

ASSIGNMENT 2

CS5691 Pattern Recognition and Machine Learning

CS5691 Assignment 2

Team Members:

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Indian Institute of Technology, Madras

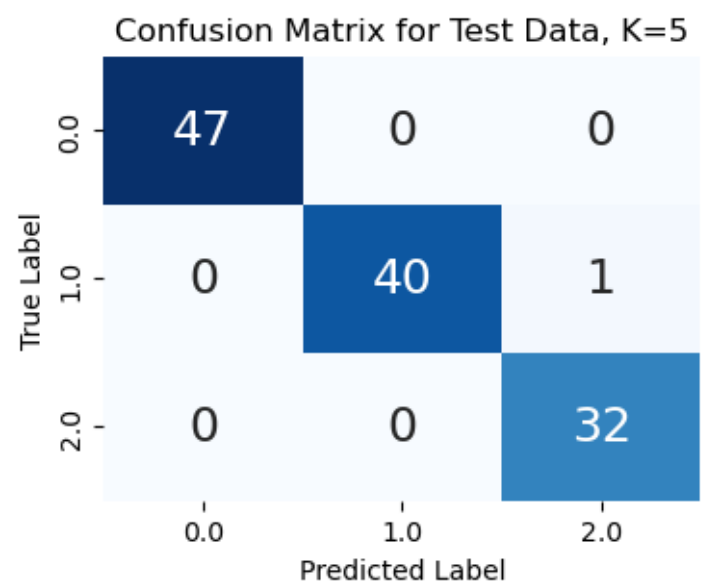
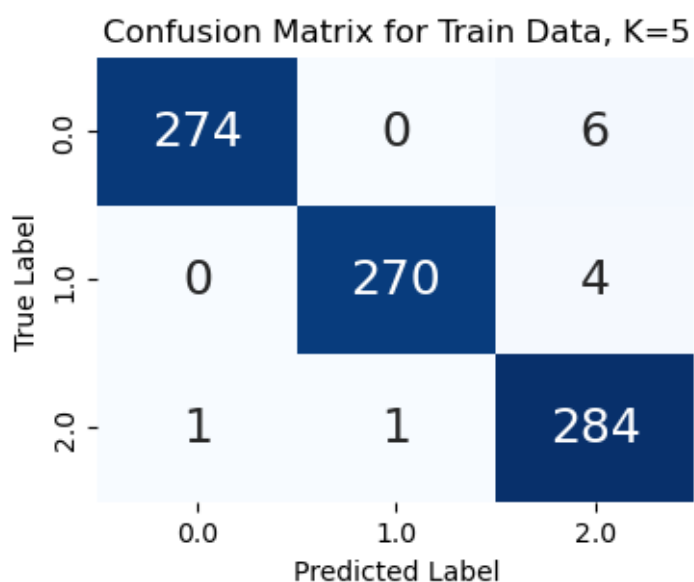
Dataset-1:

1. K-Nearest Neighbour Classifier for K=1, K=5 and K=9

Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

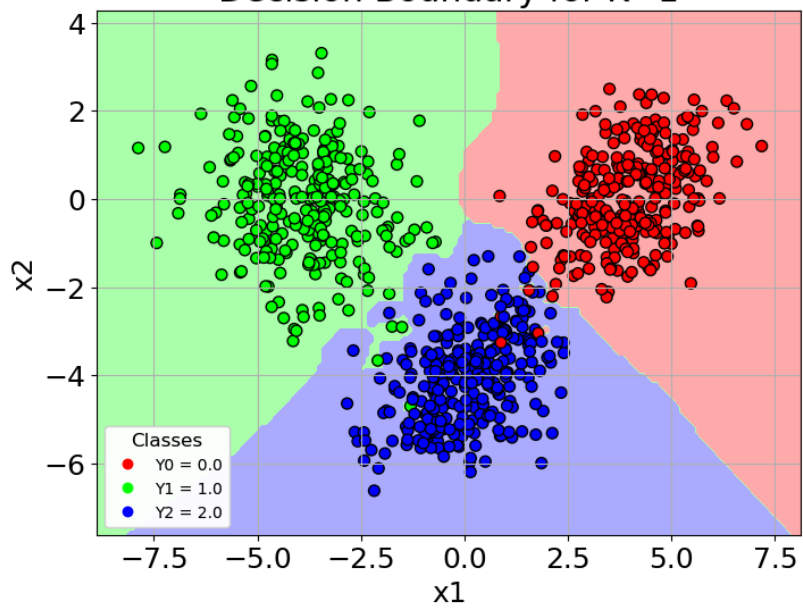
| k-value | Accuracy train | Accuracy Val | Accuracy test |
|---------|----------------|--------------|---------------|
| 1 | 1.000000 | 0.9875 | 0.991667 |
| 5 | 0.985714 | 0.9875 | 0.991667 |
| 9 | 0.986905 | 0.9875 | 0.983333 |

Confusion Matrix for the best configuration of the model, on training data and test data:

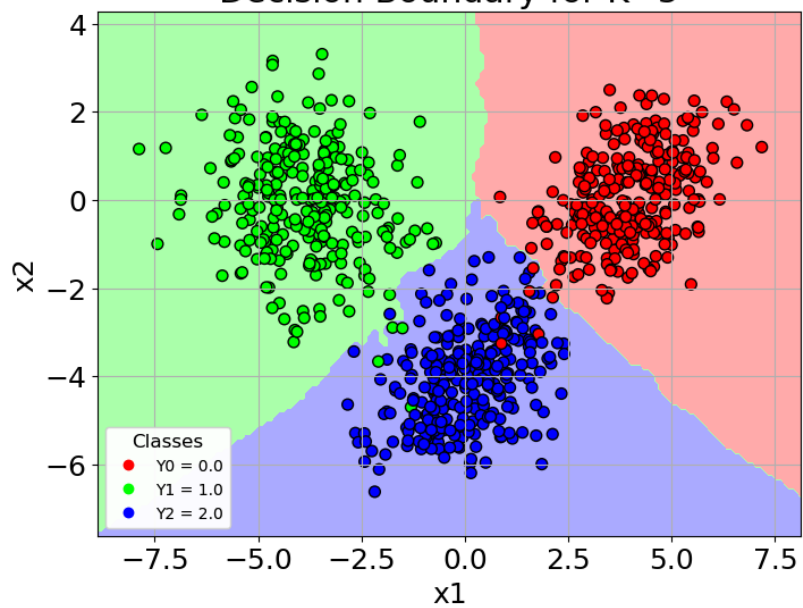


Decision Region Plots:

