Statistical Inference Course Project (Part 1)

MsGret

10 August 2020

The project consists of two parts: simulation (part 1) and basic inferential data analysis (part 2). In part 1 we investigate the exponential distribution in R and compare it with the Central Limit Theorem.

The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda. We will investigate the distribution of averages of 40 exponentials.

Simulations

Set lambda for all of the simulations, number of exponentials, number of simulations:

```
lambda <- .2
nexp <- 40
ns <- 1000
```

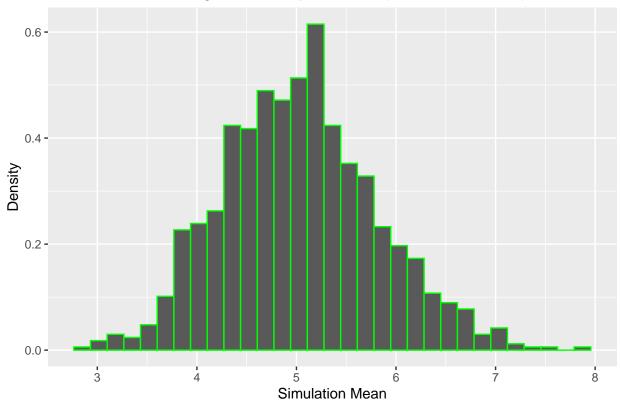
Simulate the distribution of 1000 averages of 40 exponentials:

```
set.seed(2020)
mns = NULL
for (i in 1 : ns)
    mns = as.data.frame(rbind(mns, mean(rexp(n = nexp, rate = lambda))))
names(mns) <- "average"</pre>
```

Plot result of simulation:

```
require(ggplot2)
```





Sample Mean versus Theoretical Mean

The theoretical mean of exponential distribution is 1/lambda. Find the mean from the simulation:

```
theor_mean <- 1 / lambda
theor_mean

## [1] 5
sim_mean <- mean(mns$average)
sim_mean

## [1] 5.033948
diff_mean <- abs(sim_mean - theor_mean)</pre>
```

As we can see in plot bellow Sample Mean and Theoretical Mean are very close (difference is 0.0339482).

Sample Variance versus Theoretical Variance

The theoretical standard deviation of exponential distribution is 1/lambda. Find the Theoretical Variance and Sample Variance of 40 exponentials:

```
theor_var <- (1 / lambda^2) / nexp
theor_var</pre>
```

[1] 0.625

```
sim_var <- var(mns$average)
sim_var

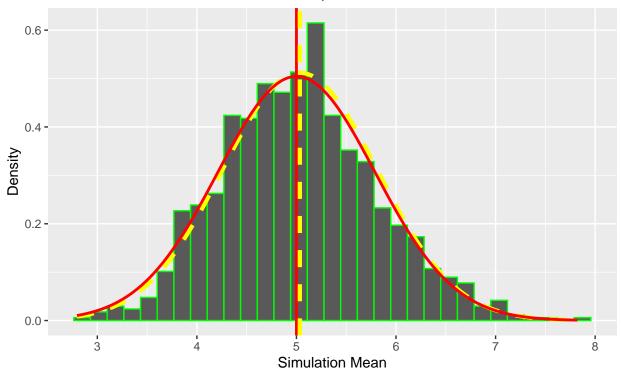
## [1] 0.6070127
diff_var <- abs(sim_var - theor_var)</pre>
```

As we can see in plot bellow Sample Variance and Theoretical Variance are very close (difference is 0.0179873).

Distribution

Plot the theoretical (red line) and simulation (yellow dashed line) means and:

Theoretical Distribution versus Sample Result



red – theoretical mean and distribution, yellow – sample mean and distribution