

22) Min. $w(\bar{x}) = 3$ — 3 marks.

Reason: — 2 marks.

- 1) Arithmetic is done in binary domain.
- 2) Minimum value of $w(\bar{x})$ is the minimum number of columns in H that add upto 0.
- 3) Minimum value of $w(\bar{x})$ is the minimum number of columns that are linearly dependent.

$$H = \begin{bmatrix} 0 & 0 & & 0 & & 1 \\ 0 & 0 & & 0 & & 1 \\ 0 & 0 & \dots & 0 & \dots & 1 \\ 0 & 1 & & 1 & & 1 \\ 1 & 0 & & 1 & & 1 \end{bmatrix}$$

Take these 3 cols as examples to show $w(\bar{x}) = 3$.

$$\text{ie. } \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}.$$