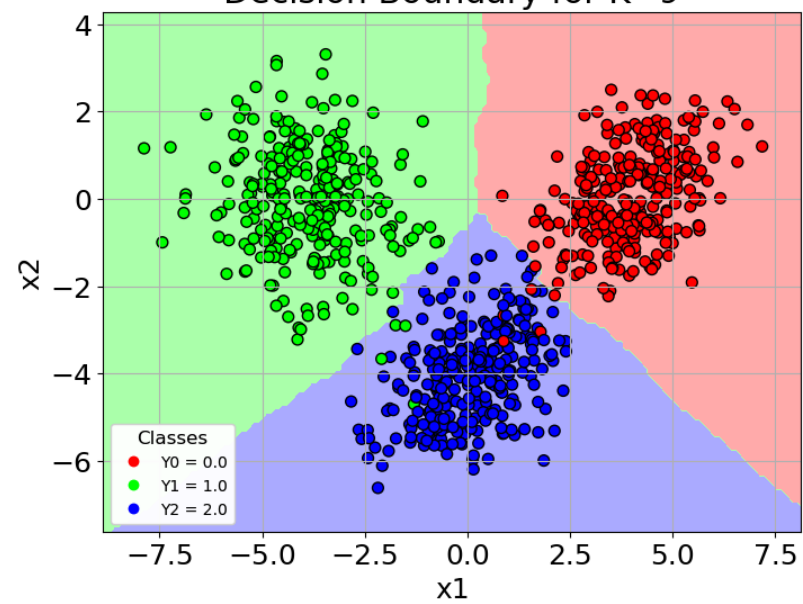
Decision Boundary for K=1



Decision Boundary for K=5



Decision Boundary for K=9



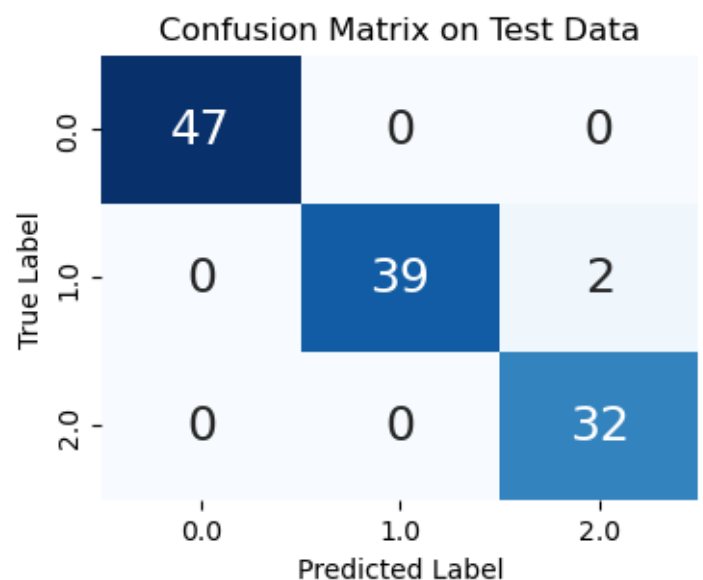
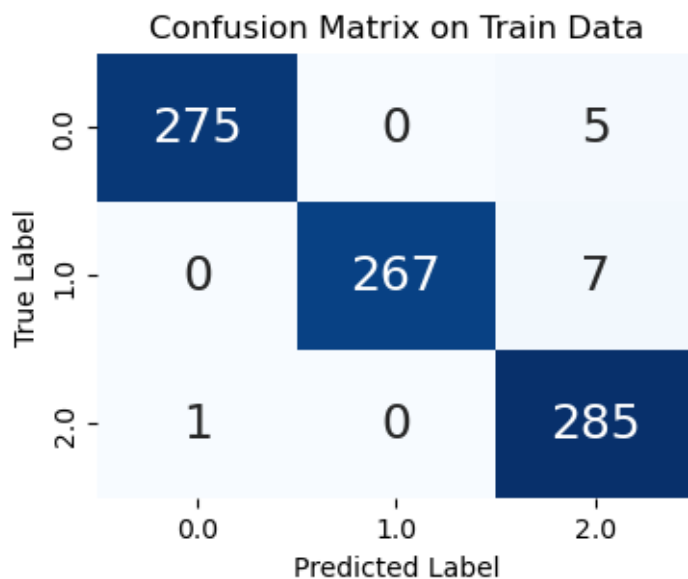
2. Bayes Classifier with a Gaussian Distribution for every class

- a. Covariance matrices for all the classes are the same

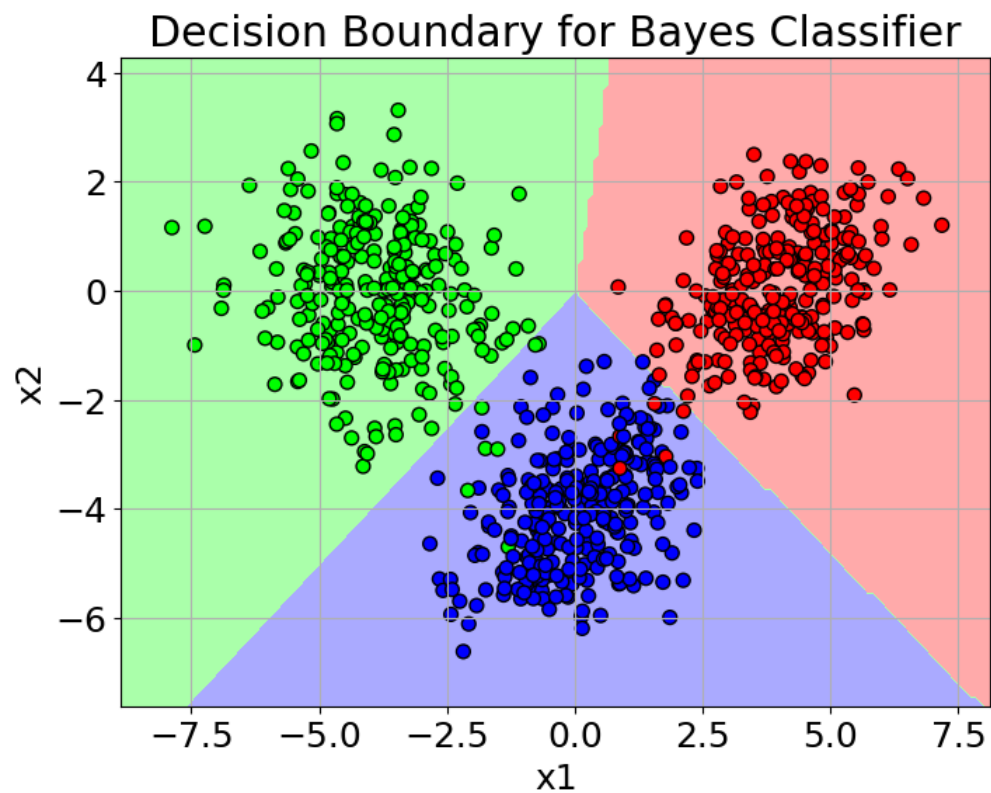
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 840 | 0.984524 |
| Validation | 240 | 0.983333 |
| Test | 120 | 0.983333 |

Confusion Matrix for the best configuration of the model, on training data and test data:

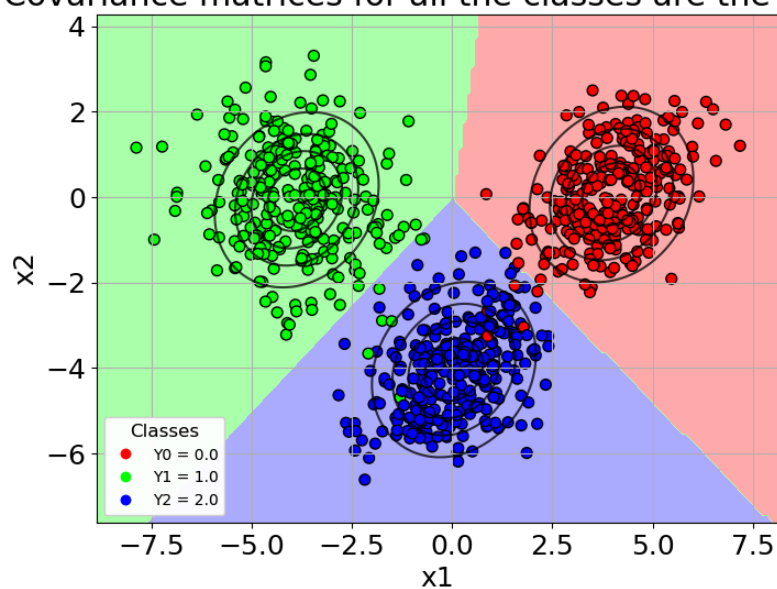


Decision Region Plot:



Decision Region Plot with Level curves on Training Data:

Decision Boundary for Bayes Classifier with Level Curves
Covariance matrices for all the classes are the same

