Introduction to python 3

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## Outline

## The basics

## SciPy

## The numpy package

- 6 Plotting with matplotlib
- Symbolic computing with Sympy

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## Python references

## The basics

- · Good python book Python 3 (2017 edition) by Johannes Ernesti and Peter Kaiser
- online documentation: https://docs.python.org/3.6/

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## Historical facts

- developed in the nineties by Guido van Rossum in Amsterdam at Centrum voor Wiskunde en Informatica the name "python" comes from the comedy "Monty Python"
- python version 3.0 was released in December 2008
- one of the most popular programming languages
- designed for functional and object oriented programming
- programs that partially use python:
- - \* Google Mail
    - Google Maps
  - - \* YouTube
    - \* Dropbox
    - reddit

    - + Battlefield 2

  - RitTorrent

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## Why python?

The basics

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### What does python offer?

- Interactive
- Interpreted Modular
- Object-oriented
- Portable
- High level
- Extensible in C++ & C

## Why is python good for scientifc computing?

- open source / free many libraries, e.g.,
- scientific computing: numpy, scipy
- symbolic math: sympy
- plotting: matplotlib excellent PDE solver software:
  - ngsolve, FEniCs, Firedrake, ...

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## How to start python?

- Python can either be used interactively: simply type "python3" or "ipython3" (to start IPython) into the shell
- we can also execute python code written in a file "file.py" by typing "python3 file.pv" into the shell

Let's start with a hello world example:

## Listing 1: hello\_world.pv

```
This is our first program """
print("Hello world!")
```

## Float

decl	ara	tio	on	of	floats
***		_	01	27	27

>>> x

987.27

division	

>>>	у =	2.27
333	v /v	

- 434.92070484581495 floor division
- >>> x//y

989.27 >>> x-y 985 97 powers

>>> x+v

>>> x\*\*2

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>>> y = 2.0

>>> x\*\*3 962294095.766583

addition and subtraction >>> x = 987.27

- >>> x\*\*0.5 # square root

#### multiplication >>> x\*y

```
Integers
                                                                                     Complex number
   calculator
   >>> 1+3
   >>> 3-10

    imaginary unit in python is j

                                       floor division

    recall (a + ib) * (c + id) := ac - db + i(bc + ad)

   >>> 30*3
                                       >>> x//y
   90
                                                                                         >>> z = 1.0 + 51 # complex number with real 1 and imag 5
                                                                                         >>> z.conjugate() # conjugate complex number
   declaration of integer
                                       conversion of float to integer
   >>> x = 987
   >>> x
                                       >>> x = 1.4
                                                                                         >>> z = complex(1,5) # equivalent to 1+5;
   987
                                       >>> v = int(x)
   >>> z = int(10.0)
                                       >>> v
                                                                                         >>> z.imag # return imaginary part
   >>> 2
                                       >>> x + 3
                                                                                         >>> z.real # return real part
   multiplication and division
   >>> y = 2
                                         remember: float + int = float
   >>> x/y
   493.5
   >>> 5/3
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Complex number (continued)
                                                                                     Strings
                                                                                         declaration of strings
                                                                                         >>> a = "hello" # assign hello
   multiplication of complex numbers
                                                                                         >>> a
   >>> z1 = 1 + 4i
                                                                                         'hello'
   >>> z2 = 2 - 41
                                                                                                                            conversion of float and integer to string
                                                                                         addition of strings
   >>> z1*z2 # multiply z1 and z2
                                                                                                                            >>> x = 987.27
   (18+41)
                                                                                         >>> a+a
                                                                                                                            >>> s1 = str(x)
                                                                                         'hellohello'
                                                                                                                            >>> 81
                                                                                         >>> a+" cool"
   >>> # Let us verify this is correct
                                                                                                                             1987.271
                                                                                         'hello cool'
                                                                                                                            >>> n = 10
   >>> a, b, c, d = z1.real, z1.imag, z2.real, z2.imag
                                                                                                                            >>> s2 = str(n)
                                                                                         referencing letters
                                                                                                                            >>> 82
   >>> a*c - b*d
                                                                                         >>> fourth = a[3] # 4th letter
   18.0
                                                                                         >>> fourth
   >>> h*c + a*d
                                                                                         >>> last = a[-1] # last letter
                                                                                         >>> last
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                                                                                                                   Kevin Sturm Python 3
```

