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Secure Classification as a Service

BACHELOR'S THESIS

Bachelor's degree programmes:
Physics and Information & Computer Engineering

Supervisors

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Graz University of Technology

Abstract

Abstract of your thesis (at most one page)

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Keywords: FHE, classification, neural network

Technologies: Microsoft SEAL (C++, nodejs), Tensorflow Keras, Numpy, xtensor, Docker, msgpack, React, Materialize, Nginx

Languages: C++, Python, JavaScript

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Chapter 1

Introduction

Goal:

Chapter 2

Background

2.1 Basics of Fully Homomorphic Encryption

Homomorphic Encryption (HE) makes it possible to operate on data without knowing it. One can distinguish three flavors of it, Partial-, Semi- and **Fully Homomorphic Encryption (FHE)**.

- Brakerski/Fan-Vercauteren (BFV) scheme for integer arithmetic
- Brakerski-Gentry-Vaikuntanathan (BGV) scheme for integer arithmetic
- Cheon-Kim-Kim-Song (CKKS) scheme for real-number arithmetic
- Ducas-Micciancio (FHEW) and Chillotti-Gama-Georgieva-Izabachene (TFHE) schemes for Boolean circuit evaluation

2.1.1 Packing

FFT in CKKS! Polynom \rightarrow Vektor mit einer FFT Vektor \rightarrow Polynom mit einer IFFT

2.1.2 HE using RSA

With unpadded RSA, some arithmetic can be performed on the ciphertext - looking at the encrypted ciphertext $\mathcal{E}(m_1) = (m_1)^r \bmod n$ of the message m_1 and m_2 respectively, the following holds:

$$\mathcal{E}(m_1) \cdot \mathcal{E}(m_2) = (m_1)^r (m_2)^r \bmod n \quad (2.1)$$

$$= (m_1 m_2)^r \bmod n \quad (2.2)$$

$$= \mathcal{E}(m_1 \cdot m_2) \quad (2.3)$$

The encryption therefore partially fulfills the properties of ring homomorphism, which in general is defined as follows:

Definition 2.1.1: Ring Homomorphism Given two rings $(R, +, \cdot)$ and (S, \oplus, \otimes) , we call a mapping $\varphi : R \rightarrow S$ a ring homomorphism when it satisfies the following conditions:

$$\forall a, b \in R : \varphi(a + b) = \varphi(a) \oplus \varphi(b) \wedge \varphi(a \cdot b) = \varphi(a) \otimes \varphi(b)$$

2.1.3 Learning with Errors (LWE)

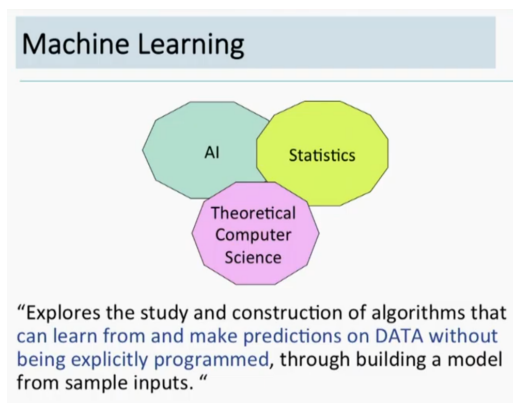
2.1.4 Ring-LWE

Learning with Errors on Rings (RLWE)

2.1.5 The BFV scheme

2.1.6 The CKKS scheme

The CKKS scheme allows us to perform approximate arithmetic on floating point numbers.



2.2 Machine Learning

As Shafi Goldwasser puts it, 'Machine Learning is somewhere in the intersection of Artificial Intelligence, Statistics and Theoretical Computer Science' [Gol18].

2.2.1 Linear Regression?

2.2.2 Gradient Descent?

2.2.3 The Backpropagation Algorithm

2.2.4 Multi-Layered Neural Networks

Matrix -> Activation Function

- Matrix Multiplication (Dense Layer)
- Convolutional Layer
- Sigmoid Activation
- Max Pooling

2.3 Post-Quantum Security

2.4 Demo

In this chapter, we provide some usage examples for glossaries and acronym lists with `glossaries` (Section 2.5), bibliography and citations with `biblatex` (Section 2.6), and more.

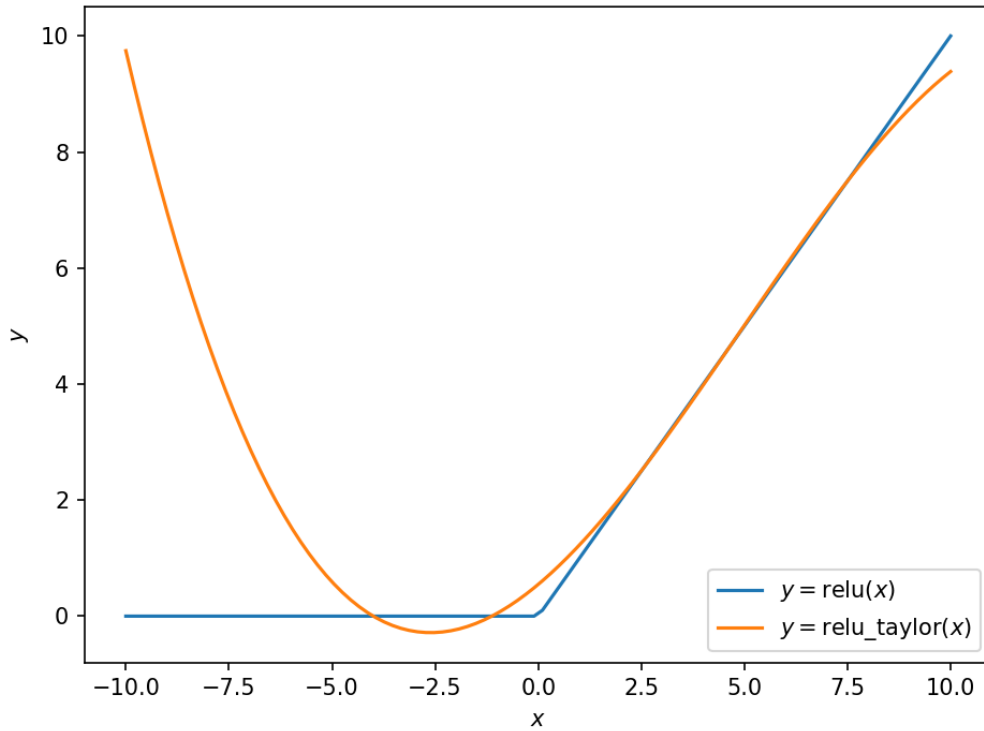


Figure 2.1: Comparison of the Relu activation function vs. its Taylor expansion

2.5 Notation and Acronyms

Symbols and acronyms are defined in the preamble, after loading the `glossaries` package, and used as follows.

In this chapter, we introduce the necessary background on the [Advanced Encryption Standard \(AES\)](#). We denote binary exclusive-or by \oplus .

2.6 Citations

This is an example of how to specify and cite a book [DR02], a journal article [Sha49]. We can also add the authors' names to the citation: [AES](#) is a block cipher defined by Daemen and Rijmen [DR02].

Chapter 3

Results

Performance

Chapter 4

Conclusion

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Notation

\oplus exclusive-or (XOR)

7

Acronyms

AES	Advanced Encryption Standard	7
FHE	Fully Homomorphic Encryption	5
HE	Homomorphic Encryption	5

Bibliography

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- [Gol18] Shafi Goldwasser. ‘From Idea to Impact, the Crypto Story: What’s Next?’ In: (2018).
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