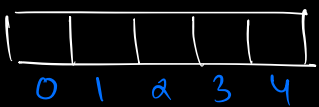
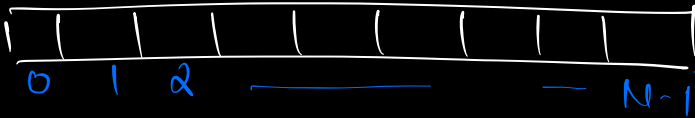


`int arr[5] →` 
↓
integer array with 5 elements

`int arr[N] →` 
↓
int. array with N elements

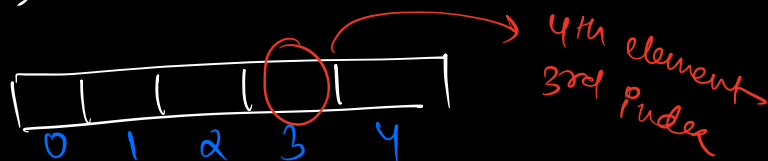
// print an entire array

```
for (i = 0; i < N; i++) {  
    print(arr[i])  
}
```

⇒ TC: $O(N)$

accessing element from i^{th} index ⇒ `arr[i] → $O(1)$`

`int arr[5] ⇒`



get the 4th element ⇒ `arr[3]`

Q. 1. Given N array element, count no. of element having at least 1 element greater than itself [no lib. func.]

arr[1] $\Rightarrow \{ \underset{\checkmark}{-3} \underset{\checkmark}{-2} \underset{\checkmark}{6} \underset{\times}{8} \underset{\checkmark}{4} \underset{\times}{8} \underset{\checkmark}{5} \} \Rightarrow \overset{\text{largest}}{8} | \text{count } 2$

Qp = 5.

arr[8] $\Rightarrow \{ \underset{\checkmark}{2} \underset{\checkmark}{3} \underset{\times}{10} \underset{\checkmark}{7} \underset{\checkmark}{3} \underset{\checkmark}{2} \underset{\times}{10} \underset{\checkmark}{8} \} \Rightarrow 10 | 2$

Qp = 6.

arr[10] $\Rightarrow \{ \underset{\checkmark}{2} \underset{\checkmark}{5} \underset{\checkmark}{1} \underset{\checkmark}{4} \underset{\checkmark}{8} \underset{\checkmark}{0} \underset{\checkmark}{8} \underset{\times}{13} \underset{\checkmark}{8} \} \Rightarrow 13 | 1$

Qp = 9.

Bruteforce

```
for (i=0; i<N; i++) {
```

```
    for (j=0; j<N; j++) {
```

```
        if (any bigger element found)
```

```
            c++; break;
```

```
    }
```

```
}
```

```
return c;
```

$\therefore \Rightarrow \underline{\underline{O(N^2)}}$

Observation

- I) every element except the largest element will have any element bigger than itself
- II) $ans =$ all element except largest elements

↓

$$ans = N - \left(\text{count of largest of element} \right)$$

pseudo

- I) iterate to get max^m
- II) iterate the get count of max^m
- III) $ans = N - \text{count of } max^m$

↗ not correct, if all element -ve, it won't work

↓
valid values

```
maxV = 0
for (i = 0; i < N; i++) {
    if (maxV < arr[i]) {
```

$maxV = INT_MIN$

```
maxV = arr[0]
    }
```

}

$C = 0$

```
for (i = 0; i < N; i++) {
    if (maxV == arr[i])
```

$C++$

}

return arr.length - c;

ex \Rightarrow arr[6] \Rightarrow [2 2 2 2 2 2]

Qp = 0.

max^m = 2

count = 6

ans = 2 - count
= 6 - 6 = 0

TC $\Rightarrow O(2N) \approx O(N)$

SC $\Rightarrow O(1)$.

Now \Rightarrow Change this code, and solve in a single loop.

Q2 Given N array elements, check if there exists a pair (i, j) such that $arr[i] + arr[j] = k$, & $i \neq j$. Note: i & j are indices, k is given sum.

arr \Rightarrow

3	-2	1	4	3	6	8
0	1	2	3	4	5	6

k = 10.

Qp = true \Rightarrow arr[3] + arr[5] = 10

arr \Rightarrow 2 4 -3 7
 0 1 2 3

k = 5

Qp \Rightarrow false.

arr \Rightarrow 2 4 -3 7
 0 1 2 3

k = 8

Qp \Rightarrow false

(arr[1] + arr[1] == 8)
 XXX not-allowed.

solⁿ

check for all pairs.