The basics

Strings (continued) Lists lower and upper case accessing letters other ways to generate lists >>> a = "hello" # assign hello >>> s = "This is a long sentence!" >>> 11 = [1]\*5 declaration of list >>> a.upper() >>> s[::3] # every third letter 555 11 >>> 1 = [] # empty list 'HELLO' 'Tas natc' >>> 1 555 0 = "g" >>> 12 = [k for k in range(5)] >>> a = "HELLO" >>> 10\*8 >>> 12 >>> 1 = [1, 2, 3] # integers list >>> a.lower() [0, 1, 2, 3, 4] >>> 1 'hello' The last command is similar to the >>> a Splitting and concatenation mathematical definition  $\{k: k =$ >>> 1 = [1.0, 3.0, 3.0] # float list 'HELLO' 0.1.2.3.4}. >>> name = "This is a long sentence." addition of lists >>> name.split() >>> a = "Hello" lists can contain anything ['This', 'is', 'a', 'long', 'sentence,'] >>> 11 = [1.2.3] >>> a.swapcase() >>> 11 = [1.2.3] >>> 12 = [4.5.6] 'hELLO' >>> 12 = ["hello", [], "new"] 'This is a long sentence.' >>> 11+12 >>> a >>> 1 = [11, 12] [1, 2, 3, 4, 5, 6] 'Hello' 555 1 inserting strings [[1, 2, 3], ['hello', [], 'new']] multiplication of lists is not sup->>> 'Insert here: {}'.format('Inserted string') ported! 'Insert here: Inserted string' イロン・ボン・ボン・モー カスの (B) (B) (E) (E) E 990 Kevin Sturm Python 3

## More on lists

>>> 1 = [1, 2, 3, 4, 4] 555 1 The list class has the following methods: [1, 2, 3, 4, 4] append >>> 1.reverse() clear 555 1 CODV [4, 4, 3, 2, 1] count >>> 1.pop(3) extend index 555 1 insert [4, 4, 3, 1] pop >>> # print every 2nd element remove >>> # start with index 1 reverse >>> # go until end of list -1 >>> # the : operation is called slicing sort >>> 1[1:-1:2]

The basics

## Tuple

 Tuple are essentially uneditable lists. We use round parenthesis. referencing possible, but no assignment to be used when list should not be modified declaration of list >>> 1 = () # empty tuple >>> 1 >>> 1 = (1, 2, 3) # tuple of integers >>> 1 (1, 2, 3) >>> 1 = tuple([1.0, 3.0, 3.0]) # conversion of list to tuple >>> 1 (1.0, 3.0, 3, 0) adding tuples

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- >>> 1+1
- (1.0, 3.0, 3, 0, 1.0, 3.0, 3, 0) >>> 4\*1
  - 3. 0. 1501 3501 3501 35 01 35 2900 Kevin Sturm Python 3

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## Bool and logical operators

bool True or False

>>> f == t

If-else example

```
Possibilities for "or":
>>> t = True
>>> t.
                                                                     x or v
>>> f = Folion
                                                   True
                                                           True
                                                                     True
>>> f
                                                                     True
                                                                     True
```

### Possibilities for "and":

False False

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>>> t and f	×	у	x and y True False False False	
False	True	True	True	
	True	False	False	
>>> t or f	False	True	False	
True	False	False	False	
>>> not f == t	1			١
True				

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## simple if-else statement

If-else

```
Listing 2: if_else.py
```

```
if condition:
    command
else:
    another command
When we have more than one condition we use elif:
```

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start and steps are optional

## Listing 3: if\_else2.py

```
if condition1:
    first command
elif condition2:
    second command
else:
    third command
                                        400 5 (5) (5) (6) (0)
```

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## Listing 4: if\_else\_ex.pv

```
if x == 1:
   print("x has value 1")
elif x == 2:
   print("x has value 2")
```

## Listing 5: if\_else\_ex2.py

```
if x == 1:
   print("x has value 1")
else:
   print("x has another value")
```

## for loop

### Listing 6: for\_loop.py

```
for n in range(10):
      print(n)

    Here n ranges from 0 to 9 and is printed after each loop.

    general syntax is range(start, stop, steps)
```

## Listing 7: for\_loop2.py

```
1 = [0, 1, 'hello', True, False]
for n in 1:
    print(n)
```





```
The basics
```

## for loop (continued)

use enumerate to count the element in the loop

## Listing 8: for\_loop\_en.py

```
1 = ['one', 'two', 'three', 'four', 'five']
for n. s in enumerate(1):
   print('Item number', n, 'item itself', s)
```

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**Functions** 

Let's have a look at an example function.

### Listing 10: func.py

```
def mv func(x):
   y = y + 10
   return x
```

- indention in python replaces brackets!!!
- @ a function always starts with def
- a return is not mandatory
- without return the function returns None.

