## 211020428-task3

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Task 3 (CNN): Download/search handwritten digit dataset (MNIST Dataset). You are given the flexibility to use any other handwritten digit dataset if found suitable. Perform the following tasks without preprocessing: [1] Apply the convolution neural network architecture to the above dataset. [2] Demonstrate the results with various learning rates. [3] Demonstrate the results with various Activation functions. [4] Demonstrate the results with all possible evaluation criteria. [5] Demonstrate the learning results in all possible visualizing ways.

```
import tensorflow as tf
import keras
from keras import backend as k
from tensorflow.keras import utils # For datasets # For math functions and array
import numpy as np
import matplotlib.pyplot as plt
from keras.datasets import mnist
from keras.models import Model
from keras.layers import Dense, Input, Flatten
from keras.layers import Conv2D, MaxPooling2D, Dropout, Flatten
from tensorflow.keras.optimizers import SGD, Adam
from tensorflow.keras.activations import relu, sigmoid
from tensorflow.keras.losses import SparseCategoricalCrossentropy
from tensorflow.keras.metrics import SparseCategoricalAccuracy, Precision,

Recall
```

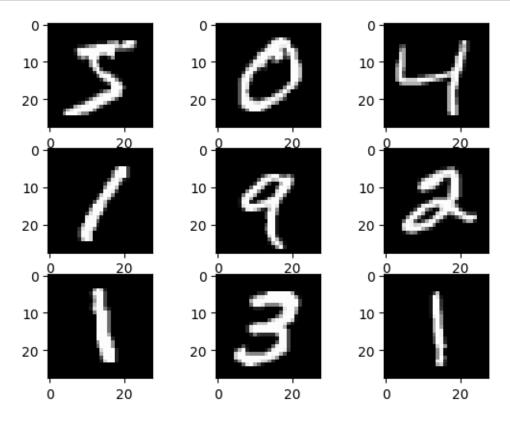
```
[10]: #Loading the MNIST dataset
   (x_train, y_train), (x_test, y_test) = mnist.load_data()
   y_train_categorical = utils.to_categorical(y_train)
   y_test_categorical = utils.to_categorical(y_test)

print("Training data shape: ", x_train.shape)
   print("Training labels shape: ", y_train.shape)
   print("Test data shape: ", x_test.shape)
   print("Test labels shape: ", y_test.shape)
```

Training data shape: (60000, 28, 28)
Training labels shape: (60000,)

Test data shape: (10000, 28, 28) Test labels shape: (10000,)

```
[11]: for i in range(9):
    plt.subplot(330 + 1 + i)
    plt.imshow(trainX[i], cmap=plt.get_cmap('gray'))
    plt.show()
```



```
img_rows, img_cols=28, 28

if k.image_data_format() == 'channels_first':
    x_train = x_train.reshape(x_train.shape[0], 1, img_rows, img_cols)
    x_test = x_test.reshape(x_test.shape[0], 1, img_rows, img_cols)
    inpx = (1, img_rows, img_cols)

else:
    x_train = x_train.reshape(x_train.shape[0], img_rows, img_cols, 1)
    x_test = x_test.reshape(x_test.shape[0], img_rows, img_cols, 1)
    inpx = (img_rows, img_cols, 1)
```

