

GATE ALL BRANCHES



General Aptitude
QUANTITATIVE APTITUDE

Lecture No.- 03

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Recap of Previous Lecture



Topic

Clocks

Time Angle?
(Relative Speed)



Topics to be Covered



Topic-1

More on Clocks



Topic-2

Average

Second Pattern:

Angle $\vartheta \rightarrow$ Time?



0° OR Coincide:

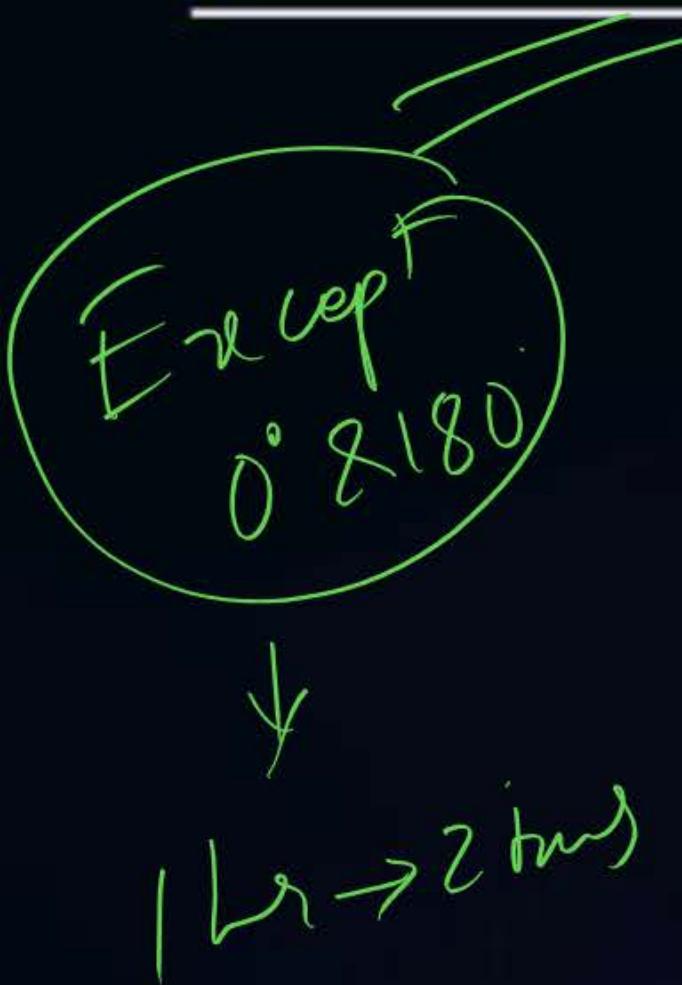
12 hours =

12 hours = 11 times

24 hours = 22 times



180° OR Opposite:



12 hours = 11 times

24 hours = 22 times



90° OR Right angle:



12 hours = 22 times

24 hours = 44 times

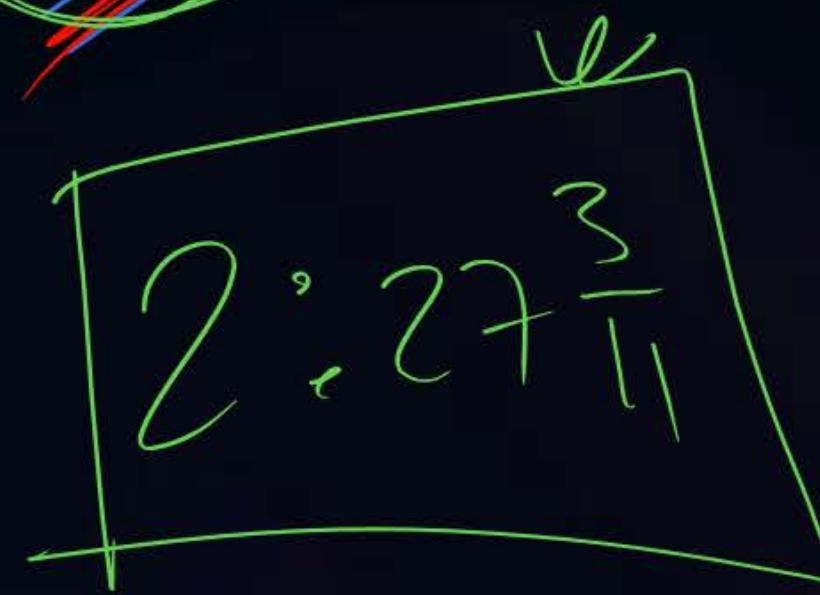


Questionnaire:

$$T = \frac{P}{S}$$

#Q. In between 2 O' clock and 3 O' clock at what time the hands of clock form

$90^\circ?$



$$\frac{150^\circ}{5.5} \times 2 = \frac{300}{11}$$

$$= 27\frac{3}{11} \text{ minutes}$$



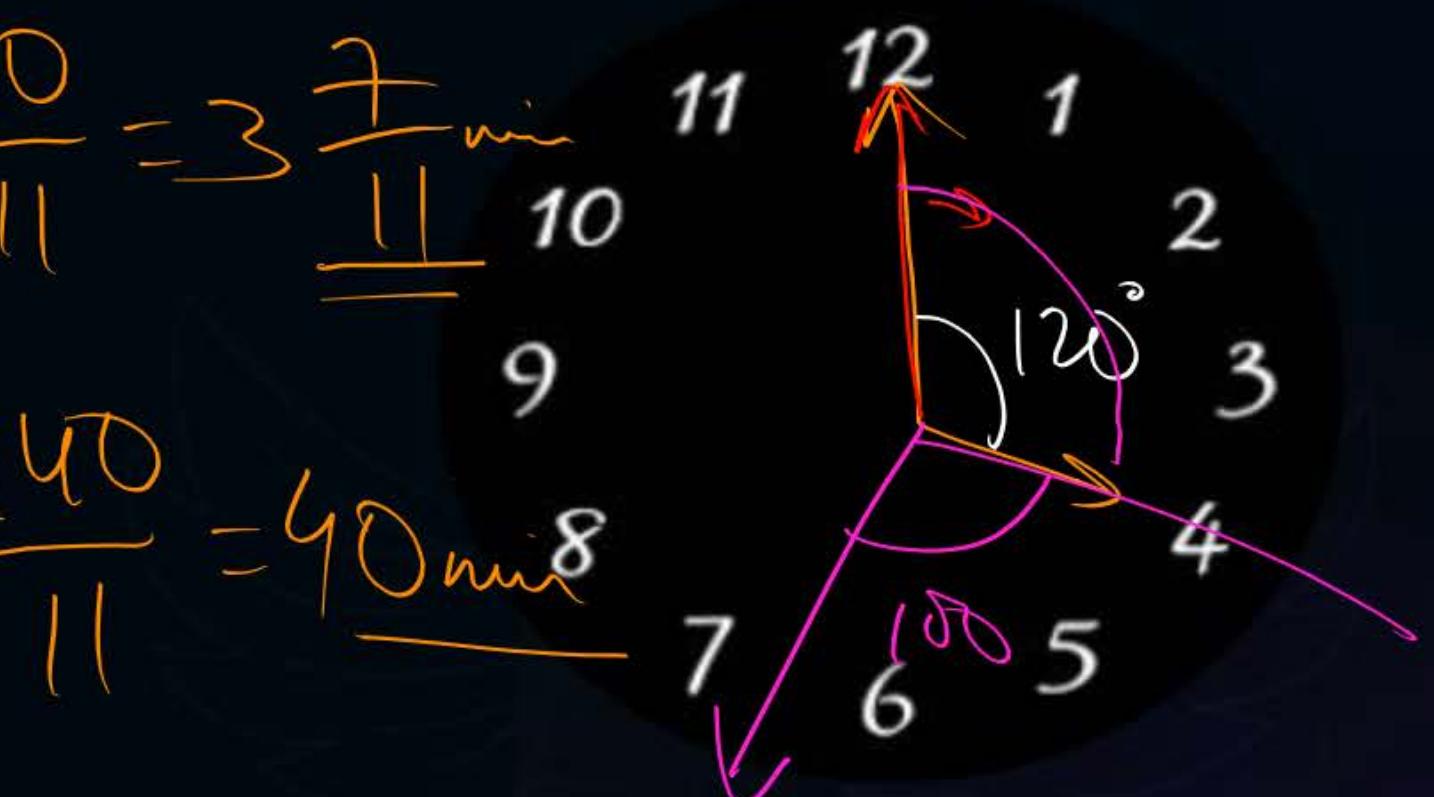
Questionnaire:

#Q. In between 4 O' clock and 5 O' clock at what time the hands of clock form

~~100°?~~

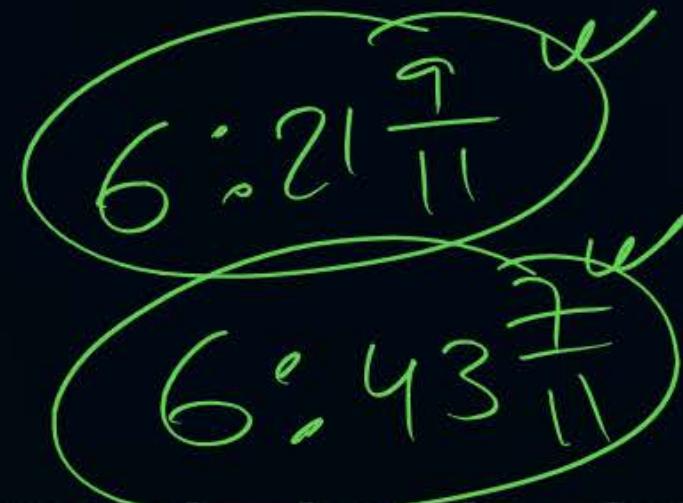
$$\frac{2\omega}{5 \cdot 5} = \frac{40}{11} = 3 \frac{7}{11} \text{ min}$$

$$\frac{22\omega}{5 \cdot 5} = \frac{440}{11} = 40 \text{ min } 8$$



Questionnaire:

①
②

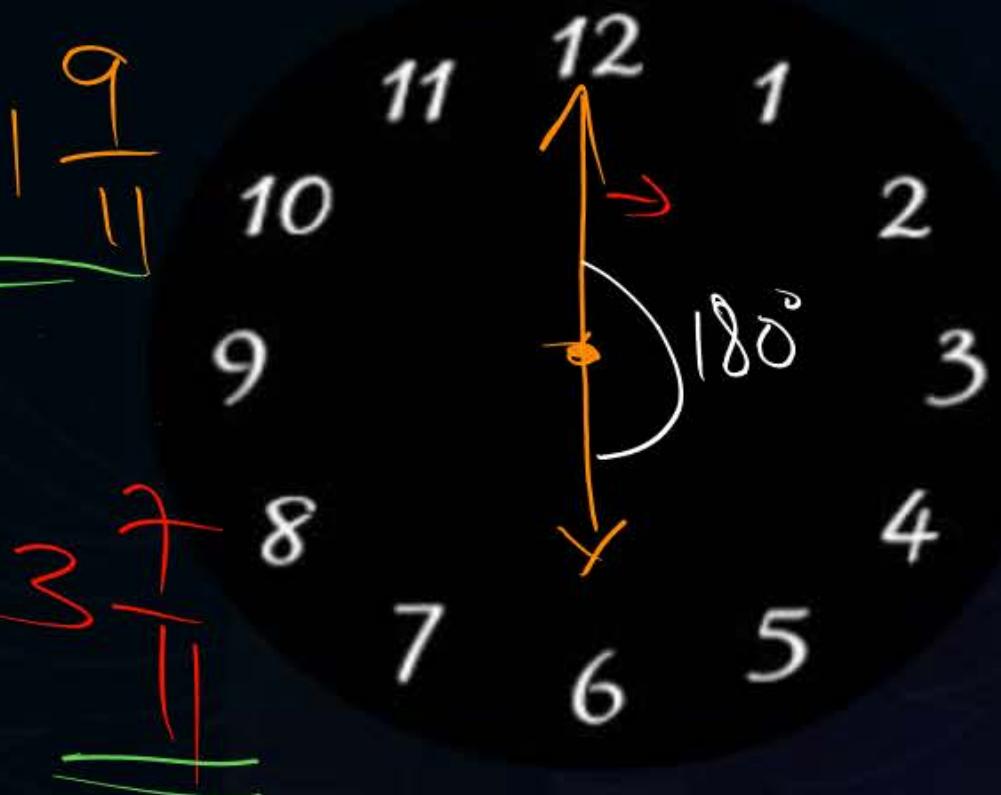


#Q. In between 6 O' clock and 7 O' clock at what time the hands of clock form 60° ? \Rightarrow

