

School of Computer Science Engineering and Technology  
Assignment-08

<b>Course-</b> B.Tech	<b>Type-</b> Core
<b>Course Code-</b>	<b>Course Name-</b> Statistical Machine Learning
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## Implement Gaussian Mixture Model using Synthetic Dataset

Challenges in K-Means can be overcome using:

- You could measure uncertainty in cluster assignment by comparing the distances of each point to all cluster centers, rather than focusing on just the closest.
- You might also imagine allowing the cluster boundaries to be ellipses rather than circles, so as to account for non-circular clusters.

A **Gaussian mixture model (GMM)** attempts to find a mixture of multi-dimensional Gaussian probability distributions that best model any input dataset. In the simplest case, GMMs can be used for finding clusters in the same manner as k-means.

However, because GMM contains a probabilistic model under the hood, it is also possible to find probabilistic cluster assignments. In Scikit-Learn this is done using the `predict_proba` method. This returns a matrix of size `[n_samples, n_clusters]` which measures the probability that any point belongs to the given cluster.

### Step -1: Generate Synthetic Data using unlabeled blobs

```
from sklearn.datasets.samples_generator import make_blobs
X, y_true = make_blobs(n_samples=400, centers=4,
cluster_std=0.7, random_state=0)
X = X[:, ::-1] # flip axes for better plotting
```

### Step-2: Visualize the uncertainty by making data point size proportional to probability

You have to use `predict_proba` and `probs_max` to predict the max probability for the Gaussian Mixture Model.

```
from matplotlib.patches import Ellipse

def draw_ellipse(position, covariance, ax=None, **kwargs):
    """Draw an ellipse with a given position and covariance"""
    ax = ax or plt.gca()
```

```

# Convert covariance to principal axes
if covariance.shape == (2, 2):
    U, s, Vt = np.linalg.svd(covariance)
    angle = np.degrees(np.arctan2(U[1, 0], U[0, 0]))
    width, height = 2 * np.sqrt(s)
else:
    angle = 0
    width, height = 2 * np.sqrt(covariance)

# Draw the Ellipse
for nsig in range(1, 4):
    ax.add_patch(Ellipse(position, nsig * width, nsig * height,
angle, **kwargs))

def plot_gmm(gmm, X, label=True, ax=None):
    ax = ax or plt.gca()
    labels = gmm.fit(X).predict(X)
    if label:
        ax.scatter(X[:, 0], X[:, 1], c=labels, s=40, cmap='viridis',
zorder=2, edgecolor='k')
    else:
        ax.scatter(X[:, 0], X[:, 1], s=40, zorder=2, cmap='viridis', edgecolor='k')
    ax.axis('equal')

w_factor = 0.2 / gmm.weights_.max()
for pos, covar, w in zip(gmm.means_, gmm.covariances_, gmm.weights_):
    draw_ellipse(pos, covar, alpha=w * w_factor)

gmm = GaussianMixture(n_components=4, covariance_type='full',
random_state=42)
plot_gmm(gmm, X_stretched)

```

### Step-3: GMM as Density Estimation and Generative Model

Using `sklearn.datasets import make_moons` we can plot the data using scatter plot.