[1] Apply the convolution neural network architecture to the above dataset.

```
[21]: inpx = Input(shape=inpx)
    layer1 = Conv2D(32, kernel_size=(3, 3), activation='relu')(inpx) #layer1 is the_
     \negConv2d layer which convolves the image using 32 filters each of size (3*3).
    layer2 = Conv2D(64, (3, 3), activation='relu')(layer1) #layer2 is again a
     →Conv2D layer which is also used to convolve the image and is using 64⊔
     \hookrightarrow filters each of size (3*3).
    layer3 = MaxPooling2D(pool_size=(3, 3))(layer2) #layer3 is the MaxPooling2Du
     • layer which picks the max value out of a matrix of size (3*3).
    layer4 = Dropout(0.5)(layer3) #layer4 is showing Dropout at a rate of 0.5.
    layer5 = Flatten()(layer4) #layer5 is flattening the output obtained from
     → layer4 and this flattens output is passed to layer6.
    layer6 = Dense(250, activation='sigmoid')(layer5) #layer6 is a hidden layer of
     →a neural network containing 250 neurons.
    layer7 = Dense(10, activation='softmax')(layer6) #layer7 is the output layer1
     →having 10 neurons for 10 classes of output that is using the softmax
     \hookrightarrow function.
[26]: model = Model([inpx], layer7)
    model.compile(optimizer=keras.optimizers.Adadelta(),
               loss=keras.losses.categorical_crossentropy,
               metrics=['accuracy'])
    history = model.fit(x_train, y_train, epochs=10, batch_size=500)
    Epoch 1/10
    accuracy: 0.4174
    Epoch 2/10
    accuracy: 0.4494
    Epoch 3/10
    accuracy: 0.4740
    Epoch 4/10
    120/120 [============ ] - 39s 325ms/step - loss: 1.6573 -
    accuracy: 0.4971
    Epoch 5/10
    accuracy: 0.5203
    Epoch 6/10
    accuracy: 0.5389
    Epoch 7/10
    accuracy: 0.5543
    Epoch 8/10
```

Model: "model\_1"

print('accuracy=', score[1]\*100)

Layer (type)	Output Shape	Param #
input_1 (InputLayer)	[(None, 28, 28, 1)]	0
conv2d (Conv2D)	(None, 26, 26, 32)	320
conv2d_1 (Conv2D)	(None, 24, 24, 64)	18496
<pre>max_pooling2d (MaxPooling2D )</pre>	(None, 8, 8, 64)	0
dropout (Dropout)	(None, 8, 8, 64)	0
flatten (Flatten)	(None, 4096)	0
dense (Dense)	(None, 250)	1024250
dense_1 (Dense)	(None, 10)	2510
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Total params: 1,045,576 Trainable params: 1,045,576 Non-trainable params: 0

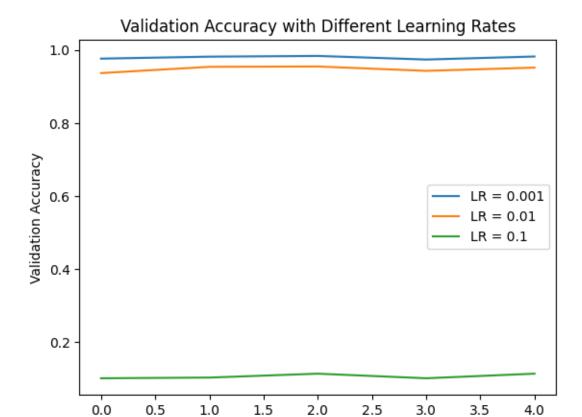
-----

loss= 0.9477853775024414 accuracy= 76.7300009727478

[2] Demonstrate the results with various learning rates.

[45]: from tensorflow.keras.models import Sequential from tensorflow.keras.layers import Conv2D, MaxPooling2D, Flatten, Dense from tensorflow.keras.optimizers import Adam

```
# Load and preprocess the MNIST dataset
(x_train, y_train), (x_test, y_test) = mnist.load_data()
# print(x_test.shape)
# print(y_test.shape)
learning_rates = [0.001, 0.01, 0.1] # Different learning rates to test
for lr in learning_rates:
    # Define CNN architecture
   model = Sequential([
        Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)),
       MaxPooling2D((2, 2)),
       Conv2D(64, (3, 3), activation='relu'),
       MaxPooling2D((2, 2)),
       Flatten(),
       Dense(64, activation='relu'),
       Dense(10, activation='softmax')
   ])
    # Compile the model with the current learning rate
   optimizer = Adam(learning_rate=lr)
   model.compile(optimizer=optimizer,
                  loss='sparse_categorical_crossentropy',
                  metrics=['accuracy'])
    # Train the model
   history = model.fit(x_train, y_train, epochs=5, validation_data=(x_test,_
 →y_test), verbose=0)
    # Plot accuracy for each learning rate
   plt.plot(history.history['val_accuracy'], label=f'LR = {lr}')
plt.title('Validation Accuracy with Different Learning Rates')
plt.xlabel('Epochs')
plt.ylabel('Validation Accuracy')
plt.legend()
plt.show()
```

