

Figure 9.16 Flowchart for Unsigned Binary Division



# Restoring division $(17)/(3)$

- Dividend  $Q = (17)_{10} = (10001)_2$   $n = 5$  as 17 requires 5 bits
- Divisor  $M = (03)_{10} = (000011)_2$   $n+1 = 6$  bits
- 2's complement of  $M = (111101)_2$



C	A	Q	Shift
0	00000	10001	Initial
			left
0	00001	0001_	
			$A = A - M = 000001 +$ $A + 2's \text{ complement of } M = 111101 = 111110$
1	11110	00010	
			Restore
0	00001	00010	



C	A	Q	Shift
0	00001	00010	Initial
			left
0	00010	0010_	
			$A = A - M = 000010 +$ $A + 2's \quad 111101 =$ $\text{complement of } M \quad 111111$
1	11111	0010 0	
			Restore
0	00010	00100	



C	A	Q	Shift
0	00010	00100	Initial
			left
0	00100	0100_	
			$A = A - M = A + 2's \text{ complement of } M$ $000100 + 111101 = 000001$
0	00001	01001	



C	A	Q	Shift
0	00001	01001	Initial
			left
0	00010	1001_	
			$A = A - M = A + 2's \text{ complement of } M$ $000010 + 111101 = 111111$
1	11111	10010	
			Restore
0	00010	10010	



C	A	Q	Shift
0	00010	10010	Initial
			left
0	00101	0010_	
			$A = A - M = A + 2's \text{ complement of } M$ $\begin{array}{r} 000101 + \\ 111101 = \\ 000010 \end{array}$
0	00010	0010 <sup>1</sup>	
			Restore
	000010 remainder	<u>0010</u> <sup>1</sup> quotient	



# Restoring division $(11)_2 / (3)_2$

- Dividend  $Q = (11)_{10} = (1011)_2$   $n = 4$  as 11 requires 4 bits
- Divisor  $M = (03)_{10} = (00011)_2$   $n+1 = 5$  bits
- 2's complement of  $M = (11101)_2$





# 1<sup>st</sup> Cycle

C	A	Q	Shift
0	0000	1011	Initial
			left
0	0001	011_	
			$A = A - M = 00001 +$ $A + 2's \text{ complement of } M = 11101 =$ $11110$
1	1110	0110	



C	A	Q	Shift
0	0001	0110	Initial
			left
0	0010	110_	
			$A = A - M = A + 2's \text{ complement of } M$ $00010 + 11101 = 11111$
1	1111	1100	
			Restore
0	0010	1100	



C	A	Q	Shift
0	0010	1100	Initial
			left
0	0101	100_	
			$A = A - M = 00101 + 11101 = 00010$ <p>2's complement of M</p>
0	0010	1001	