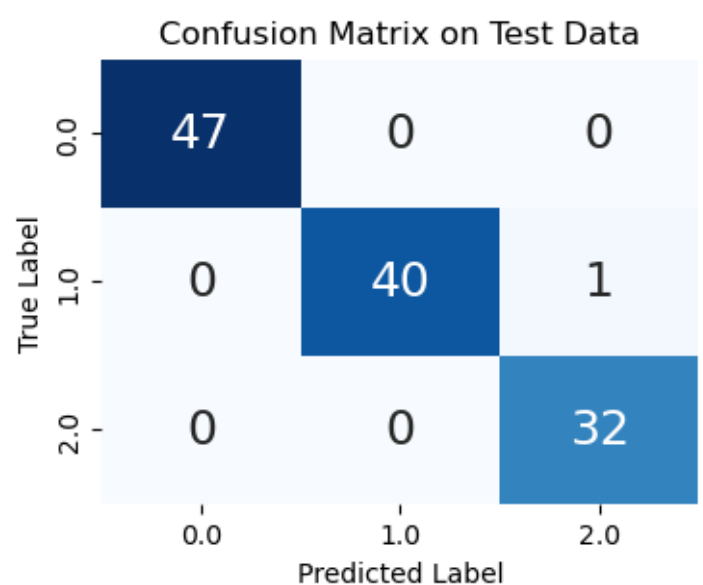
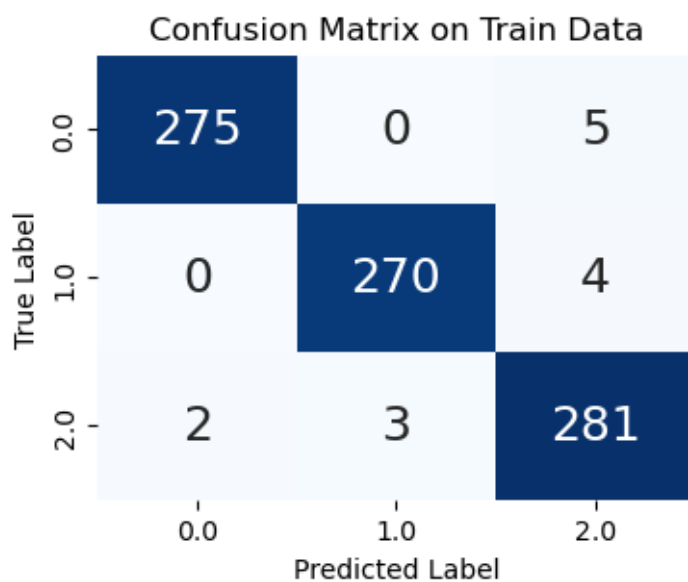


b. Covariance matrices are different

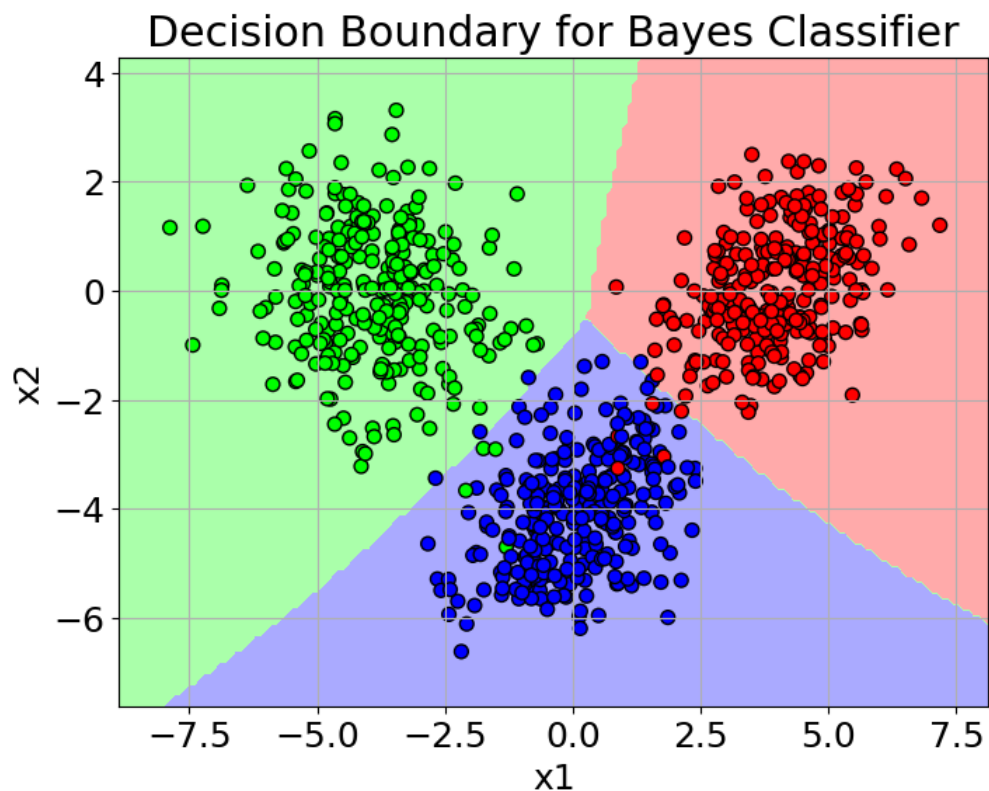
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 840 | 0.983333 |
| Validation | 240 | 0.991667 |
| Test | 120 | 0.991667 |

Confusion Matrix for the best configuration of the model, on training data and test data:

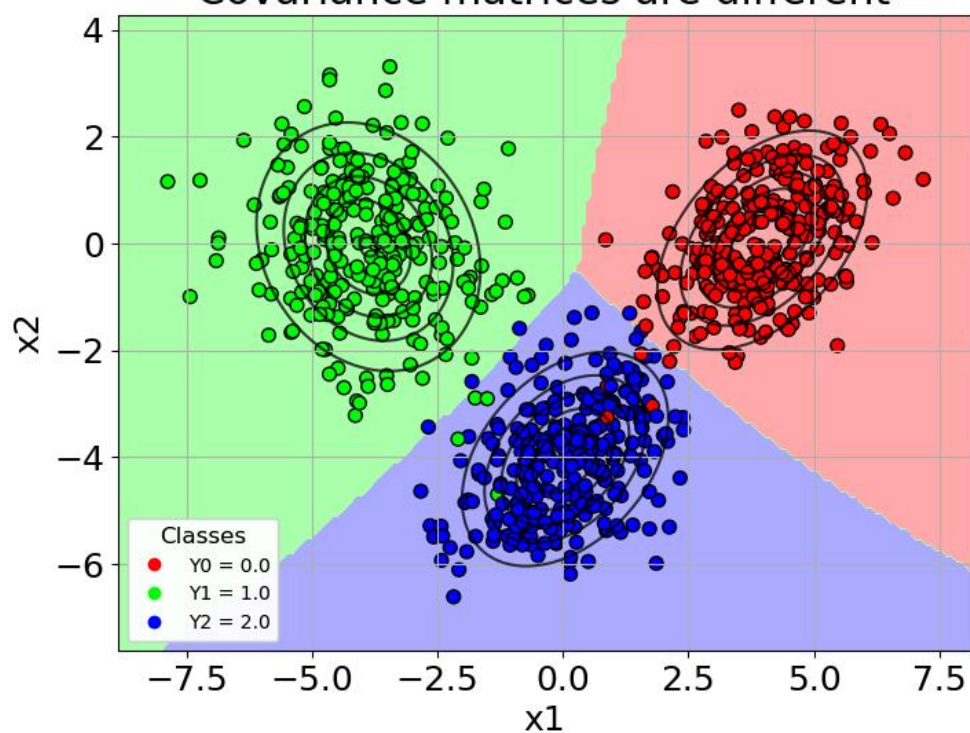


Decision Region Plot:



Decision Region Plot with Level curves on Training Data:

Decision Boundary for Bayes Classifier with Level Curves
Covariance matrices are different



