

## 1) Notations:

$X$  - Input Image  
 $K$  - Kernel/Filter  
 $Z$  - Conv Output Map  
 $A$  - ReLU Activation  
 $P$  - Pooled Map  
 $F$  - Flattened Vector  
 $W, b$  - Weights & Bias  
 $\alpha$  - Learning Rate  
 $\hat{y}$  - Predicted Probabilities

CNN  
from  
Scratch

## 3) Loss Function:

$$J = \text{Cross-Entropy}$$
$$J = -\ln(\text{pred}[y])$$

## 4) Gradient Descent:

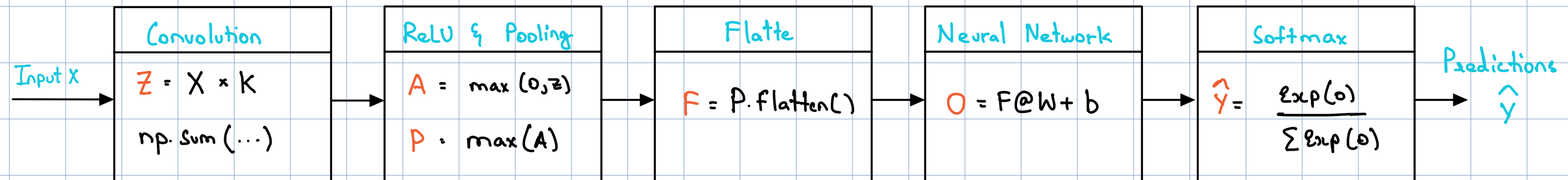
$$W = W - \alpha \cdot \partial W$$
$$b = b - \alpha \cdot \partial b$$

- kernels  $K$  are static

## 5) Accuracy:

$$\text{Accuracy} = \frac{1}{m} \sum 1(\text{argmax}(\hat{y}) == y)$$

## 2) Forward Propagation:



## 6) Backward Propagation:

$$\partial O = \hat{y} - y$$
$$\text{grad}[\text{label}] = 1$$

### Dense Weights $\partial W$ :

$$\partial W = (\hat{y} - y) \cdot F^T$$
$$\text{np.outer}(\text{self.x}, \text{grad})$$

### Dense Bias $\partial B$ :

$$\partial B = (\hat{y} - y) \cdot 1$$
$$\text{grad}(\text{for batch} = 1)$$

by  
P. Toshith