60°

$$\frac{120}{5.5} = \frac{240}{11} = 21\frac{9}{11}$$

$$\frac{240}{5.5} = 480 = 43\frac{7}{11}$$



Questionnaire:

①

1:23 $\frac{7}{11}$ u

②

1:52 $\frac{8}{11}$

#Q. In between 1 O' clock and 2 O' clock at what time the hands of clock form

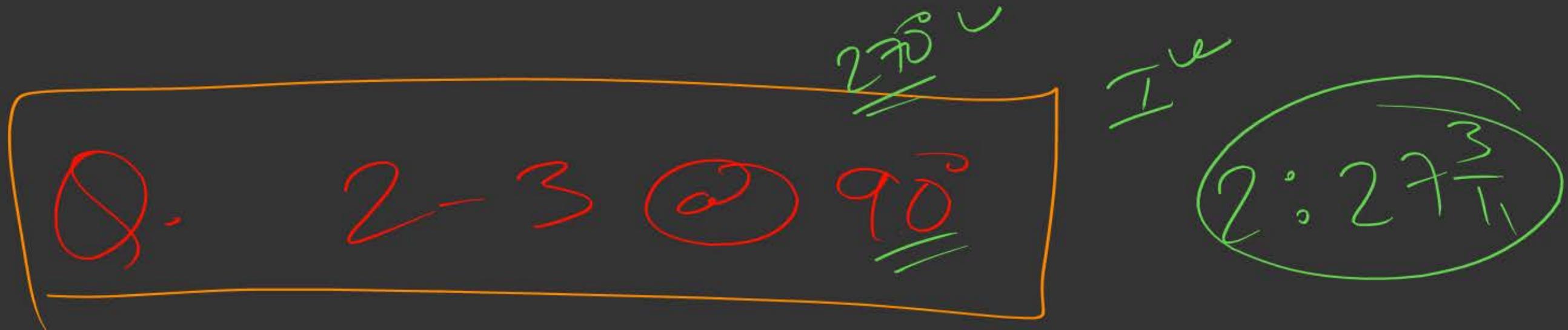


$$\frac{130}{5 \cdot 5} = \frac{260}{11}$$

$$= 23\frac{7}{11} \text{ min}$$

$$\Rightarrow \frac{290}{5 \cdot 5} = \frac{580}{11} = 52\frac{8}{11}$$





$$\frac{150}{5.5} = \frac{300}{\pi} = 27\frac{3}{\pi}$$



$$\frac{330}{5.5} = \frac{660}{\pi} = \cancel{60}$$

Questionnaire:

1 - 2 @ 100°

$$1. \text{ } S = \frac{8}{\pi}$$

$$\frac{40}{5.5} = \frac{80}{11}$$

$$(-) = 7 \frac{3}{11} \text{ min}$$



Third Pattern:

Gain OR Lose

IS°

Questionnaire:

+5

- #Q. A Clock which gains 5 minutes in every one hour was set correct at 5am.
What would be the time shown by that clock at 1pm the same day?

1 : 40

Questionnaire:

#Q. A clock which loses 10 minutes in every one hour was set correct at 4am,
what would be the time shown by that clock at 4pm the same day?

Chain Rule

$$12 \times 10 = 120$$

2PM

#Q. At what time between 6AM and 7AM will the minute hand and hour hand of a clock make an angle closest to 60° ?

~~6:22 AM~~

- A 6:22 AM
- B 6:27 AM
- C 6:38 AM
- D 6:45 AM

$$\frac{120}{5.5} = \frac{240}{11} = 21\frac{9}{11} (180^\circ)$$



$$\frac{240}{5.5} = \frac{480}{11} = 43\frac{7}{11}$$

~~6:21 9/11~~

~~6:43 7/11~~

#Q. A worker noticed that the hour hand on the factory clock had moved by 225 degrees during her stay at the factory. For how long did she stay in the factory?

- A 3.75 hours
- B 4 hours 15 minutes
- C 8.5 hours
- D 7.5 hours

$$H \cdot H \geq 0.5^\circ/\text{min}$$

$$\frac{225}{0.5} = 450 \text{ min}$$

$$\frac{15}{450} \text{ hour}$$

$$= 7.5 \text{ hours}$$

#Q. It is quarter past three in your watch. The angle between the hour hand and the minute hand is?