## While loop

## The syntax of a python while loop is as follows.

```
while statement:
   do stuff
```

The basics

- . "do stuff" is executed as long as statement is true. notice again the indention!
- use break to leave a while loop
- use continue to go to the next loop

## Listing 9: while\_loop.py

```
counter = 10
while counter > 0:
   print("counter is", counter)
   counter -= 1
```

```
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```

## Functions (continued)

## anonymous functions can be defined using lambda keyword

```
>>> f = lambda x: x**2 # define lambda function f
>>> f(2)
a more complicated example
>>> f = lambda x: x**2 if x < 0 else x**3
>>> f(2)
```

#### Listing 11: lambda\_func.py

```
def f(x):
    if v < 0.
        return x**2
    else:
        return x**3
```

## Functions (optional arguments)

## It is possible to give functions optional arguments.

### Listing 12: func\_opt.py

```
def f(x, v=None):
    if v == None:
        return x**2
       return x**2 + y**2
print(f(1))
print(f(1,2))
```

## **Dictionaries**

```
make a dictionary with {} and : to signify a key and a value
>>> value1 = 1.0
>>> value2 = 2.0
```

The basics

>>> print(my\_dict) f'kev1': 1.0, 'kev2': 2.0}

>>> mv dict = {'kev1':value1.'kev2':value2}

>>> my\_dict['key1'] # access value1

>>> 'key2' in my\_dict

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```
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```

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## Dictionaries (continued)

#### Accessing the values and the keys

```
>>> # Make a dictionary with {} and : to signify a key and a value
>>> value1 = 1.0
>>> value2 = 2.0
>>> my_dict = {'key1':value1,'key2':value2}
```

```
>>> print(my_dict.values()) # return values of dictionary
dict_values([1.0, 2.0])
```

```
>>> print(mv dict.items()) # return items
dict_items([('key1', 1.0), ('key2', 2.0)])
```

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sets are unordered lists

Sets

>>> S2 = {2,3,4} declaration of sets >>> S = set([1,2,3,4]) # def. a set S >>> S1 - S2 # subtract S1 from S2

f1, 2, 3, 4} >>> S2 - S1 # subtract S2 from S1 >>> S = {1,2,3,4} # equiv. definition >>> S1 | S2 # union of S1 and S2

>>> 9 {1, 2, 3, 4}

f1, 2, 3, 4} >>> S1~S2 # summetric difference

union ∪ and subtraction \ of sets

>>> S1 = {1,2,3}

{1, 4}

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The basics SciPy The numpy package The scipy package Plotting with matplotlib ic computing with Sympy

## Sets (continued)

alternative definition

>>> S1 = {2,3,4,5}

>>> S2 = {1,2,3,4}

>>> S2.union(S1)

{1, 2, 3, 4, 5}

>>> S1.intersection(S2)
{2, 3, 4}

>>> S1.difference(S2)

```
>>> S1 = set([1,2,3])
>>> S2 = set([2,3,4])
>>> S1 = Set([2,3,4])
>>> S1 = S2 # S1/S2
(1) S2 = S1 # S2/S1
(4)
>>> S1 | S2 # union of S1 and S2
(1,2,3,4)
adding and deleting elements
>>> S1.add(10) # add 10 to list
>>> S1
```

f10, 1, 2, 3}

union ∪ and subtraction \ of sets

>>> \$1.discard(10) # remove element 10 >>> \$1 {1, 2, 3}

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## Importing modules

- import a module with command import module\_name
- a function func in module\_name can be accessed by module\_name.func

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- including with different name use import module\_name as mn
- import specific function: from module\_name import func
- import everything with from module\_name import \*

## Python key words

- We already know a few python key words.
- The keywords are part of the python programming language.

The basics

you cannot use these names for variables or functions

and	def	finally	in	or	while
as	del	for	is	pass	with
assert break class continue	elif else except False	from global if import	lambda None nonlocal not	raise return True try	yield

Figure: List of python keywords

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The basics Scilly

## Math modul

```
>>> import math # import math module and use name "math"
>>> math pi
3.141592653589793
>>> del(math) # remove math package
```

Let us consider as an example the math package.

```
>>> import math as m # import math module with name "m" >>> m.pi
```

```
>>> m.pi
3.1 41592653589793
>>> del(m)
```

```
>>> from math import pi # import constant pi from math
>>> pi
3.141592653589793
```

```
>>> from math import pi as pipi # import constant pi from math with name "pipi" >>> pipi
```

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# Immutable vs mutable datatypes (continued)

The basics

## Immutable vs mutable datatypes

- Python distinguishes two datatypes: mutable and immutable.
- immutable: float, int, string, tuple
- mutable: set, list, dict

```
The build-in function id(variable) shows the unique identity of a python object.
>>> s1 = "CompMath"
```

```
>>> s2 = "CompMath"
```

>>> id(s1) 140017699196080 >>> id(s2)

140017699196080 >>> 81 is 82 # check if 81 is 82

>>> 81 == 82 # check if s1 has same values as s2

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Let us now check lists >>> 11 = [0.1, "CompMath"]

>>> 12 = [0.1, "CompMath"]

>>> id(11) 140017702123272 >>> 1d(12) 140017702152648

>>> 11 is 12 # check if l1 is l2

>>> 11 == 12 # check if l1 has same values as 12

So both lists are different, but have exactly the same values.

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>>> 11 = [0.1, "CompMath"]

>>> 11[0] = 0.0

>>> 11 [0.0, 'CompMath'] >>> 12 [0.0, 'CompMath']

Immutable vs mutable datatypes (continued)

## Immutable vs mutable datatypes (continued)

>>> 12 = 11 >>> 11 is 12 # check if s1 is s2 >>> 11 == 12 # check if s1 has same values as s2 >>> 1d(11) 140017702570248 >>> id(12) 140017702570248

