

Introduction to Digital Computing

Homework 12 - *flip flops, counters, shift registers, and pulse*

Student's Name _____

Instructions:

- Show all work to receive full credit.

Reference

| Function Table – NOR S-R Flip flop | | | | |
|------------------------------------|---|---------|----|-----------|
| Inputs | | Outputs | | Comments |
| S | R | Q | Q~ | |
| 0 | 0 | Q | Q~ | No Change |
| 0 | 1 | 0 | 1 | Reset |
| 1 | 0 | 1 | 0 | Set |
| 1 | 1 | Invalid | | |

| Function Table – J-K Flip flop | | | | |
|--------------------------------|---|---------|----|-----------------------------------|
| Inputs | | Outputs | | Comments |
| J | K | Q | Q~ | |
| 0 | 0 | Q | Q~ | No Change |
| 0 | 1 | 0 | 1 | Reset |
| 1 | 0 | 1 | 0 | Set |
| 1 | 1 | Q~ | Q | Toggle, invert the previous state |

| Function Table – D Flip flop | | | | |
|------------------------------|-------|---------|----|-----------|
| Input | | Outputs | | Comments |
| D | Clock | Q | Q~ | |
| 0 | 0 | Q | Q~ | No Change |
| 0 | 1 | 0 | 1 | Reset |
| 1 | 0 | Q | Q~ | No Change |
| 1 | 1 | 1 | 0 | Set |

| Transition at output | PRESENT State Q(N) | NEXT State Q(N+1) | J | K |
|-------------------------|--------------------|-------------------|---|---|
| 0 → 0 | 0 | 0 | 0 | x |
| 0 → 1 | 0 | 1 | 1 | x |
| 1 → 0 | 1 | 0 | x | 1 |
| 1 → 1 | 1 | 1 | x | 0 |
| J-K FF excitation table | | | | |

555 Timer

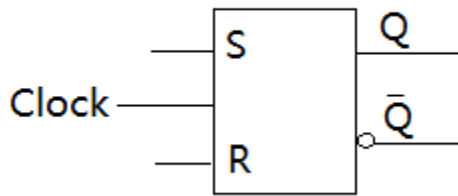
$$T_{HI} = 0.693 \cdot (R_1 + R_2) \cdot C_1$$

$$T_{LO} = 0.693 \cdot R_2 \cdot C_1$$

$$\text{Duty cycle} = (T_{HI} / \text{Period}) \cdot 100\%$$

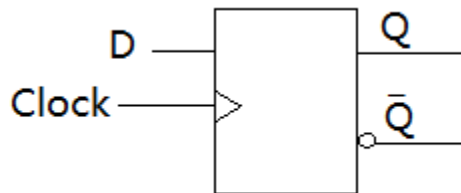
$$\text{Period} = T = T_{HI} + T_{LO}$$

Question 1) For a given S-R FF, find the output Q and \bar{Q} assuming that $Q_{\text{initial}} = 1$



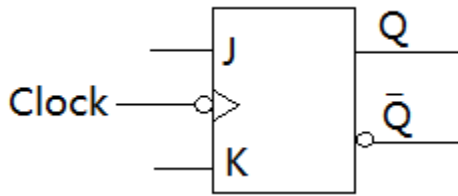
| Clock | | | | | | | | |
|-----------|---|---|---|---|---|---|---|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| S | | | | | | | | |
| R | | | | | | | | |
| Q | | | | | | | | |
| \bar{Q} | | | | | | | | |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |

Question 2) For the following D-FF, sketch output Q assuming $Q_{\text{initial}} = 0$



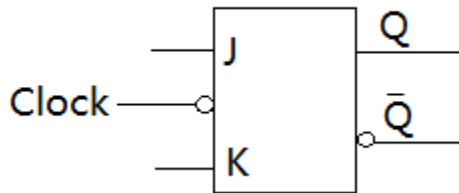
| Clock | | | | | | | | |
|-----------|---|---|---|---|---|---|---|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| D | | | | | | | | |
| Q | | | | | | | | |
| \bar{Q} | | | | | | | | |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |

Question 3) For the following J-K-FF, sketch output Q assuming Q_{initial} = 1



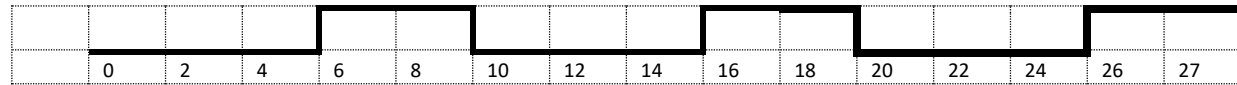
| Clock | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|-------|---|---|---|---|---|---|---|---|---|
| J | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| K | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Q | | | | | | | | | |
| Q~ | | | | | | | | | |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

Question 4) For the following J-K-FF, sketch output Q assuming Q_{initial} = 0

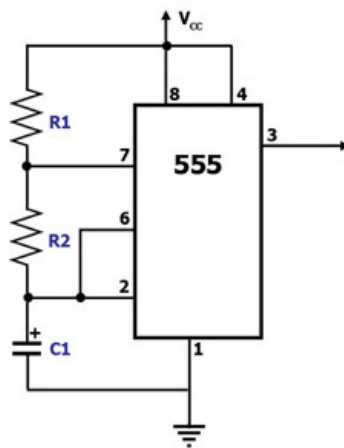


| Clock | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|-------|---|---|---|---|---|---|---|---|---|
| J | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| K | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Q | | | | | | | | | |
| Q~ | | | | | | | | | |
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

c. Duty cycle



c. Duty cycle



- Series IN / Series OUT
- Series IN / Parallel OUT
- Parallel IN / Series OUT
- Parallel IN / Parallel OUT
- Rotate left
- Rotate right

Shift register name: _____.