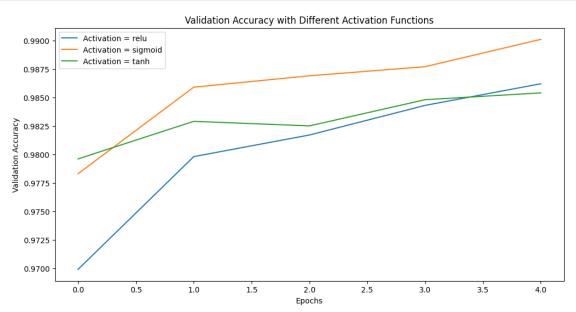


```
[]: acc1 = history.history['val_accuracy']
```

Epochs

[3] Demonstrate the results with various Activation functions.

```
MaxPooling2D((2, 2)),
       Flatten(),
       Dense(64, activation=activation),
       Dense(10, activation='softmax')
   ])
    # Compile the model
   model.compile(optimizer=Adam(),
                  loss='sparse_categorical_crossentropy',
                 metrics=['accuracy'])
    # Train the model
   history = model.fit(x_train, y_train, epochs=5, validation_data=(x_test,_
 →y_test), verbose=0)
    # Plot validation accuracy for each activation function
   plt.plot(history.history['val_accuracy'], label=f'Activation =__
 plt.title('Validation Accuracy with Different Activation Functions')
plt.xlabel('Epochs')
plt.ylabel('Validation Accuracy')
plt.legend()
plt.show()
```



[4] Demonstrate the results with all possible evaluation criteria.

```
[35]: import numpy as np
      import tensorflow as tf
      from tensorflow.keras.datasets import mnist
      from tensorflow.keras.layers import Conv2D, MaxPooling2D, Flatten, Dense
      from tensorflow.keras.optimizers import Adam
      from sklearn.metrics import classification_report
      from tensorflow.keras.models import Sequential
      # Load the MNIST dataset
      (x_train, y_train), (x_test, y_test) = mnist.load_data()
      # Define CNN architecture
      model = Sequential([
         Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)),
         MaxPooling2D((2, 2)),
         Conv2D(64, (3, 3), activation='relu'),
         MaxPooling2D((2, 2)),
         Flatten(),
         Dense(64, activation='relu'),
         Dense(10, activation='softmax')
      ])
      # Compile the model
      model.compile(optimizer=Adam(),
                    loss='sparse_categorical_crossentropy',
                   metrics=['accuracy'])
      # Train the model
      model.fit(x_train, y_train, epochs=5, validation_data=(x_test, y_test),__
       ⇔verbose=0)
      # Predict on test data
      y_pred = model.predict(x_test)
      y_pred_classes = np.argmax(y_pred, axis=1) # Get the predicted classes along_
      y_true = y_test # Keep the true labels as they are
      # Calculate evaluation metrics
      report = classification_report(y_true, y_pred_classes, target_names=[str(i) for_
      →i in range(10)], digits=4)
      print(report)
     313/313 [=========== ] - 1s 4ms/step
```