N = 5 \Rightarrow { 0 1 2 3 4 }

pairs \Rightarrow

(0,0)	(1,0)	(2,0)	(3,0)	(4,0)
(0,1)	(1,1)	(2,1)	(3,1)	(4,1)
(0,2)	(1,2)	(2,2)	(3,2)	(4,2)
(0,3)	(1,3)	(2,3)	(3,3)	(4,3)
(0,4)	(1,4)	(2,4)	(3,4)	(4,4)

Bruteforce

```
for (i = 0; i < N; i++) {  
    for (j = 0; j < N; j++) {  
        if (i == j) continue;  
        if (arr[i] + arr[j] == 2 * k)  
            return true  
    }  
}  
return false
```

iterations $\Rightarrow N * N \Rightarrow N^2$

TC $\Rightarrow O(N^2)$

SC $\Rightarrow O(1)$

Optimised

```
for (i = 0; i < N; i++) {  
    for (j = i + 1; j < N; j++) {  
        if (arr[i] + arr[j] == 2 * k)  
            return true  
    }  
}  
return false
```

$$N-1 \rightarrow 1$$

$$N-1$$

$$N-1 - 1 + 1$$

$$= N-2$$

i	j	iterations
0	[1-(N-1)]	N-1
1	[2-(N-1)]	N-2
2	[3-(N-1)]	N-3
⋮	⋮	⋮
N-1	[N-(N-1)]	<u>0</u>

$$N-1 + N-2 + N-3 + \dots + 3 + 2 + 1 + 0$$

$$\Rightarrow 1 + 2 + 3 + \dots + N-1$$

$$\Rightarrow \frac{(N-1) \times (N-1 + 1)}{2} \Rightarrow \frac{N(N-1)}{2} \text{ iterations}$$

$$B.F \Rightarrow N^2 \text{ iterations} \Rightarrow TC \Rightarrow O(N^2)$$

$$\text{Optimised} \Rightarrow \frac{N(N-1)}{2} \text{ iterations} \Rightarrow TC \Rightarrow O(N^2)$$

building

Java revisited

How to do it in Java

Recursion topics

Q3. Given an array, reverse entire array. | Sc: $O(1)$.

arr \Rightarrow

-1	4	7	6	-2	7	8	10
0	1	2	3	4	5	6	7

rev. arr \Rightarrow

10	8	7	-2	6	7	4	-1
0	1	2	3	4	5	6	7

Sc $\Rightarrow O(1) \rightarrow$ no extra array
 given array itself should change (get reversed)

arr \Rightarrow

0	1	2	3	4	5	6	7
-1	4	7	6	-2	7	8	10

Result \Rightarrow

10	8	7	-2	6	7	4	-1
----	---	---	----	---	---	---	----

arr \Rightarrow

0	1	2	3	4	5	6
-1	6	3	-2	8	9	10

i	j	
0	6	\rightarrow swap.
1	5	\rightarrow swap.
2	4	\rightarrow swap.
3	3	\rightarrow swap.

pseudo

reverse(arr, N) {

 i = 0

 j = N-1

 while(i <= j) {

 swap(arr[i], arr[j])

 i++

 j--

 }

 return arr

}

TC $\Rightarrow O(N)$

SC $\Rightarrow O(1)$

Q4. Given N array elements, & $[Si, Ei]$, reverse array from $[Si - Ei]$, note $\Rightarrow Si \leq Ei$.

arr \Rightarrow 0 1 2 3 4 5 6 7 8
 -3 4 2 8 7 9 6 2 10

$Si = 3$

$Ei = 7$

rev arr \Rightarrow -3 4 2 2 6 9 7 8 10.

pseudo

reversePart(arr, Si, Ei) {

i = Si, j = Ei

while (i <= j) {

swap(arr[i], arr[j])

i++

j--

}

}

TC $\Rightarrow O(N)$

SC $\Rightarrow O(1)$

Q5. Given N array elements, rotate array from last to first by k times.

