Übungsaufgaben zur VU Computermathematik Serie 6

Test your code with examples.

Exercise 6.1: Breaking down integers.

- (a) Write a function int_break(n) that takes an integer n and returns a list l where the entry l[k] contains the (k+1)th digit of n.
- (b) Write a second function counter(n), which takes the list generated by int_break(n) and reverses its order. You are not allowed to use the list function reverse().

Hint: Use the math function floor.

Exercise 6.2: Counting odd and even numbers.

- (a) Write two functions odd and even that get as input an integer n and as output the number of odd and even digits, respectively.
- (b) Extend the functions of item (a) to floats and count the number of odd and even fractional digits (Nachkommastellen).
- (c) Write a function, which takes an integer n and counts the number of digits that are a prime number.

Exercise 6.3: Sequences. I

Let N be an arbitrary natural number. Then we define $a_0 := N$, $a_{n+1} := a_n/2$ if a_n is even, $a_{n+1} := 3a_n + 1$ if a_n is odd, for all $n \ge 0$.

- (a) Write a code that implements the sequence (a_n) .
- (b) Verify (numerically) that for arbitrary initial value N, the sequence ends up in the cycle $4 \to 2 \to 1 \to 4$.

Exercise 6.4: Sequences. II

- (a) Write a code that numerically tests Fermat's last problem. Fermat's last problem states that for integers n > 2, $a, b, c \ge 1$ the equation $a^n + b^n = c^n$ does not hold.
- (b) Write a function that implements the sequences $x_{n+1} := \frac{2x_n^3}{3x_n^2-1}$ and $y_{n+1} := \frac{1}{2}\left(y_n + \frac{1}{y_n}\right)$. Choose an initial value > 2. What is the exact limit of both sequences?

Exercise 6.5: Print.

- (a) Write a function which takes two strings s1 and s2 and joins them together and then prints them.
- (b) Write a function which takes a string flips the first and last word of the sentence. Don't forget the capitalization.

2 4 8 3 9 27 4 16 64 125 5 25 (c) Write a function which produces the following output 36 216 49 343 8 64 512 9 81 729 10 100 1000

Exercise 6.6: Vector product, tensor product.

The tensor product between two number $a \in \mathbb{R}^{n_1} = \mathbb{R}^{n_1 \times 1}$ and $b \in \mathbb{R}^{n_2} = \mathbb{R}^{n_2 \times 1}$ is defined by $a \otimes b := ab^{\top}$.

(a) Write a function $vec_prod(a, b)$ which takes two lists a, b of length 3 and returns the vector product $a \times b$.

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(b) Write a function $tensor_prod(a, b)$ which takes two lists a, b (not necessarily the same length) and returns the tensor product.

Exercise 6.7: Dictionaries.

(a) • Grab the string 'get me' from the following dictionary.

```
d = {'key1':[1,2,{'key2':['do not get confused',{'tough':[1,2,[['get me']]]}]}]}
```

• Grab the string 'get me' from the dictionary

```
d = {'key2':[1,[[],{'bug':{'bug':'get me'}}]]}
```

(b) Write a function which takes a dictionary and reverses all of its keys, but not the values.

Exercise 6.8: Debugging

Go to the webpage https://docs.python.org/3.6/library/pdb.html and study the module pdb (p stands for python and db for debugger).

(a) What does the following code do?

```
import pdb; pdb.set_trace()
```

(b) Use (a) to set a debug point at line 6 of

```
from math import sin

print("This is a debugging test.")

def f(x):

    x = x + 1.0
    a
    return sin(x)**2 + x

print("value of f(x)", f(1))
```

Read the section *Debugger Commands* on the webpage and explain what the commands "n", "s", "l" and "c" do. Now save the previous code in a file "my_debug.py" and run **python3 my_debug.py** in the command line. Use the commands n, l, s and c to navigate in debug mode.