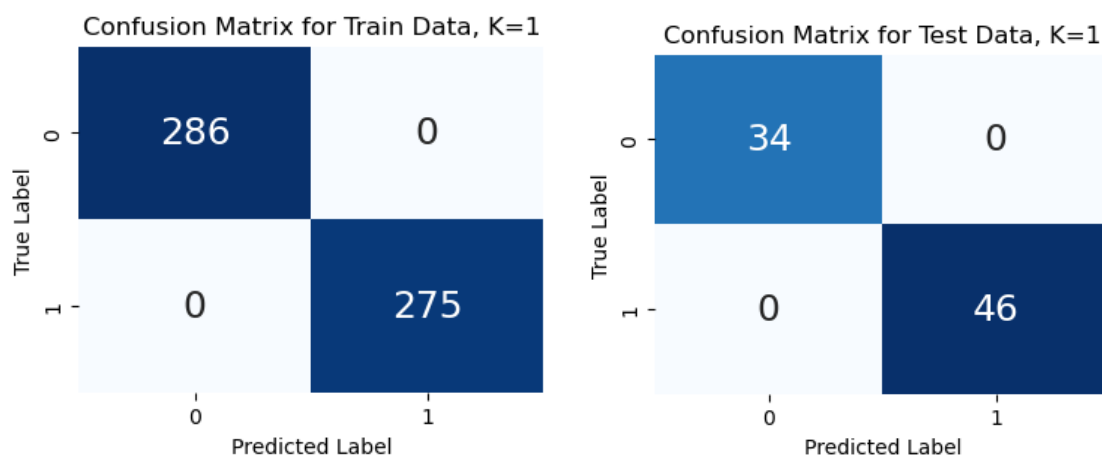
Dataset-2:

1. K-Nearest Neighbour Classifier for K=1, K=5 and K=9

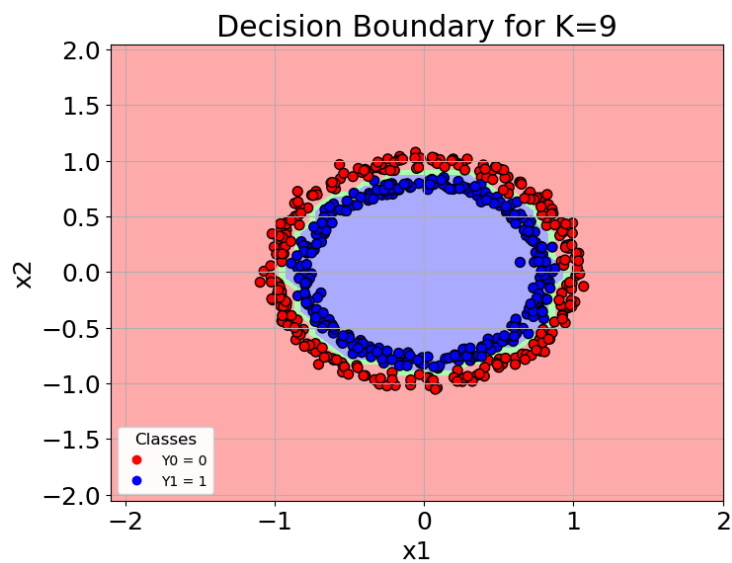
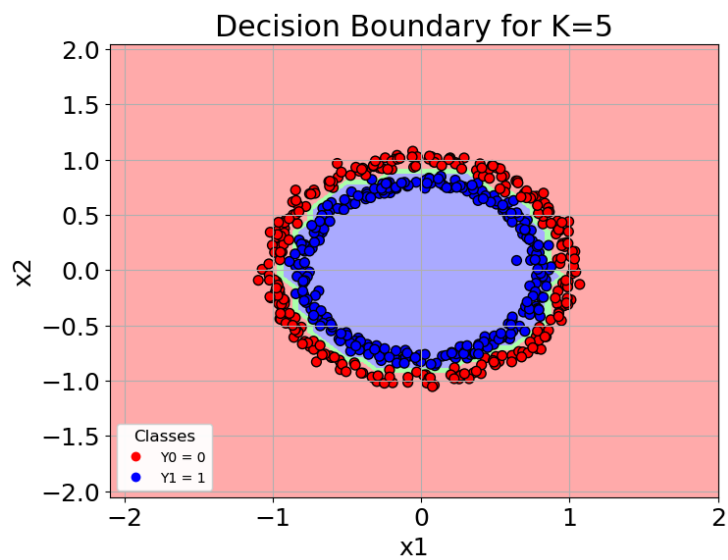
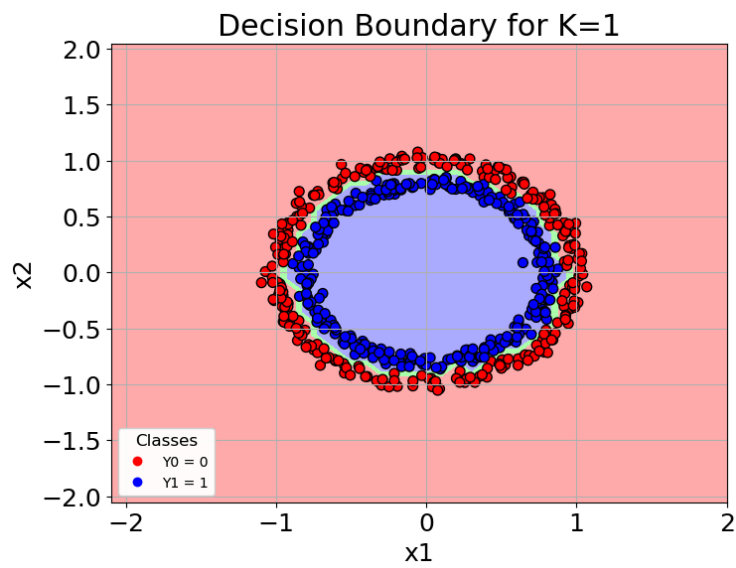
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| k-value | Accuracy train | Accuracy Val | Accuracy test |
|---------|----------------|--------------|---------------|
| 1 | 1.000000 | 1.000000 | 1.0 |
| 5 | 1.000000 | 0.981132 | 1.0 |
| 9 | 0.994652 | 0.993711 | 1.0 |

Confusion Matrix for the best configuration of the model, on training data and test data:



Decision Region Plots:

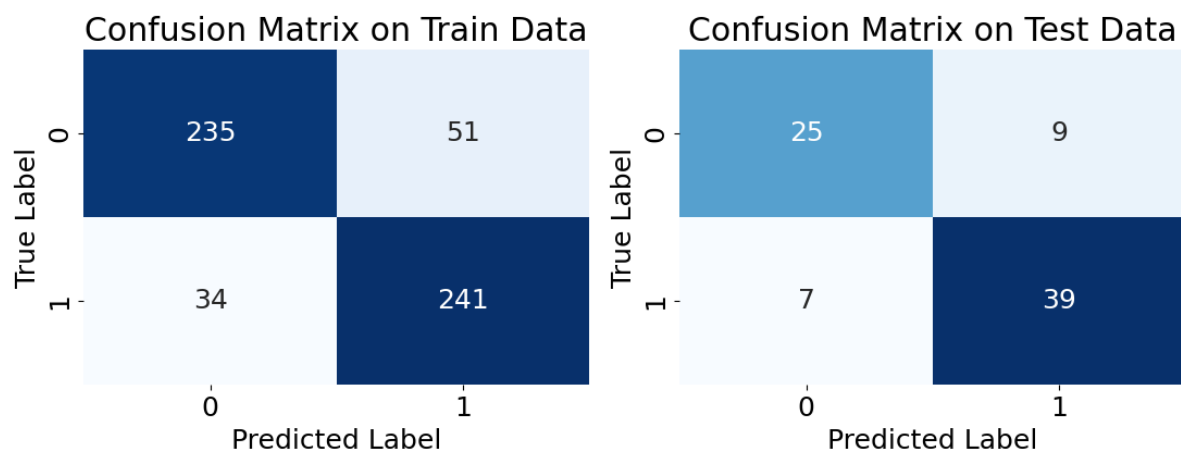


2. K-nearest representatives classifier, for K=1, K=3 and K=5: Use 10 representatives per class

Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

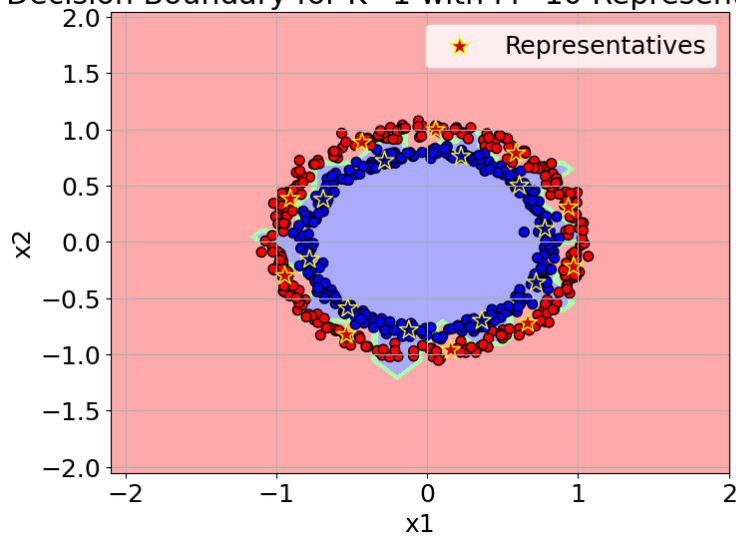
| k-value | Accuracy Train | Accuracy Val | Accuracy Test |
|---------|----------------|--------------|---------------|
| 1 | 0.848485 | 0.798742 | 0.8000 |
| 3 | 0.582888 | 0.635220 | 0.6625 |
| 5 | 0.597148 | 0.572327 | 0.5875 |

Confusion Matrix for the best configuration of the model, on training data and test data:

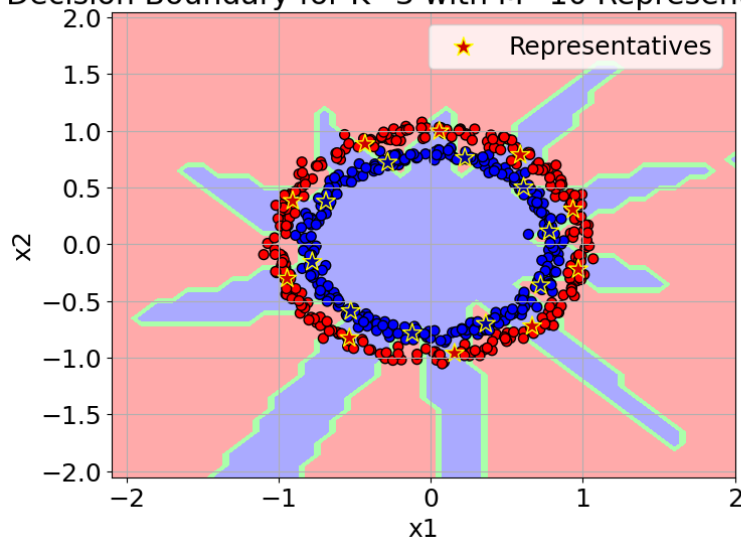


Decision Region Plots:

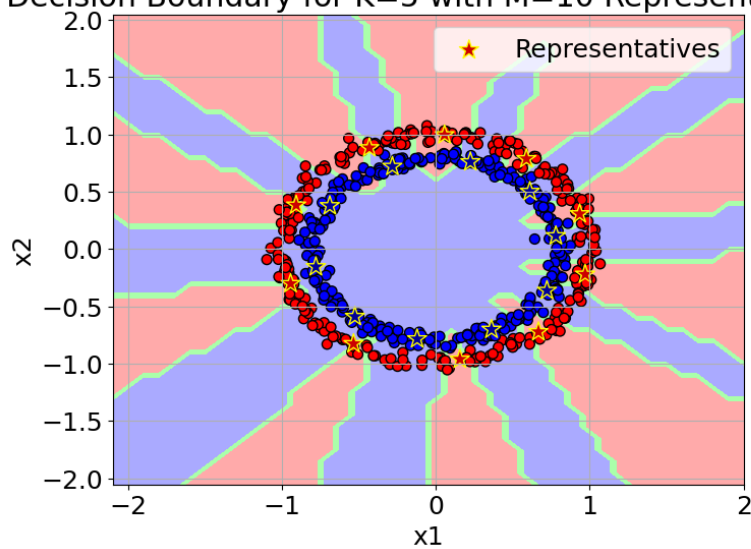
Decision Boundary for $K=1$ with $M=10$ Representatives



Decision Boundary for $K=3$ with $M=10$ Representatives



Decision Boundary for $K=5$ with $M=10$ Representatives



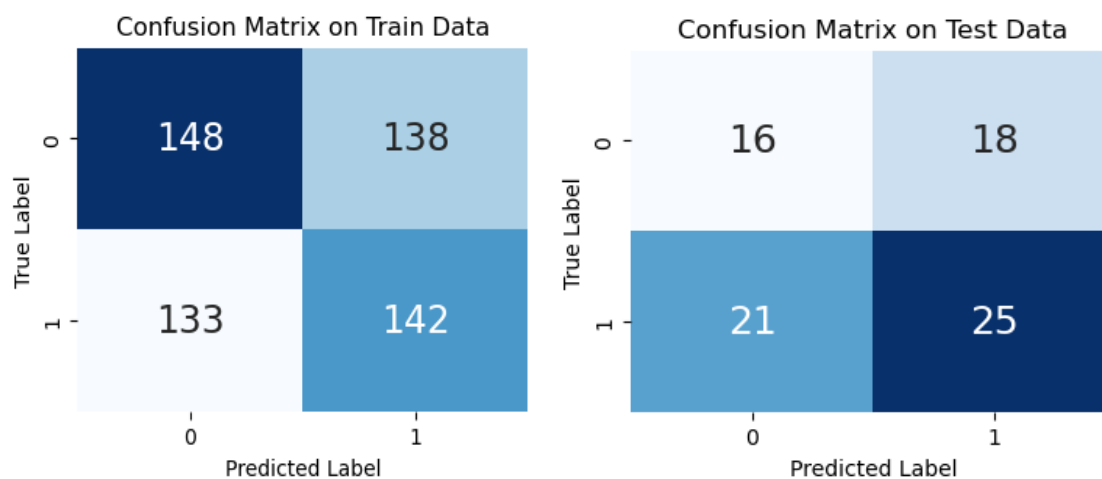
3. Bayes Classifier with a Gaussian Distribution for every class

- a. Covariance matrices for all the classes are the same

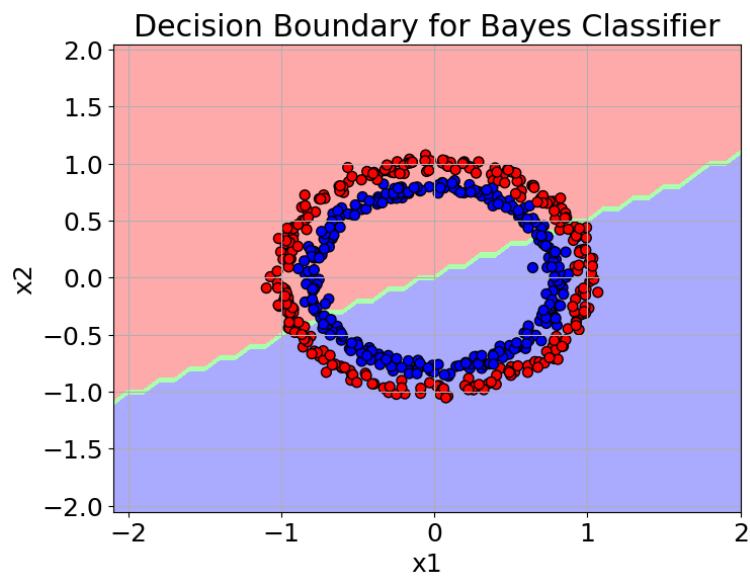
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 561 | 0.516934 |
| Validation | 159 | 0.427673 |
| Test | 80 | 0.512500 |

Confusion Matrix for the best configuration of the model, on training data and test data:

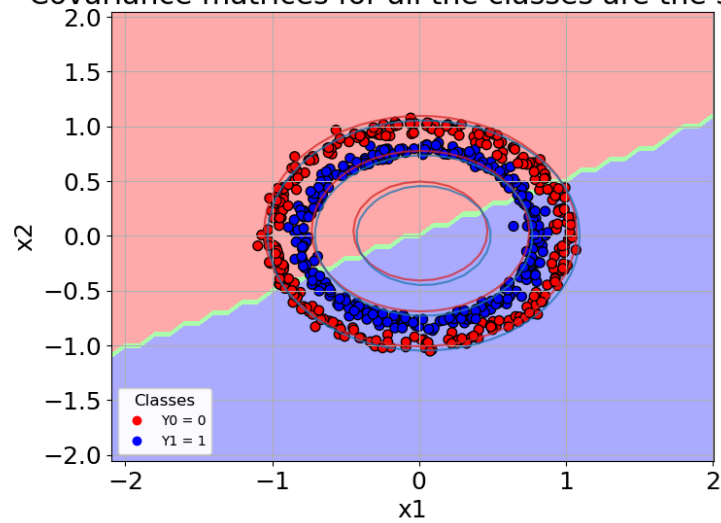


Decision Region Plot:



Decision Region Plot with Level curves on Training Data:

Decision Boundary for Bayes Classifier with Level Curves
Covariance matrices for all the classes are the same

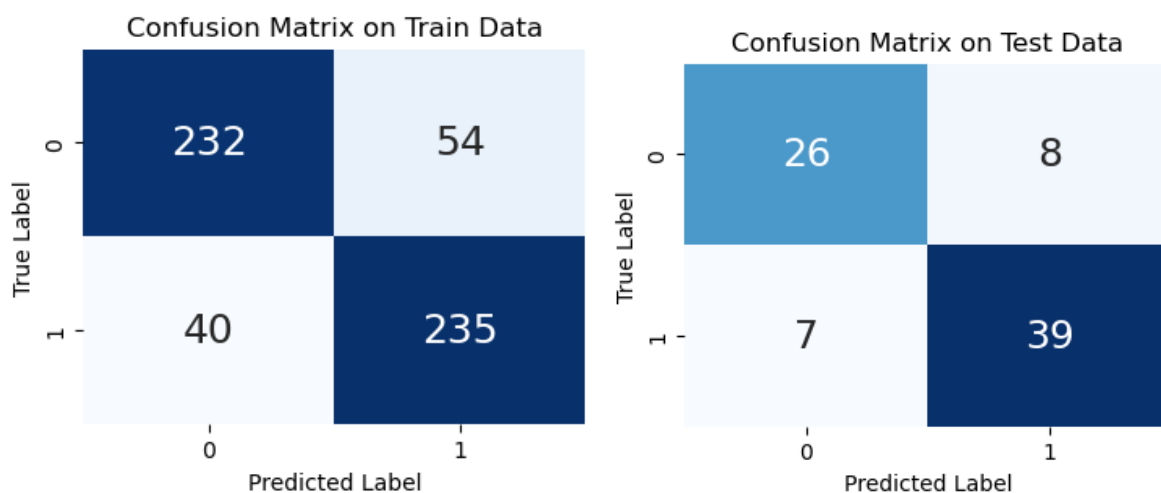


b. Covariance matrices are different

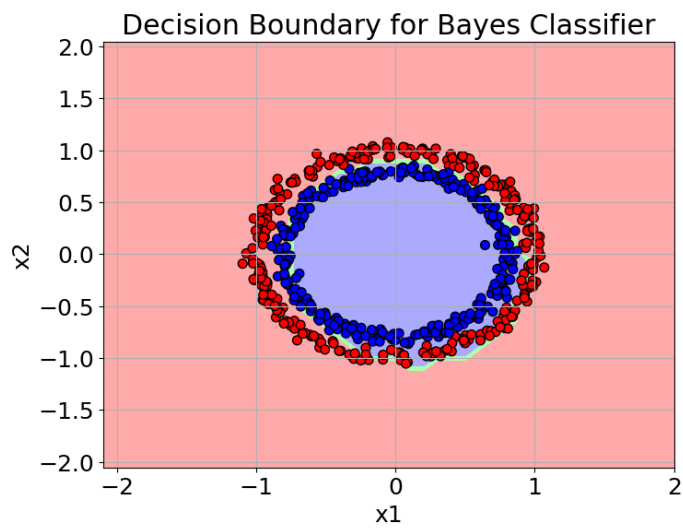
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 561 | 0.832442 |
| Validation | 159 | 0.786164 |
| Test | 80 | 0.812500 |

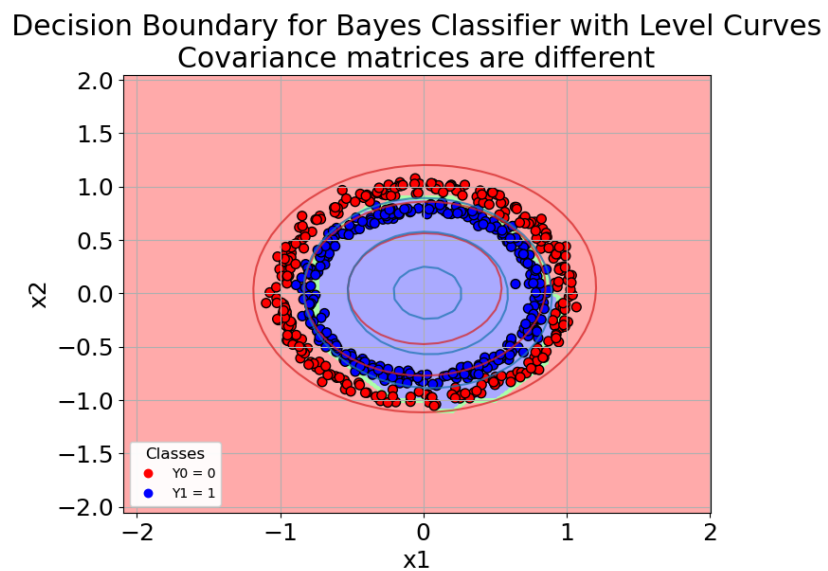
Confusion Matrix for the best configuration of the model, on training data and test data:



Decision Region Plot:



Decision Region Plot with Level curves on Training Data:



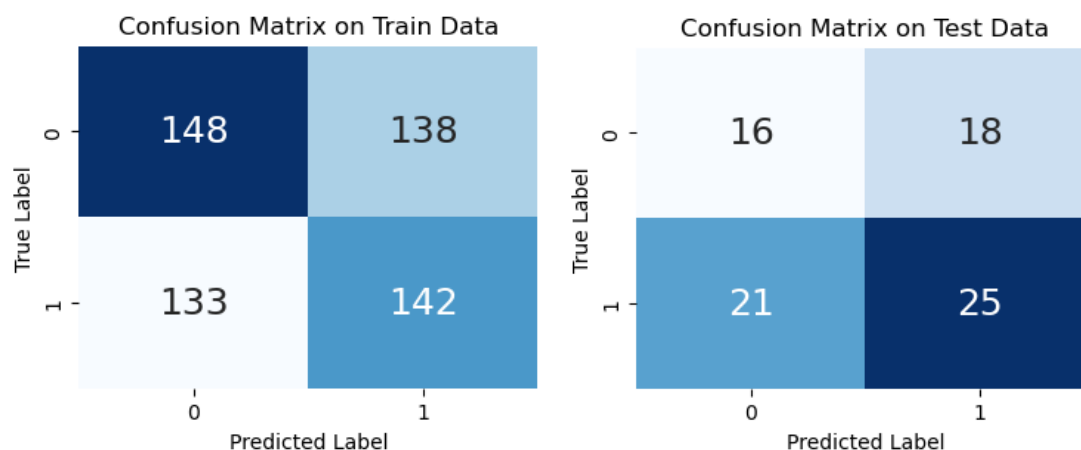
4. Naive-Bayes classifier with a Gaussian distribution for every class:

- a. Covariance matrices for all the classes are the same

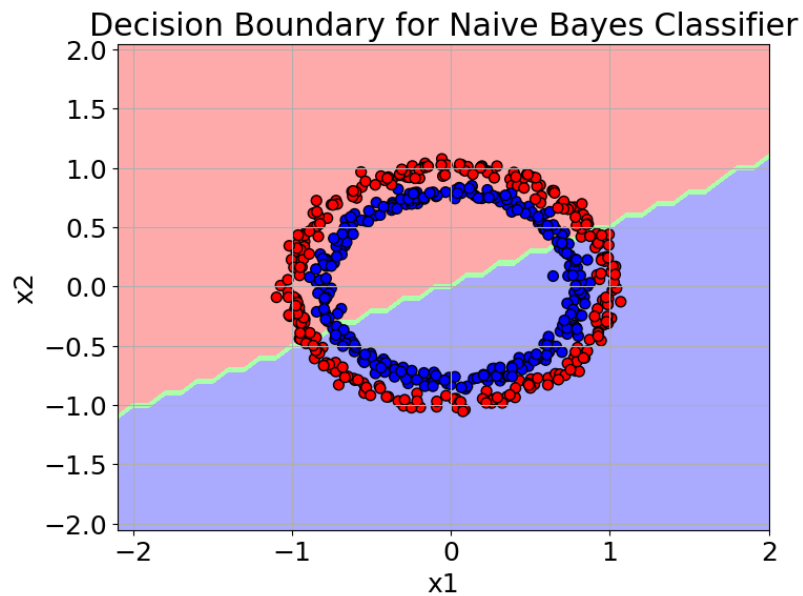
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 561 | 0.516934 |
| Validation | 159 | 0.427673 |
| Test | 80 | 0.512500 |

Confusion Matrix for the best configuration of the model, on training data and test data:

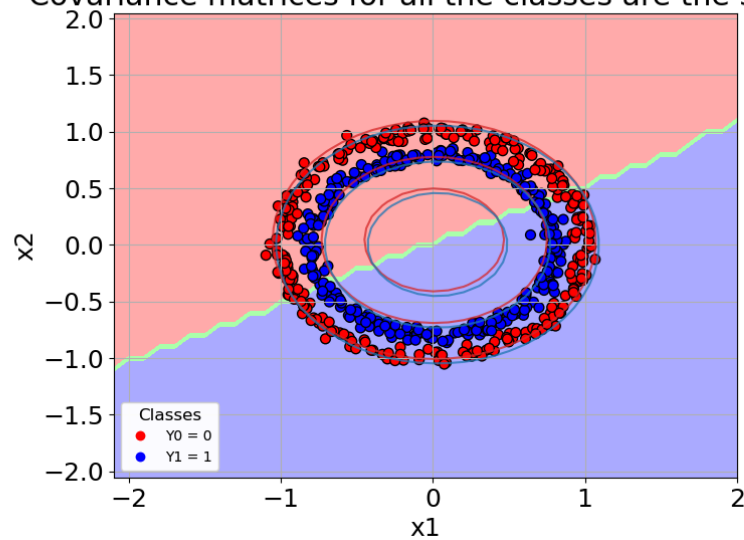


Decision Region Plot:



Decision Region Plot with Level curves on Training Data:

Decision Boundary for Naive Bayes Classifier with Level Curves
Covariance matrices for all the classes are the same

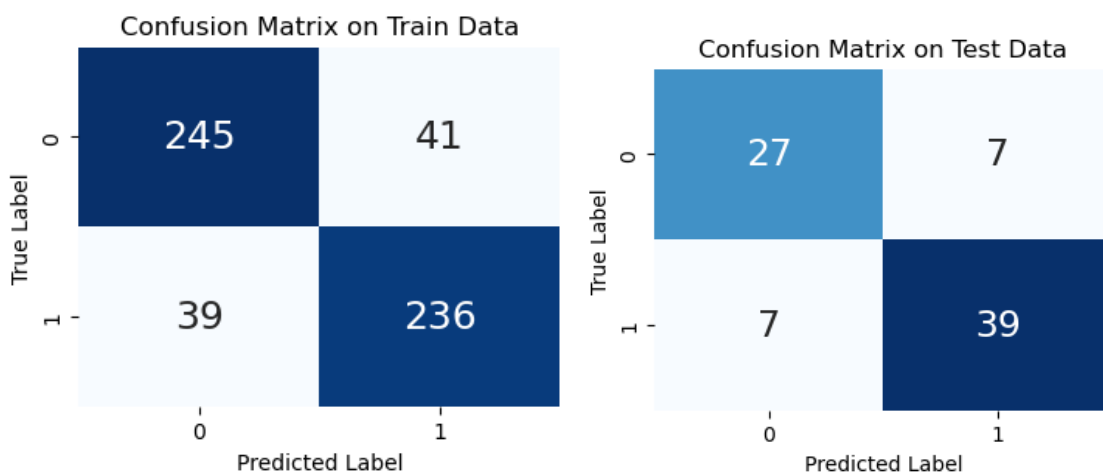


b. Covariance matrices are different

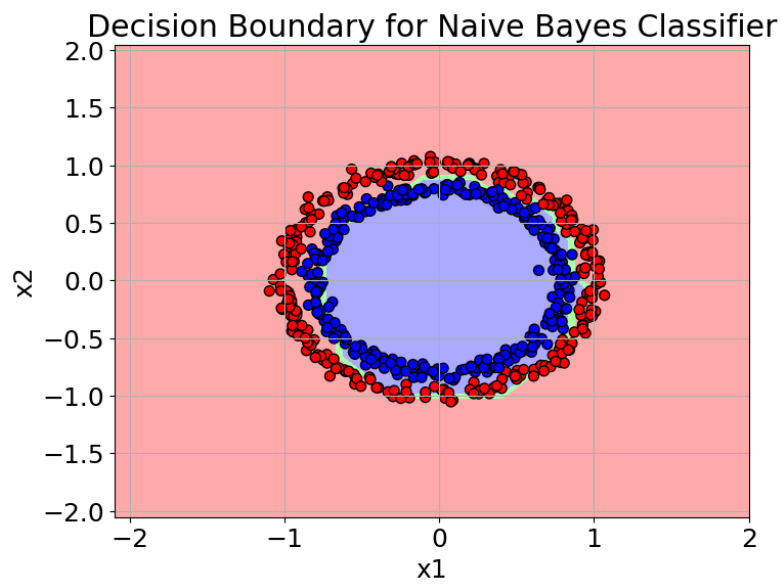
Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 561 | 0.857398 |
| Validation | 159 | 0.773585 |
| Test | 80 | 0.825000 |

Confusion Matrix for the best configuration of the model, on training data and test data:

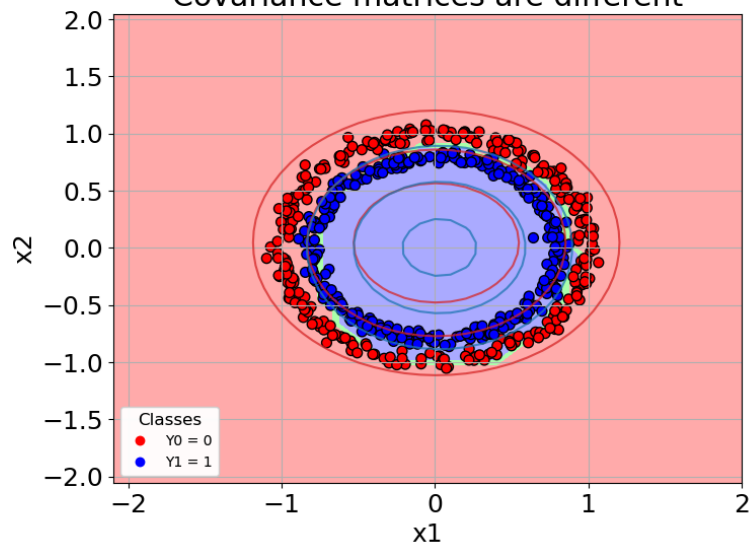


Decision Region Plot:



Decision Region Plot with Level curves on Training Data:

Decision Boundary for Naive Bayes Classifier with Level Curves
Covariance matrices are different



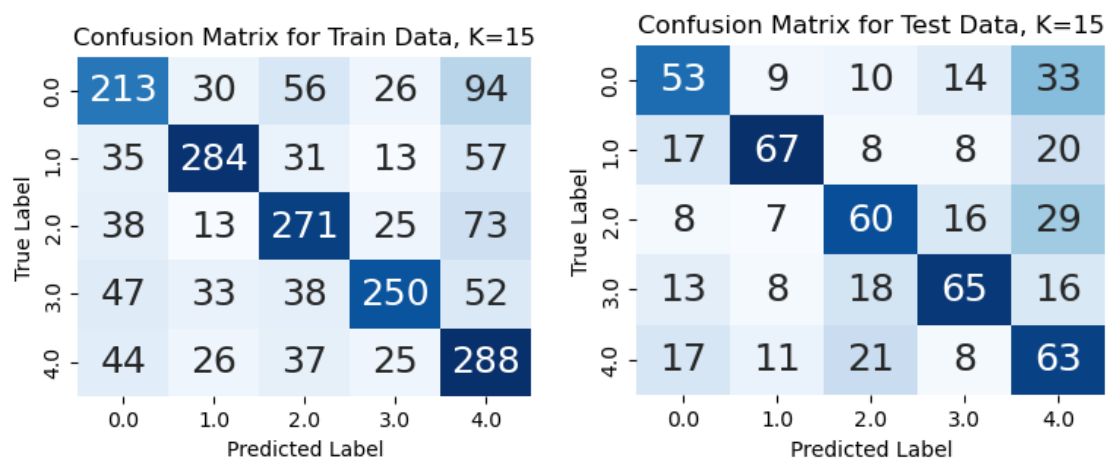
Dataset 3:

1. K-nearest neighbours classifier, for K=1, K=9 and K=15

Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| k-value | Accuracy train | Accuracy Val | Accuracy test |
|---------|----------------|--------------|---------------|
| 1 | 1.000000 | 0.387960 | 0.405676 |
| 9 | 0.669366 | 0.418060 | 0.490818 |
| 15 | 0.622201 | 0.421405 | 0.514190 |

Confusion Matrix for the best configuration of the model, on training data and test data:

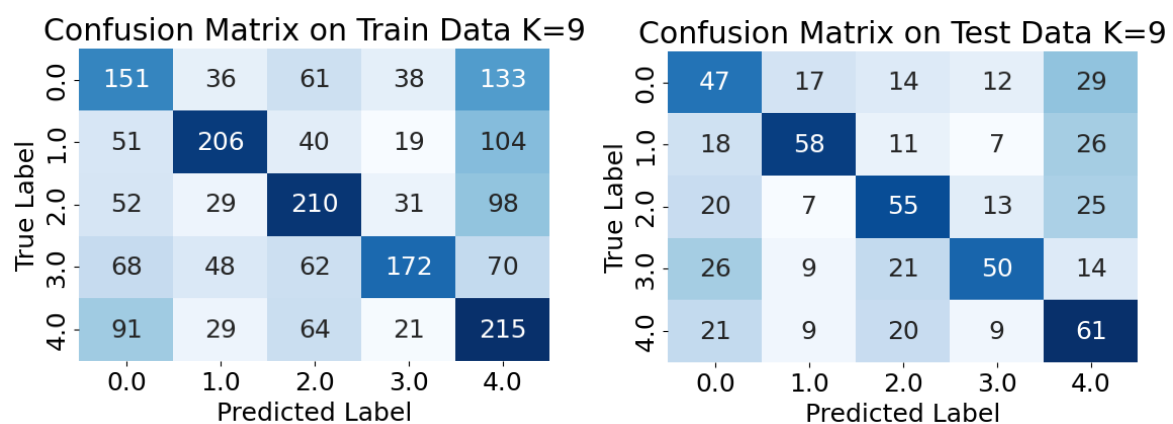


2. K-nearest representatives classifier, for K=1, K=5 and K=9: Use 10 representatives per class

Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| k-value | Accuracy Train | Accuracy Val | Accuracy Test |
|---------|----------------|--------------|---------------|
| 1 | 0.597427 | 0.384615 | 0.485810 |
| 5 | 0.501191 | 0.444816 | 0.479132 |
| 9 | 0.454502 | 0.481605 | 0.452421 |

Confusion Matrix for the best configuration of the model, on training data and test data:

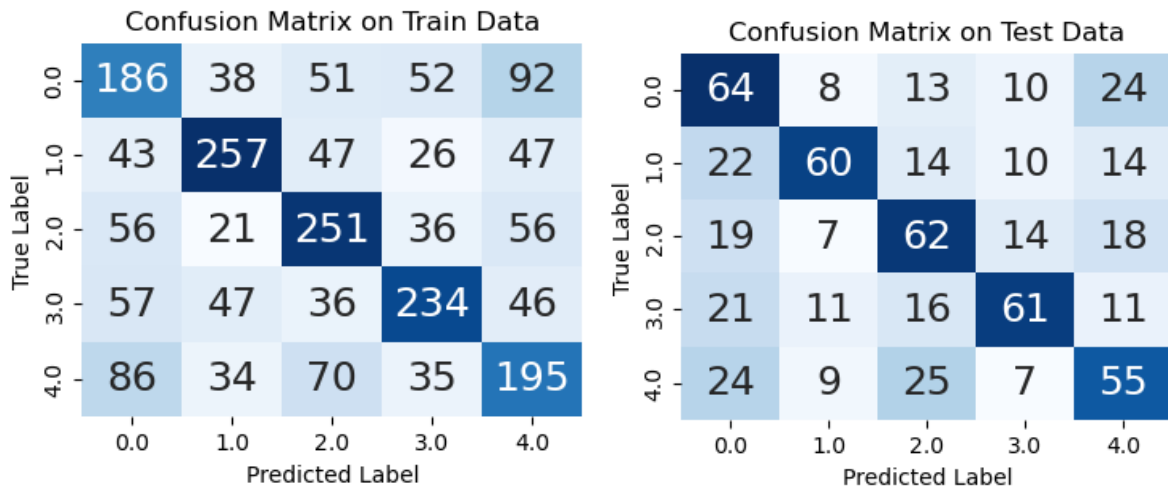


3. Bayes classifier with a Gaussian distribution for every class

Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Dataset | Size | Accuracy |
|------------|------|----------|
| Train | 2099 | 0.535017 |
| Validation | 299 | 0.451505 |
| Test | 599 | 0.504174 |

Confusion Matrix for the best configuration of the model, on training data and test data:



4. Naive-Bayes classifier with a Gaussian distribution for every class

Table of Classification Accuracies of the Model for Training data, Validation data, and Test data:

| Index | Type | Count | Score |
|-------|------------|-------|----------|
| 0 | Train | 2099 | 0.476894 |
| 1 | Validation | 299 | 0.461538 |
| 2 | Test | 599 | 0.494157 |

Confusion Matrix for the best configuration of the model, on training data and test data:

