Qinyun Lin (NUID: 001582464)

Program Structures & Algorithms Fall 2021

Assignment No. 1

Task:

- Run experiments for several values of n(steps), and run several times for each n
- Deduce the relationship between the steps and the random walking distance
- o Demonstrate the relationship(expression) via graphs

Relationship Conclusion: $D = 0.88659\sqrt{n}$

Evidence to support the conclusion:

1. Output

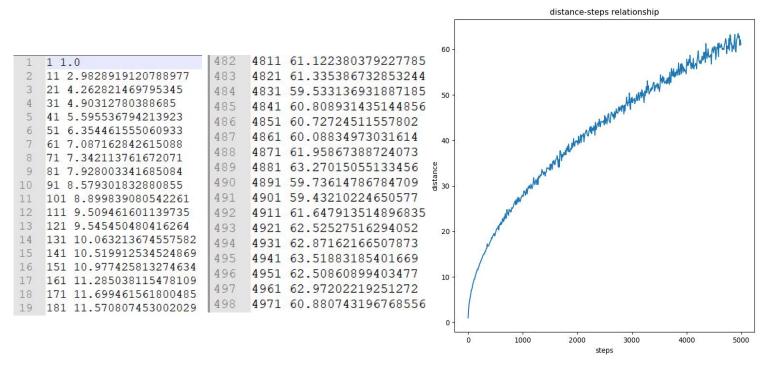
Run experiments with n from 1 to 5000, step 10; run each n for 1000 times

```
1 steps: distance = 1.0 over 1000 experiments
11 steps: distance = 2.9828919120788977 over 1000 experiments
21 steps: distance = 4.262821469795345 over 1000 experiments
31 steps: distance = 4.90312780388685 over 1000 experiments
41 steps: distance = 5.595536794213923 over 1000 experiments
51 steps: distance = 6.354461555060933 over 1000 experiments
61 steps: distance = 7.087162842615088 over 1000 experiments
71 steps: distance = 7.342113761672071 over 1000 experiments
81 steps: distance = 7.928003341685084 over 1000 experiments
91 steps: distance = 8.579301832880855 over 1000 experiments
101 steps: distance = 8.899839080542261 over 1000 experiments
111 steps: distance = 9.509461601139735 over 1000 experiments
121 steps: distance = 9.545450480416264 over 1000 experiments
131 steps: distance = 10.063213674557582 over 1000 experiments
141 steps: distance = 10.519912534524869 over 1000 experiments
151 steps: distance = 10.977425813274634 over 1000 experiments
161 steps: distance = 11.285038115478109 over 1000 experiments
```

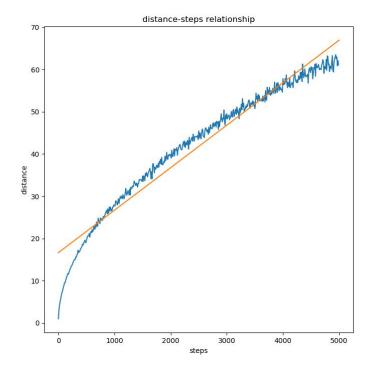
```
4861 steps: distance = 60.08834973031614 over 1000 experiments
4871 steps: distance = 61.95867388724073 over 1000 experiments
4881 steps: distance = 63.27015055133456 over 1000 experiments
4891 steps: distance = 59.73614786784709 over 1000 experiments
4901 steps: distance = 59.43210224650577 over 1000 experiments
4911 steps: distance = 61.647913514896835 over 1000 experiments
4921 steps: distance = 62.52527516294052 over 1000 experiments
4931 steps: distance = 62.87162166507873 over 1000 experiments
4941 steps: distance = 63.51883185401669 over 1000 experiments
4951 steps: distance = 62.50860899403477 over 1000 experiments
4961 steps: distance = 62.97202219251272 over 1000 experiments
4971 steps: distance = 60.880743196768556 over 1000 experiments
4981 steps: distance = 62.09859522366502 over 1000 experiments
4991 steps: distance = 61.12769149230631 over 1000 experiments
Process finished with exit code 0
```

2. Graphical Representation

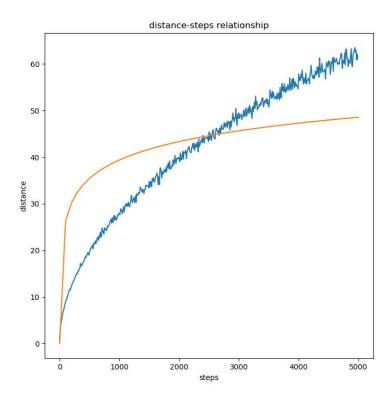
(1) Save the experiment results to .csv file, then use python to process these data



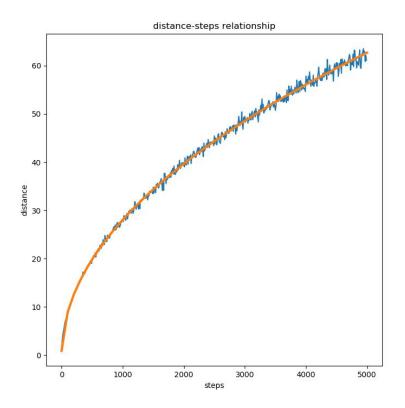
- (2) I tried 3 kinds of functions and used LSE(least squares method) to fit it, the result is shown below:
 - a. Linear function:



b. Log function:



c. Square root function:



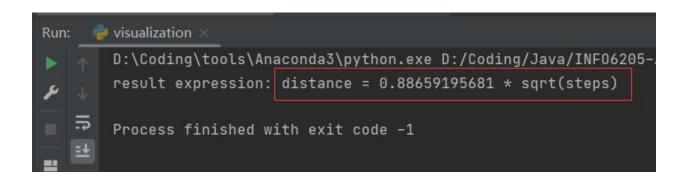
(3) It is obvious that the Square root function fits it much better, so I deduce the relationship between n(steps) and d(distance) should be described by this kind of function. The LSE related code and result in python are shown below:

```
def cal_by_lse_2():
    def func(p, x):
        # guess the function format should be y = k * sqrt(x) via the graph
        k = p
        return k * np.sqrt(x)

def error(p, x, y):
    return func(p, x) - y

# calculate the expression via LSE(least squares method)
    xi = np.asarray(steps)
    yi = np.asarray(distance)
    p0 = np.asarray([1 / 25.0]) # guess the init value of k via the graph

p = leastsq(error, p0, args=(xi, yi))
    k = p[0][0]
```



Unit tests result: