

The wave equation, Lorenz force law and classical mechanics

| Light | Sound |
|--|--|
| $c = \sqrt{\frac{1}{\epsilon_0 \mu_0}}$ | $v = \sqrt{\gamma \frac{P}{\rho}}$ |
| Can propagate in vacuum. So the velocity is w.r.t. what? | Needs a medium. The velocity is w.r.t the medium (like air, water) |

The ether frame is a hypothetical inertial frame in which the speed of light was supposed to be c

$$\vec{F} = q \left(\vec{E} + \vec{v} \times \vec{B} \right)$$

Velocity may be different in different inertial frames

So how is the force going to be same in all inertial frames?

Maxwell's equations are NOT invariant under a Gallilean transformation

What does :: Laws of physics are same in all inertial frames :: mean ?

Suppose $Z = X * Y$ is a law of physics.

In an inertial frame (S) some one measures the quantities to be X, Y and Z

In another inertial frame (S') one measures the quantities to be X', Y' and Z'

S will find $Z = X * Y$

S' will find $Z' = X' * Y'$

Further S will be able to predict what X', Y', Z' will be measured in the other frame.

This is the job of the transformation equations.

In general X,Y,Z and X',Y', Z' will not be same.

What if time (or time interval) is one of the quantities ? For example half life of a radioactive substance.

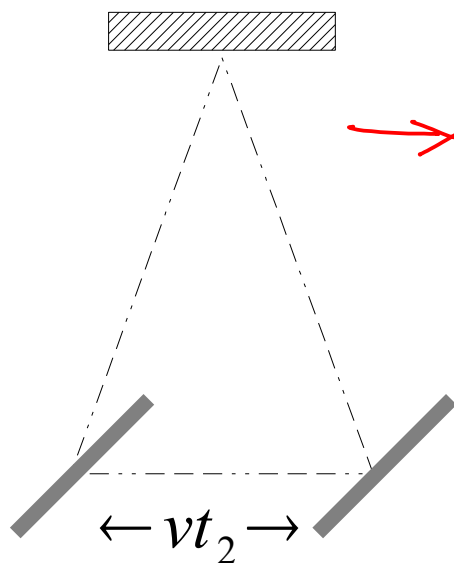
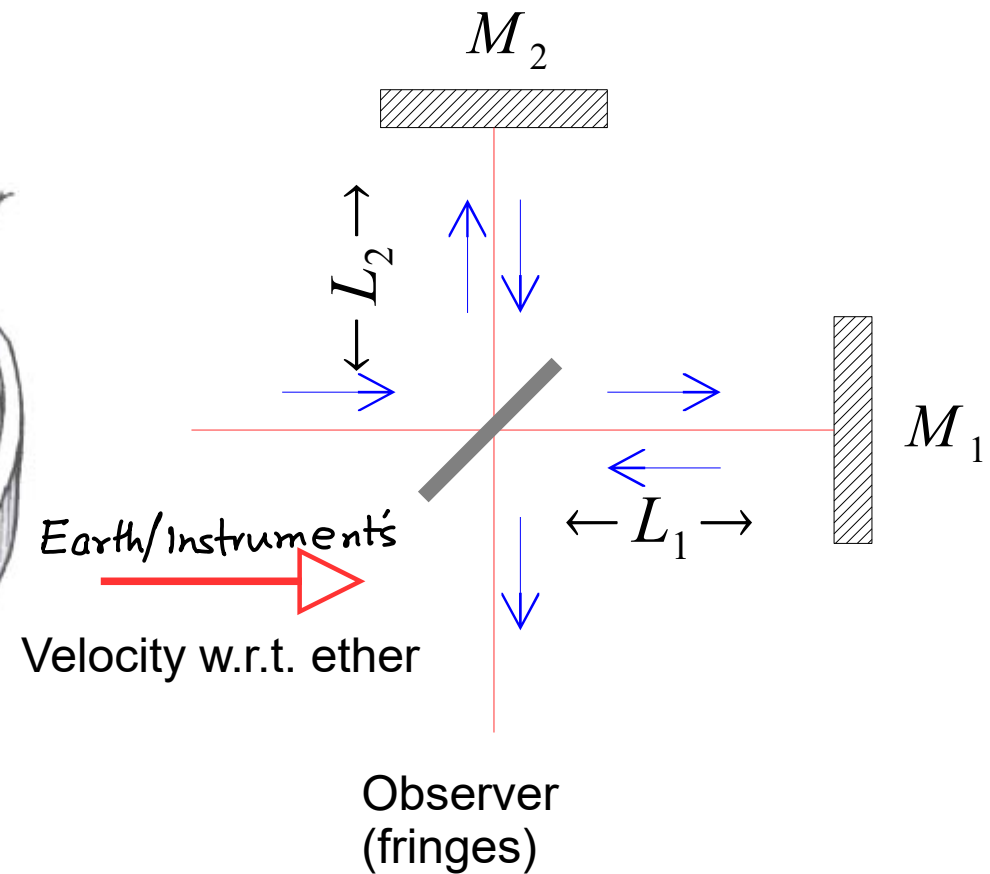
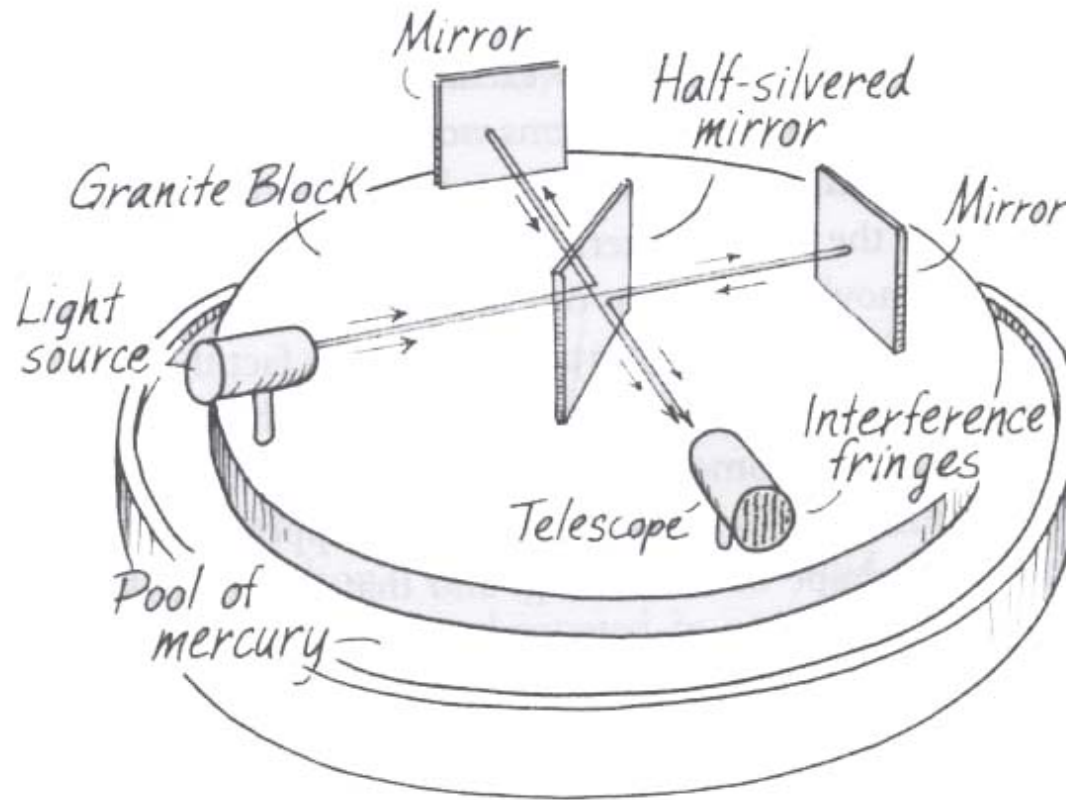
Time was thought to be universal....but that is NOT unambiguous.