```
So how can we copy a list?
>>> 11 = [0.1, "CompMath"]
>>> 12 = 11[:] # this generates a copy of l1
>>> 11 is 12 # check if s1 is s2
>>> 11 == 12 # check if s1 has same values as s2
>>> 1d(11)
140017702152648
>>> id(12)
140017702123272
```

- if list elements are mutable itself the previous copying does not work as one might expect
- >>> change = [0, 0, 0] >>> 11 = [1, 2, change]
- >>> 12 = 11[:] # change is not copied here

In this case one can use deepcopy of the module copy.

- >>> change = [0, 0, 0]
- >>> 11 = [1, 2, change] >>> import copy
- >>> 12 = copv.deepcopv(11)

- a is b vs a==b
  - The way python 3 is implemented the integer numbers [-5, 256] are cached. For integers in this range python only returns a reference to the same element.
  - >>> a = 1 >>> c = 1000 >>> h = 1 >>> d = 1000 222 14(0) 222 14(c) 140017702160560

The basics

- >>> id(b) >>> id(d) 94324142568192 140017702161520
- >>> a is b ## a and b same >>> c is d ## two different references True

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- >>> a == b >>> c == d
  - True True

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print(f(0.1))

Local vs global variables

Local vs global variables - example

How to figure our which variables are defined so far?

- · dir() list defined variables in scope
- globals() dict of global variables
- locals() dict of local variables in scope (including values)

Listing 13: dirs.py

```
b = 0.
def f(x):
    a = 0.0
    print("local variables in f", locals())
    print("local variables f", dir())
    return x
```

print("local variables in current scope", locals())

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Classes

Classes

## Listing 14: class\_ex.py

```
class simple:
   pass
```

- keyword class defines a class with name simple
- keyword pass means that the class simple does nothing

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```
Listing 15: class_ex2.pv
```

```
class simple_two:
    a = 0.1
    s = "hello"
t = simple_two() # define class instance
print(t.a) # print variable a
```

The basics

- keyword class defines a class with name simple
- · keyword pass means that the class simple does nothing

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Classes - methods

### Classes - constructor

#### Listing 16: class\_construct.pv

```
class test:
    def __init__(self, a = 0.0): # constructor
        self.a = a
C1 = test(0.1) # create instance C1 with value a = 0.1
C2 = test() # create instance C2 with default value
print(C1.a) # print value of variable a
```

- a class constructor is defined by init, which is called upon initialisation of the class
- the class test has an optimal argument a, which is by default 0.0 Kevin Sturm Python 3

## Listing 17: class\_method.pv

```
class test:
   def __init__(self):
       print("This is the constructor.")
   def func(self):
       print("This is the func.")
C = test() # create instance C
C.func() # call func()
```

- the first argument of a method (here func(self)) must be self function is accessed via C.func()
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```
The basics
                                                                                                                The basics
                                                                                  What is self?
Classes - methods

    self is basically a reference to the class instance

                       Listing 18: class_method2.py
                                                                                        • the name does not have to be "self", but it is recommended
   class test:

    the first argument of a method in a class is always self

                                                                                                               Listing 19: self.py
       def init (self):
           print("This is the constructor.")
                                                                                      class test:
       def func2(self, b):
                                                                                          def __init__(self):
           print("This is func2 with b = {}".format(b))
                                                                                              print("This is the constructor.")
   C = test()
                                                                                          def we call self(self):
   C.func2(0.3) # call func2(0.3)
                                                                                              print("This is self", self)
                                                                                      C = test()
      • the first argument of a method (here func(self)) must be self (see next slide)
                                                                                      C.we_call_self()
                                                                                                                                     4 D 2 (B) 4 E 2 4 E 2 B 4 Q C
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                                                                                                               Kevin Sturm
```

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Inheriting classes

statement-N

```
As in C++ we can inherit classes. The basic syntax is as follows:

class Derived_ClassName(Base_ClassName):
    statement-1
    .
.
```

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Inheriting classes: example

def g(self, x, y):

return x + y

```
Listing 20: inherit.py

class Base_Class:

def f(self, x):
    return x

class Derived_Class(Base_Class):
```

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```
    Base_Class() contains the functions f(x)

    Derived Class extends Base Class() by g(x, y)
```

Writing to files

The basics

## Reading files

### • we can read a file with open("filename", 'r')

We now want to read the file

## Listing 21: readme.txt

```
This is CompMath.
We want to read this file.
```

```
>>> file = open("code/code lec2/readme.txt", 'r')
>>> print(file.readlines())
['This is CompMath.\n', '\n', 'We want to read this file.\n']
>>> file.close()
```

```
we can write to a file with open("filename", 'w')
@ if "filename" is not there it will be created
```

```
file = open("code/code lec2/writeme.txt", 'w+')
file.write("We write this into writeme.txt")
file.close()
```

```
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```

## Further options of

#### The function open has the following options. (Taken from help(open)).

