# Greedy

Huffman coding.

Coreman section 16.3

### Divide and Conquer

**Local Minimal:** The local minimal of a sequence

$$P_1, P_2, P_3, \ldots, P_n$$

is P<sub>i</sub> such that

- <sub>1.</sub> 1 < i < n
- 2.  $P_{i-1} > P_i$  and  $P_i < P_{i+1}$

#### Input:

- 1. An integer,  $n \ge 3$  representing the number of coins.
- 2. A sequence

$$P_1, P_2, P_3, \ldots, P_n$$

Here,  $P_1 > P_2 \& P_n > P_{n-1}$ 

NB: this condition ensures that there is always a local minimal.

#### Output:

A local minimal of the sequence.

#### **Solution:**

Similar to: <a href="https://drive.google.com/open?id=0By-BfovJ3XAWVXF6OUMwb0hyVG8">https://drive.google.com/open?id=0By-BfovJ3XAWVXF6OUMwb0hyVG8</a>

### Online - 3

### **Dynamic Programming**

#### Input:

- 3. An integer, n representing the number of coins.
- 4. A sequence

$$P_1, P_2, P_3, \ldots, P_n$$

Here  $P_i$  = probability of getting head if i-th coin is flipped.

5. An integer, k <= n

#### Output:

- 1. The probability of getting exactly k heads if all the coins are flipped.
- 2. Print the DP table.

NB: the problem must be solved using bottom up approach.

#### **Solution:**

#### **Recurrence relation:** [see from offline folder]

T(n, k) = Probability if n th coin gives head + Probability if n th coin does not give head

$$= P_n * T (n - 1, k - 1) + (1 - P_n) * T(n - 1, k)$$

#### **Base Cases:**

- 1. T(n, n)
- 2. T(n, 0)

Code: http://ideone.com/ylt19F

Running Time: O(nk)

### **Branch & Bound**

#### Input:

- 1. An integer, n, the number of processors
- 2. An array of times taken by some processes

$$A_1, A_2, A_3, \ldots, A_n$$

Where Ai = time taken by i-th process

#### Output:

1. Output according to the greedy algorithm.

#### Solution:

[see greedy algorithm from offline – 4 folder]

## Graph

#### Input:

- 1. An undirected unweighted graph
- 2. A node, u

#### Output:

- 1. Whether it has a spanning tree
- 2. Shortest path from the node u to all the other vertices.

#### Solution:

See the "online 5" folder.