arr[7] \Rightarrow

k = 1

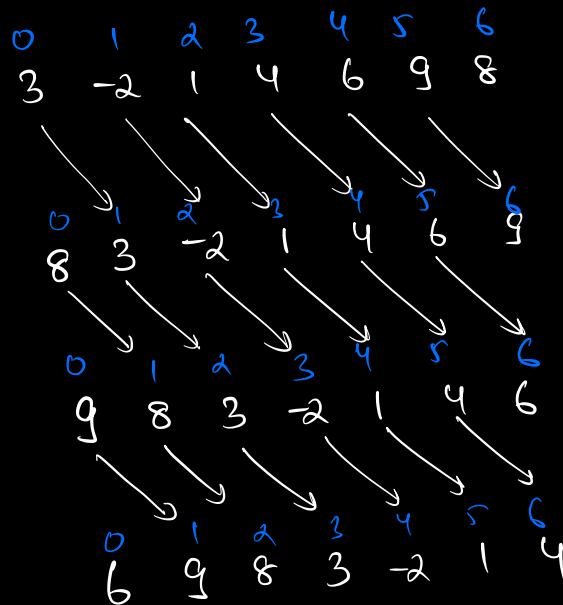
rotated array \Rightarrow

k = 2

rotated array \Rightarrow

k = 3

rotated array \Rightarrow



arr[9] = 4 1 6 9 2 14 7 8 3
 $k=4$

rot arr = 14 7 8 3 4 1 6 9 2

arr[10] = -2 3 1 4 6 2 8 7 9 3
 $k=3$

rot arr = 7 9 3 -2 3 1 4 6 2 8

last 3 element of original \Rightarrow first 3 elements of rotated array

first 7 elements of original \Rightarrow last 7 element of rotated array

arr[13] \Rightarrow $a_0 a_1 a_2 a_3 a_4 a_5 a_6 a_7$ $a_8 a_9 a_{10} a_{11} a_{12}$

$k=5$

rot arr \Rightarrow $a_8 a_9 a_{10} a_{11} a_{12} a_0 a_1 a_2 a_3 a_4 a_5 a_6 a_7$

reverse \Rightarrow $a_{12} a_{11} a_{10} a_9 a_8 a_7 a_6 a_5 a_4 a_3 a_2 a_1 a_0$

reverse first k element

reverse last (N-k) element

$a_8 a_9 a_{10} a_{11} a_{12} a_0 a_1 a_2 a_3 a_4 a_5 a_6 a_7$

pseudo

$$\Rightarrow k \geq \underline{k \% N}$$

i) reverse the entire array $\rightarrow \text{reversePart}(\text{arr}, 0, N-1)$

ii) reverse the first k element $\rightarrow \text{reversePart}(\text{arr}, 0, k-1)$

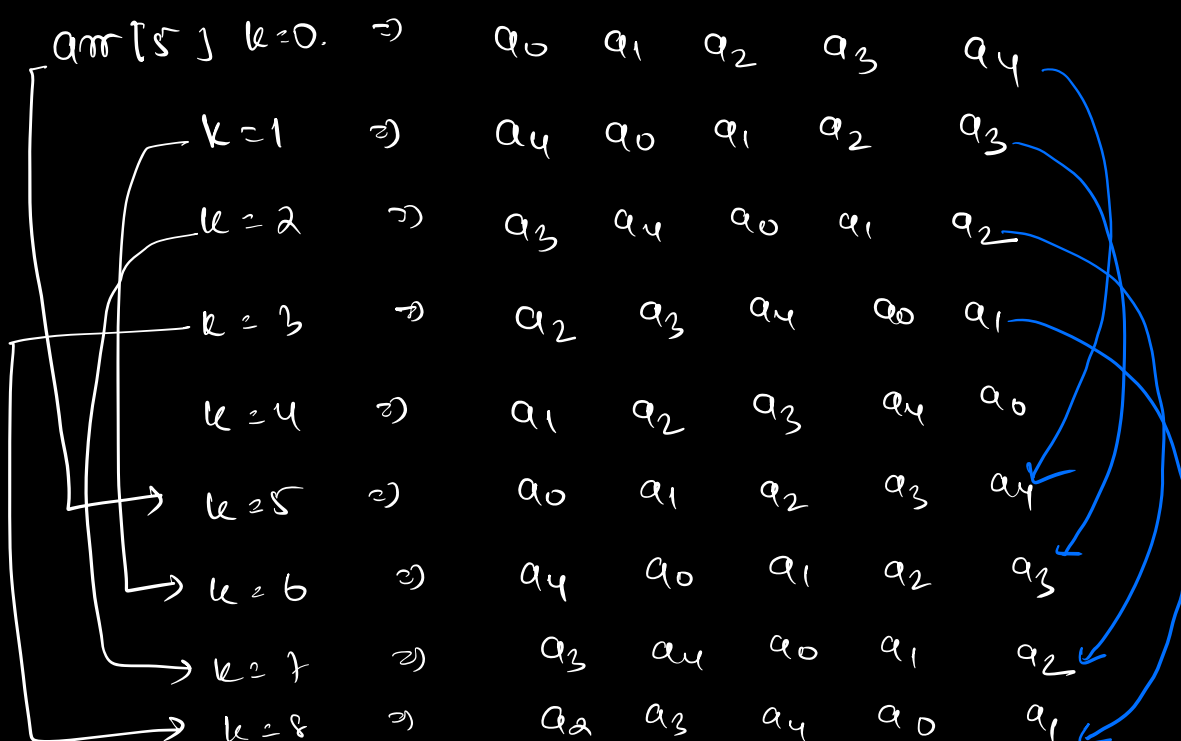
iii) reverse the last $N-k$ element $\rightarrow \text{reversePart}(\text{arr}, k, N-1)$