```
open for reading (default)
open for writing, truncating the file first
create a new file and open it for writing
open for writing, appending to the end of the file if it exists
binary mode
text mode (default)
open a disk file for updating (reading and writing)
universal newline mode (deprecated)
```

## Reading and writing lines

Now suppose we want to add text to the beginning of the file prepend.txt file = open("prepend.txt", 'a+') # open file prepend.txt file.seek(0) # start at beginning of file s = ["This text should go at the beginning."] file.writelines(s) file.close()

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## **Doc-Strings**

## What is a doc string?

 doc-string is convenient way do describe document modules, functions, classes. and methods

### How do we define a doc string?

a doc-string has the syntax """ documentation here """

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#### How do we use a doc string?

The doc string can be accessed with .\_\_doc\_\_.

## Doc-String: example

```
Listing 22: doc_string.pv
```

```
""" This is a doc string. """
def f(x, y = 0.0):
    This function adds numbers x and y.
    The variable y is optional. Default is y = 0.0
    return x + y
#print("call doc string with f.__doc__:", f.__doc__)
print("alternatively use help(f):", help(f))
```

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Decorators - Example 1

## Decorators

### The basic decorator code structure is as follows:

```
def decor(func):
    def inner():
        func()
    return inner
Usage:
```

### dec = decor(func)

- · decor is a wrapper function essentially a function that returns a function
- the decorator gets as argument a function (func()) and returns another function (inner())
- the "actual" coding happens inside the inner function

## Listing 23: decorator\_.py

```
from math import exp
def f(x, v):
    return exp(x*y) + y
def deco(func).
    y = 0.0 \# define value for y
    def f1(x):
        return func(x, y)
    return f1
```

The basics

## Decorators - Example 3

## Listing 24: decorator2\_.py

```
from math import exp
def f(x, y):
    return exp(x*v) + v
def deco(func, v): # decorator has v as argument
    def f1(x):
        return func(x, v)
    return f1
de = deco(f, 5)
print(de(0.1))
```

```
Listing 25: decorator3..pv
from math import sin, cos
 def func_comp(fun1, fun2):
     def f1(x):
         return fun1(fun2(x))
      return f1
  de = func_comp(cos, sin)
 print(de(0.1))
```

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Recursion without loops

## Recursion without loops

Suppose we want to implement the factorial n. A loop approach would be as follows:

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## Listing 26: factorial\_loop.py

```
def fac(n):
    val = 1
   for k in range(1, n+1):
        val = val*k
    return val
print(fac(10))
```

#### As second approach without loops is

## Listing 27: factorial\_loop\_free.pv

```
def fac(n):
    if n == 1:
       return 1
    else:
       return n*fac(n-1) ## function fac called with n-1
print(fac(10))
```

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## Recursion without loops

 $\ensuremath{\bullet}$  using second approach avoid calling function multiple times!! Consider

$$x_{n+1} = \frac{1}{2} \left( x_n + \frac{1}{x_n} \right).$$

## Listing 28: babylon\_bad.py

```
def babylon(n):
    x0 = 10
    if n == 1:
        return x0
else:
        return (1/2)*(babylon(n-1) + 2/babylon(n-1))
```

problem: if  $a_n$  is number of function calls, then  $a_n=2a_{n-1}$  and hence  $a_n=2^n$  function calls are need. In total to compute recursion at stage n we need  $\sum_{n=0}^{n}a_n = 2^{n+1} - 1_2$ 

```
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The basics
SciPy
The numpy package
The scipy package
Plotting with matlotlib
```

\*args and \* \* kwargs

- sometimes the number of arguments a function gets is unknown. Then we can use \*arg and \*\*kwargs.
- kwargs keyword arguments; args normal arguments
- The actual names args and kwargs are irrelevant, we could also use \*va, only the star \* matters; same for kwargs.

Basic syntax is as follows:

```
def f(farg, *args, **kwargs):
    # do something with args, farg and kwargs
```

- inside the function f args will be a tuple and kwargs a dictionary.
- the order of farg, args and kwargs matters: positional argument follows keyword argument

## Recursion without loops

using second approach avoid calling function multiple times!! Consider

The basics

$$x_{n+1} = \frac{1}{2} \left( x_n + \frac{1}{x_n} \right).$$

### Listing 29: babylon\_good.py

```
def babylon(n):
    x0 = 10
    if n == 1:
        return x0
else:
    xn = babylon(n-1)
    return (1/2)*(xn + 2/xn)
```

better: here we have  $a_n=a_{n-1}$ , so  $a_n=a_0=1$  and hence in total  $\sum_{\ell=0}^n a_\ell = n+1$  for n=1.

