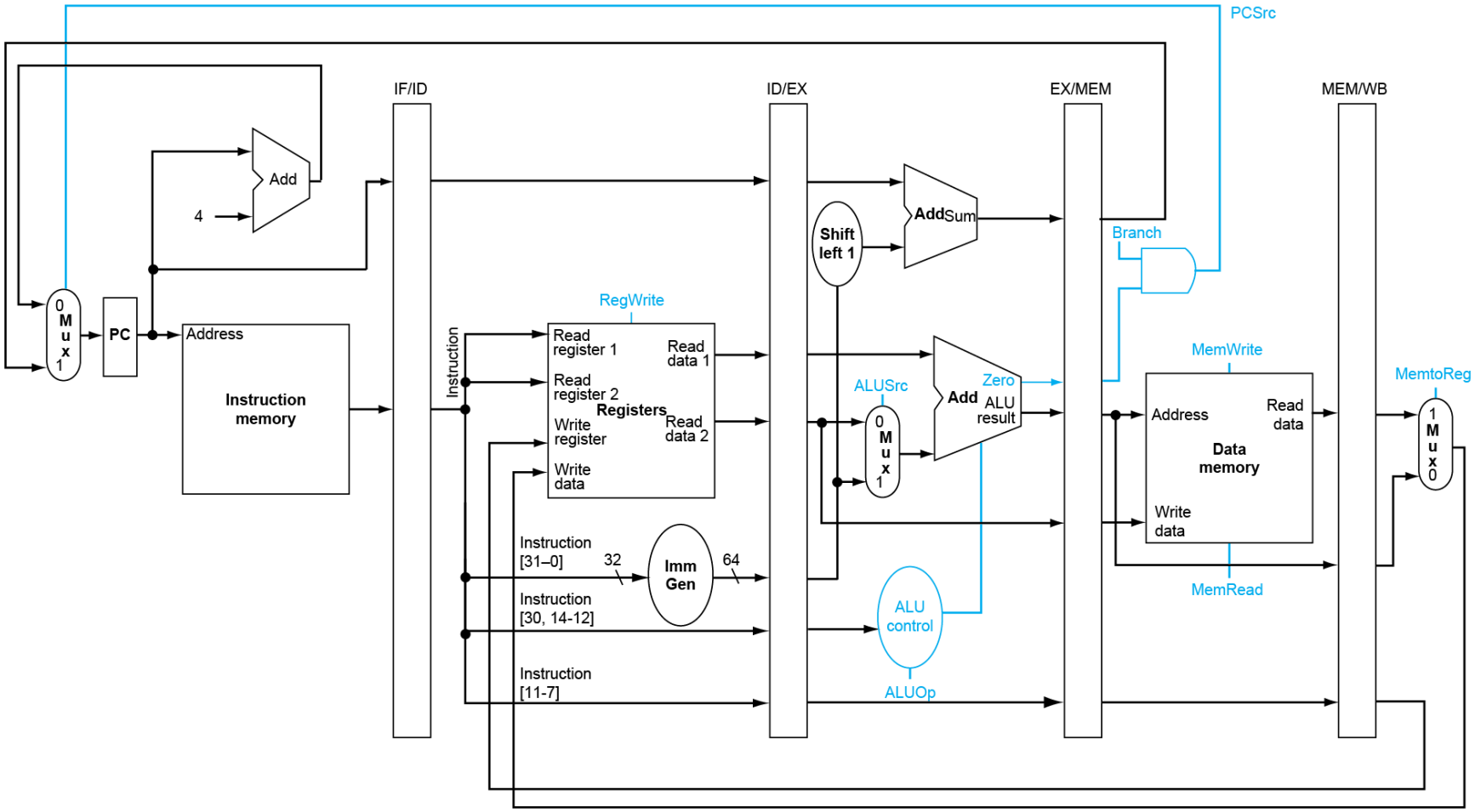


Single-Cycle Pipeline Diagram

- State of pipeline