# REAL-TIME INTERACTION WITH AN ELECTROPHYSIOLOGICAL CANCER CELL MODEL

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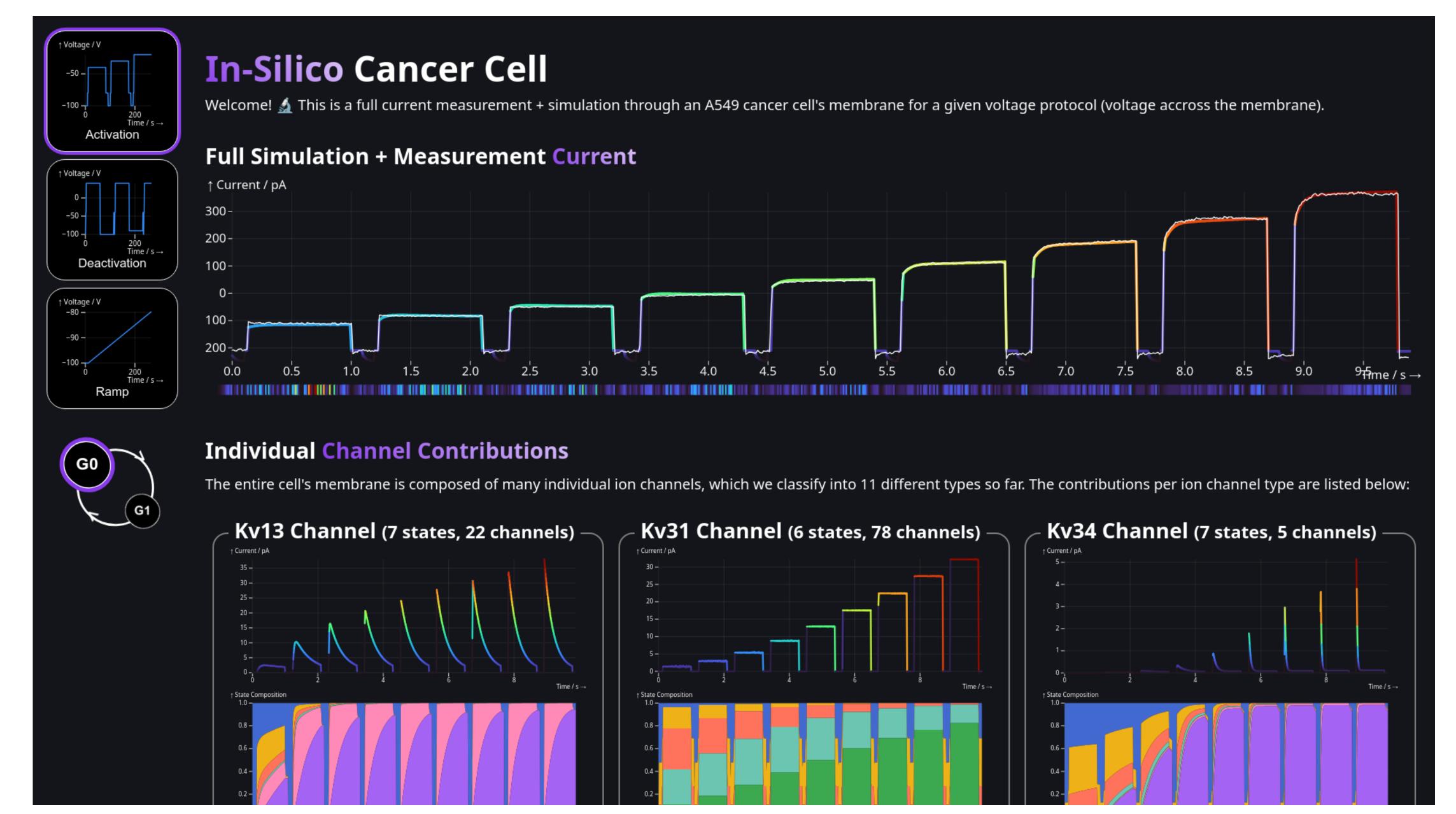
#### Introduction

We extend the previous work [1] by a faster, in-browser implementation in using compilation to WebAssembly.

