



$$\Omega^2 R_0 \cos \lambda \text{ (centrifugal)}$$

\hat{y} axis is vertically inward into the page (Eastward)
 $(\hat{x}, \hat{y}, \hat{z})$ forms a right handed cartesian system.

Estimates

$$\Omega = 7.3 \times 10^{-5} \text{ rad/s}$$

$$R_0 \approx 10^7 \text{ m}, R = R_0 \cos \lambda$$

$$\Omega^2 R_0 \approx 54 \times 10^{-10} \times 10^7 \text{ m/s}^2$$

$$\frac{\Omega^2 R_0}{g} \approx \frac{0.05}{10} \approx 0.5\%$$

$$\vec{\Omega} = -\cos \lambda \hat{i} + \sin \lambda \hat{k}$$

$$\Omega^2 R \text{ (centrifugal)}$$

$$\begin{aligned} \vec{a}_{rel} &= \vec{a}_{in} + 2 \vec{v}_{rel} \times \vec{\Omega} - \vec{\Omega} \times (\vec{\Omega} \times \vec{r}) \\ &= -g \hat{z} + \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ v_x & v_y & v_z \\ -\cos \lambda & 0 & \sin \lambda \end{vmatrix} 2\Omega + \Omega^2 R_0 \cos \lambda \begin{pmatrix} \sin \lambda \\ 0 \\ \cos \lambda \end{pmatrix} \end{aligned}$$

v_z will turn out to be negligible

$$(1) \quad \ddot{x} = 2\Omega v_y \sin \lambda + \Omega^2 R_0 \cos \lambda \sin \lambda$$

$$(2) \quad \ddot{y} = (-v_x \sin \lambda - v_z \cos \lambda) 2\Omega$$

$$(3) \quad \ddot{z} = -g + v_y \cos \lambda \cdot 2\Omega + \Omega^2 R_0 \cos^2 \lambda$$

Diff terms are diff order in Ω . Can ignore Ω^2 terms right at the beginning.

lowest order soln. $\ddot{z} \approx -g \Rightarrow \dot{z} = -gt + v_z(0) \Rightarrow z = -\frac{1}{2}gt^2 + v_z(0)t + z(0)$

Initial vel. along \hat{z} Initial posn along \hat{z}

\ddot{x} is max $\mathcal{O}(\Omega)$;

if we substitute v_x in \ddot{y} eqn then 1st term is of $\mathcal{O}(\Omega^2)$, ignore.

$$(2) \quad \ddot{y} \approx -2\Omega v_z \cos \lambda = -2\Omega \cos \lambda (-gt + v_z(0))$$

$$= 2\Omega \cos \lambda gt - 2\Omega \cos \lambda v_z(0)$$

$$\dot{y} = \Omega \cos \lambda gt^2 - 2\Omega \cos \lambda v_0 t + \dot{y}(0)$$

(case b)

$$y = \Omega \cos \lambda gt^3 - 2\Omega \cos \lambda v_0 t^2$$

$$= \Omega \cos \lambda t^2 \left(\frac{gt}{3} - v_0 \right)$$

So depending v_0 , H dir displacement

Can be towards east or west.

BUT- if case (a) $v_z(0) = v_0 = 0$ displacement always East.

b) projected vertically from ground $v_z(0) = v_0$

But, $y(0) = 0, \dot{y}(0) = 0$
 In Both cases..

T1 = v_0/g
 T2 = $2v_0/g$

Net Displacement
 for T1 : East
 for T2 : West