in a given cycle

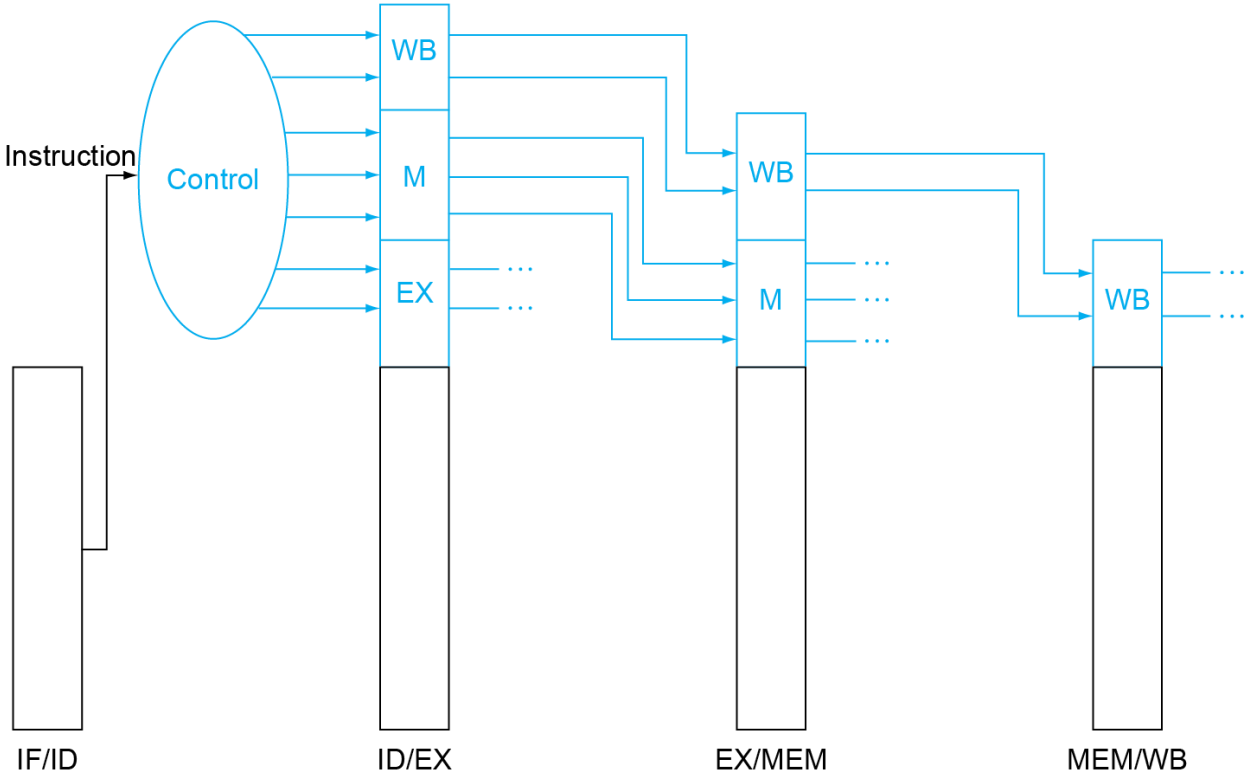


Pipelined Control (Simplified)