```
Plotting with mat
Symbolic computing with
```

\*args- example 1

## Listing 30: args\_ex1.py

```
def f(*args):
    print(type(args))
    print(args)

5 f(1,2,3)
6 f([1,1,3,4,'hello')
```

\*args- example 2

- To illustrate \*args, we want implement the polynomial  $p(x) = a_n x^n + \cdots + a_1 x + a_n.$
- The number n of coefficients  $a_0, \ldots, a_n \in \mathbb{R}$  is variable; hence we can define a python function polynom(x, \*args)

```
*args- example 2
```

```
Listing 31: args_ex2.py
def polynom(x, *args):
    n = len(args)
    0.0 = 1 \text{ Gy}
    print(type(args))
    for k in range(n):
        val += args[k]*x**k
    return val
a = (1, 2, 3, 4)
print(polvnom(0.1, *a))
                                              4 m x 4 m x 4 2 x 4 2 x 2 x 4 0 9 9 9
print(polynom(0.1, 1,
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```

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\*kwargs - example 1

With kwargs we can give a function an arbitrary number of optional keyword arguments.

```
Listing 32: kwargs_ex1.pv
```

```
def f(**kwargs):
   print(type(kwargs))
   print(kwargs)
f(a=1, b=2, c=3)
d = {'a':1, 'b':1, 'c':1}
f(**d)
```

Measuring time - in ipython shell

- in the ipython shell one can use time to measure the time a function call takes
- usage: %time sin(1) to find the time it took to eval sin at 1.
- to get more accurate average use %timeit which runs 1000000 loops

## Measuring time

. to measure time of code segments we can use the time module

## Listing 33: measuring\_time.pv

```
import time # time module
def tic(): # start measuring time
   global start
   start = time.time()
def toc(): # end measuring time
   if 'start' in globals():
       print("time: {}.".format(str(time.time()-start)))
   else:
       print("toc(): start time not set")
```

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What is time time()

- The function time.time() return time since epoch in second.
- For Unix system, January 1, 1970, 00:00:00 at UTC is epoch.

#### We test this:

```
>>> import time
>>> time.time() # epoch time in second
>>> time.time()/(60*60*24*365.25) # convert in years
>>> T = time.time()/(60*60*24*365.25)
>>> 2019 - T
1969.6624800312309
```

Measuring time (continued)

Let us now use the functions tild and too to measure for instance the time to evaluate sin and cos

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### Listing 34: measuring\_time.py

```
from measure_time import tic, toc
from math import sin, cos
sin(1.0)
cos(1.0)
 toc()
```

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## Measuring time of function evals

- we can now combine our knowledge of decorators, \*args and \*\*kwargs and the time measurement to write a function which measures the execution time of a function
- rather than putting tic and toc before and after a function in the code, we want to have a function calculate time(func) which measures the execution of func

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## Measuring time of function evals - example 1

The basics

## Measuring time of function evals - example 1

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```
Listing 35: measuring_time.py
import time
def calculate time(func):
   def inner1(*args, **kwargs):
      begin = time.time()
      func(*args, **kwargs)
       end = time.time()
      print("Total time taken in : ", func.__name__, end
           - begin)
                                       400 (8) (8) (8) (8)
```

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```
Listing 36: measuring_time2.pv
from measure_time_func import calculate_time
 import math
# test how long it takes to eval sin
SIN = calculate_time(math.sin)
STN(10)
```

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return inner1

Call by value

```
Call by reference vs. call by value
```

## Listing 37: func\_call\_by\_ref.py

```
1 1 = [1,2]
 print('id', id(1)) # print identity of 1
 print('1', 1, '\n') # print list 1
  def add(1):
     1 += [1]
  add(1) # call add()
 print('id', id(1))
 print('1', 1)
```

```
    function calls in python are call by reference if the object that is passed is

   mutable
```

· for immutable objects (e.g., float, tuple, int) only a copy is passed

## Call by reference

print('a', a)

94324142568224

## Evaluating functions at multiple values

The basics

## Listing 38: func\_call\_by\_val.py a = 1 print('id', id(a)) print('a', a) def add(a): a += 1 print('id', id(a))

```
    How to evaluate a function f(x) for a list of values, say.

     1 = [1, 2, 3, 4, 4, 4]?
   o solution: use map(f, 1)
>>> f = lambda x: x**4
>>> 1 = [1, 2, 3, 4, 4, 4]
>>> map(f, 1)
<map object at 0x7f586960ce10>
>>> print(list(map(f,1)))
[1, 16, 81, 256, 256, 256]
```

a+=1 vs. a = a+1for mutable objects a += b returns the same reference of a for mutable objects a = a + b return a new object a

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>>> a = 1 >>> a = [1,2,3] >>> id(a) >>> id(a) 94324142568192 140017702104968 >>> a += 1 >>> a = a + [1] >>> id(a) >>> id(a) 94324142568224 140017702025160 >>> a = [1,2,3] >>> a = 1 >>> a = a + 1 >>> id(a) >>> id(a) 140017702026696

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>>> a += [1] >>> id(a) 140017702026696