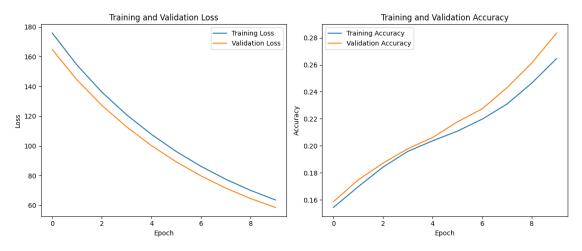
```
2
                0.9865
                          0.9893
                                   0.9879
                                               1032
          3
                0.9911
                          0.9871
                                   0.9891
                                               1010
          4
                0.9808
                          0.9878
                                   0.9843
                                                982
          5
                0.9854
                          0.9832
                                   0.9843
                                                892
          6
                0.9824
                          0.9896
                                                958
                                   0.9860
          7
                0.9941
                          0.9815
                                   0.9878
                                               1028
          8
                0.9948
                          0.9825
                                   0.9886
                                                974
          9
                0.9841
                          0.9832
                                   0.9836
                                               1009
                                   0.9876
                                              10000
   accuracy
                          0.9874
                                   0.9875
                                              10000
  macro avg
                0.9876
weighted avg
                0.9876
                          0.9876
                                   0.9876
                                              10000
```

[5] Demonstrate the learning results in all possible visualizing ways.

```
[22]: import matplotlib.pyplot as plt
      import tensorflow as tf
      from tensorflow.keras.datasets import mnist
      from tensorflow.keras.layers import Dense, Input
      from tensorflow.keras.models import Model
      # Load the MNIST dataset
      (x_train, y_train), (x_test, y_test) = mnist.load_data()
      # Define input layer
      inpx = Input(shape=(784,))
      # Define layer7 (replace this with your actual layer)
      layer7 = Dense(128, activation='relu')(inpx)
      output layer = Dense(10, activation='softmax')(layer7) # Output layer with 1011
       ⇔units for 10 classes
      # Define model
      model = Model(inputs=inpx, outputs=output_layer)
      model.compile(optimizer=tf.keras.optimizers.Adadelta(),
                    loss=tf.keras.losses.categorical_crossentropy,
                    metrics=['accuracy'])
      # Reshape input to a flat vector
      x_train_flat = x_train.reshape((-1, 28 * 28))
      x_{test_flat} = x_{test.reshape}((-1, 28 * 28))
      # Convert labels to one-hot encoding
      y_train_onehot = tf.keras.utils.to_categorical(y_train, 10)
      y_test_onehot = tf.keras.utils.to_categorical(y_test, 10)
      # Train the model
```

```
history = model.fit(x_train_flat, y_train_onehot, epochs=10, batch_size=500,__
 →validation_data=(x_test_flat, y_test_onehot))
# Plot training loss and accuracy
plt.figure(figsize=(12, 5))
# Plot Loss
plt.subplot(1, 2, 1)
plt.plot(history.history['loss'], label='Training Loss')
plt.plot(history.history['val_loss'], label='Validation Loss')
plt.xlabel('Epoch')
plt.ylabel('Loss')
plt.title('Training and Validation Loss')
plt.legend()
# Plot Accuracy
plt.subplot(1, 2, 2)
plt.plot(history.history['accuracy'], label='Training Accuracy')
plt.plot(history.history['val_accuracy'], label='Validation Accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.title('Training and Validation Accuracy')
plt.legend()
plt.tight_layout()
plt.show()
# Evaluate the model on the test set
score = model.evaluate(x_test_flat, y_test_onehot, verbose=0)
print('Test loss:', score[0])
print('Test accuracy:', score[1] * 100)
Epoch 1/10
120/120 [============= ] - 1s 8ms/step - loss: 175.8418 -
accuracy: 0.1543 - val_loss: 164.7406 - val_accuracy: 0.1585
Epoch 2/10
120/120 [============= ] - 1s 6ms/step - loss: 154.2967 -
accuracy: 0.1696 - val_loss: 144.3174 - val_accuracy: 0.1747
Epoch 3/10
120/120 [============= ] - 1s 6ms/step - loss: 136.1447 -
accuracy: 0.1842 - val_loss: 127.2395 - val_accuracy: 0.1871
Epoch 4/10
120/120 [============= ] - 1s 6ms/step - loss: 120.8824 -
accuracy: 0.1958 - val_loss: 112.7741 - val_accuracy: 0.1978
Epoch 5/10
120/120 [============= ] - 1s 6ms/step - loss: 107.7293 -
```

```
accuracy: 0.2036 - val_loss: 100.1964 - val_accuracy: 0.2061
Epoch 6/10
accuracy: 0.2108 - val_loss: 89.2716 - val_accuracy: 0.2177
Epoch 7/10
accuracy: 0.2197 - val_loss: 79.8096 - val_accuracy: 0.2274
Epoch 8/10
accuracy: 0.2309 - val_loss: 71.6182 - val_accuracy: 0.2430
Epoch 9/10
accuracy: 0.2464 - val_loss: 64.5827 - val_accuracy: 0.2613
Epoch 10/10
accuracy: 0.2646 - val_loss: 58.5979 - val_accuracy: 0.2835
```