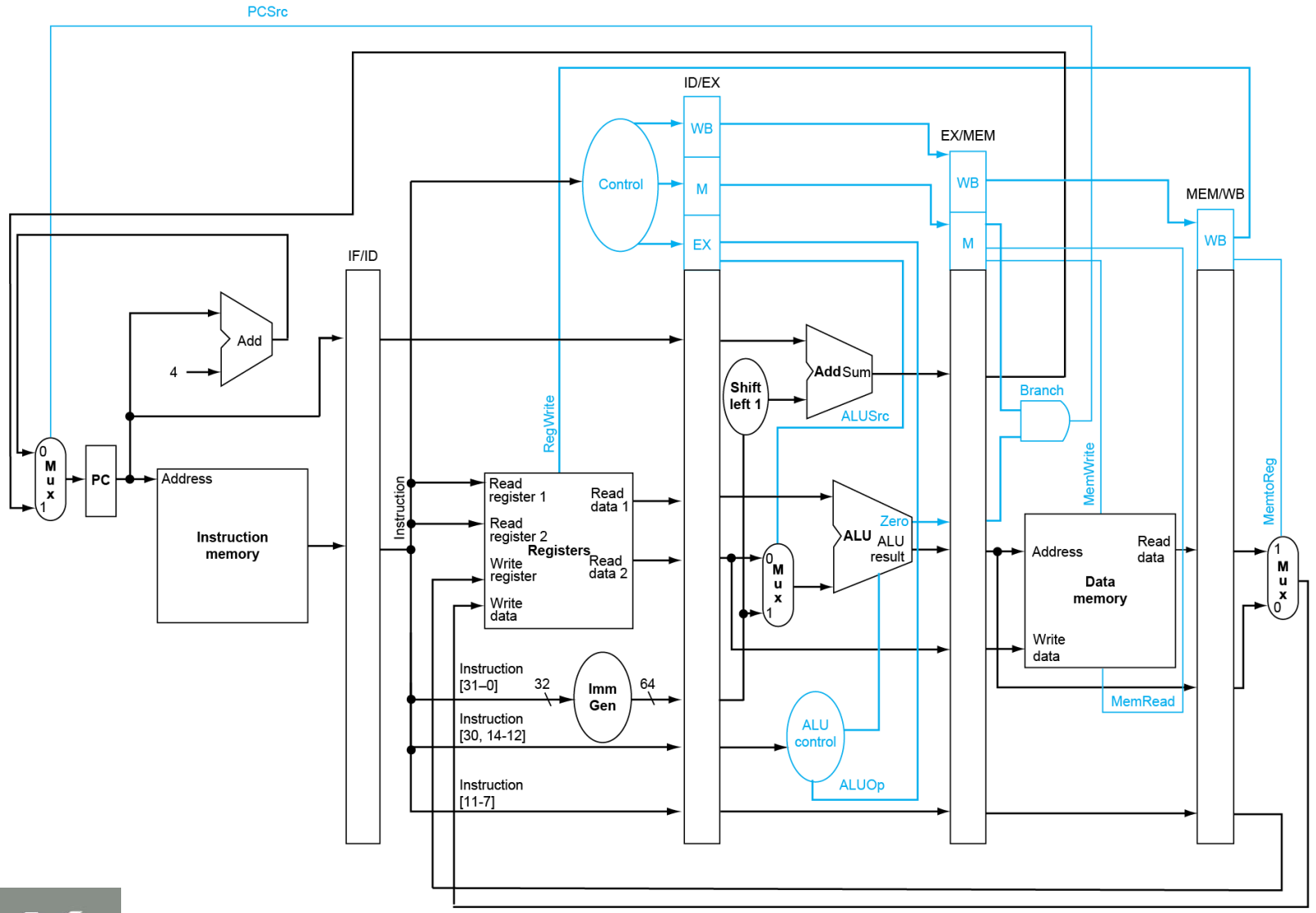


Pipelined Control

- Control signals derived from instruction
  - As in single-cycle implementation



Pipelined Control

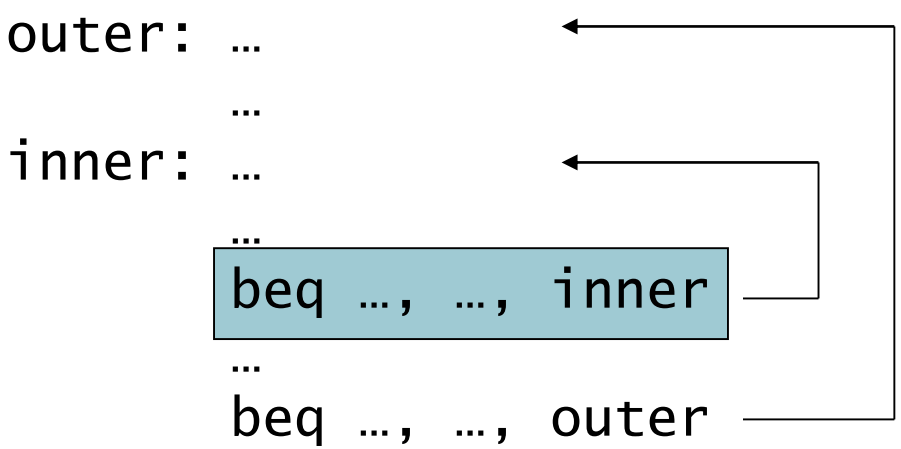


Dynamic Branch Prediction

- In deeper and superscalar pipelines, branch penalty is more significant
- Use dynamic prediction
  - Branch prediction buffer (aka branch history table)
  - Indexed by recent branch instruction addresses
  - Stores outcome (taken/not taken)
  - To execute a branch
    - Check table, expect the same outcome
    - Start fetching from fall-through or target
    - If wrong, flush pipeline and flip prediction