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### Online resources

SciPv is collection of open source software for scientific computing in Python:

numpy

sympy

 SCIDV matplotlib IPvthon

a and more ...

pandas

Online documentation: https://scipv.org/doc.html

The numpy package

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The numpy package

The numpy package

## The numpy package

The numpy module offers the following functionalities:

- a powerful N-dimensional array object
- sophisticated (broadcasting) functions
- basic linear algebra functions
- basic Fourier transforms
- sophisticated random number capabilities
- tools for integrating Fortran code tools for integrating C/C++ code

The numpy package is import by

import numpy as np

## Numpy arrays

arrays are defined by a = np.array([], dtype = datatype)

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- dtvpe is optional
- · each entry of an array has to hold same data type (unlike python arrays)
- exampe: a = np.array([1,2], dtype = float) or shorter a = np.array([1,2])

For a thorough intro of operations on arrays we refer to https://scipy-lectures.org/intro/numpy/operations.html.

## Accessing arrays

```
>>> # let's define an array
                                    >>> # accessing arrays
>>> a = np.array([1,2,3])
                                    >>> A = np.array([[1,2,3], [2,2,2]])
>>> a
                                    >>> A
array([1, 2, 3])
                                    array([[1, 2, 3],
>>> type(a)
<class 'numpy.ndarray'>
                                    >>> A[0,1] # element (0,1)
                                    >>> A[0][1] # element (0,1)
```

```
>>> A[0] # first row
>>> A[0][:] # same
arrav([1, 2, 3])
>>> A[:, 0] # first column
```

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The numpy package

## Array multiplication

array([[2, 3],

- Matrix multiplication between arrays via np.dot(A,B) or A@B
- A\*B multiplies A and B elementwise!!!

```
>>> A = np.array([[1,2], [2,3]])
                                   >>> A*B
>>> B = np.array([[0,1], [1,1]])
>>> A@B # matrix prod of A and B
array([[2, 3],
>>> np.dot(A.B) # same
```

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Accessing arrays (continued)

```
>>> # let's define an array
                                   >>> # accessing arrays
>>> a = np.array([[1,2,3], [0,-1,2])>>> A = np.array([[1,2,3], [2,2,2]])
                                    >>> A
>>> ind = [0, 1]
                                    array([[1, 2, 3],
>>> a[:,ind]
                                    >>> A[0,1] # element (0,1)
array([[ 1, 2],
                                    >>> A[0][1] # element (0,1)
                                   >>> A[0] # first row
                                    >>> A[0][:] # same
                                    arrav([1, 2, 3])
                                   >>> A[:, 0] # first column
```

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array([[1. 2].

## More standard operations on array

```
    tensor product of array a and b via np.dot(a,b) or

  a[:.np.newaxis]*b[np.newaxis.:]
```

sum all elements of array A via A.sum(); sum only first axis A.sum(axis=1)

```
>>> A = np.array([[1,2], [2,3]])
                                   >>> a = np.array([1,2,3])
>>> B = np.array([[0,1], [1,1]])
                                   >>> b = np.array([3,4,5])
                                   >>> np.outer(a,b) # tensor product
>>> A0R
                                   array([[ 3, 4, 5],
                                          [ 6. 8. 10].
                                          [ 9, 12, 15]])
>>> np.dot(A,B)
                                   >>> a[np.newaxis].T*b[np.newaxis] # same --
                                   array([[ 3, 4, 5],
                                          [ 6. 8. 10].
                                          [ 9, 12, 15]])
>>> A
```

array([-2, 4, -2])

## Standard matrices

```
    numpy implements standard matrices such as the identity
```

```
>>> I = np.identity(4)
                                            >>> F = np.eye(3)
>>> T
                                            >>> F
array([[1., 0., 0., 0.].
       [0., 1., 0., 0.],
                                                   [0., 1., 0.],
       [0., 0., 1., 0.],
                                                   [0., 0., 1.]])
       [0., 0., 0., 1.]])
                                            >>> F = np.eye(4,2)
>>> I_c = np.identity(4, dtype=complex)
                                            >>> F
>>> I c
                                            array([[1., 0.].
array([[1.+0.1. 0.+0.1. 0.+0.1. 0.+0.1].
                                                   ſ0., 1.].
                                                   [0., 0.],
       [0.+0.1. 0.+0.1. 1.+0.1. 0.+0.1].
                                                   [0.. 0.11)
       [0.+0.i. 0.+0.i. 0.+0.i. 1.+0.il])
```

```
Standard matrices (continued)
```

```
>>> F = np.eve(4.k=2)
                             >>> E = np.ones(3)
>>> F
                             >>> E
                             array([1., 1., 1.])
       [O., O., O., 1.].
       [O., O., O., O.].
                             >>> E = np.ones((2,3))
       [0., 0., 0., 0.]])
                             array([[1., 1., 1.],
>>> F = np.eve(4.k=-2)
>>> F
                             >>> F = np.full((3,2),1/3)
       [0.. 0.. 0.. 0.].
                             >>> F
       [1., 0., 0., 0.],
                             array([[0.33333333, 0.33333333],
```

