

E213 : Analysis of Decays of heavy vector boson Z^0

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1 Introduction

2 Prerequisite Knowledge

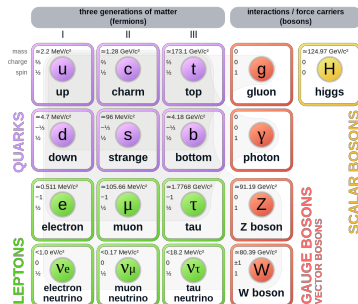
- Standard Model
- Electroweak Theory
- Physics Related to the Z^0 Resonance
 - Angular Dependence of γ/Z^0 Mediated Processes
 - Forward-Backward Asymmetry
 - Background Processes: Radiative Corrections
 - Breit Wigner Distribution
 - LEP Experiment and OPAL Detector

Introduction

- Goal: to understand how data from a particle accelerator is analysed and to deduce different properties of the Z^0 boson
- Important physical quantities: Z^0 mass and decay width
- Data collected from the OPAL (Omni-Purpose Apparatus at LEP) detector
- Part I: Carried out event display analysis on smaller datasets to understand how to separate out different Z^0 decay channels
- Part II: Cuts (constraints) imposed on the data are refined and statistical analysis done on larger real world data → deduce physical quantities

Standard Model

- Standard Model: provides the most fundamental description of nature by incorporating the elementary particles and their interactions
- Two families: fermions (half integer spins), and bosons (integer spins)
 - EM interactions \rightarrow photon (γ)
 - Strong force \rightarrow gluons (g)
 - Weak force $\rightarrow W^{\pm}, Z^0$
 - Gravity \rightarrow graviton (hypothesized; not included in SM)



Standard Model ¹

¹Standard Model. https://en.wikipedia.org/wiki/Standard_Model.

Standard Model

- Fermions: three generations of quarks and leptons
 - Six flavours of quarks: up (u), down (d), charm (c), strange (s), top (t) and bottom (b)
 - Six flavours of leptons: electron (e), muon (μ) and tau (τ), and associated neutrinos (ν_e , ν_μ and ν_τ)
- Composite particles: three quark combinations, called baryons ($qqq/\bar{q}\bar{q}\bar{q}$) or quark-antiquark pairs, called mesons ($q\bar{q}$)
- Mathematically, elementary particles \rightarrow elements of representations of certain symmetry groups
- Gauge fields coupling to these particles \rightarrow consequence of invariance of corresponding Lagrangian under local phase transformations ²
- Gauge symmetry that governs the Standard Model is given by:

$$SU(3)_{\text{Colour}} \times SU(2)_{\text{Left chiral}} \times U(1)_{\text{Y(Weak hypercharge)}}$$

²Mark Thomson. *Modern Particle Physics*. Cambridge University Press, 2013. DOI: 10.1017/CB09781139525367.

Electroweak Theory

- Initially, EM and the theory of weak interactions formulated separately
- At higher energies ($\sim 246 \text{ GeV}$ ³), unified into single force \rightarrow GSW electroweak model - 1960s
- Impose local gauge invariance on $SU(2)_L$ symmetry group \rightarrow three gauge fields: $W^{(1)}$, $W^{(2)}$ and $W^{(3)}$
- Physical W^+ and W^- bosons found to be linear combinations:

$$W_{\mu}^{\pm} = \frac{1}{\sqrt{2}} \left(W_{\mu}^{(1)} \mp i W_{\mu}^{(2)} \right) \quad (1)$$

³J. Erler and A. Freitas. *Electroweak Model and Constraints on New Physics*. English. Mar. 2018. URL: <https://pdg.lbl.gov/2019/reviews/rpp2019-rev-standard-model.pdf>.

Electroweak Theory

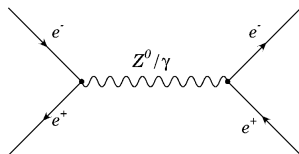
- $W_\mu^{(3)}$ field (no physical interpretation ?)
- Additional symmetry, the $U(1)_Y$ group is introduced
- B_μ field arising from $U(1)_Y$ symmetry (no physical meaning ?)
- Linear combinations of $W_\mu^{(3)}$ and B_μ fields \rightarrow photon and the Z^0 boson:

$$\begin{pmatrix} A_\mu \\ Z_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_W & \sin \theta_W \\ -\sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} B_\mu \\ W_\mu^{(3)} \end{pmatrix} \quad (2)$$

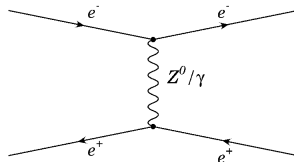
θ_W : weak mixing/Weinberg angle

Angular Dependence of γ/Z^0 Mediated Processes

- $e^+e^- \rightarrow e^+e^-$: t-channel as well as s-channel component
- $e^+e^- \rightarrow f\bar{f}$ (f other than e^-): only s-channel



s-channel Bhabha scattering



t-channel Bhabha scattering

Angular Dependence of γ/Z^0 Mediated Processes

- s channel angular dependence:

$$\left(\frac{d\sigma}{d\Omega}\right)_s \propto (1 + \cos^2 \theta)$$

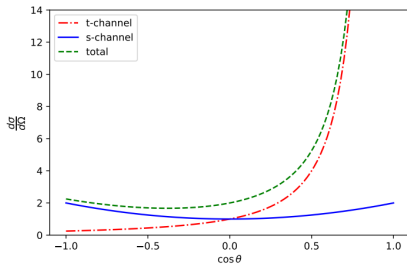
Cross section has a major contribution at large angles (or small values of $\cos \theta$)

- t channel angular dependence:

$$\left(\frac{d\sigma}{d\Omega}\right)_t \propto (1 - \cos \theta)^{-2}$$

Cross section increases asymptotically at small angles (or large values of $\cos \theta$)⁴

- Essential step ! : Remove t -channel contribution while finding inherent forward backward asymmetry in $e^+e^- \rightarrow e^+e^-$ process



s and t -channel angular distribution

⁴Universität Bonn. Instructions for E213: Analysis of Z^0 decay.