1-Bit Predictor: Shortcoming

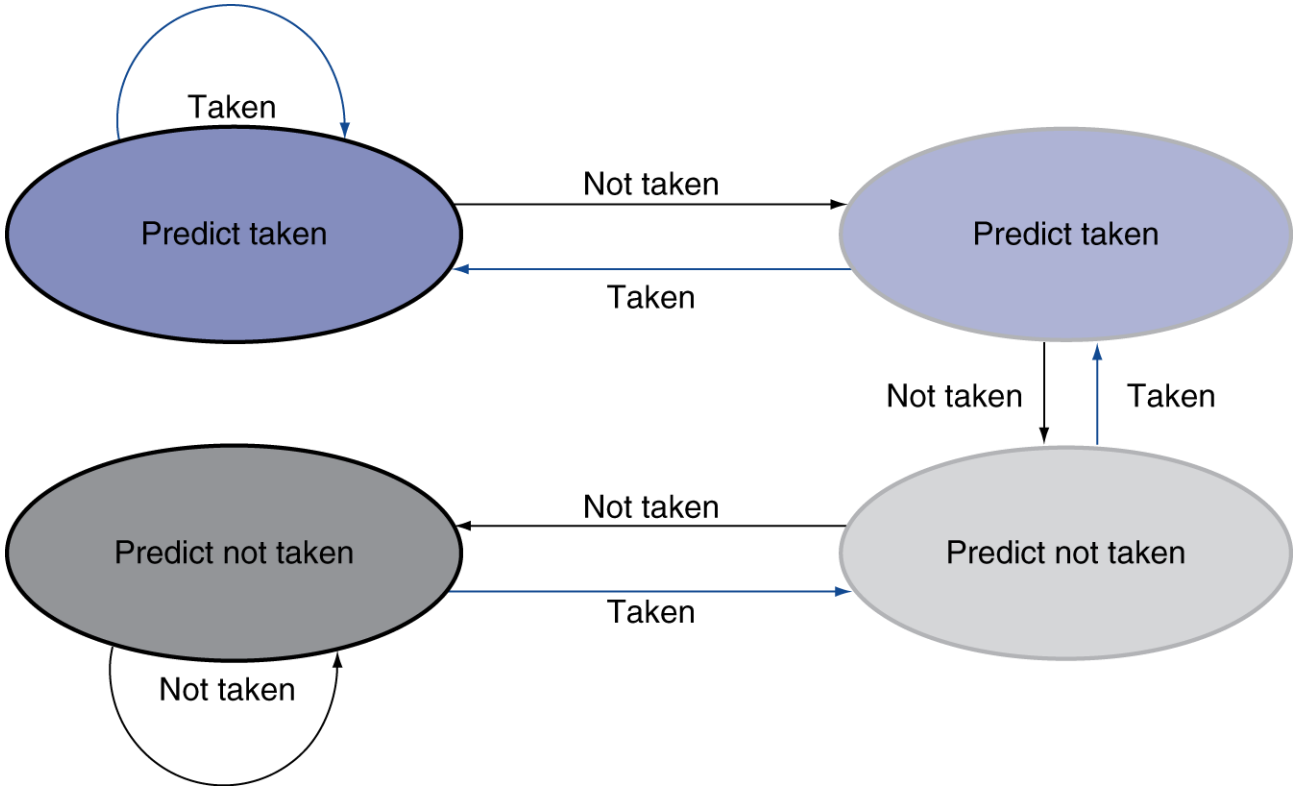
- Inner loop branches mispredicted twice!



  - Mispredict as taken on last iteration of inner loop
  - Then mispredict as not taken on first iteration of inner loop next time around

2-Bit Predictor

- Only change prediction on two successive mispredictions



Calculating the Branch Target

- Even with predictor, still need to calculate the target address
  - 1-cycle penalty for a taken branch
- Branch target buffer
  - Cache of target addresses
  - Indexed by PC when instruction fetched
    - If hit and instruction is branch predicted taken, can fetch target immediately

Exceptions and Interrupts

- “Unexpected” events requiring change in flow of control
  - Different ISAs use the terms differently
- Exception
  - Arises within the CPU
    - e.g., undefined opcode, syscall, …
- Interrupt
  - From an external I/O controller
- Dealing with them without sacrificing performance is hard

Handling Exceptions

- Save PC of offending (or interrupted) instruction
  - In RISC-V: Supervisor Exception Program Counter (SEPC)
- Save indication of the problem
  - In RISC-V: Supervisor Exception Cause Register (SCAUSE)
  - 64 bits, but most bits unused
    - Exception code field: 2 for undefined opcode, 12 for hardware malfunction, …
- Jump to handler
  - Assume at 0000 0000 1C09 0000_{hex}

An Alternate Mechanism

- Vectored Interrupts
  - Handler address determined by the cause
- Exception vector address to be added to a vector table base register:
  - Undefined opcode 00 0100 0000_{two}
  - Hardware malfunction: 01 1000 0000_{two}
  - …: …
- Instructions either
  - Deal with the interrupt, or
  - Jump to real handler

Handler Actions

- Read cause, and transfer to relevant handler
- Determine action required
- If restartable
  - Take corrective action
  - use SEPC to return to program
- Otherwise
  - Terminate program
  - Report error using SEPC, SCAUSE, …