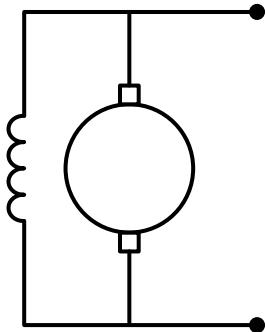


1. A 300V, 15A, 1000rpm DC shunt motor is having an armature resistance of  $0.1 \Omega$  and field winding resistance of  $200 \Omega$  (Applied voltage to the motor is 300V and it draws 15A from the source and runs at 1000rpm while driving the full load). Determine:

- Armature current on full load. (0.5)
- Armature current at 50% of full load. (0.5)
- Current drawn from the source while driving 50% of full load. (0.5)
- Back EMF on full load. (0.5)
- Back EMF and speed while driving 50% of full load. (1)



$$Sol \Rightarrow I_F = \frac{300}{R_F} = \frac{300}{200} = 1.5 \text{ A}$$

~~$I_a = I_L - I_F = 15 - 1.5 \text{ A} = 13.5 \text{ A}$~~

~~$\checkmark \text{ at } 50\% \text{ load } I'_a = \frac{I_{a \text{ full load}}}{2} = \frac{13.5 \text{ A}}{2} = 6.75 \text{ A}$~~

~~$\checkmark \text{ current drawn from source} = I'_a + I_F$~~ 

$$= 6.75 + 1.5 = 8.25 \text{ A}$$

~~$\checkmark V_{in} = E_b + I_a R_a = E_b + 13.5 \times 0.1$~~ 

$$\Rightarrow E_b = 300 - 13.5 \times 0.1 = 298.65 \text{ V}$$

$$\left| \begin{array}{l} E'_b = 300 - I'_a R_a \\ E'_b = 300 - 6.75 \times 0.1 \\ E'_b = 299.325 \end{array} \right.$$

~~$E_b = K \phi \omega \text{ here } K \text{ & } \phi \text{ are constant}$~~

$$\therefore \frac{E_b}{E'_b} = \frac{\omega}{\omega'} \Rightarrow \frac{298.65}{299.325} = \frac{1000}{\omega'} \therefore \underline{\underline{\omega' = 1002.26}}$$

2. The rotor speed of 3-phase, 50 Hz induction motor while driving a full load is 291 rpm. Determine:

- a. Number of poles and synchronous speed. (0.5+0.5)
- b. Speed of the rotor field with respect to rotor. (0.5)
- c. Speed of the rotor field with respect to stator. (0.5)
- d. Frequency of rotor current at starting (speed of rotor=0) (0.5)
- e. Frequency of rotor current when  $N_r = 291$  rpm. (0.5)

$S \leq 4\%$

Sol  $\Rightarrow$  a) as motor is operating at 50 Hz  $f = 50$

$$N_s = \underline{\underline{300 \text{ rpm}}} \text{ as } N_s = 291 \text{ and } S \leq 4\%.$$

$$\therefore 300 = \frac{120f}{P} \Rightarrow P = \frac{120 \times 50}{300} = \underline{\underline{20}}$$

b) speed of rotor field  $= N_s = \underline{\underline{300 \text{ rpm}}}$

$$\therefore \text{speed of rotor field w.r.t. rotor} = N_s - N_r = 300 - 291 = \underline{\underline{9 \text{ rpm}}}$$

c) speed of rotor field w.r.t to stator will be  $N_s$   
as stator is stationary  $= \underline{\underline{300 \text{ rpm}}}$

d) When speed of rotor  $= 0$ , the rotor will have a current of frequency which is equal to stator current.