Forward-Backward Asymmetry

- Consider Z^0 mediated s-channel process $e^+e^- \rightarrow f\bar{f}$
- Angular dependence:

$$\left(\frac{d\sigma}{d\Omega}\right)_{s(Z^0)} \propto a(1 + \cos^2 \theta) + 2b \cos \theta$$

- No. of fermions in forward dir., $(\theta > \pi/2) \neq$ no. of fermions in backward dir., $(\theta < \pi/2)$
- Asymmetry term b : Due to unequal coupling of Z^0 to right handed and left handed fermions

$$b = \left[(g_L^e)^2 - (g_R^e)^2 \right] \left[(g_L^f)^2 - (g_R^f)^2 \right]$$

- g_L^f : coupling of Z^0 to left handed fermions
- g_R^f : coupling of Z^0 to right handed fermions

Forward-Backward Asymmetry

- FB asymmetry factor given as the ratio:

$$\mathcal{A}_{fb} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3b}{4a}$$

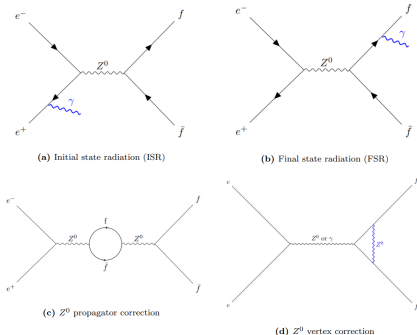
- σ_F, σ_B : cross sections in forward and backward directions respectively
- At Z^0 resonance, \mathcal{A}_{fb} simplifies to ⁵:

$$\mathcal{A}_{fb}^f \approx 3 \left(\frac{g_V^f}{g_A^f} \right) = 1 - 4 \sin^2 \theta_W$$

- From this, ratio of g_V^f to g_A^f can be found
- In turn gives us the Weinberg (weak mixing) angle θ_W

⁵Thomson, *Modern Particle Physics*.

Background Processes: Radiative Corrections



Some radiative corrections

To test out predictions of the Standard Model at high precision, need to account for higher order processes ⁶:

- **ISR:** radiation of photons in the initial state \rightarrow decreases \sqrt{s} and affects Z^0 peak parameters
- **FSR:** radiation of photons or gluons in final state \rightarrow partial widths increase
- **Electroweak corrections:** Virtual processes like loops in Z^0 propagator and vertex corrections

⁶G. Abbiendi et al. and "The OPAL" Collaboration. "Precise determination of the Z resonance parameters at LEP: "Zedometry"". In: *The European Physical Journal C - Particles and Fields* 19.4 (Mar. 2001), pp. 587–651. ISSN: 1434-6052. DOI: 10.1007/s100520100627. URL: <https://doi.org/10.1007/s100520100627>.

Breit Wigner Distribution

- Contribution of Z^0 boson exchange propagator to the matrix element:

$$\mathcal{M}_{Z^0} \propto \frac{g_{Z^0}^2}{q^2 - m_{Z^0}^2} = \frac{g_{Z^0}^2}{s - m_{Z^0}^2}$$

- Around the Z^0 resonance ($\sqrt{s} \sim m_{Z^0}$), propagator diverges
- Correction \rightarrow modify propagator for a decaying state
- For unstable particle having decay rate Γ , wavefunction modified to:

$$\psi \propto e^{-imt} \rightarrow e^{-imt} e^{-\Gamma t/2}$$

- Equivalent to introducing an additional imaginary term in the mass:

$$m \rightarrow m - i\frac{\Gamma}{2}$$

- Z^0 propagator then changes to:

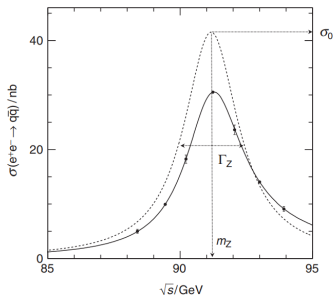
$$\frac{1}{s - m_{Z^0}^2} \rightarrow \frac{1}{s - (m_{Z^0} - i\Gamma_{Z^0}/2)^2}$$

Breit Wigner Distribution

- Complete form of cross section in process $e^+e^- \rightarrow Z^0 \rightarrow f\bar{f}$ is:

$$\sigma_f(s) = \frac{12\pi}{M_Z^2} \frac{s\Gamma_e\Gamma_f}{(s-M_Z^2)^2 + \left(\frac{s\Gamma_Z}{M_Z}\right)^2} (\hbar^2 c^2)$$

- Breit-Wigner distribution:**
Probability distribution that characterizes this dependence of cross section on centre of mass energy
- Various physical parameters can be extracted by fitting this theoretical distribution to the observed data








Breit Wigner distribution of the cross section for $e^+e^- \rightarrow q\bar{q}$ process ⁷

⁷Thomson, *Modern Particle Physics*.

The LEP Experiment

OPAL Detector and its Components

References

-  Abbiendi et al., G. and "The OPAL" Collaboration. "Precise determination of the Z resonance parameters at LEP: "Zedometry"". In: *The European Physical Journal C - Particles and Fields* 19.4 (Mar. 2001), pp. 587–651. ISSN: 1434-6052. DOI: 10.1007/s100520100627. URL: <https://doi.org/10.1007/s100520100627>.
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