Stat. UEM

1) X1,.., Xn iid ~ M(m, 02), Ho: M=10.

ran tower of the left-sided 2-test: Ha: M< Mo.

 $\frac{\lambda}{100} = \frac{\lambda}{100} \times \frac{\lambda$

 $= \int \left(-\frac{1}{24-\alpha} + \frac{\frac{10-\mu}{64\pi}}{64\pi}\right).$

16) Ampact on the test power: The test power is a monotonously increasing function of Mo, n and a m. decreasing function of a, M and T.

(2) Data 1: 8,8 10,5 12,5 9,7 9,6 13,2 Deta 2: 8,4 10,1 12,0 9,3 9,0 13,0

We have paired samples and assume that the differences are $\sim N(\mu d, \delta_d^2)$. Ho: $\mu d = 0$. We know that $t = \frac{T-0}{st/fm} \approx_{Ho} t_{m-1}$; we choose $\alpha = 0.05$ and decide to reject Ho if $|t| > t_{1-s/k}$, $n-1 \iff 7.68$. > 2.57... $\iff T$. The p-value is P(|t| > 7.68...) = $F_t(-7.68$...) + $(1-F_t(7.68$...)) ≈ 0.0006 , which supports our conjecture that $\mu d \neq 0$.

 $\sqrt{\frac{x_1}{y_2}} = 5,275$ $\sqrt{\frac{x_2}{s_2}} = 5,240$ $\sqrt{\frac{x_3}{s_2}} = 400$, $\sqrt{\frac{x_4}{s_2^2 + s_2^2}} = 400$.

(A) Use 95% CI to estimate Mn-M2: X1-X2 ± 21-42 \ m \times [-24,5] 24,5] he have the appearant and calculate the CI every time, it would contain the tree value in 95% of the experiments.

(b) Test Ho: $\mu_1 - \mu_2 = 0$ Nos. H₁: $\mu_1 - \mu_2 \neq 0$: $\frac{1}{x_1 - x_2 - 0} = 0$ $\frac{1}{x_1 - x_2 - 0} = 0$

 $2 = \frac{\chi_1 - \chi_2 - 0}{\sqrt{54 + 52}} \approx_{H_0} \mathcal{N}(0, 1). \quad \text{Reject if } |2| > 2_1 - 4_2 \iff 0,028 > 1,9599 \iff 1.$

p-value = PHO (12) > 0,028...) = 2\$\overline{L}(-0,028) = 0,898.

Interprehabion: If Ho is due, the probability of obtaining or result at least as extreme as the result actually observed is ~99,8%.

(c) Test Ho vs H1: M1-M2 > 0: The p-value is now PH $(7>0,028)=1-\overline{\Phi}(0,028)\approx 0,489$, which is smaller. Neverthelen, we would not rejet the. (d) Test Ho: M-1/2 = 25 vs. M1-M2 = 25. Compar to (b). $z = \frac{x_1 - x_2 - 25}{\sqrt{s_1^2 + s_2^2}} = -1,9972$ ~ $|z| = 1,9972 > 1,9599 \Rightarrow reget.$ P-value = PHo (121 > 1,9972) = 2 (-1,9972) ≈ 0,046 < 0,05. (e) What assumptions where necessary for (a) - (d)? -only one test per data set - independent samples - choose test before duty is observed 5) 1: HS: 131 74 129 96 2: HF: 44 70 69 43 3: FB: 15 14 21 29 53 21 3: FB: (a) HS vs. HF: We have independent somples. We have sample mire 5<30 and assume unequal variances. The 95% CI is $\overline{x}_1 - \overline{x}_2 \pm t_{\alpha/2}(\varphi)\sqrt{\frac{s_1^2 + s_2^2}{n}} \approx [18,0;79,2] \subseteq \mathbb{R}^t$. b) the 95% (I for M2-M3 is ≈ [19,7; 51,8] ⊆ Rt. (high five for 3 seconds).