#### **Number of Channels**

<b>Channel Type</b>	$N_k$ [1]	Our $N_k$
Kv13	22	13
Kv31	78	247
Kv34	5	10
Kv71	1350	1176
KCa11	40	38
KCa31	77	7
Task1	19	24
CRAC1	200	188
TRPC6	17	15
TRPV3	12	10
CLC2	13	234

## Live, In-Browser Cell Simulation Interface



Available live on in-silico.hce.tugraz.at.

## Model

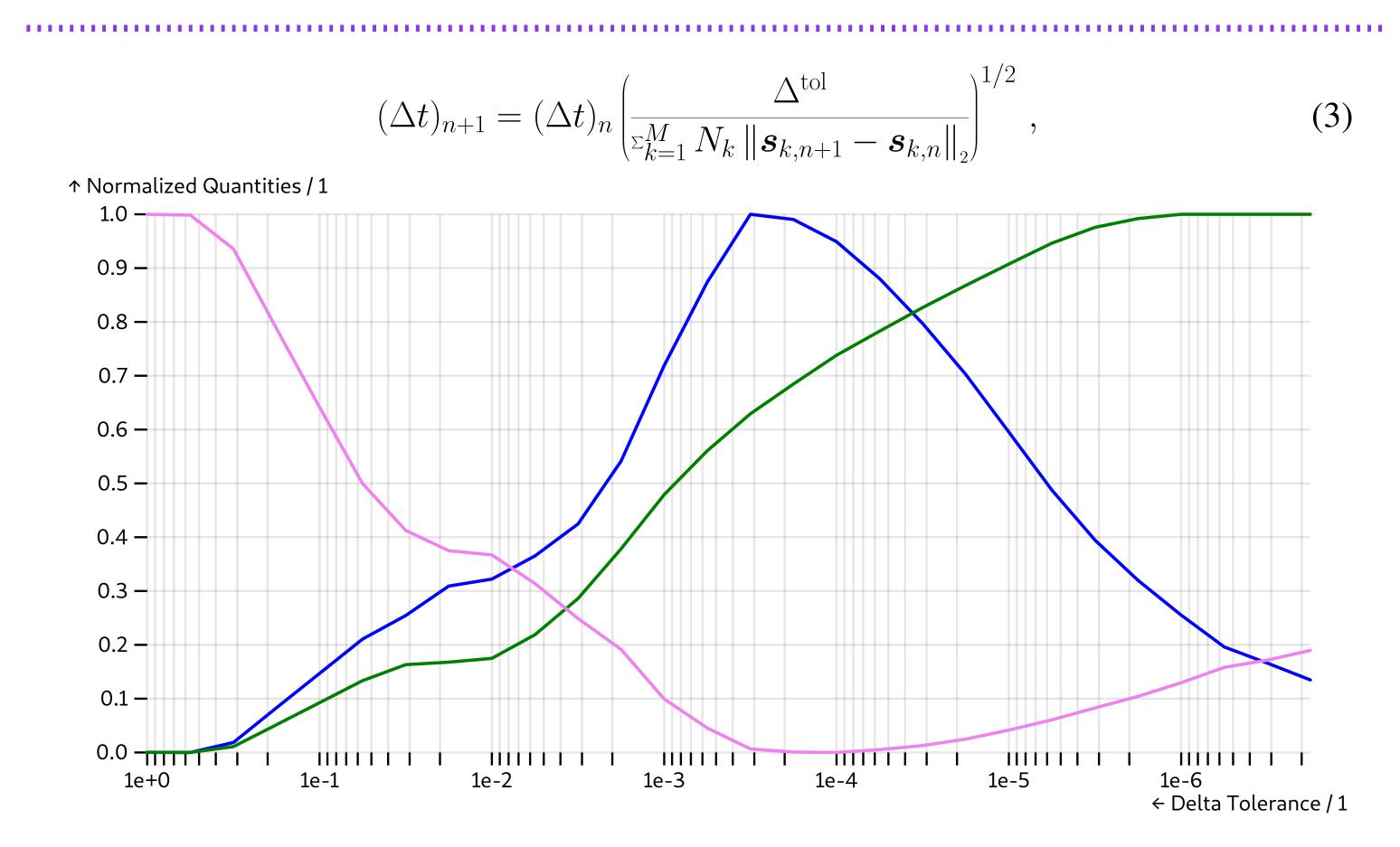
The whole cell current  $I:T\to\mathbb{R}$  over time  $t\in T\subset\mathbb{R}^+$  is the sum of all individual channel contributions  $I_k, k \in \{1, ..., M\}$  over  $M \in \mathbb{N}$  channel types

