## Color Model Composition

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#### 1 Introduction

We have models, represented by  $\theta(\text{name})$ , which are sets of parameters describing a specified color. These models are derived from Randal Monroe's Color Survey data. All of these models are contained within LUX, a system designed by Brian MacMahan. Within the lexicon there exist color labels that are compositions of other labels, such as 'green' and 'blue' combining to create 'green-blue'. These color compositions are currently all stated within the lexicon. If we can derive a composition function,  $f(\theta(x), \theta(y)) = \theta'(x, y)$ , then we can simplify the LUX lexicon by removing the composed colors, thus reducing the number of parameters.

There are a few steps that are required in order to determine what this composition function is. The first step is an evaluation metric in order to determine whether or not two  $\theta$ s are the same. Afterwards, we can construct a composition function and test how well it does. Preliminary work also shows us a special case of composition functions, that will be discussed later.

### 2 Twins

In order for us to determine whether or not our f is generating a  $\theta$  that is comparable to the one already present within LUX, we must first find a baseline for  $\theta$ s in LUX that should already be identical. Within LUX, there exist  $\theta$ s, called "twins", where both  $\theta(x,y)$  and  $\theta(y,x)$  exist. We propose that these two  $\theta$  are the same, namely that  $\theta(x,y) == \theta(y,x)$ . If that is

true, then we can use the same evaluation metric on  $\theta$ 's when comparing them to  $\theta$ s, and that will tell us whether or not the two are the same.

The evaluation metrics that can be used can either be  $r^2$  or log-likelihood values, both being used on the other twin's data set. The same metric would then be applied to the  $\theta'$ , and would give us an idea of how accurate they are. Preliminary results using  $r^2$  on the twins tells us that on average, the twins have a  $r^2$  metric of .76. More can be seen in Appendix A

Figuring out what the evaulation metric result for the twins, to be used for the composition function f, doesn't actually tell us if they are the same. Rather it tells us if they are the same, then what the metrics will tell us. In order to determine whether or not they are the same, we believe that a survey needs to be conducted on each of the twins. By having people rate on a scale of 1-10 how close two colors are to each other, we can get a human perspective on which colors are the same. The twins should all have very high values, averaging anywhere from 7-10, whereas non-twin colors should have significantly lower values, averaging anywhere from 1-4. If so, then we can say with high confidence that the twins are the same, and that  $\theta(x,y) == \theta(y,x)$ , which then means that we can use the evaluation metrics to compare other distributions.

### 3 Composition f

Once we determine an evaluation metric, then we can create the composition function f. f should probably be a machine learning regressor, in the hopes that such a machine will be able to determine relationships between different parameters in the model that might not be otherwise obvious.

There are many ways to structure the inputs into f. Every one of the  $\theta$ s has a property  $\phi$ , or availability, which states how "popular" the  $\theta$  is. One way of ordering the inputs into f would be to organize them by availability, under the assumption that the more popular a  $\theta$  is, the larger of an impact it has on the resulting  $\theta'$ . Another way is to organize the inputs by their order in  $\theta'$ 's name, under the assumption that the order implies some significance in which  $\theta$  is more impactful in the composition to produce  $\theta'$ . The final, and most intuitive ordering, is to order the  $\theta$ s by their relative positions on the

color wheel, under the assumption that the mix of colors is more towards an average of the two  $\theta$ s than anything else. Such an ordering would allow for the easiest discovery of such a fact.

# 4 Special Cases of f, Noun-Colors

### Appendix

# A Twins $r^2$ Values

All values are the  $r^2$  values for the X model on the Y's data points.

First Color	Second Color	First on Second	Second on First
green-grey	grey green	0.909311	0.921990
grey-brown	brown-grey	0.541379	0.784039
red-brown	brown-red	0.875762	0.838473
purple-pink	pink-purple	0.756994	0.841505
red-pink	pink-red	0.902846	0.904270
orange-red	red-orange	0.934824	0.945147
blue-green	green-blue	0.680046	0.817502
green-brown	brown-green	0.891857	0.837641
purple blue	blue-purple	0.955867	0.943420
blue-grey	grey blue	0.923963	0.912297
violet red	red violet	0.719531	0.459585
yellow-brown	brown yellow	0.575357	0.781066
yellow-orange	orange-yellow	0.470531	0.788876
red-purple	purple-red	-0.408986	0.511436
violet blue	blue violet	0.789110	0.622474
grey purple	purple grey	0.851877	0.901247
orange-brown	brown-orange	0.512578	0.787795
green-yellow	yellow-green	0.955530	0.949561

The average is 0.760741727251.