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## Concatenating matrices

#### We can "glue" matrices together with np.concatentate.

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```
>>> A = np.array([[1,2,3],[2,2,2]])
>>> A
arrav([[1, 2, 3],
>>> B = np.ones((3,2))
>>> AB = np.concatenate((A,B.T), axis=1)
>>> AB
array([[1., 2., 3., 1., 1., 1.],
       [2., 2., 2., 1., 1., 1.]])
```

## Arrays and functions

- functions can be evaluated at arrays (similarly to map with list)
- · return value is of the shape of input array
- this avoids loops and is fast

```
>>> def f(x):
       return x**2
>>> a = np.array([[1,2,3], [2,3,4]])
>>> print(f(a))
[[1 4 9]
[ 4 9 16]]
```

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Python 3

## Arrays and functions (continued)

```
>>> def f(x):
       return x**2
>>> a = np.array([[1,2,3], [2,3,4]])
>>> print(f(a))
[[ 1 4 9]
F 4 9 16]]
```

This code corresponds to

$$f(a) = \begin{pmatrix} f(a_{00}) & f(a_{01}) & f(a_{02}) \\ f(a_{10}) & f(a_{11}) & f(a_{12}) \end{pmatrix}.$$

## Arrays and functions (continued)

This code corresponds to

$$f(a, b) = \begin{pmatrix} f(a_{00}, b_{00}) & f(a_{01}, b_{01}) & f(a_{02}, b_{02}) \\ f(a_{00}, b_{00}) & f(a_{01}, b_{01}) & f(a_{02}, b_{02}) \end{pmatrix}.$$

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## Arrays and functions (continued)

## Arrays and functions (continued)

```
>>> def f(x, y):
        return x[0]**2 + x[1]**2*v[0] + v[1]**2
>>> a = np.array([[1,2,3], [2,3,4]])
>>> b = np.array([[0,5,6], [0,2,4]])
>>> f(a,b)
array([ 1, 53, 121])
This code corresponds to
```

$$f(\mathbf{a},b) = \left(f\left(\begin{pmatrix}a_{00}\\a_{10}\end{pmatrix},\begin{pmatrix}b_{00}\\b_{10}\end{pmatrix}\right) \quad f\left(\begin{pmatrix}a_{01}\\a_{11}\end{pmatrix},\begin{pmatrix}b_{01}\\b_{11}\end{pmatrix}\right) \quad f\left(\begin{pmatrix}a_{02}\\a_{12}\end{pmatrix},\begin{pmatrix}b_{02}\\b_{12}\end{pmatrix}\right)\right).$$

- >>> [f(a[:,0],b[:,0]), f(a[:,1],b[:,1]), f(a[:,2],b[:,2])]

- What is the advantage of arrays over python lists? Answer: speed
- · Reason: numpy arrays are saved into contiguous blocks in the memory, while python lists are scattered over the memory. (Note: this is not true for dtype = object)

>>> r = np.random.rand(10000) # Random array of length 10000 >>> from time import time

```
return x**2 + np.sin(x**3)
>>> a = time()
>>> arr1 = f(r)
>>> print(time() - a)
```

- >>> a = time() >>> arr2 = np.arrav(list(map(f.r)))
  - >>> print(time() a)



### some functions need to be rewritten to support evaluation on arrays

For instance the function:

$$\Theta(x) := \left\{ \begin{array}{ll} 1 & x > 0 \\ 0 & x \leq 0 \end{array} \right..$$

In this case no where (cond. vall. val2) is helpful, which returns vall if cond is True and val2 if cond is False

```
>>> a = np.array([1,2,-3])
                                   >>> a = np.array([1,2,3])
>>> def theta1(x):
                                   >>> def theta2(x):
                                           return np.where(x>0,1,0)
        if x>0:
            return 1
       alea.
                                   >>> theta2(a)
            return 0
                                   array([1, 1, 1])
```

>>> #theta1(a) gives error

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## Broadcasting arrays

### Now why is this useful? For instance:

```
>>> a = np.array([1,2,3,1])
>>> a = a + 1 # new array is created with each element +1
array([2, 3, 4, 2])
```

>>> 
$$a \mathrel{+=} 1$$
 # each element of a is increased by 1

array([3, 4, 5, 3])

## Broadcasting arrays

- . typically only arrays of the same dimension are added; however it is also possible to add arrays of different dimension
- in this case a new array is created and the dimension missing is "filled up"

What happens is for instance the following:

$$\begin{pmatrix} a_1 & a_2 & a_2 \end{pmatrix} + \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} a_1 & a_2 & a_3 \\ a_1 & a_2 & a_3 \\ a_1 & a_2 & a_3 \end{pmatrix} + \begin{pmatrix} b_1 & b_1 & b_1 \\ b_2 & b_2 & b_2 \\ b_3 & b_3 & b_3 \end{pmatrix}$$

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## The scipy package