$$I(t) := \sum_{k=1}^{M} N_k I_k(t) = \sum_{k=1}^{M} N_k g_k p_{o,k} \left( V(t) - E_k \right) , \qquad (1)$$

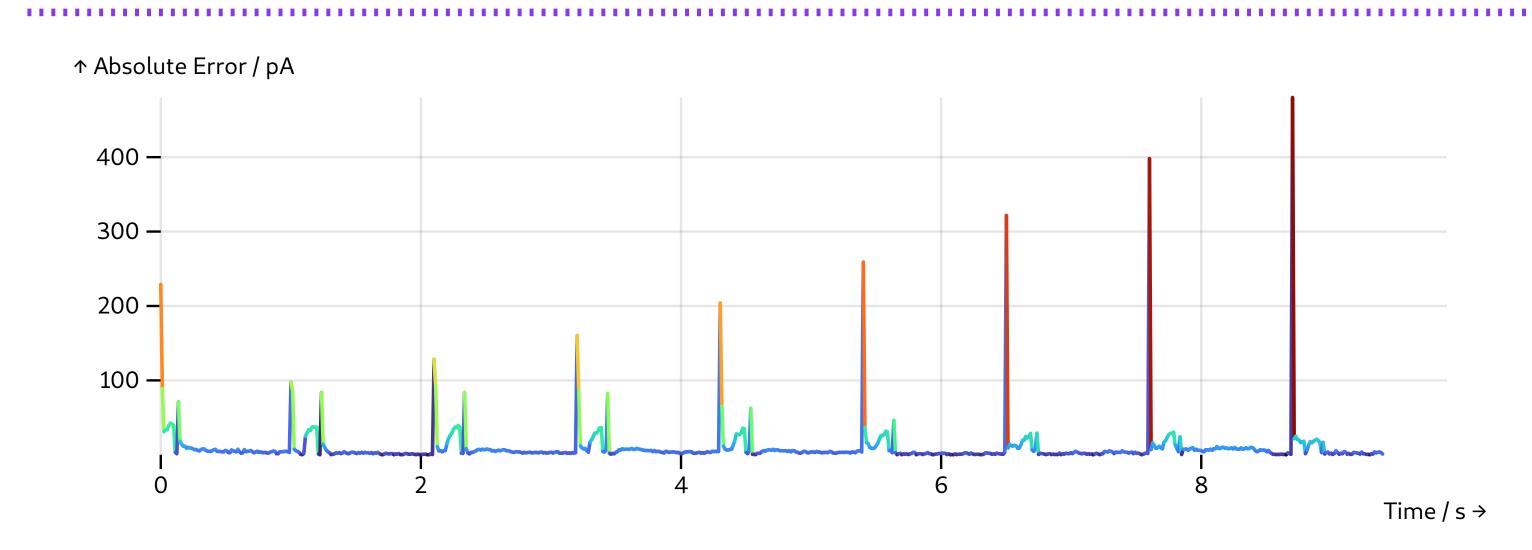
At each time step,

$$\boldsymbol{s}_{k,n+1} = H_k(V(t_n), \boldsymbol{C}(t_n), t_n) \, \boldsymbol{s}_{k,n}$$
(2)

