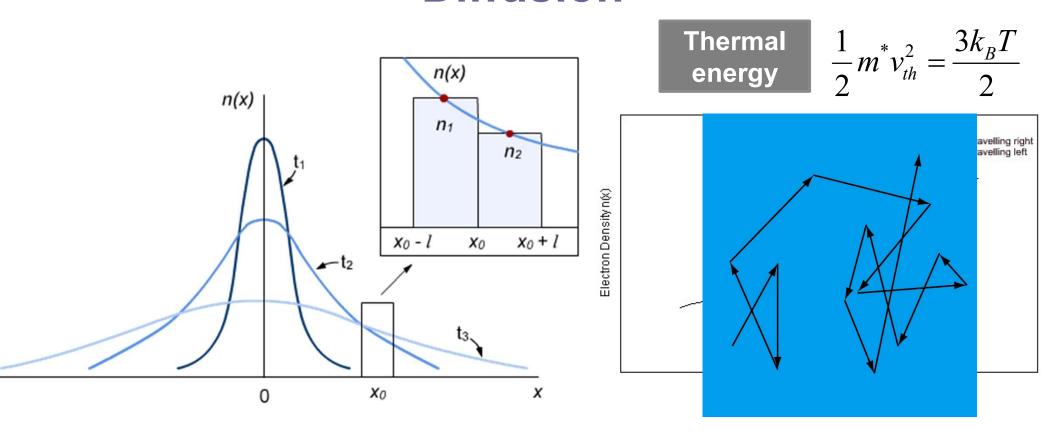
#### **Diffusion**

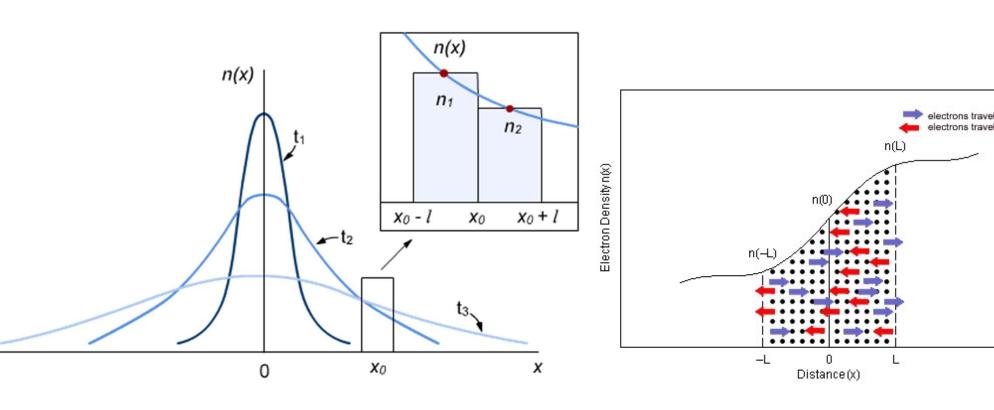


Transport of particles (electrons here) due to a concentration gradient

**Driven by thermal motion of particles (electrons)** 

Flux (particle current) is proportional to concentration gradient

### **Diffusion current**



$$\frac{1}{2}v_{th}\cdot n(-l/2)$$

Flux to the right 
$$\frac{1}{2}v_{th} \cdot n(-l/2)$$
  $\frac{1}{2}v_{th} \cdot n(+l/2)$  Flux to the left

$$\Phi = \frac{1}{2}v_{th} \cdot n\left(-\frac{l}{2}\right) - \frac{1}{2}v_{th} \cdot n\left(+\frac{l}{2}\right)$$

Net flux

Diffusion coefficient 
$$D = \frac{lv_{th}}{2} = \frac{l^2}{2\tau}$$

$$\Phi = \frac{lv_{th}}{2} \frac{n\left(-\frac{l}{2}\right) - n\left(+\frac{l}{2}\right)}{l} \simeq -D\frac{dn}{dx}$$