# 4<sup>th</sup> Cycle

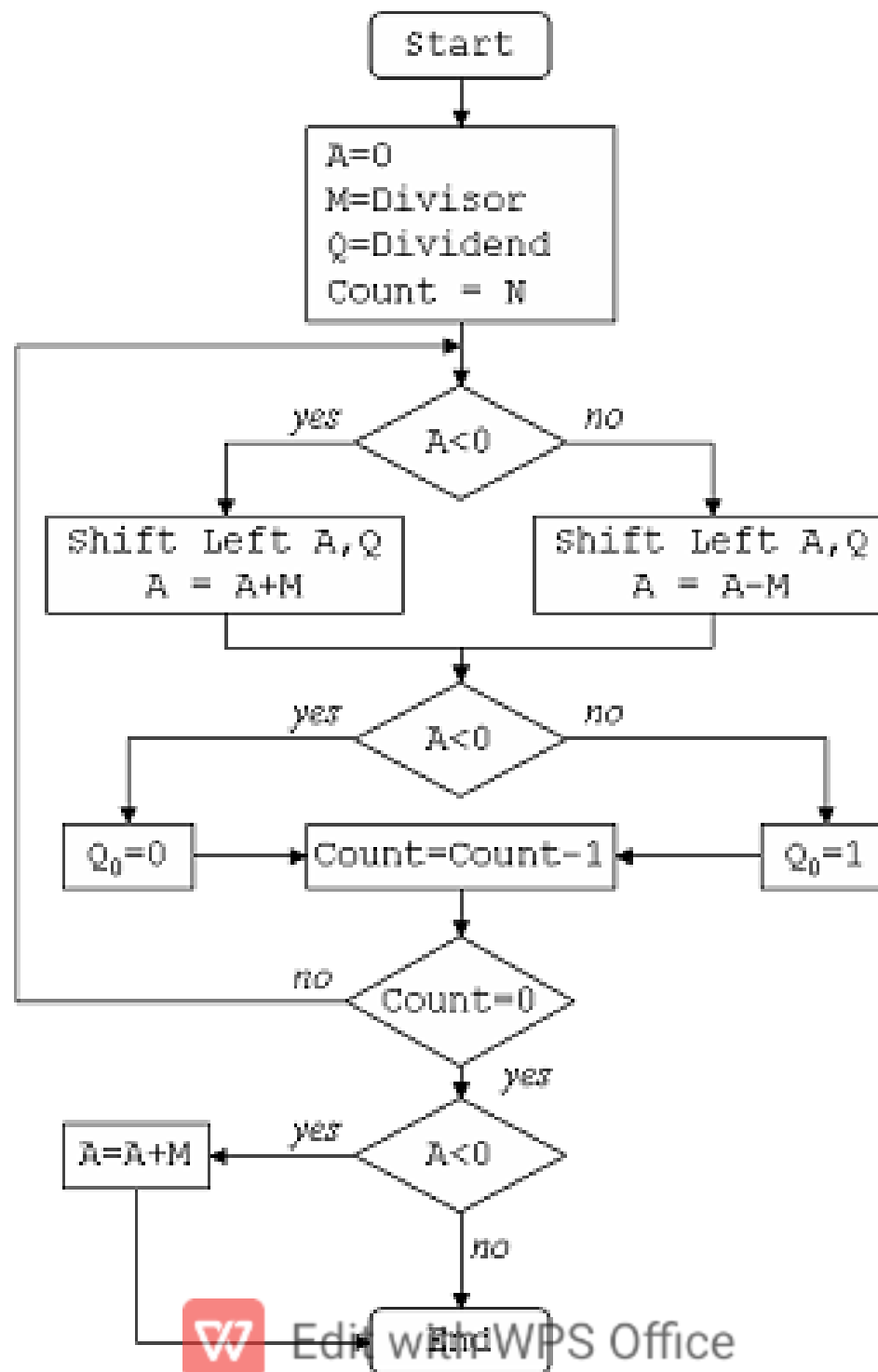
C	A	Q	Shift
0	0010	1001	Initial
			left
0	0101	001_	
			$A = A - M = A + 2's \text{ complement of } M$ $00101 + 11101 = 00010$
0	0010	0011	
	remainder	quotient	



# Non restoring Division



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# Non Restoring division $(11)/(3)$

- Dividend  $Q = (11)_{10} = (1011)_2$   $n = 4$  as 11 requires 4 bits
- Divisor  $M = (03)_{10} = (00011)_2$   $n+1 = 5$  bits
- 2's complement of  $M = (11101)_2$



C	A	Q	Shift
0	0000	1011	Initial
			left
0	0001	011_	
			$A = A - 00001 +$ $M = A + 11101 =$ 2's complement of M 11110
1	1110	0110	





# 2<sup>nd</sup> Cycle

C	A	Q	Shift
1	1110	0110	Initial
			left
1	1100	110_	
			<div> <div>A = A +M</div> <div> 11100 + 00011 = 11111 </div> </div>
1	1111	1100	



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# 3<sup>rd</sup> Cycle

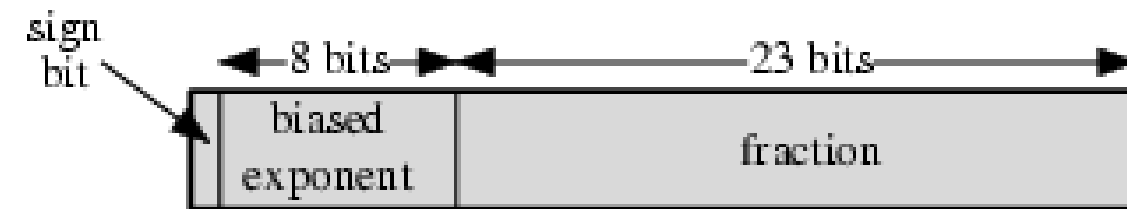
C	A	Q	Shift
1	1111	1100	Initial
			left
1	1111	100_	
			$  \begin{array}{r}  A = A \\  +M = 11111 + \\  00011 = \\  00010  \end{array}  $
0	0010	1001	