## **Adaptive Timestepping**



## Pointwise Error between Simulation and Measurements



# Formulation as a Quadratic Program

We want to find

$$N_{\text{opt}} = \underset{N \in \mathbb{N}_0^M}{\operatorname{arg min}} \frac{1}{2} \|RN - I_{\text{meas}}\|_2^2 ,$$
 (4)

with  $I_{\text{meas}} \in \mathbb{R}^{N_t}$  the experimentally measured current and  $R \in \mathbb{R}^{N_t \times M}$  the matrix of all currents  $I_k$  per channel type. Letting  $\boldsymbol{d} := \boldsymbol{I}_{\text{meas}}$  for brevity,

$$oldsymbol{N}_{ ext{opt}} pprox rg \min_{oldsymbol{x} \in \mathbb{R}_+^M} f(oldsymbol{x}) = rg \min_{oldsymbol{x} \in \mathbb{R}_+^M} {}^1\!/_{\!2} \left\| Roldsymbol{x} - oldsymbol{d} 
ight\|_2^2 \; ,$$

with cost function  $f: \mathbb{R}^M \to \mathbb{R}^+$ , which we manipulate to

$$f(\boldsymbol{x}) = \frac{1}{2}(R\boldsymbol{x} - \boldsymbol{d})^{T}(R\boldsymbol{x} - \boldsymbol{d})$$

$$= \frac{1}{2}(\boldsymbol{x}^{T}R^{T}R\boldsymbol{x} - \boldsymbol{x}^{T}R^{T}\boldsymbol{d} - \boldsymbol{d}^{T}R\boldsymbol{x} + \boldsymbol{d}^{T}\boldsymbol{d})$$

$$= \frac{1}{2}(\boldsymbol{x}^{T}P\boldsymbol{x} + \boldsymbol{x}^{T}\boldsymbol{q} + \boldsymbol{q}^{T}\boldsymbol{x}) + \mathcal{O}(1)$$

$$= \frac{1}{2}\boldsymbol{x}^{T}P\boldsymbol{x} + \boldsymbol{q}^{T}\boldsymbol{x} + \mathcal{O}(1)$$

where we let  $P:=R^TR\in\mathbb{R}^{M\times M}$  and  $\boldsymbol{q}:=-R^T\boldsymbol{d}\in\mathbb{R}^M$  and leave out the constant  $d^Td$  as  $\mathcal{O}(1)$ . We can express the nonnegativity constraint  $x \geq 0$  as an equality constraint using a slack variable  $s \in \mathbb{R}^{M}_{+}$ ,

$$-x+s=0 \Leftrightarrow Ax+s=b$$

where we set  $A:=-\mathbb{1}\in\mathbb{R}^{M\times M}$  and  $\boldsymbol{b}:=\boldsymbol{0}\in\mathbb{R}^{M}$ . This leaves us with a constrained quadratic program,

$$\min_{\boldsymbol{x} \in \mathbb{R}^{M}} \frac{1}{2} \boldsymbol{x}^{T} P \boldsymbol{x} + \boldsymbol{q}^{T} \boldsymbol{x}, 
s.t. A \boldsymbol{x} + \boldsymbol{s} = \boldsymbol{b}, \ \boldsymbol{s} \in \mathbb{R}_{+}^{M}.$$
(5)

$$s.t. A\boldsymbol{x} + \boldsymbol{s} = \boldsymbol{b}, \ \boldsymbol{s} \in \mathbb{R}_{+}^{M}. \tag{6}$$

The integer solution can then be obtained from rounding,

$$oldsymbol{N}_{ ext{opt}} = \lfloor oldsymbol{x} 
ceil \in \mathbb{N}_0^M$$
 .

#### Comparison of Optimization Methods

Algorithm	Abbreviation	Runtime / ms	RMSE / pA
Particle Swarm Optimization	PSO	22571	27.69
Gradient Descent + More Thuente	GD	18924	32.34
Limited-Memory BFGS + Hager Zhang	LBFGS	4845	32.20
Non-Negative Least Squares [3]	NNLS	318	28.00
Ouadratic Program	OP	18	28.13

#### References