$$J = eD\frac{dn}{dx}$$

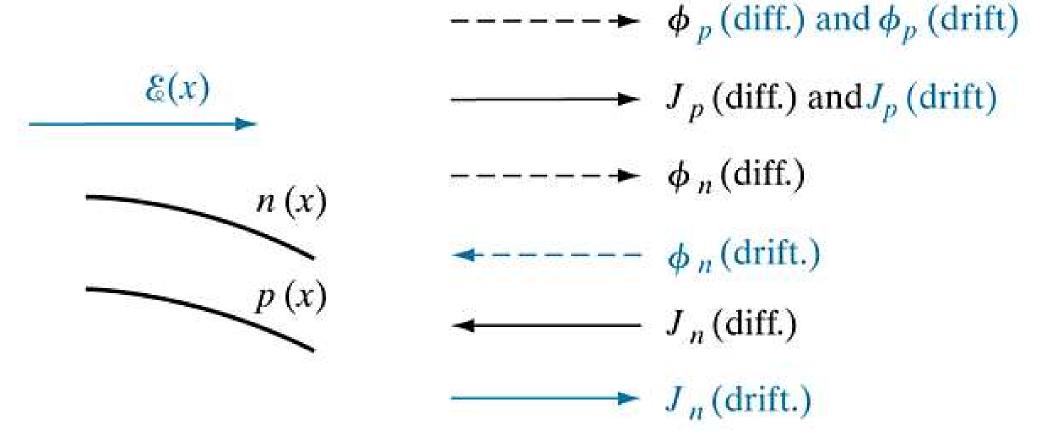
**Diffusion current** 

### **Drift and diffusion currents**

$$J_n = ne\mu_n \mathcal{E} + eD_n \frac{dn}{dx}$$

**Drift-diffusion** 

$$J_p = pe\mu_p \mathcal{E} - eD_p \frac{dp}{dx}$$



### **Equilibrium Fermi level**

Rate of transfer of electrons from one spatial point to another

$$R_{1\to 2} \propto N_1(E) f_1(E) \cdot N_2(E) [1 - f_2(E)]$$

$$\mathbf{R}_{2\rightarrow 1} \propto N_2(E) f_2(E) \cdot N_1(E) \left[ 1 - f_1(E) \right]$$

**Equilibrium → Detailed Balance** 

$$R_{1\rightarrow 2} = R_{2\rightarrow 1} \Longrightarrow f_1 = f_2$$

Fermi level is flat in equilibrium

#### **Einstein Relation**

**Drift-diffusion** 

$$J_{p} = pe\mu_{p}\mathcal{E} - eD_{p}\frac{dp}{dx}$$

**Equilibrium** 

$$J_p = 0 \Longrightarrow \mathcal{E} = \frac{D_p}{p\mu_p} \frac{dp}{dx}$$

$$E_i = E_{i0} - qV$$

$$p_0 = n_i e^{(E_i - E_F)/kT}$$

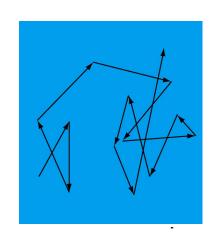
**Carrier statistics** 

$$\frac{D_p}{\mu_p} \frac{1}{k_B T} \left[ \frac{dE_i}{dx} - \frac{dE_F}{dx} \right] = \mathcal{E} \cong -\frac{dV}{dx} = \frac{1}{e} \frac{dE_i}{dx}$$

Equilibrium 
$$\frac{dE_F}{dx} = 0$$

$$D_p = \frac{\mu_p k_B T}{e}$$

$$D_n = \frac{\mu_n k_B T}{e}$$



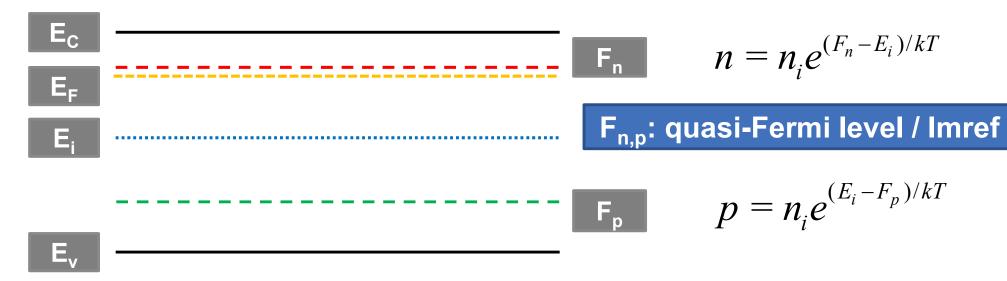
**Carrier-statistics** dependent?

Fluctuation-Dissipation

# Non-equilibrium: quasi-Fermi levels

Bulk semiconductor under steady-state illumination

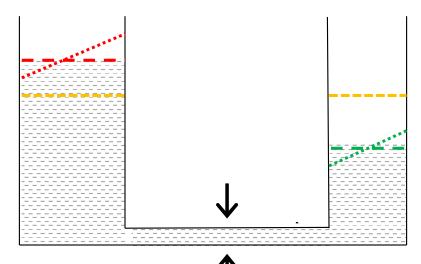
→ excess electrons and holes



Non-equilibrium ≈ Local equilibrium

Electrons (holes) in local equilibrium within conduction (valence) band

Other instances of local equilibrium?



## **Drift-diffusion with quasi-Fermi levels**

**Drift-diffusion** 

$$J_n = ne\mu_n \mathcal{E} + eD_n \frac{dn}{dx}$$

**Carrier statistics** 

$$n = n_i e^{(F_n - E_i)/kT}$$

$$J_{n} = ne\mu_{n} \left( \frac{1}{e} \frac{dE_{i}}{dx} \right) + eD_{n} \frac{n}{k_{B}T} \left( \frac{dF_{n}}{dx} - \frac{dE_{i}}{dx} \right)$$

**Einstein relation** 

$$D_n = \mu_n k_B T / e$$

$$J_{n} = n\mu_{n} \frac{dE_{i}}{dx} + e\left(\frac{\mu_{n}k_{B}T}{e}\right) \frac{n}{k_{B}T} \left(\frac{dF_{n}}{dx} - \frac{dE_{i}}{dx}\right)$$

First and third terms cancel out; significance?

**Drift-diffusion** 

$$J_n = n\mu_n \frac{dF_n}{dx}$$
 Holes?

### **Finis**

#### **Artwork Sources:**

- 1. Prof. Sanjay Banerjee
- 2. www.pveducation.org
- 3. <u>britneyspears.ac</u>