# 4<sup>th</sup> Cycle

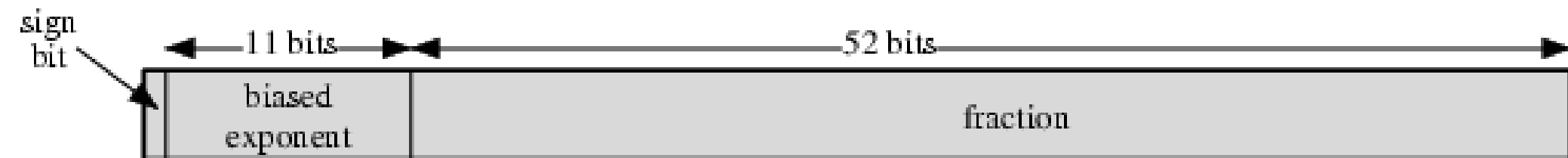
C	A	Q	Shift
0	0010	1001	Initial
			left
0	0101	001_	
			$A = A - M = 00101 +$ $A + 2's \text{ complement of } M = 11101 =$ $00010$
0	0010 remainder	001 <sup>1</sup> quotient	



# IEEE 754 Formats



(a) Single format



(b) Double format



# IEEE 754 Format Parameters

Parameter	Single	Single Extended	Double	Double Extended
Word width (bits)	32	$\geq 43$	64	$\geq 79$
Exponent width (bits)	8	$\geq 11$	11	$\geq 15$
Exponent bias	127	unspecified	1023	unspecified
Maximum exponent	127	$\geq 1023$	1023	$\geq 16383$
Minimum exponent	-126	$\leq -1022$	-1022	$\leq -16382$
Number range (base 10)	$10^{-38}, 10^{+38}$	unspecified	$10^{-308}, 10^{+308}$	unspecified
Significand width (bits)*	23	$\geq 31$	52	$\geq 63$
Number of exponents	254	unspecified	2046	unspecified
Number of fractions	$2^{23}$	unspecified	$2^{52}$	unspecified
Number of values	$1.98 \times 2^{31}$	unspecified	$1.99 \times 2^{63}$	unspecified

\* not including implied bit



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# Interpretation of IEEE 754 Floating-Point Numbers

	Single Precision (32 bits)				Double Precision (64 bits)			
	Sign	Biased exponent	Fraction	Value	Sign	Biased exponent	Fraction	Value
positive zero	0	0	0	0	0	0	0	0
negative zero	1	0	0	-0	1	0	0	-0
plus infinity	0	255 (all 1s)	0	$\infty$	0	2047 (all 1s)	0	$\infty$
minus infinity	1	255 (all 1s)	0	$-\infty$	1	2047 (all 1s)	0	$-\infty$
quiet NaN	0 or 1	255 (all 1s)	$\neq 0$	NaN	0 or 1	2047 (all 1s)	$\neq 0$	NaN
signaling NaN	0 or 1	255 (all 1s)	$\neq 0$	NaN	0 or 1	2047 (all 1s)	$\neq 0$	NaN
positive normalized nonzero	0	$0 < e < 255$	f	$2^{e-127}(1.f)$	0	$0 < e < 2047$	f	$2^{e-1023}(1.f)$
negative normalized nonzero	1	$0 < e < 255$	f	$-2^{e-127}(1.f)$	1	$0 < e < 2047$	f	$-2^{e-1023}(1.f)$
positive denormalized	0	0	$f \neq 0$	$2^{-126}(0.f)$	0	0	$f \neq 0$	$2^{-1022}(0.f)$
negative denormalized	1	0	$f \neq 0$	$-2^{-126}(0.f)$	1	0	$f \neq 0$	$-2^{-1022}(0.f)$

