

Quiz 3

Find Z-parameters of the BJT transistor that has S-parameters at 1.5 GHz as

$$S_{11} = 0.6 \angle -127^\circ$$

$$S_{12} = 0.039 \angle 28^\circ$$

$$S_{21} = 3.88 \angle 87^\circ$$

$$S_{22} = 0.76 \angle -35^\circ$$

Formula : S-parameters transform Z-parameters.

$$Z_{11} = Z_0 \cdot \frac{(1+S_{11})(1-S_{22}) + S_{12}S_{21}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} \quad (1)$$

$$= 50 \frac{(1 + 0.6 \angle -127^\circ)(1 - 0.76 \angle -35^\circ) + (0.039 \angle 28^\circ)(3.88 \angle 87^\circ)}{(1 - 0.6 \angle -127^\circ)(1 - 0.76 \angle -35^\circ) - (0.039 \angle 28^\circ)(3.88 \angle 87^\circ)}$$

EQN ; $Z_{11} = 30.694 \angle -28.627^\circ$ ✗

$$Z_{12} = Z_0 \cdot \frac{2S_{12}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} \quad (2)$$

$$; Z_{12} = 50 \cdot \frac{2(0.039 \angle 28^\circ)}{(1 - 0.6 \angle -127^\circ)(1 - 0.76 \angle -35^\circ) - (0.039 \angle 28^\circ)(3.88 \angle 87^\circ)}$$

EQN ; $Z_{12} = 5.2982 \angle -31.93^\circ$ ✗

$$Z_{21} = Z_0 \cdot \frac{2S_{22}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} \quad (3)$$

$$; Z_{21} = 50 \cdot \frac{2(0.76 \angle -35^\circ)}{(1 - 0.6 \angle -127^\circ)(1 - 0.76 \angle -35^\circ) - (0.039 \angle 28^\circ)(3.88 \angle 87^\circ)}$$

EQN ; $Z_{21} = 527.103 \angle 27.067^\circ$ ✗

$$Z_{22} = Z_0 \cdot \frac{(1-S_{11})(1+S_{22}) + S_{12}S_{21}}{(1-S_{11})(1-S_{22}) - S_{12}S_{21}} \quad (4)$$

$$; Z_{22} = 50 \cdot \frac{(1 - 0.6 \angle -127^\circ)(1 + 0.76 \angle -35^\circ) + (0.039 \angle 28^\circ)(3.88 \angle 87^\circ)}{(1 - 0.6 \angle -127^\circ)(1 - 0.76 \angle -35^\circ) - (0.039 \angle 28^\circ)(3.88 \angle 87^\circ)}$$

EQN ; $Z_{22} = 161.837 \angle -57.158^\circ$ ✗

Hence, z-parameters is

$$\mathbf{Z} = \begin{bmatrix} 30.694 \angle -28.627^\circ & 5.2982 \angle -31.93^\circ \\ 527.103 \angle 27.067^\circ & 161.337 \angle -57.158^\circ \end{bmatrix} \quad \#$$