$$TC \Rightarrow O(N + k + N - k)$$

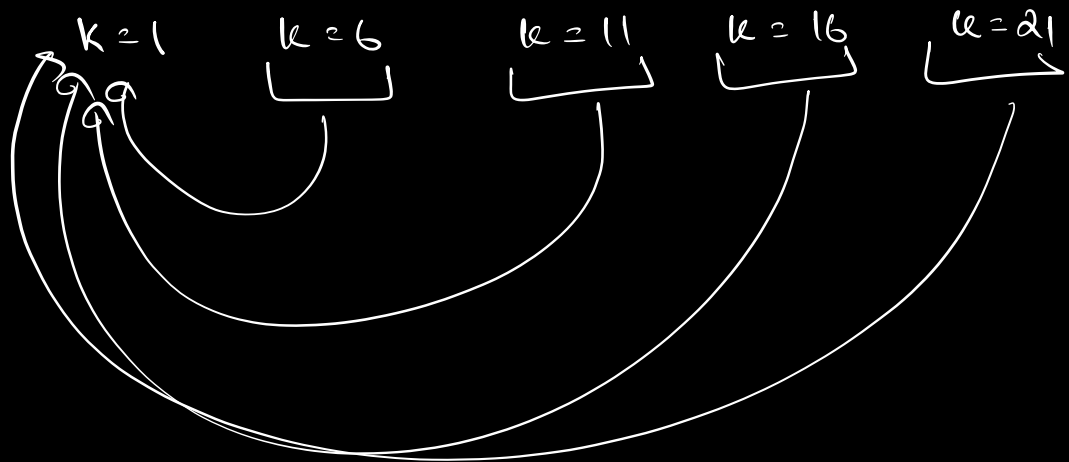
$$= O(\underline{2N}) \approx O(N)$$

$$SC \Rightarrow O(1)$$

$$k > \underline{N} \Rightarrow \text{reversePart}(\text{arr}, 0, \underbrace{(k-1)}_{\geq N-1})$$



N = 5



$k = k \% N$
↓
rotate for k

Optional

How \Rightarrow Rotate k time ($L \rightarrow R$)

Static length array \rightarrow arr[5] \rightarrow fixed arrays.

dynamic arrays \rightarrow arrays with dynamic length

C++ \rightarrow vector

Java \rightarrow arraylist

Python \rightarrow list

C# \rightarrow arraylist / list

Js \rightarrow array

C \rightarrow change to C++ / Java.

list <int> l

↓ ↓

datatype name

$$l.size() \rightarrow 0$$

```
l.insert()
```

↳ insert(2)

(. insert(3)

l.me() $\rightarrow 3$

$\text{point}(l, \text{get}(1)) \rightarrow \underline{\underline{2}}$

TC \Rightarrow

$(\cdot \text{get}())$]	<u><u>$O(1)$</u></u>
$(\cdot \text{insert}())$		
$(\cdot \text{b're}())$		

11 print all elements of a list—

$$\text{for } i=0, i < (\text{size}), i++) \{$$

```
print(l.get(1))
```

3