Test loss: 58.597923278808594 Test accuracy: 28.349998593330383

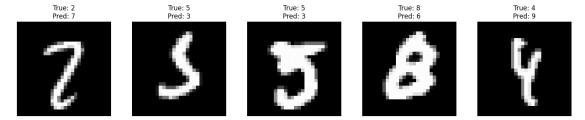
```
[20]: import random

# Select random samples for visualization
num_samples = 5
random_indices = random.sample(range(len(x_test_flat)), num_samples)

plt.figure(figsize=(15, 3))
for i, idx in enumerate(random_indices):
    plt.subplot(1, num_samples, i + 1)
    plt.imshow(x_test_flat[idx].reshape(28, 28), cmap='gray')
    true_label = y_test[idx]
    pred_probs = model.predict(np.expand_dims(x_test_flat[idx], axis=0))
```

```
incorrect_indices = np.where(y_pred_classes != y_test)[0]
num_incorrect_samples = min(5, len(incorrect_indices))

plt.figure(figsize=(15, 3))
for i, idx in enumerate(incorrect_indices[:num_incorrect_samples]):
    plt.subplot(1, num_incorrect_samples, i + 1)
    plt.imshow(x_test[idx].reshape(28, 28), cmap='gray')
    true_label = y_test[idx]
    pred_label = y_pred_classes[idx]
    plt.title(f'True: {true_label}\nPred: {pred_label}')
    plt.axis('off')
plt.show()
```



- B) Perform all above tasks with any preprocessing techniques.
- [1] Apply the convolution neural network architecture to the above dataset.

```
[28]: #Import Requests
     import matplotlib.pyplot as plt
     import numpy as np
     import tensorflow as tf
     from tensorflow.keras.datasets import mnist
     from tensorflow.keras.layers import Conv2D, MaxPooling2D, Flatten, Dense
     from tensorflow.keras.models import Sequential
     from sklearn.metrics import classification_report
     # Load the MNIST dataset
     (x_train, y_train), (x_test, y_test) = mnist.load_data()
     # Normalize pixel values to [0, 1]
     x_train = x_train.astype('float32') / 255.0
     x_test = x_test.astype('float32') / 255.0
     # Add channel dimension for CNN input
     x_train = x_train[..., np.newaxis]
     x_test = x_test[..., np.newaxis]
     # Convert labels to one-hot encoding
     y_train = tf.keras.utils.to_categorical(y_train, 10)
     y_test = tf.keras.utils.to_categorical(y_test, 10)
[29]: # Define CNN architecture
     model = Sequential([
         Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)),
         MaxPooling2D((2, 2)),
         Conv2D(64, (3, 3), activation='relu'),
         MaxPooling2D((2, 2)),
         Flatten(),
         Dense(64, activation='relu'),
         Dense(10, activation='softmax')
     ])
     # Compile the model
     model.compile(optimizer='adam',
                   loss='categorical_crossentropy',
                   metrics=['accuracy'])
     # Train the model
     history = model.fit(x_train, y_train, epochs=5, batch_size=64,__
       ⇔validation_data=(x_test, y_test), verbose=1)
     Epoch 1/5
```

accuracy: 0.9489 - val\_loss: 0.0764 - val\_accuracy: 0.9758

Model: "sequential\_4"