- A 0°
- B 15°
- C 7.5°
- D 22.5°

3:15

$3 > 90^\circ$

$$\begin{array}{r} 15 \times 5.5 \rightarrow 82.5^\circ \\ \hline 7.5^\circ \end{array}$$

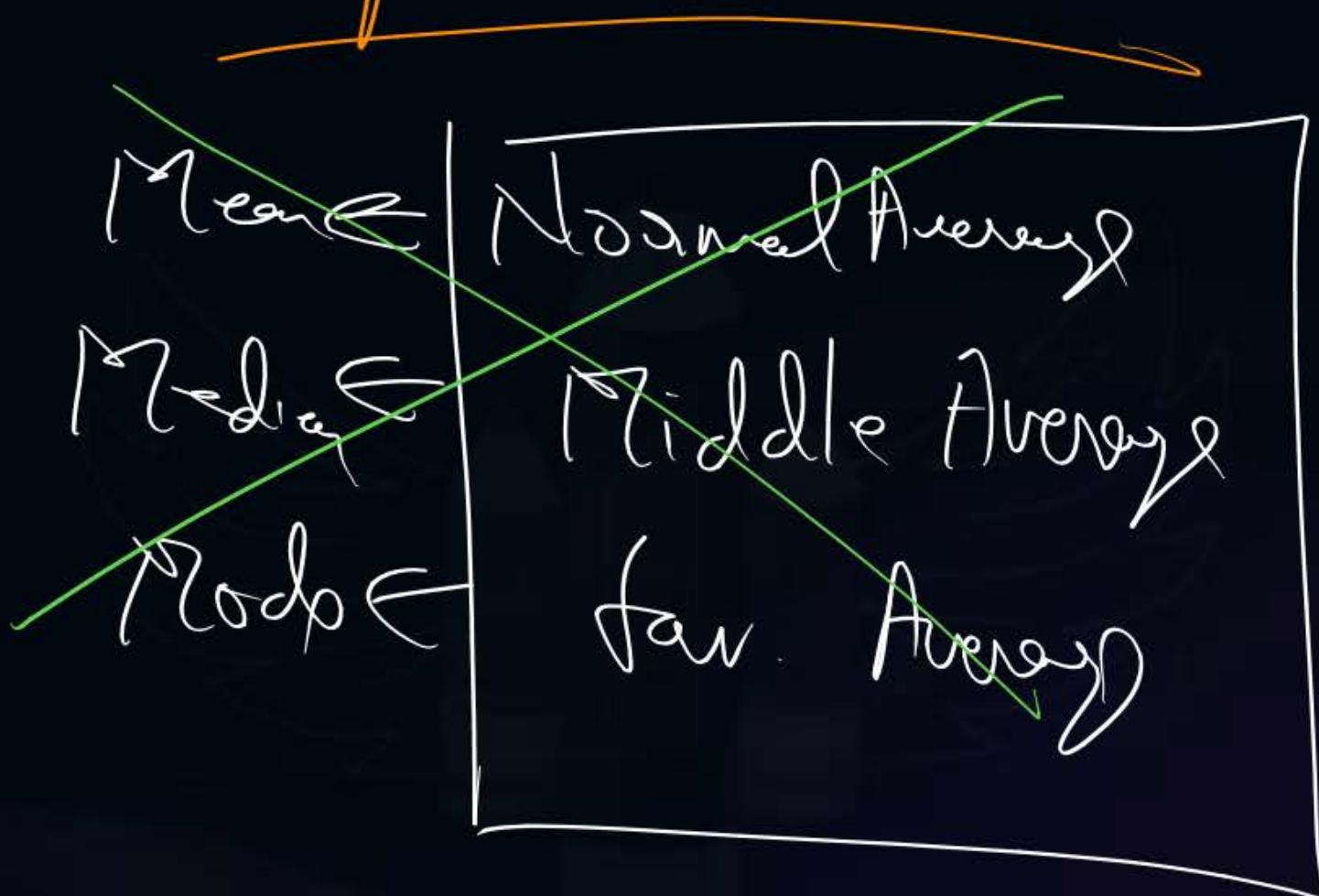
AVERAGE

A. Mean

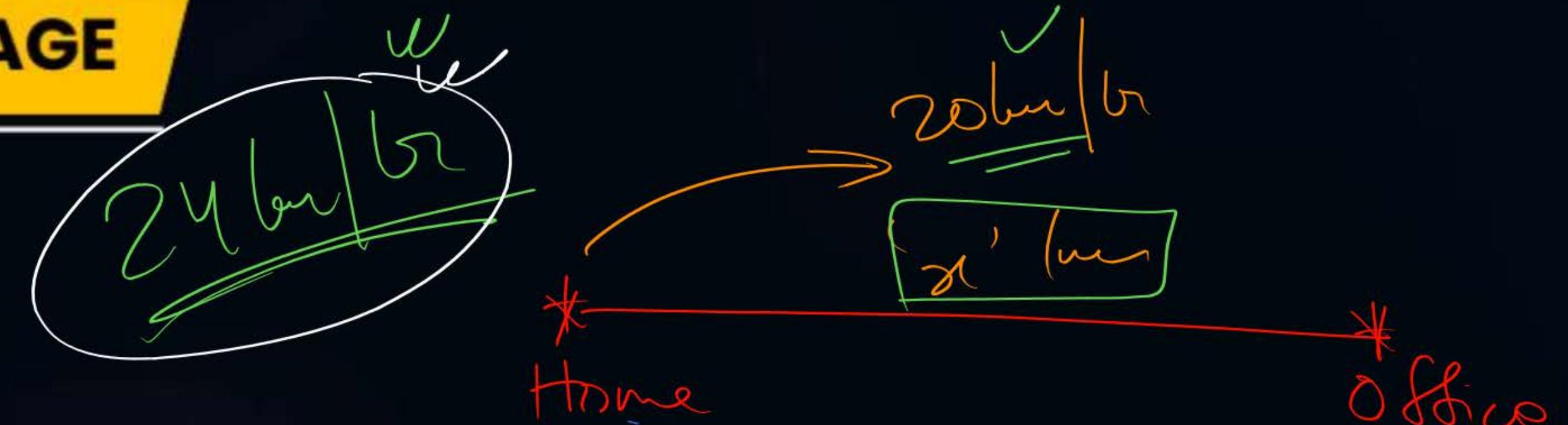
$\hat{\alpha}$?

=

→ Equal Distribution



AVERAGE



$$\frac{2x}{\text{A.S.}} = \frac{x}{20} + \frac{x}{30}$$

$$\frac{6x}{60} = \frac{2x}{\text{A.S.}}$$

(12)

$$\text{A.S.} = 24 \text{ km/hr}$$

$$\frac{30}{\text{A.S.}} =$$

$$S = \frac{P}{T}$$

$$S \times T = P$$

$$T = \frac{P}{S}$$

AVERAGE

$$\bar{x}_n = \frac{\sqrt{n+1}}{2}$$

Sum of obs. / No. of obs. = Average

$$\underline{N} \geq$$

$$\frac{n+1}{2}$$

D.

1, 2, 3, 4, ... 50

$$\bar{x} = \frac{\sum x}{n}$$

$$= 1275$$

$$\begin{aligned} x &= 1+2+3+4+\dots+49+50 \\ x &= 50+49+48+\dots+2+1 \end{aligned}$$

$$2x = 50 \times 51$$

[MCQ]

#Q. What would be the average of:

1, 2, 3, 4, 5, 49, 50.

P
W

$$\frac{n+1}{n}$$

$$\frac{n}{n}$$

$$\frac{25}{5}$$

$$\text{Set } \{1, 3, 5, 7, 9\}$$

$$\Rightarrow 2, 4, 6, 8, 10 \Rightarrow 6$$

$$\text{Set } \{1, 3, 5\}$$

$$\Rightarrow 2, 4, 6, 8, 10, 12 \Rightarrow 7$$

Average of Even & Odd

$$\frac{(n+1)}{2}$$

(1) Average = $\frac{\text{Sum}}{\text{No.}}$

$$A \times \text{No.} = \text{Sum}$$

$$(n+1) \times n = \frac{n(n+1)}{2}$$

Sum of even
no.

$$n \times n = n^2$$

Sum of odd no.

Sum of Even & Odd

$$\frac{n(n+1)}{2}$$

$$\frac{n^2}{2}$$



2 mins Summary



Topic

Average



THANK - YOU