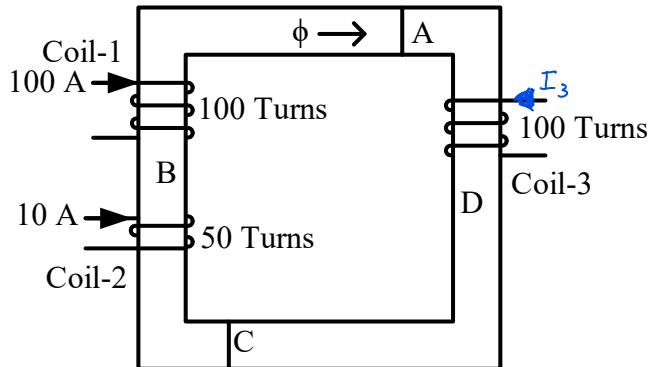
$$\therefore \underline{\underline{50 \text{ Hz}}}$$

e) When  $N_r = 291$ , the rotor will have a current corresponding to slip frequency

$$\therefore N_{\text{slip}} = N_s - N_r = \underline{\underline{9 \text{ rpm}}}$$

$$9 = \frac{120f}{P} \Rightarrow f = \underline{\underline{1.5 \text{ Hz}}}$$

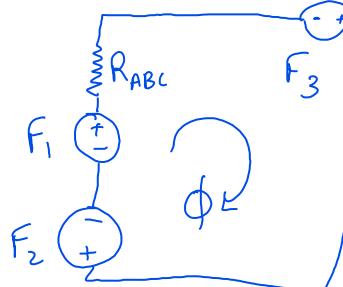
3. Magnetic Circuit has 2 portions ABC and ADC of identical dimensions (no air gap).  $\mu_r$  of portion ABC is 3 times that of the portion ADC. The reluctance of ADC is 750. Coil-1 and coil-2 are carrying a current of 100 A and 10 A respectively in the direction shown. If the flux  $\phi = 1 \text{ wb}$  is to be produced in the direction shown. Determine:



- The magnitude and direction of the current in coil-3. (2)
- What should be the magnitude and direction of current in coil-3 for producing the same flux in the opposite direction to that shown in figure. (1)

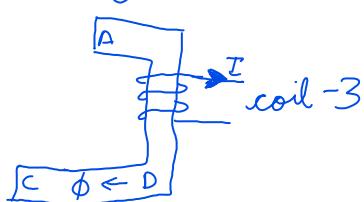
$$R_{ADC} = 750, \mu_{rABC} = 3 \times \mu_{rADC}, \phi = 1 \text{ wb}$$

$$R_{ABC} = \frac{R_{ADC}}{3} = 250$$



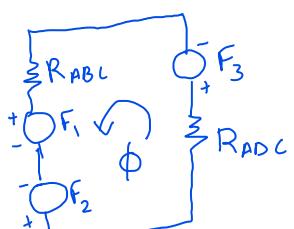
$$\begin{aligned} 0 &= F_1 + F_3 - F_2 - \phi(R_{ABC} + R_{ADC}) \\ 0 &= 10000 + F_3 - 500 - 1[750 + 250] \end{aligned}$$

$$F_3 = -8500 \text{ AT}$$



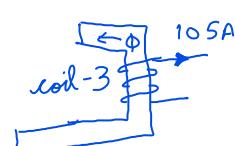
$$F_3 = I_3 N = -8500 \text{ O} \quad I_3 = -85 \text{ A}$$

b)



$$\begin{aligned} \phi &= 1 \text{ wb} \\ 0 &= F_2 - F_1 - F_3 - \phi(R_{ABC} + R_{ADC}) \\ &= 500 - 10000 - F_3 - 1000 \end{aligned}$$

$$F_3 = -10500 = N I_3 \Rightarrow I_3 = -105 \text{ A}$$



4. Assume that the following passive components and power supplies are available to you.

- i. 3 Phase variable voltage variable frequency supply.
- ii. 3 Phase R-L bank. (R- Resistor; L-Inductor)
- iii. Variable voltage DC source.
- iv. Variable resistor.

You have been told that 3 phase induction motor draws 6-7 times the rated current during starting if rated voltage at rated frequency is applied.

- a. Suggest an elegant method to reduce this current using one of the above mentioned component/supply. (0.5)
- b. Justify your answer. (Be Precise.) (0.5)

(Note: Credit for part (a) will be given only if the answer to part (b) is correct)

Sol  $\Rightarrow$

- a) Using a variable voltage variable frequency 3  $\phi$  supply.
- b) When using a variable frequency drive we can reduce the relative speed between  $N_s$  and  $N_r$ . hence the current requirement will be low.