Newton : The universe HAS a clock.

Leibnitz : The universe IS a clock.

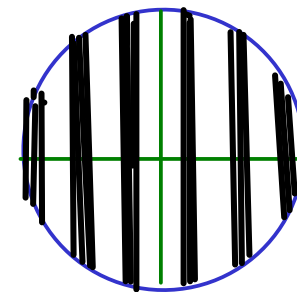
What is the difference ?

Michaelson Morley interferometer experiment



$\rightarrow v$ Instrument's Speed wrt Ether

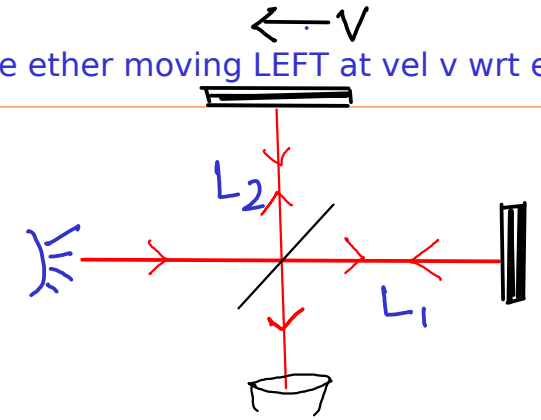
The reflection from M2
as seen by an observer
in the ether frame



Fringes

Michaelson Morley interferometer experiment: Assume ether moving LEFT at vel v wrt earth

$$\left. \begin{array}{l} \text{To reach } M_1 \text{ light takes} : \frac{L_1}{c-v} \\ \text{To come back} : \frac{L_1}{c+v} \end{array} \right\} t_1 = \frac{2L_1 c}{c^2 - v^2}$$



$$\text{To reach } M_2 \text{ and come back : } L_2^2 + \left(\frac{vt_2}{2} \right)^2 = \left(\frac{ct_2}{2} \right)^2$$

takes $t_2 = \frac{2L_2}{\sqrt{c^2 - v^2}}$ ←

$$\begin{aligned} \Delta t &= t_1 - t_2 \\ &= \frac{2L_1 c}{c^2 - v^2} - \frac{2L_2}{\sqrt{c^2 - v^2}} \end{aligned}$$

Now turn the whole apparatus by 90°

$$\begin{aligned} \Delta t' &= t_1' - t_2' \\ &= \frac{2L_1}{\sqrt{c^2 - v^2}} - \frac{2L_2 c}{c^2 - v^2} \end{aligned}$$

$$\Delta t - \Delta t' = \frac{2(L_1 + L_2)c}{c^2 - v^2} - \frac{2(L_1 + L_2)}{\sqrt{c^2 - v^2}}$$

$$\approx \left(\frac{L_1 + L_2}{c} \right) \frac{v^2}{c^2}$$

() $\frac{1}{c^2(1 - v^2/c^2)}$ → () $\frac{1}{c\sqrt{1 - v^2/c^2}}$

path diff λ
one fringe shift

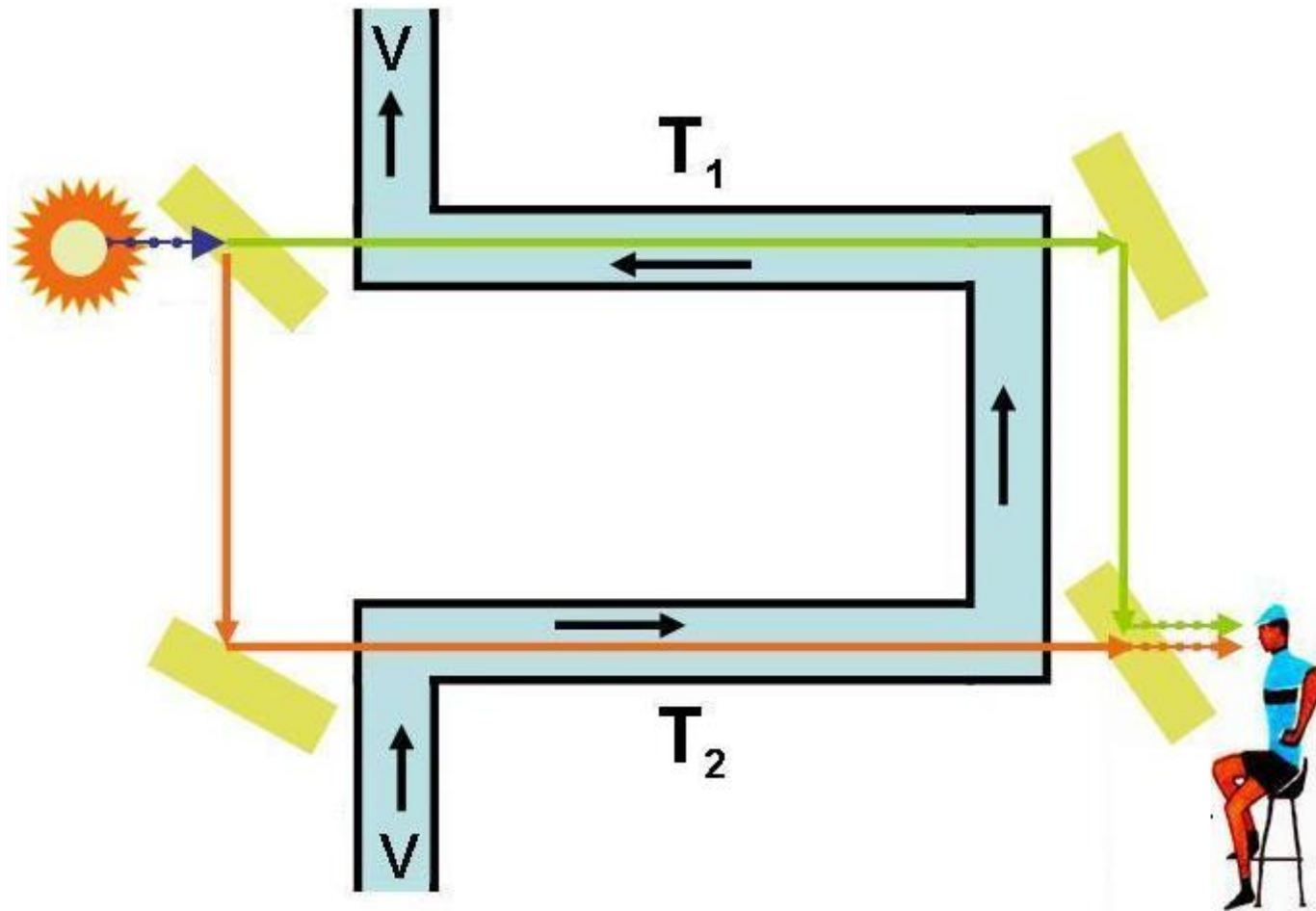
In experiment : $L_1 + L_2 \approx 22 \text{ mt}$: $\lambda = 500 \text{ nm}$

sensitivity 1/100 fringe : expect ~ 0.4 fringe shift for $\frac{v}{c} \approx 10^{-4}$

$$\mathcal{N} = \frac{\Delta T}{T}, T = \frac{1}{\nu}, c = \nu \lambda$$

NO SHIFT was observed

Light in a moving medium : Fizeau



Fringe pattern changes when the flow is stopped

Infer the velocity of light from the fringe shift data

Light appears to be partially "dragged" by the flowing medium.

$$v_{light} = \frac{c}{n} + v_{water} \left(1 - \frac{1}{n^2} \right) \quad \text{Empirical}$$