Shift register name: _____.

Shift register name: _____.

Shift register name: _____.

Question 8) Design a synchronous counter that will display odd number as the following:

1→3→5→6 repeats (COUNTER SEQUENCE)

Step 1: Write and sketch the sequence of the synchronous counter (3 points)

Step 2: Determine the number of flip flops that you need and the module number (3 points)

Step 3 and 4: Construct a truth table of the transition state with the PRESENT state and the NEXT state, and complete the J-K input for each flip flop using sequence diagram from Step 1.

| Decimal | PRESENT state | | | NEXT state | | | J-K State | | | | | |
|---|---------------|---|---|------------|---|---|----------------|----------------|----------------|----------------|----------------|----------------|
| | C | B | A | C | B | A | J _C | K _C | J _B | K _B | J _A | K _A |
| 0 | 0 | 0 | 0 | | | | | | | | | |
| 1 | 0 | 0 | 1 | | | | | | | | | |
| 2 | 0 | 1 | 0 | | | | | | | | | |
| 3 | 0 | 1 | 1 | | | | | | | | | |
| 4 | 1 | 0 | 0 | | | | | | | | | |
| 5 | 1 | 0 | 1 | | | | | | | | | |
| 6 | 1 | 1 | 0 | | | | | | | | | |
| 7 | 1 | 1 | 1 | | | | | | | | | |
| Circuit excitation table for sequence 1,3,5,6 | | | | | | | | | | | | |

Step 5: Create a k-map table for each J and K input and find the SOP equation of each.

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|-----------|-----------|-----|------------------|--|--|------------|--|--|------|--|--|------------|--|--|--|--|-----------|-----|------------------|--|--|------------|--|--|------|--|--|------------|--|--|--|--|-----------|-----|------------------|--|--|------------|--|--|------|--|--|------------|--|--|
| <p style="text-align: center;">J_C</p> <table border="1" style="margin: auto; border-collapse: collapse;"> <tr> <td></td><td style="text-align: center;">\bar{C}</td><td style="text-align: center;">C</td></tr> <tr> <td style="text-align: center;">$\bar{A}\bar{B}$</td><td></td><td></td></tr> <tr> <td style="text-align: center;">$\bar{A}B$</td><td></td><td></td></tr> <tr> <td style="text-align: center;">AB</td><td></td><td></td></tr> <tr> <td style="text-align: center;">$A\bar{B}$</td><td></td><td></td></tr> </table> <p>SOP :</p> | | \bar{C} | C | $\bar{A}\bar{B}$ | | | $\bar{A}B$ | | | AB | | | $A\bar{B}$ | | | <p style="text-align: center;">J_B</p> <table border="1" style="margin: auto; border-collapse: collapse;"> <tr> <td></td><td style="text-align: center;">\bar{C}</td><td style="text-align: center;">C</td></tr> <tr> <td style="text-align: center;">$\bar{A}\bar{B}$</td><td></td><td></td></tr> <tr> <td style="text-align: center;">$\bar{A}B$</td><td></td><td></td></tr> <tr> <td style="text-align: center;">AB</td><td></td><td></td></tr> <tr> <td style="text-align: center;">$A\bar{B}$</td><td></td><td></td></tr> </table> <p>SOP:</p> | | \bar{C} | C | $\bar{A}\bar{B}$ | | | $\bar{A}B$ | | | AB | | | $A\bar{B}$ | | | <p style="text-align: center;">J_A</p> <table border="1" style="margin: auto; border-collapse: collapse;"> <tr> <td></td><td style="text-align: center;">\bar{C}</td><td style="text-align: center;">C</td></tr> <tr> <td style="text-align: center;">$\bar{A}\bar{B}$</td><td></td><td></td></tr> <tr> <td style="text-align: center;">$\bar{A}B$</td><td></td><td></td></tr> <tr> <td style="text-align: center;">AB</td><td></td><td></td></tr> <tr> <td style="text-align: center;">$A\bar{B}$</td><td></td><td></td></tr> </table> <p>SOP:</p> | | \bar{C} | C | $\bar{A}\bar{B}$ | | | $\bar{A}B$ | | | AB | | | $A\bar{B}$ | | |
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| $\bar{A}\bar{B}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| | \bar{C} | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| $A\bar{B}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | \bar{C} | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\bar{A}\bar{B}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\bar{A}B$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| AB | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $A\bar{B}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | \bar{C} | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $\bar{A}\bar{B}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| AB | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| $A\bar{B}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Step 6: Complete and sketch the counter circuit using the SOP equation found in **step 5**

----- Homework Ends Here -----