Layer (type)	Output Shape	Param #
conv2d_8 (Conv2D)	(None, 26, 26, 32)	320
<pre>max_pooling2d_8 (MaxPooling 2D)</pre>	(None, 13, 13, 32)	0
conv2d_9 (Conv2D)	(None, 11, 11, 64)	18496
<pre>max_pooling2d_9 (MaxPooling 2D)</pre>	(None, 5, 5, 64)	0
flatten_4 (Flatten)	(None, 1600)	0
dense_21 (Dense)	(None, 64)	102464
dense_22 (Dense)	(None, 10)	650
		========

------

Total params: 121,930 Trainable params: 121,930 Non-trainable params: 0

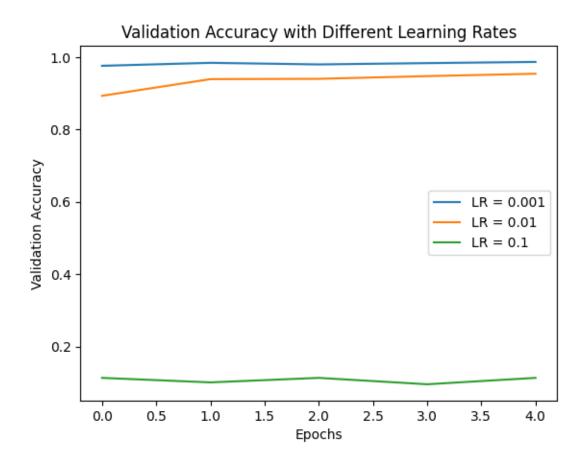
\_\_\_\_\_\_

loss= 0.030073685571551323 accuracy= 98.989999294281

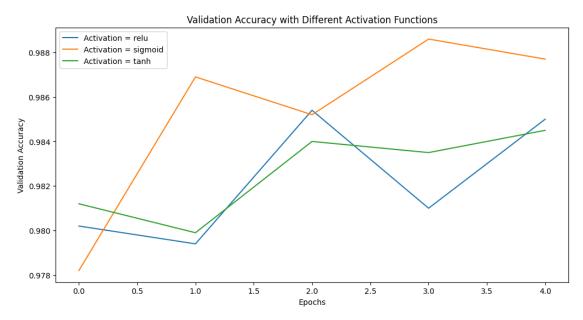
<sup>[2]</sup> Demonstrate the results with various learning rates.

```
[32]: from tensorflow.keras.models import Sequential
      from tensorflow.keras.layers import Conv2D, MaxPooling2D, Flatten, Dense
      from tensorflow.keras.optimizers import Adam
      learning rates = [0.001, 0.01, 0.1] # Different learning rates to test
      for lr in learning_rates:
          # Define CNN architecture
          model = Sequential([
              Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)),
              MaxPooling2D((2, 2)),
              Conv2D(64, (3, 3), activation='relu'),
              MaxPooling2D((2, 2)),
              Flatten(),
              Dense(64, activation='relu'),
              Dense(10, activation='softmax')
          ])
          # Compile the model with the current learning rate
          optimizer = Adam(learning_rate=lr)
          model.compile(optimizer=optimizer,
                        loss='sparse_categorical_crossentropy',
                        metrics=['accuracy'])
          # Train the model
         history = model.fit(x_train, y_train, epochs=5, validation_data=(x_test,__

y_test), verbose=0)
          # Plot accuracy for each learning rate
          plt.plot(history.history['val_accuracy'], label=f'LR = {lr}')
      plt.title('Validation Accuracy with Different Learning Rates')
      plt.xlabel('Epochs')
      plt.ylabel('Validation Accuracy')
      plt.legend()
      plt.show()
```



[3] Demonstrate the results with various Activation functions.



[4] Demonstrate the results with all possible evaluation criteria.

```
import numpy as np
import tensorflow as tf
from tensorflow.keras.datasets import mnist
from tensorflow.keras.layers import Conv2D, MaxPooling2D, Flatten, Dense
from tensorflow.keras.optimizers import Adam
from sklearn.metrics import classification_report
from tensorflow.keras.models import Sequential
```

```
# Define CNN architecture
model = Sequential([
    Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)),
    MaxPooling2D((2, 2)),
    Conv2D(64, (3, 3), activation='relu'),
    MaxPooling2D((2, 2)),
    Flatten(),
    Dense(64, activation='relu'),
    Dense(10, activation='softmax')
])
# Compile the model
model.compile(optimizer=Adam(),
              loss='sparse_categorical_crossentropy',
              metrics=['accuracy'])
# Train the model
model.fit(x_train, y_train, epochs=5, validation_data=(x_test, y_test),__
 →verbose=0)
# Predict on test data
y_pred = model.predict(x_test)
y_pred_classes = np.argmax(y_pred, axis=1) # Get the predicted classes along_
\hookrightarrow axis 1
y_true = y_test # Keep the true labels as they are
# Calculate evaluation metrics
report = classification_report(y_true, y_pred_classes, target_names=[str(i) for_

    in range(10)], digits=4)

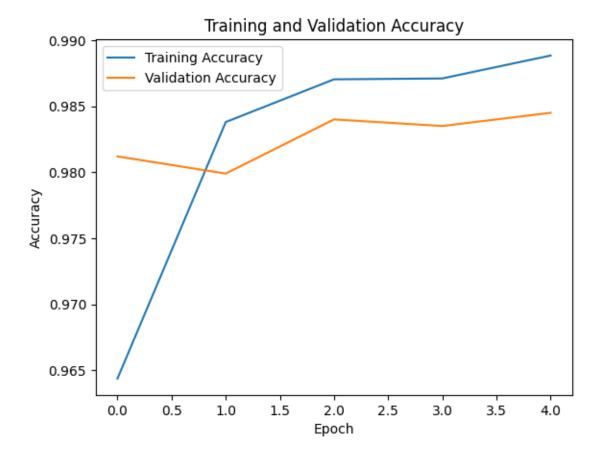
print(report)
```

313/313	[====	=======	======	====] - 1s	4ms/step
		precision	recall	f1-score	support
	0	0.9908	0.9929	0.9918	980
	1	0.9938	0.9938	0.9938	1135
	2	0.9846	0.9942	0.9894	1032
	3	0.9863	0.9950	0.9906	1010
	4	0.9928	0.9898	0.9913	982
	5	0.9810	0.9854	0.9832	892
	6	0.9916	0.9864	0.9890	958
	7	0.9912	0.9825	0.9868	1028
	8	0.9959	0.9918	0.9938	974
	9	0.9861	0.9822	0.9841	1009
accu	ıracy			0.9895	10000

```
macro avg 0.9894 0.9894 0.9894 10000 weighted avg 0.9895 0.9895 0.9895 10000
```

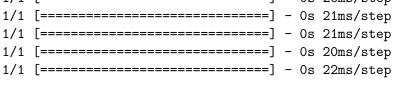
[5] Demonstrate the learning results in all possible visualizing ways.

```
[38]: # Plot accuracy for each epoch
plt.plot(history.history['accuracy'], label='Training Accuracy')
plt.plot(history.history['val_accuracy'], label='Validation Accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.title('Training and Validation Accuracy')
plt.legend()
plt.show()
```



```
[39]: # Select random samples for visualization
num_samples = 5
random_indices = np.random.choice(len(x_test), num_samples, replace=False)

plt.figure(figsize=(15, 3))
for i, idx in enumerate(random_indices):
```





```
[41]: conv1_layer = model.get_layer('conv2d_28')
    conv1_weights = conv1_layer.get_weights()[0]

plt.figure(figsize=(10, 5))
    for i in range(16):
        plt.subplot(4, 4, i + 1)
        plt.imshow(conv1_weights[:, :, 0, i], cmap='gray')
        plt.axis('off')
    plt.suptitle('Learned Convolutional Filters')
    plt.show()
```

## Learned Convolutional Filters

